

1 **Arctic sea level variability from high-resolution model simula-**
2 **tions and implications for the Arctic observing system**

3 Guokun Lyu^{1,2}, Nuno Serra², Meng Zhou¹, and Detlef Stammer²

4 ¹ School of Oceanography, Shanghai Jiao Tong University, Shanghai, 200030, China

5 ² Center for Earth System Research and Sustainability (CEN), University of Hamburg, Hamburg, 20146, Ger-
6 many

7 *Correspondence to:* Guokun Lyu (guokun.lyu@sjtu.edu.cn)

8 **Abstract.** Two high-resolution model simulations are used to investigate the spatio-temporal variability of the
9 Arctic Ocean sea level. The model simulations reveal barotropic sea level variability at periods <30 days, which
10 is strongly captured by bottom pressure observations. The seasonal sea level variability is driven by volume
11 exchanges with the Pacific and Atlantic Oceans and the redistribution of the water by the wind. Halosteric ef-
12 fects due to river runoff and evaporation minus precipitation (EmPmR), ice melting/formation also contribute in
13 the marginal seas and seasonal sea ice extent regions. In the central Arctic Ocean, especially the Canadian Basin,
14 the decadal halosteric effect dominates sea level variability. The study confirms that satellite altimetric observa-
15 tions and Gravity Recovery and Climate Experiment (GRACE) could infer the total freshwater content changes
16 in the Canadian Basin at periods longer than one year, but they are unable to depict the seasonal and subseasonal
17 freshwater content changes. The increasing number of profiles seems to capture freshwater content changes
18 since 2007, encouraging further data synthesis work with a more complicated interpolation method. Further, in-
19 situ hydrographic observations should be enhanced to reveal the freshwater budget and close the gaps between
20 satellite altimetry and GRACE, especially in the marginal seas.

21 **1 Introduction**

22 The Arctic Ocean is experiencing pronounced changes (e.g., Perovich et al., 2020; AMAP, 2019). Observa-
23 tions have revealed increased warm inflows through the Bering Strait (Woodgate et al., 2012) and the Fram
24 Strait (Polyakov et al., 2017), and an unprecedented freshening of the Canadian Basin, especially the Beaufort
25 Gyre (Proshutinsky et al., 2019). The rapid changes potentially impact the weather and climate of the northern
26 hemisphere (Overland et al., 2021).

27 As an integrated indicator, sea level change reflects changing ocean conditions caused by ocean dynamics,
28 atmospheric forcing, and terrestrial processes (Stammer et al., 2013). Satellite altimetry, together with bottom
29 pressure observations from Gravity Recovery and Climate Experiment (GRACE), has been applied to infer
30 ocean temperature and salinity changes that are not measured directly in the Arctic Ocean (e.g., Armitage et al.,
31 2016) and in the deep ocean (e.g., Llovel et al., 2014), enhancing our ability to monitor ocean changes.

32 Over the past decades, coupled ocean-sea ice models and observations have advanced our understanding of
33 the Arctic Ocean variability. Proshutinsky and Johnson (1997) demonstrated wind-forced cyclonic/anticyclonic
34 ocean circulation patterns accompanied by dome-shaped sea levels variation using a barotropic model simula-
35 tion. Further, ocean circulation changes in the Canadian Basin result in freshwater accumulation and release,
36 which is very well correlated to sea level changes (Koldunov et al., 2014; Proshutinsky et al., 2002). Given that
37 sea level changes reflect freshwater content changes in the Canadian Basin, Giles et al. (2012) and Morison et al.
38 (2012) proposed to use satellite altimetry observations and GRACE observations to infer freshwater content
39 changes. The method was then applied to explore the freshwater content changes in the Beaufort Gyre
40 (Armitage et al., 2016; Proshutinsky et al., 2019) at seasonal to decadal timescales. In the Barents Sea, Volkov et
41 al. (2013) used altimetric sea level observations and the ECCO reanalysis (Forget et al., 2015) to explore sea-
42 sonal to interannual sea level anomalies, revealing different roles of mass-related changes, thermosteric and
43 halosteric effects on different regions of the Barents Sea.

44 However, the sparseness of in-situ profiles, coarse resolution and significant uncertainties of satellite altim-
45 etry and GRACE observations result in large gaps in understanding the spatio-temporal variability of the Arctic
46 sea level and its relations to the thermo/halosteric effects and mass changes (Ludwigsen and Andersen, 2021).
47 Previous studies mainly focus on the decadal sea level variability (e.g., Koldunov et al., 2014; Proshutinsky et al.,
48 2007; Proshutinsky and Johnson, 1997), and no study has yet fully explored the Arctic sea level variability at
49 different spectral bands, and its dependence on the mass component and the vertical oceanic variability. Such a
50 study could help identify critical regions and environmental parameters that need to be observed coordinately
51 and point out observational gaps that need to be filled in the future.

52 Our study systematically explores the Arctic sea level variability as a function of timescale and geographic
53 location using daily and monthly outputs of two high-resolution model simulations. Contributions from
54 barotropic changes expressed in bottom pressure variations and baroclinic processes represented by
55 thermo/halosteric changes are quantified at different timescales. Altimetric and GRACE measurements, in-situ
56 hydrographic observations mapped with different interpolation schemes (e.g., Haine et al., 2015; Polyakov et al.,
57 2008; Rabe et al., 2014; Rabe et al., 2011), and ocean reanalyses have been used to infer the basin-scale
58 freshwater changes during the unprecedented freshwater changes since the 2000s. However, Solomon et al.
59 (2021) pointed out that significant uncertainties and discrepancies remain in revealing the regional patterns. This
60 study further discusses the existing Arctic observing system's capability to monitor the Arctic freshwater content

61 variability and identify observational gaps.

62 The structure of the remaining paper is as follows: the numerical models and the observations from the bot-
63 tom pressure sensor, GRACE, and satellite altimetry are described in Section 2, together with different compo-
64 nents of sea level changes. We compare the model simulations against observations in Section 3. Section 4 ana-
65 lyzes sea level variability and associated mechanisms at high frequency (<30 days), seasonal cycles, and decadal
66 timescales. The relations with bottom pressure and thermos/halosteric components are demonstrated, pointing
67 out key regions and parameters we need to observe. Further, we analyze the ability of satellite altimetry,
68 GRACE, and the in-situ profiler system to monitor the Arctic freshwater content variability in Section 5. Sec-
69 tion 6 provides a summary and conclusions.

70 **2 Model Simulations and observations**

71 **2.1 Atlantic-Arctic simulations**

72 This study relies on two ocean high-resolution numerical simulations using the MIT general circulation
73 model (Marshall et al., 1997). A dynamic thermodynamic sea ice model (Hibler, 1979, 1980;Zhang and
74 Rothrock, 2000), implemented by Losch et al. (2010), is employed to simulate sea ice processes. The model
75 domain covers the entire Arctic Ocean north of the Bering Strait and the Atlantic Ocean north of 33°S. In the
76 horizontal, the model uses a curvilinear grid with resolutions of ~8 km (ATLARC08km) and ~4 km (AT-
77 LARC04km). In the vertical, ATLARC08km has 50 levels with resolution ranging from 10 m over the top 130
78 m to 456.5 m in the deep basin. And ATLARC04km has 100 z-levels ranging from 5 m over the top 200 m to
79 185 m in the deep basin.

80 At the ocean surface, the model simulations are forced by momentum, heat, and freshwater fluxes comput-
81 ed using bulk formulae and either the 6-hourly NCEP RA1 reanalysis (Kalnay et al., 1996) (ATLARC08km) or
82 the 6-hourly ECMWF ERA-Interim reanalysis (Dee et al., 2011) (ATLARC04km). A virtual salt flux parame-
83 terization is used to mimic the dilution and salinification effects of rainfall, evaporation, and river discharge.
84 The models are forced by the monthly output from the GECCO2 (Köhl, 2015) global model configuration at the
85 open boundaries. The river runoff is applied at river mouths by seasonal climatology (Fekete et al., 2002). Bot-
86 tom topography is derived from the ETOPO 2-min (Smith and Sandwell, 1997) database. ATLARC08km is
87 initialized with annual mean temperature and salinity from the World Ocean Atlas 2005 (Boyer et al., 2005) and
88 covers 1948 to 2016, and ATLARC04km starts from the initial condition, including velocity, temperature, and
89 salinity, of ATLARC08km at the start of the year 2002. Table 1 summarizes both the simulations and their main
90 characteristics.

91 Table 1. Summary of model simulations used in this study.

	<i>Horizontal resolution</i>	<i>Vertical grid</i>	<i>Surface forcing</i>	<i>periods</i>	<i>Output Frequency</i>	<i>Variables used</i>
<i>ATLARC08km</i>	~8 km	50 z-levels	NCEP-RA1	1948-2016 05.01.2003- 01.12.2010	monthly daily	Potential temperature Salinity Sea surface height

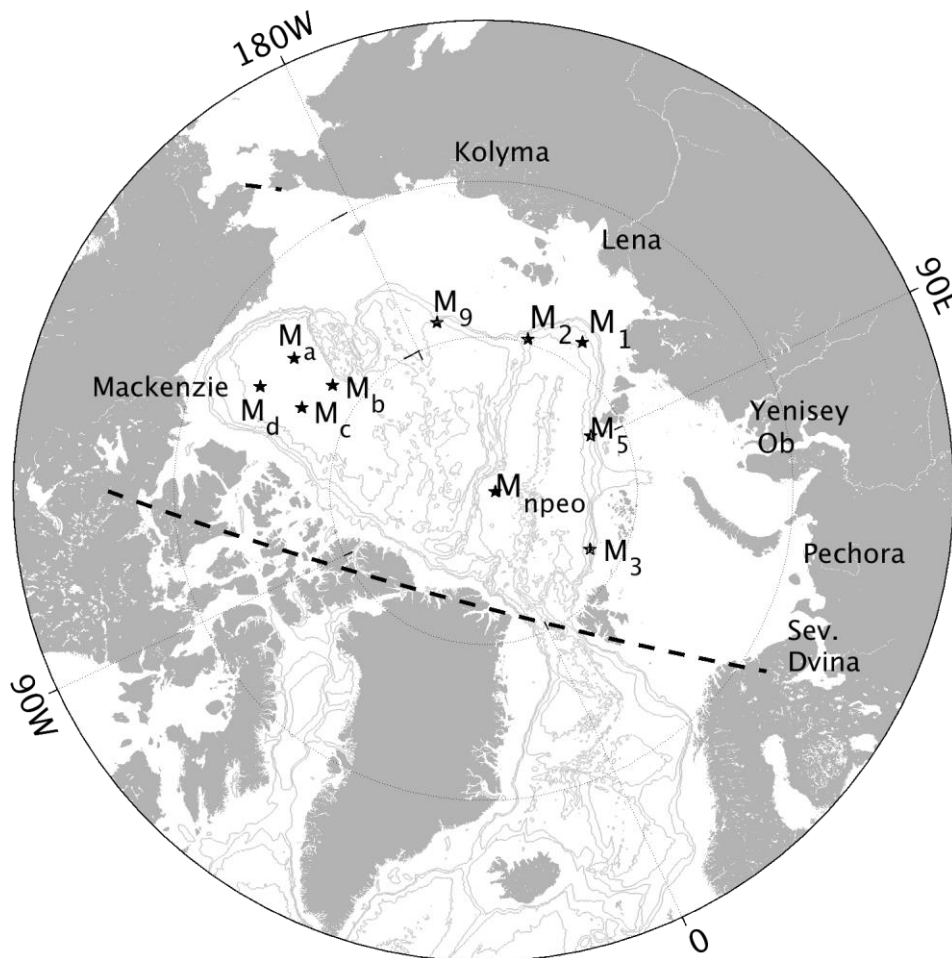
ATLARC04km	~4 km	100 z-levels	ERA-Interim	01.01.2003-23.08.2012	daily	Wind stress
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93 **2.2 Satellite and in-situ observations**

94 Koldunov et al. (2014) have validated ATLARC08km against tide gauge observations. We further compare
 95 the two model simulations against in-situ bottom pressure observations, GRACE observations, and satellite
 96 altimetric observations.

97 The monthly altimetric sea level observations from Armitage et al. (2016,
 98 http://www.cpom.ucl.ac.uk/dynamic_topography/) and GRACE measurements (Chambers and Bonin, 2012,
 99 doi:10.5067/TEOCN-3AJ64) are used in comparison with the model simulations. For the very high-frequency
 100 variability, bottom pressure records supplied by the Beaufort Gyre Exploration Project (BGEP, M_a, M_b, M_c, and
 101 M_d in Fig. 1, <https://www2.whoi.edu/site/beaufortgyre/data/mooring-data/>) and the North Pole Environmental
 102 Observatory (NPEO, M_{npeo} in Fig.1, ftp://northpoleftp.apl.washington.edu/NPEO_Data_Archive/) are used.
 103 Tidal signals are removed using the T_TIDE Matlab program (Pawlowicz et al., 2002) since the model did not
 104 include tidal forcing.



105

106 **Figure 1.** A map of the pan-Arctic Ocean presenting the locations of moorings deployed by the Nansen and
 107 Amundsen Basin Observational System (NABOS, black pentagrams labeled with M₁, M₂, M₃, M₅, and M₉), by
 108 the Beaufort Gyre Exploration Project (BGEP, black pentagrams marked with M_a, M_b, M_c, M_d), and by the

109 North Pole Environmental Observatory (NPEO, black pentagram labeled with M_{npeo}). The black dashed lines
 110 enclose the Arctic regions used in the following sections. Bathymetry contours of 500, 1000, 2000, 3000, and
 111 4000 m are drawn with grey lines. Main rivers are labeled with their names near the river mouths.

112 **2.3 Relation between sea level, bottom pressure, and thermo/halosteric components**

113 Following Ponte (1999) and Calafat et al. (2013), sea level anomaly η' , can be separated into a steric com-
 114 ponent η'_s due to density change, an inverse barometer effect η'_{IB} , and a mass (measured by bottom pressure
 115 observations) component η'_m :

$$116 \eta' = -\frac{1}{\rho_0} \int_{-H}^0 \rho' dz + \frac{1}{\rho_0 g} (\bar{P}'_a - P'_a) + \frac{1}{\rho_0 g} (P'_b - \bar{P}'_a) \quad (1)$$

117 where $g=9.8 \text{ m s}^{-2}$ is the gravitational acceleration. The first term on the right-hand side represents the steric
 118 effect η'_s , with ρ_0 being a reference density (1025.0 kg/m^3 in this study) and ρ' being the density change. The
 119 second term is the inverse barometer effect η'_{IB} : \bar{P}'_a and P'_a represent air pressure anomalies average over the
 120 global ocean and at the observing location, respectively. The last term defines the mass component η'_m . P'_b is the
 121 bottom pressure anomalies in equivalent meters of water.

122 Since the model simulations do not include the impacts of surface air pressure anomalies, the model-
 123 simulated sea level changes due to steric and mass components are simplified as:

$$124 \eta' = -\frac{1}{\rho_0} \int_{-H}^0 \rho' dz + \frac{1}{\rho_0 g} (P'_b) \quad (2).$$

125 Separating density changes into temperature and salinity changes, we decompose the steric height η'_s into
 126 thermosteric height η'_{st} (due to temperature anomalies) and halosteric height η'_{ss} (due to salinity anomalies):

$$127 \eta'_{st} = -\frac{1}{\rho_0} \int_{-H}^0 (\rho(T, \bar{S}, p) - \rho(\bar{T}, \bar{S}, p)) dz \quad (3),$$

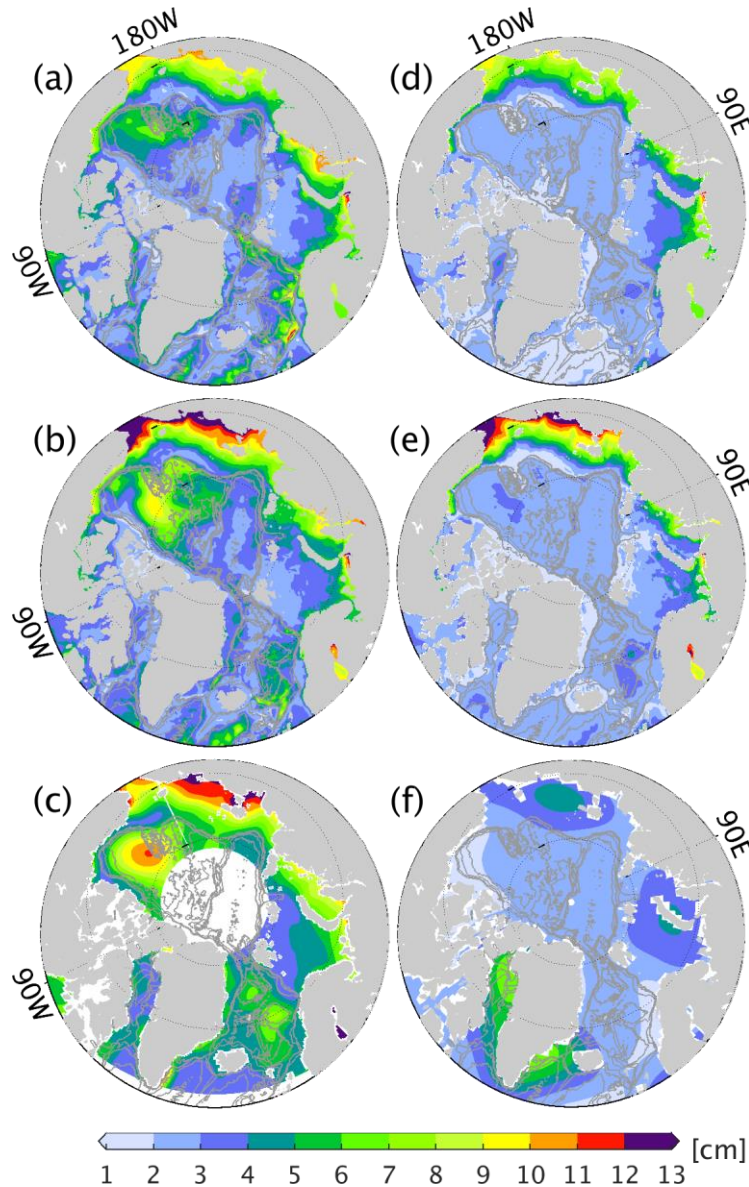
$$128 \eta'_{ss} = -\frac{1}{\rho_0} \int_{-H}^0 (\rho(\bar{T}, S, p) - \rho(\bar{T}, \bar{S}, p)) dz \quad (4),$$

129 where T , S , and p represent seawater temperature, salinity, and pressure. The overbars denote the average over
 130 the simulation time.

131 Before comparing the model simulation with the GRACE measurements and mooring-based bottom pres-
 132 sure observations, we remove air pressure anomalies averaged over the global ocean \bar{P}'_a , and then global-mean
 133 mass changes from GRACE-based bottom pressure observations since the virtual salt flux parameterization does
 134 not include mass transfer from land to ocean. In total, this process removes a seasonal cycle with an amplitude
 135 of ~ 1 - 1.5 cm from the measurements.

136 **3 Testing simulations against observations**

137 Koldunov et al. (2014) have demonstrated that the interannual sea level variability in ATLARC08km and
 138 tide gauges match very well. In the present study, we further evaluate the skill of the model-simulated sea level
 139 and bottom pressure variability by comparing the root mean square (RMS) variability of sea level and bottom
 140 pressure against altimetric data (Armitage et al., 2016) and GRACE data (Chambers and Willis, 2010). In addi-
 141 tion, high-frequency bottom pressure observations from BGEP and NPEO are compared with the two model
 142 simulations.



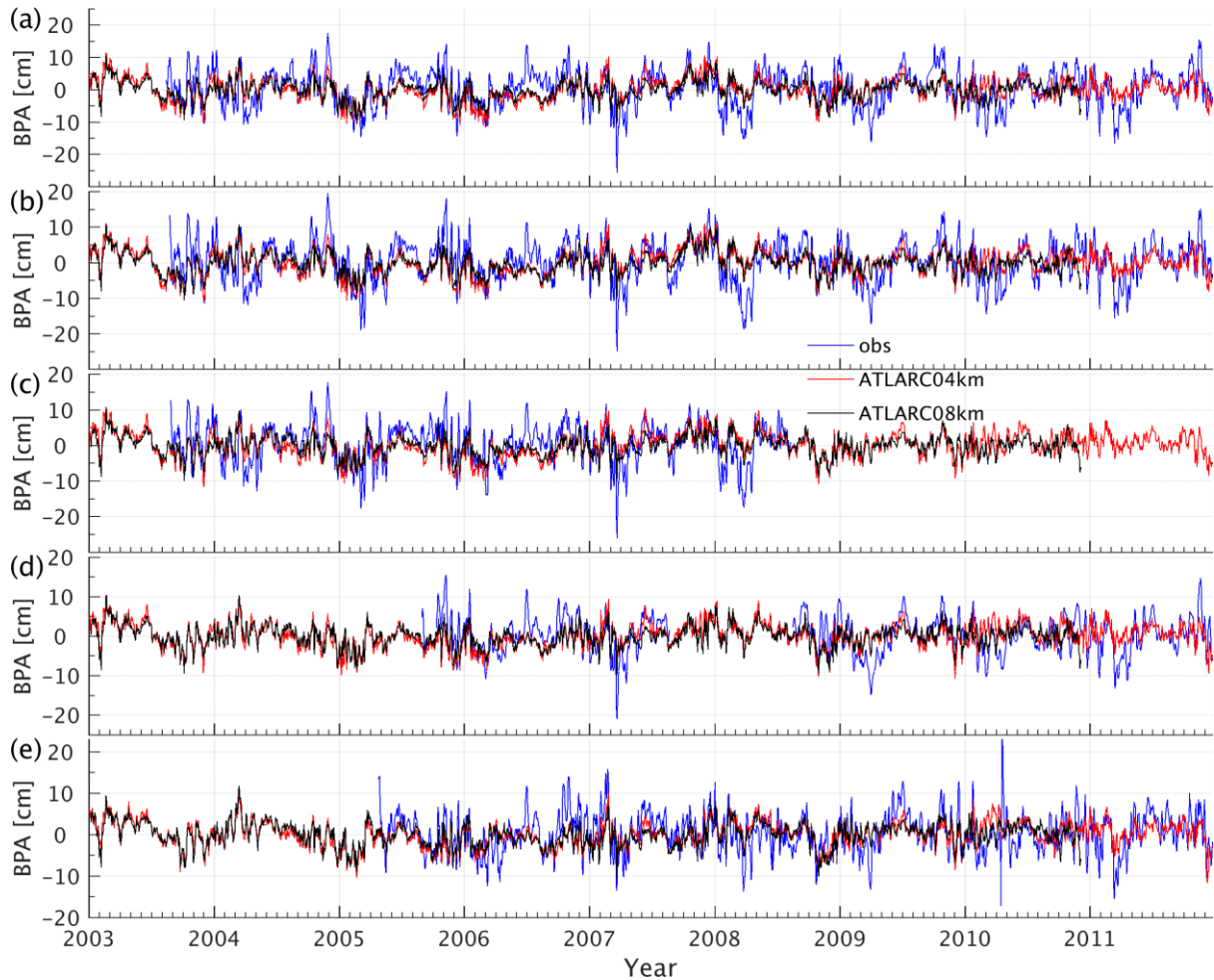
143

144 **Figure 2.** RMS variability of (a-c) sea level and (d-f) bottom pressure in (a, d) ATLARC08km, (b, e) ATLARC04km, (c)
 145 satellite altimetry, and (f) GRACE. We computed the RMS variability using monthly data from January 2003 to December
 146 2011. Bathymetry contours of 500, 1000, 2000, and 3000 m are drawn with grey lines.

147 The model simulations (Figs. 2a, b) and satellite altimetry (Fig. 2c) reveal pronounced sea level variability
 148 in the Canadian Basin and along the coast. In the Canadian Basin, where a characteristic scale of the Rossby
 149 radius is $\sim 10\text{--}15$ km (Nurser and Bacon, 2014), ATLARC04km starts to resolve transient eddies and thereby
 150 simulates more significant sea level variability than ATLARC08km, and matches better with the observed sea
 151 level variability. Still, ATLARC04km and ATLARC08km underestimate the observed sea level variability in
 152 the Canadian Basin. Along the Arctic coast, the pronounced sea level variability is related to the seasonal river
 153 runoff, the redistribution of water due to the shifting of basin-scale cyclonic/anticyclonic wind (Proshutinsky
 154 and Johnson, 1997). Again, ATLARC04km simulates much stronger sea level variability than ATLARC08km
 155 and is comparable to the altimetric observations. Bottom pressure shows significant variability in the Arctic
 156 marginal seas (Figs. 2d-f), especially in the East Siberian Sea. However, due to the smoothing process applied
 157 on GRACE measurements (a 500 km Gaussian filter), both the model simulations simulate much stronger RMS

158 variability of bottom pressure. The coarse GRACE resolution, uncertainties in the altimetric measurements, and
 159 a lack of in-situ hydrographic observations results in gaps in closing the budget of sea level trend and changes,
 160 especially in the Kara, Laptev, and the East Siberian seas (Ludwigsen and Andersen, 2021) where in-situ hydro-
 161 graphic data are rare and altimetric measurements are less correlated with tide gauge data (Armitage et al.,
 162 2016).

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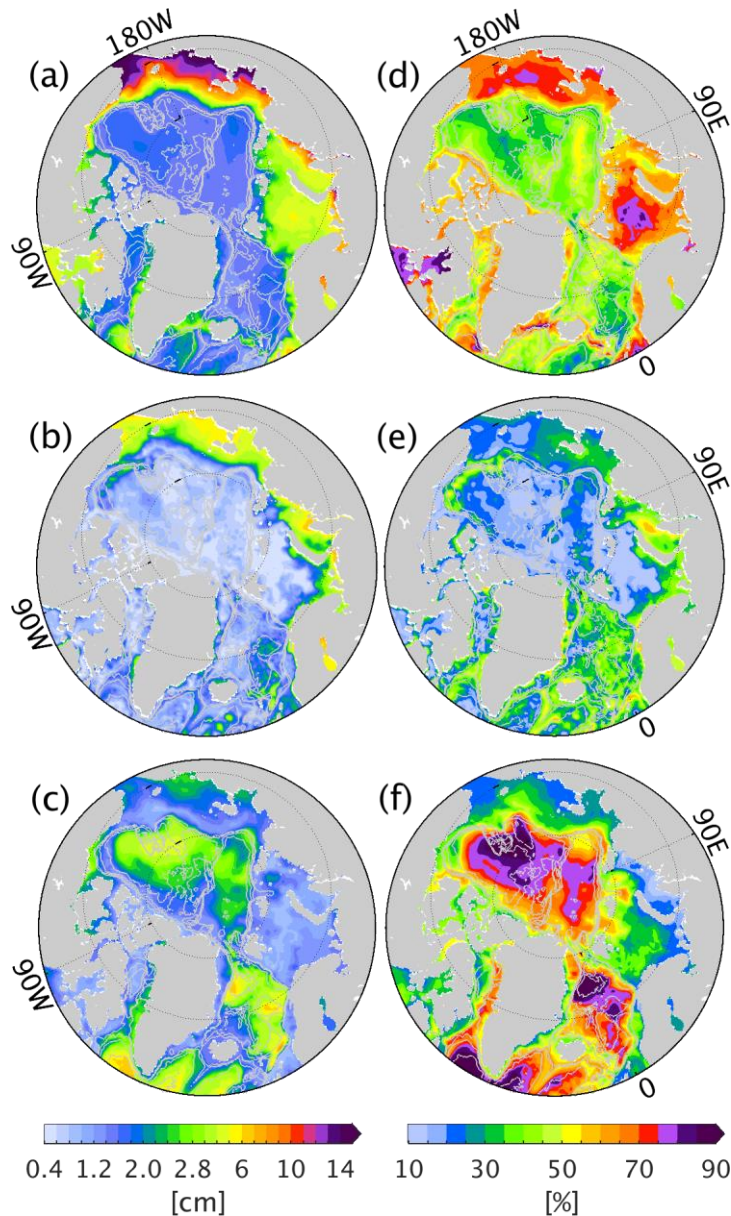
165 Figure 3. Time series of bottom pressure anomalies in ATLARC08km, ATLARC04km, and in-situ observations.
 166 Observations are derived from (a) mooring A, (b) mooring B, (c) mooring C, and (d) mooring D of BGEP. Panel
 167 (e) is from the NEPO moorings. Mooring locations are marked in Fig. 1.

168 Besides monthly to decadal variability of bottom pressure, both the model simulations and the in-situ ob-
 169 servations also demonstrate significant high-frequency bottom pressure anomalies (Fig. 3). Both model simula-
 170 tions correlate well with the observations ($\sim 0.45-0.55$) in the five shown locations, but ATLARC04km and
 171 ATLARC08km underestimate the RMS variability by $\sim 30-50\%$, with ATLARC04km showing relatively
 172 stronger RMS variability.

173 The comparisons above indicate that the model simulations reasonably reproduce the observed sea level
 174 and bottom pressure variability at both high-frequency and low-frequency bands. In the following parts, we will
 175 use the daily output of ATLARC04km to reveal spatial variability of sea level at high frequency and seasonal
 176 periods and use the monthly output of ATLARC08km to explore the decadal sea level variability.

177 **4 Sea level variability and its relation with bottom pressure and steric height**

178 A model study (Proshutinsky et al., 2007) and satellite observations (Armitage et al., 2016) showed that the
 179 Arctic sea level presents distinctive seasonal to decadal variability. In situ bottom pressure observations also
 180 reveal energetic variability at sub-monthly frequencies. Here, we concentrate on sea level variability at very
 181 high-frequency (<30 days), on the seasonal cycle, and at decadal timescales (>4 years).



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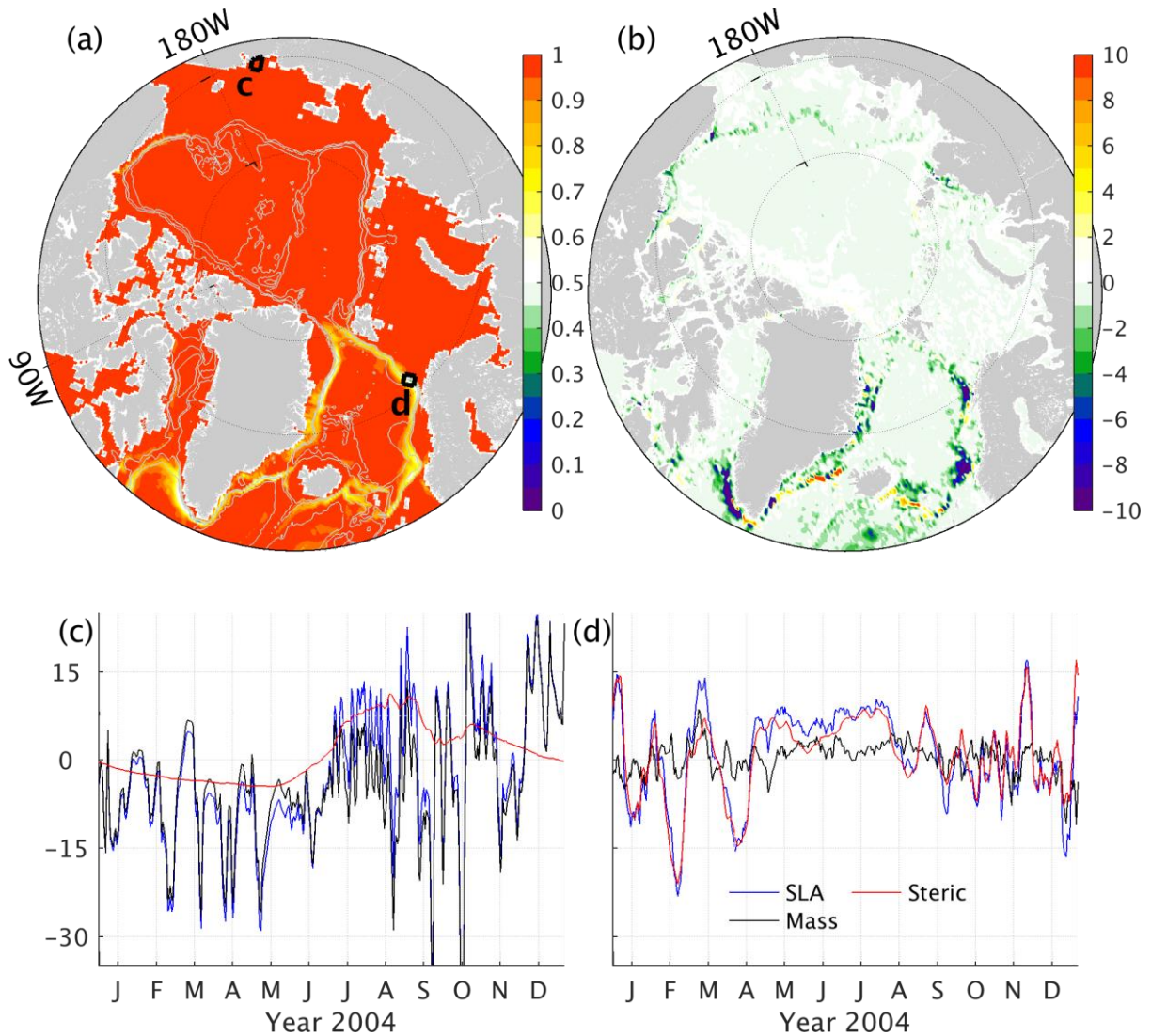
183 Figure 4. RMS variability (cm) of sea level (a) in the high-frequency band (<30 days), (b) at the seasonal cycle,
 184 and (c) at decadal periods (>4 years). Panels (d)-(f) are the corresponding ratios (%) to the total sea level vari-
 185 ance that panels (a)-(c) explained. The high-frequency and seasonal variability (a, b, d, and e) uses the daily
 186 output of ATLARC04km, and decadal variability (c and f) uses the monthly output from ATLARC08km. The
 187 grey lines denote bathymetry contours of 500, 1000, 2000, and 3000 m.

188 At period <30 days, RMS variability of sea level up to 14 cm appears in the marginal seas and along the
 189 coasts (Fig. 4a), accounting for 60%~80% of the local sea level variance (Fig. 4d). The seasonal sea level varia-

190 bility is pronounced in the marginal seas and southern edge of the Beaufort Sea, and it explains 20%-40% of the
 191 total sea level variance. In the deep regions of the pan-Arctic Ocean, the decadal variability dominates the sea
 192 level variability, and it explains more than 70%~90% of the sea level variability. Overall, in the marginal seas,
 193 sea level variability is dominated by sub-monthly and seasonal signals. In contrast, decadal sea level variability
 194 dominates in the deep regions of the pan-Arctic Ocean. Besides, seasonal variability is also visible in the south-
 195 ern periphery of the Beaufort Sea, indicating possible exchanges between the marginal seas and the Beaufort
 196 Sea.

197 **4.1 High-frequency (<30 days) variability**

198 With a coarse resolution model simulation, Vinogradova et al. (2007) demonstrated that sea level variabil-
 199 ity is coherent with and virtually equivalent to bottom pressure in the mid-latitude and subpolar regions at peri-
 200 ods <100 days, reflecting the barotropic nature of high-frequency variability (Stammer et al., 2000). Here, we
 201 revisit the high-frequency sea level variability in the pan-Arctic Ocean with high-resolution model simulations
 202 and a transfer function (Vinogradova et al., 2007) of sea level and bottom pressure.



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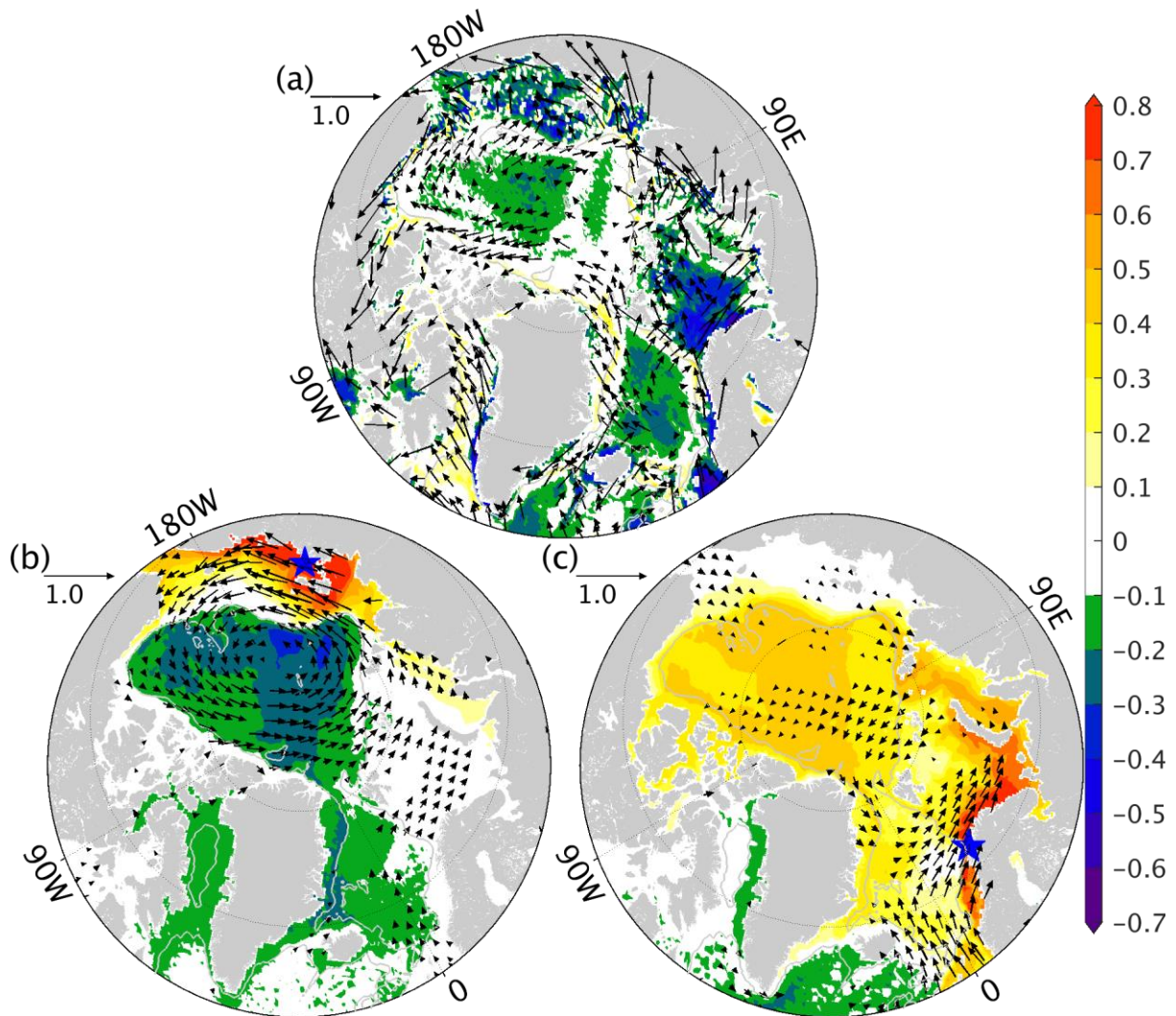
204 Figure 5. (a) Amplitude and (b) phase of the transfer function between sea level anomaly and bottom pressure
205 anomaly at periods <30 days. Time series of sea level anomaly (blue lines), mass component (black lines), and
206 steric component (red lines) averaged (c) in the East Siberian Sea (black box c in panel (a)) and (d) along the
207 NwAC (black box d in panel (a)).

208 Except for the Norwegian Atlantic Current (NwAC) and the East/West Greenland Current (EGC/WGC),
209 the amplitude of the transfer function between sea level and mass component is ~ 1 (Fig. 5a) in most of the pan-
210 Arctic regions. The phases (Fig. 5b) are ~ 0 in the entire Arctic Ocean, indicating that the high-frequency sea
211 level variability is mostly barotropic. However, in the strong current regions, including NwAC, EGC, and WGC,
212 an amplitude of the transfer function of ~ 0.4 is observed, revealing that both barotropic and baroclinic processes
213 contribute to the high-frequency sea level variability.

214 Sub-regions in the East Siberian Sea (c in Fig. 5a) near the maximum RMS variability and along the
215 NwAC (d in Fig. 5a) are used to reveal details of the high-frequency sea level variability. It is clear that the sea
216 level anomaly in the East Siberian Sea (Fig. 5c) is almost equivalent to the bottom pressure anomaly, and the
217 steric component contributes slightly to the seasonal timescale. Along the NwAC (Fig. 5d), pronounced steric
218 height variability with timescales of 20-60 days is visible, which may be caused by baroclinic instability, and
219 the mass component shows high-frequency variability.

220 The high-frequency sea level variability is mainly related to wind forcing (Fukumori et al., 1998) at high
221 latitudes. Correlations to the wind forcing and sea level anomalies are used to explain the driving mechanisms of
222 the high-frequency SLA variability. The negative correlations between high-frequency sea level variability and
223 wind stress curl (shading in Fig. 6a) in the Canadian Basin and GIN seas (-0.3) and in the marginal seas (-0.3 ~
224 0.5) reveal that local sea level increase/decrease is partially related to wind-induced convergence/divergence
225 (vectors and shading in Fig. 6a) of water. In addition, the high correlations of SLA to wind stress (vectors in Fig.
226 6a) along the coast reveal that cyclonic along-shore wind distributes water to the coast through Ekman transport,
227 increasing sea level there.

228 To further explore the propagating features of the strong SLA variability along the coasts, we show
229 correlations of SLA in sub-regions of the East Siberian Sea (blue pentagon Fig. 6b) and Norwegian coast (blue
230 pentagon Fig. 6c) to SLA (shading), and wind stress (vectors). Fig. 6b demonstrates that anticyclonic wind
231 stress distributes water to the coast through Ekman transport which interacts with topography, rising coastal sea
232 levels. SLA in the Norwegian coast is also driven by along-shore wind (vectors in Fig. 6c) through Ekman
233 transport, and the SLA signals propagate along the coast to the Barents Sea and the central Arctic Ocean
234 (shading in Fig. 6c).



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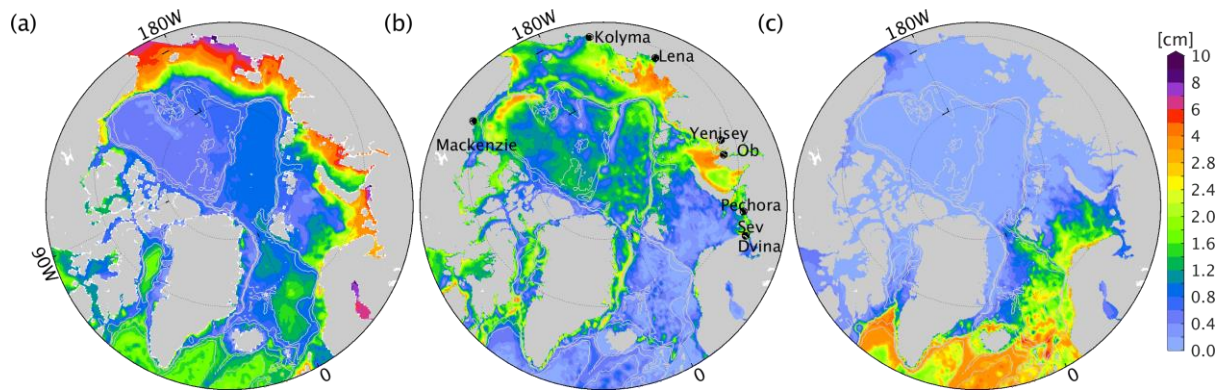
237 Figure 6. (a) Coefficients of the correlation between sea level anomalies and wind stress curl (shading), wind
 238 stress (vectors) at periods < 30 days. (b) Correlations of sea level anomalies in sub-regions of the East Siberian
 239 Sea (blue pentagram in panel (b)) to wind stress (vectors) and sea level anomalies (shading). Panel (c) are the
 240 same as panel (b) but for sea level anomalies in the Norwegian shelf (blue pentagram in panel (c)). Correlation
 241 coefficients with 95% significance levels are plotted.

242 Overall, both the model simulations and the several bottom pressure records demonstrate high-frequency
 243 bottom pressure variability in the Arctic Ocean (Fig. 3). The model simulations reveal that the high-frequency
 244 variability is barotropic primarily in response to wind-induced Ekman transport and propagations of the ba-
 245 rotropic signals. In the strong current regions, steric effects also contribute to local sea level variability caused
 246 by baroclinic processes.

247 4.2 Seasonal variability

248 Seasonal sea level variability could be related to the redistribution of water from the deep ocean to the
 249 marginal seas due to cyclonic/anticyclonic wind stress (Proshutinsky and Johnson, 1997), a seasonal variation of
 250 the Arctic Ocean volume (Armitage et al., 2016). In addition, the steric effect due to warm Atlantic inflow and

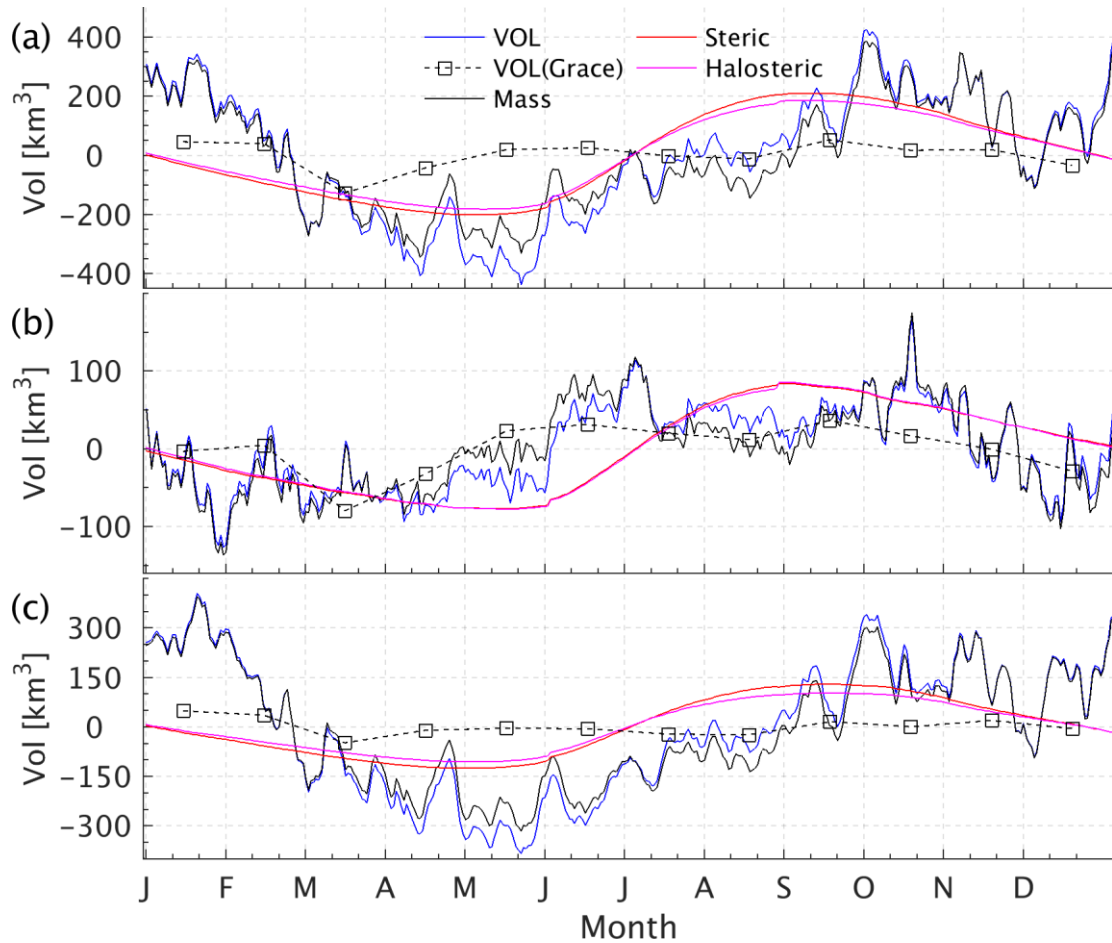
251 sea ice formation/melting contribute to regional sea level variability in the Barents Sea (Volkov and Landerer,
252 2013). This section focuses on the spatial-varying Arctic sea level variability at seasonal periods and its mecha-
253 nism.



254

255 Figure 7. RMS variability of (a) mass, (b) halosteric, and (c) thermosteric components at the seasonal periods.

256 Like the high-frequency sea level variability, the mass component still dominates the seasonal sea level
257 variability in the marginal seas (Fig. 4b and Fig. 7a). Halosteric effects are significant near the river mouth,
258 seasonal ice edge, and along the coast of Alaska (Fig. 7b), indicating the spreading of freshwater driven by oce-
259 anic flows. Pathways of freshwater from rivers and marginal seas to the Makarov Basin and the periphery of the
260 Beaufort Sea can also be inferred from the significant halosteric effect. The thermosteric effects dominate the
261 ice-free region in the GIN seas and the Barents Sea, and it is remarkably weakened as it penetrates the ice-
262 covered Arctic Ocean (Fig. 7c).



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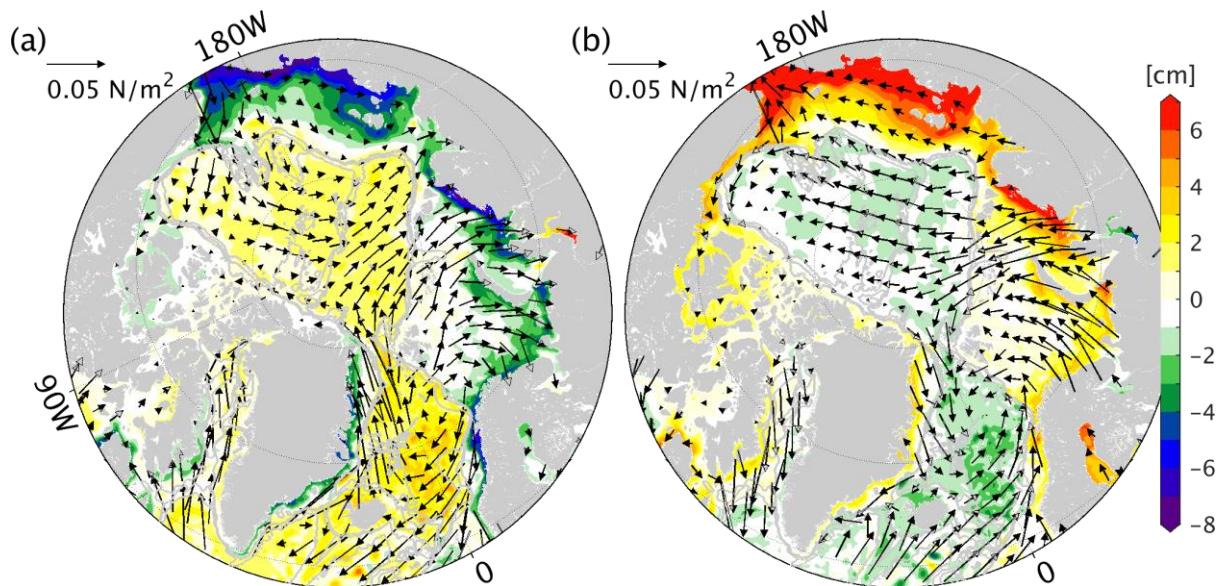
264 Figure 8. (a) Time series of total volume (VOL) anomaly in the Arctic Ocean (see Fig. 1 for the regions) and the
 265 contributions from mass changes (Mass) and steric effects (Steric). The halosteric component (Halosteric) and
 266 the GRACE-observed mass component are also shown. Panels (b) and (c) show the corresponding values in (b)
 267 the deep basin (>500 m) and (c) the shallow water (<500m).

268 Sea level changes reflect total volume changes. The Arctic volume anomalies, dominated by mass compo-
 269 nent, shows a clear seasonal cycle overlaid with sub-seasonal variability (Fig. 8a). Since the surface freshwater
 270 flux is treated as a virtual salt flux, river runoff and evaporation minus precipitation do not change the total
 271 volume directly. The seasonal volume variability, especially the mass component, is driven by volume exchang-
 272 es with the Pacific and Atlantic Oceans. The steric component (red lines in Fig. 8), especially the halosteric
 273 component (magenta lines in Fig. 8), causes the volume to decrease in the winter season and increase in the
 274 summer season due to the sea ice formation/melting.

275 The model simulates more substantial seasonal mass variability than the GRACE measurement. Still, it
 276 fails to reproduce the secondary peak from May to July (Fig. 8a), which may relate to river discharge in the
 277 marginal seas. Splitting the total Arctic volume changes into contributions from the deep basin and coastal seas,
 278 we note that the secondary peak is related to volume changes in the deep basin from May to July (Fig. 8b) in
 279 both the model simulation and the GRACE observations. At the same time, volume anomalies are negative in
 280 the marginal seas. This antiphase of the volume anomalies in the deep basin and marginal seas seems to be driv-
 281 en by the cyclonic/anticyclonic wind pattern in the summer/winter season (Proshutinsky and Johnson, 1997).

282 Mean sea level anomalies from June to August (Fig. 9a) and from December to February (Fig. 9b) further reveal
283 the antiphase of the sea level changes between the deep basin and the shallow waters. The mean pattern of wind
284 stress anomalies (vectors in Fig. 9) indicates that wind-driven Ekman transport drives the water toward/away
285 from the marginal seas, resulting in the antiphase of seasonal sea level variability in the deep basin and shallow
286 waters.

287 The model simulation demonstrates the critical importance of exchanges with the Pacific and Atlantic
288 Oceans for the Arctic volume changes at seasonal periods. The wind stress will further redistribute water in the
289 Arctic Ocean, resulting in the antiphase pattern of sea level changes in the shallow waters and deep basins. Us-
290 ing a one-dimensional model, Peralta-Ferriz and Morison (2010) demonstrated that river runoff and evaporation
291 minus precipitation (EmP) drive the basin-scale seasonal mass variation of the Arctic Ocean. This process is not
292 included in our model simulations due to the virtual salt flux parameterization. But it should be noted that either
293 input from river runoff and EmP (Peralta-Ferriz and Morison, 2010) or exchanges with the Pacific and Atlantic
294 Oceans is large enough to drive the Arctic volume changes. Moreover, the wind stress will further redistribute
295 the water to different regions. It is also expected that volume input from the rivers ($\sim 700 \text{ km}^3$) could signifi-
296 cantly alleviate the negative volume anomalies from May to August in the marginal seas.



297

298 Figure 9. SLA (shading) and wind stress anomalies (vectors) to the climatology averaged from (a) June to Au-
299 gust and (b) December to February. The daily output of ATLARC4km is used.

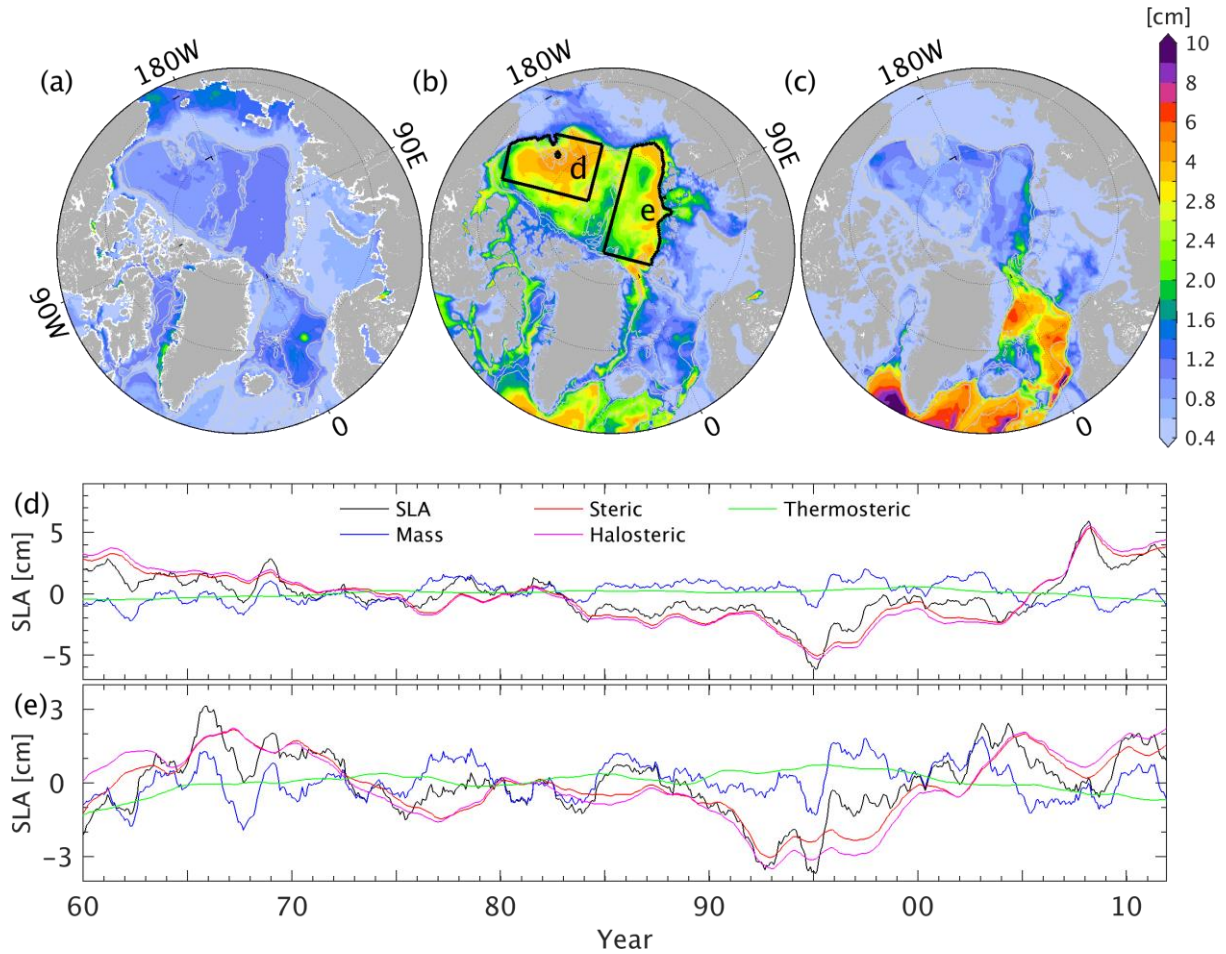
300 4.3 Decadal variability

301 The Arctic sea level shows significant decadal variability driven by cyclonic/anticyclonic wind patterns
302 (Proshutinsky and Johnson, 1997), accompanied by freshwater content changes (Häkkinen and Proshutinsky,
303 2004; Köhl and Serra, 2014). Satellite altimetry observations were used to infer Arctic freshwater content in-
304 creases (Armitage et al., 2016; Giles et al., 2012; Proshutinsky et al., 2019; Rose et al., 2019) and complement

305 freshwater content estimate using in-situ observations (Haine et al., 2015;Polyakov et al., 2020;Rabe et al.,
306 2014;Rabe et al., 2011). This section examines the spatial variability of Arctic decadal sea level and addresses
307 its relation to the mass, halosteric, and thermosteric components.

308 The ATLARC08km simulation revealed that the pronounced decadal sea level variability in the Canadian
309 and Eurasian Basins (Fig. 4c) is mainly due to the halosteric effect (Fig. 10b), with the mass components ac-
310 counting for 20-30%. The thermosteric effect dominates in the GIN seas, mainly relating to the convection pro-
311 cesses (Brakstad et al., 2019;Ronski and Budéus, 2005). Brakstad et al. (2019, see their Fig. A1) demonstrated
312 that a change from shallow convection to deep convection can lead to temperature changes of more than $-0.2\text{ }^{\circ}\text{C}$
313 over the upper 600 m and salinity changes of 0.02 PSU over the upper 200 m, resulting in a significant thermo-
314 steric effect. In the north Atlantic Ocean, the thermosteric effect dominates. At the same time, the halosteric
315 effect compensates for the thermosteric effect in this region, rendering more considerable thermosteric height
316 variability than decadal total sea level variability.

317 Timeseries of sea level anomalies and their different components confirm that sea level variability is most-
318 ly halosteric in the Canadian (Fig. 10d, Armitage et al., 2016;Giles et al., 2012;Morison et al., 2012) and Eura-
319 sian basins (Fig. 10e) and that the thermosteric component contributes with a linear trend (not shown here). In
320 addition, the mass components contribute to the interannual sea level variability (blue lines in Fig. 10d and e) in
321 both the basins. We note that the mass changes are highly correlated in the Canadian and Eurasian basins
322 ($r>0.98$ with 95% significance level). They are positively correlated to the mass changes in the deep basin of the
323 GIN seas and the Arctic Ocean and are negatively correlated to mass changes in the Arctic marginal shelves,
324 especially in the East Siberian Sea, representing a barotropic response of sea level to changes of the intensity
325 and locations of the Icelandic low and the East Siberian high (e.g., Proshutinsky and Johnson, 1997). The halo-
326 steric component shows clearly decadal variability and is in phase with that in the Canadian Basin. The thermo-
327 steric component slightly compensates for the halosteric component.



328

329 Figure 10. RMS variability at the decadal period of (a) bottom pressure anomaly, (b) the halosteric component,
 330 and (c) the thermosteric component. Panels (d) and (e) show the time series of sea level anomaly and mass,
 331 steric, and thermo/halosteric components in the Canadian and the Eurasian basins (see the regions in panel (b)),
 332 respectively. Linear trends in all the time series are removed in panels (d) and (e).

333 5 Capability of the observing system to monitor freshwater content variability

334 Observing Arctic freshwater content changes remains challenging (Proshutinsky et al., 2019). The results
 335 above and previous studies (Giles et al., 2012; Morison et al., 2012; Proshutinsky et al., 2019) have indicated that
 336 satellite altimetry could infer freshwater content changes. International efforts try to enhance the profiles ob-
 337 serving system, including ice-tethered profilers (ITPs, Toole et al. (2016), doi:10.7289/v5mw2f7x), shipboard
 338 observations, and moorings. Here, we test their capability to monitor the freshwater changes in an idealized
 339 setting in which 1) we do not consider influences of observational errors and 2) we assume the profiles sample
 340 the top 800 m and the moorings sample from 65-800 m. Freshwater inventory is defined, as in Rabe et al. (2011)
 341 and Schauer and Losch (2019), as the freshwater fractions relative to a conventional reference salinity $S_0 = 34.8$
 342 PSU integrated over depth, and freshwater content is the total freshwater inventory over a region:

$$343 \quad FWC = \int FWI dA = \int \int_H^0 \frac{S_0 - S}{S_0} dz dA \quad (5)$$

344 with H being the depth of the 34.8 isohaline. The reference salinity indicates the mean salinity within the Arctic
 345 Ocean and can differ slightly in previous studies, which mainly impacts the mean state of freshwater content.

346 5.1 Satellite altimetry and GRACE measurements

347 Giles et al. (2012) used altimetric sea level observations, GRACE-based bottom pressure, and a static 1.5-
348 layer model to infer freshwater changes in the Canadian Basin. They assumed that freshwater changes lead to
349 sea level and isopycnal changes simultaneously, changing the water column's layer thickness and total mass. In
350 this case, freshwater change in the water column is estimated as follows:

$$351 \Delta FW = \frac{S_2 - S_1}{S_2} \cdot \Delta h = \frac{S_2 - S_1}{S_2} \cdot \left(\eta' \cdot \left(1 + \frac{\rho_1}{\rho_2 - \rho_1} \right) - \frac{\Delta m}{\rho_2 - \rho_1} \right) \quad (6),$$

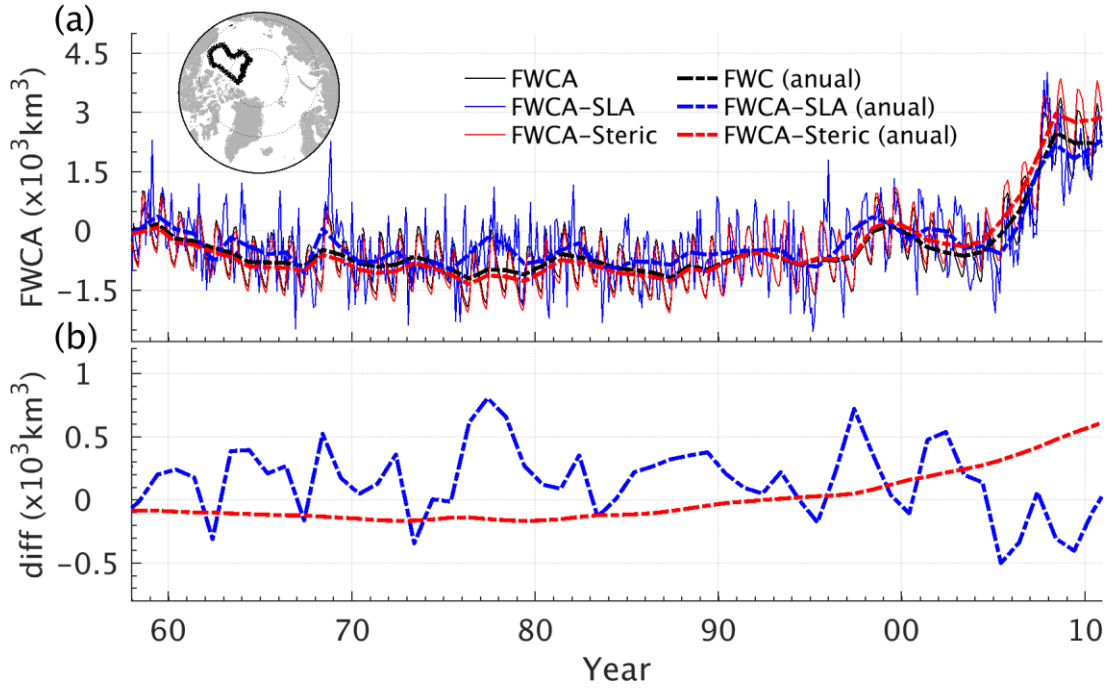
352 where $\rho_1 = 1025.0 \text{ kg m}^{-3}$ and $\rho_2 = 1028.0 \text{ kg m}^{-3}$ are the mean density in the top and bottom layers. $S_1 = 33.0 \text{ PSU}$
353 is the mean salinity in the top layer, and $S_2 = 34.8 \text{ PSU}$ is a reference salinity. η' and Δm are the sea level anomaly
354 and bottom pressure anomalies observations. Morison et al. (2012) suggest that freshwater changes depend on
355 steric height changes linearly and could be approximated by:

$$356 \Delta FW = \alpha \cdot \eta'_s \quad (7),$$

357 where α is an empirical constant estimated from in-situ profile observations and is set to 35.6 following
358 Morison et al. (2012). The choice of α just contributes a static offset to freshwater content estimation in Eq. (7).

359 In the Canadian Basin, freshwater content changes and the two estimates show similar decadal variabilities,
360 but differences remain in the seasonal and long-term trends (Figs. 11a and b). Since the halosteric effect dominates
361 the steric effect, estimation using Eq. (7) matches the seasonal freshwater cycle well (red and black lines),
362 considering the amplitude and phase. However, it overestimates the long-term trend (Fig. 11b) since Eq. (7)
363 attributes the thermosteric effect to freshwater changes. Eq. (6) infers a much more substantial seasonal variability
364 of freshwater content, and the phase does not always match the real freshwater content changes (blue and
365 black lines).

366
367



368

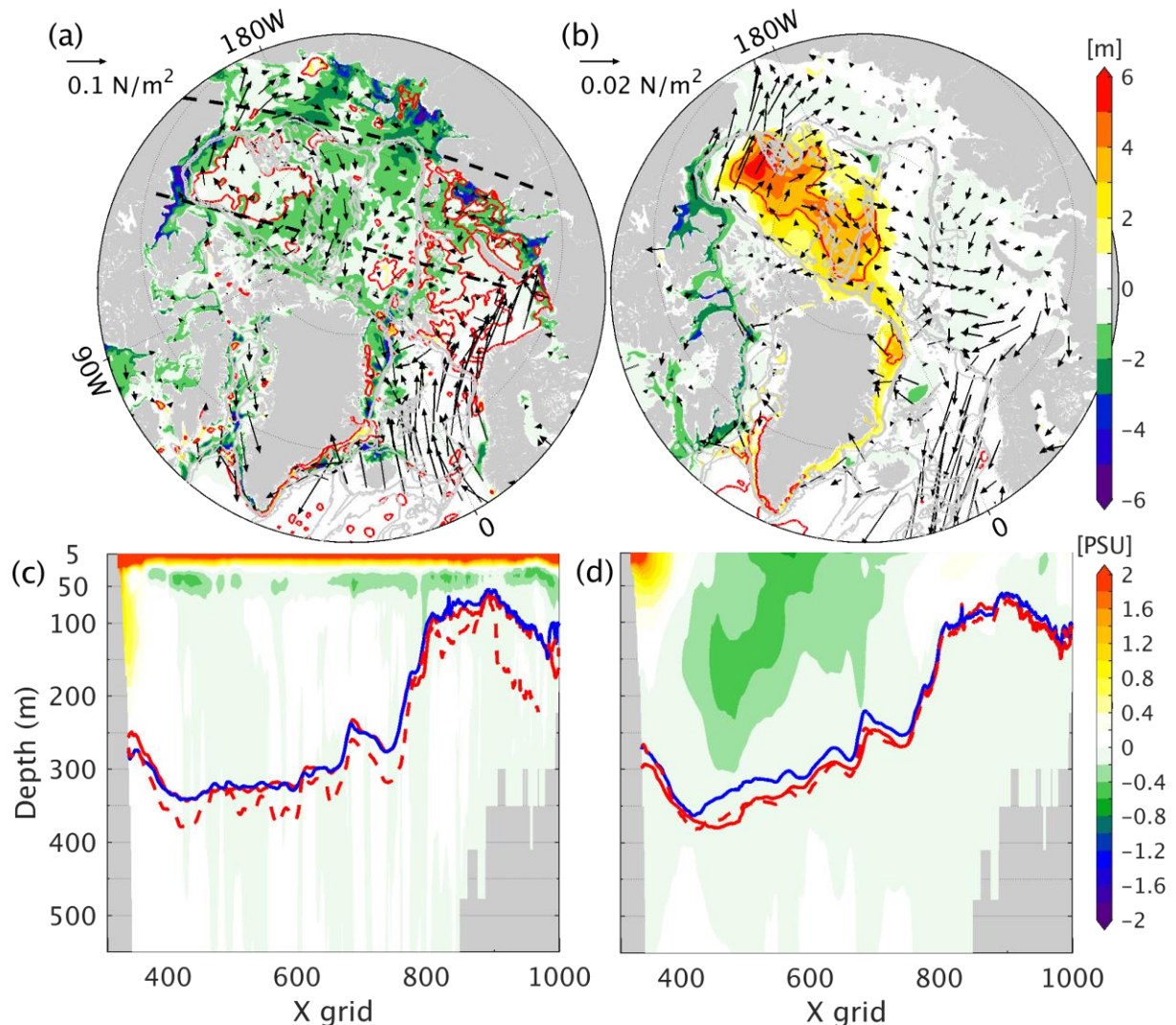
369 Figure 11. (a) Freshwater content anomalies (10^3 km^3) and approximated based on Eq. (6) in blue and Eq. (7) in
 370 red using the monthly output of ATLARC08km. The thick dashed lines are the annual mean values. (b) The
 371 differences of the approximated annual mean freshwater content anomalies based on Eq. (6) in blue and Eq. (7)
 372 in red to the annual mean freshwater content anomalies.

373 Eq. (6) assumes the upper layer adjusts simultaneously with sea level anomaly, which may not apply in the
 374 presence of baroclinic effects. To illustrate the limitation of Eq. (6), we take the differences between Feb. 2003
 375 and Sep. 2002 (in which Eq. (6) fails to reproduce the phase and the amplitude of freshwater content changes)
 376 and between 2008-2010 and 1994-1996 (when Eq. (6) reproduces the freshwater changes well).

377 From Sep. 2002 to Feb. 2003 (Fig. 12a), anticyclonic wind stress anomalies occur in the Beaufort Sea, re-
 378 sulting in positive SLA through Ekman transport. However, freshwater content is reduced during this period.
 379 The salinity difference averaged over the central Arctic Ocean reveals that salinity increases in the top 30 m
 380 were caused by ice formation. At the same time, the isopycnal (27.9 kg m^{-3}) did not deepen (Fig. 12c) as pre-
 381 dicted by Eq. (6). The assumption that freshwater content changes are captured by freshwater column thickness
 382 changes $\eta \cdot \left(1 + \frac{\rho_1}{\rho_2 - \rho_1}\right)$ (red dashed lines in Fig. 12c) fails to infer freshwater content changes in this case.

383 From 1994-1996 to 2008-2010, anticyclonic wind stress anomalies appeared in the Canadian Basin, ac-
 384 companied by positive SLA and freshwater content anomalies (Fig. 12b). During that period, Ekman pumping
 385 deepens the isopycnals (blue and red lines in Fig. 12), accumulating more freshwater and reducing the local
 386 salinity over the top 300 m (Fig. 12d). In this scenario, the water column thickness change dominates the fresh-
 387 water content variability, which is approximated by $\eta \cdot \left(1 + \frac{\rho_1}{\rho_2 - \rho_1}\right)$ (red dashed lines in Fig. 12d). Therefore, Eq.
 388 (6) captures the interannual freshwater content changes using satellite altimetric observations. Caution needs to
 389 be taken when inferring Arctic Ocean freshwater content changes using satellite altimetry observations and

390 GRACE measurements. In addition, Figs. 12b and 12d indicate that Eq. (6) can be only used in the Canadian
 391 Basin where wind drives the sea level changes and the deepening/shoaling of the isopycnals.

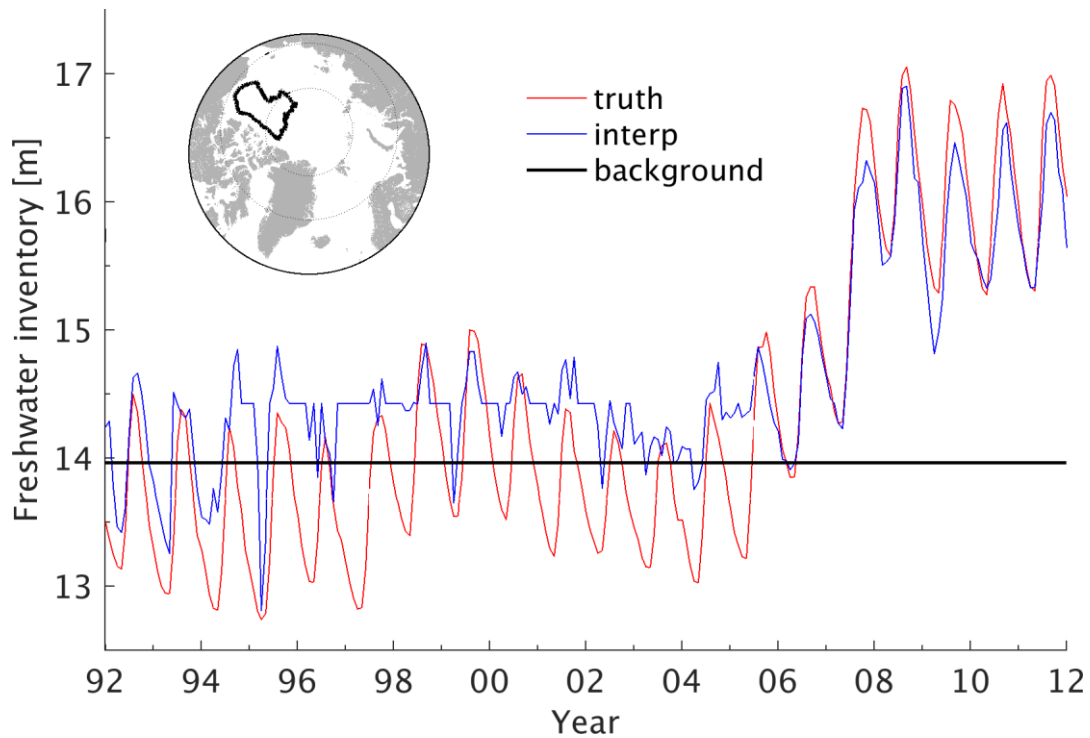


392 Figure 12. The differences of freshwater inventory in meters (shading), sea level anomaly (0.15 m contour,
 393 black lines), and wind stress(vectors) between (a) Feb. 2003 and Sep. 2002, and (b) 2008-2010 and 1994-1996.
 394 Panels (c) and (d) are the corresponding salinity differences (shading) average over the central Arctic Ocean
 395 (black dashed lines in panel (a)). The blue lines denote the 27.9 kg m⁻³ isopycnal in Sep. 2002 and 1994-1996,
 396 respectively. The red lines and red dashed lines are the 27.9 kg m⁻³ isopycnal and the diagnosed 27.9 kg m⁻³
 397 isopycnal with SLA and Eq. (5) in Feb. 2003 and 2008-2010, respectively.

398 5.2 In-situ profilers

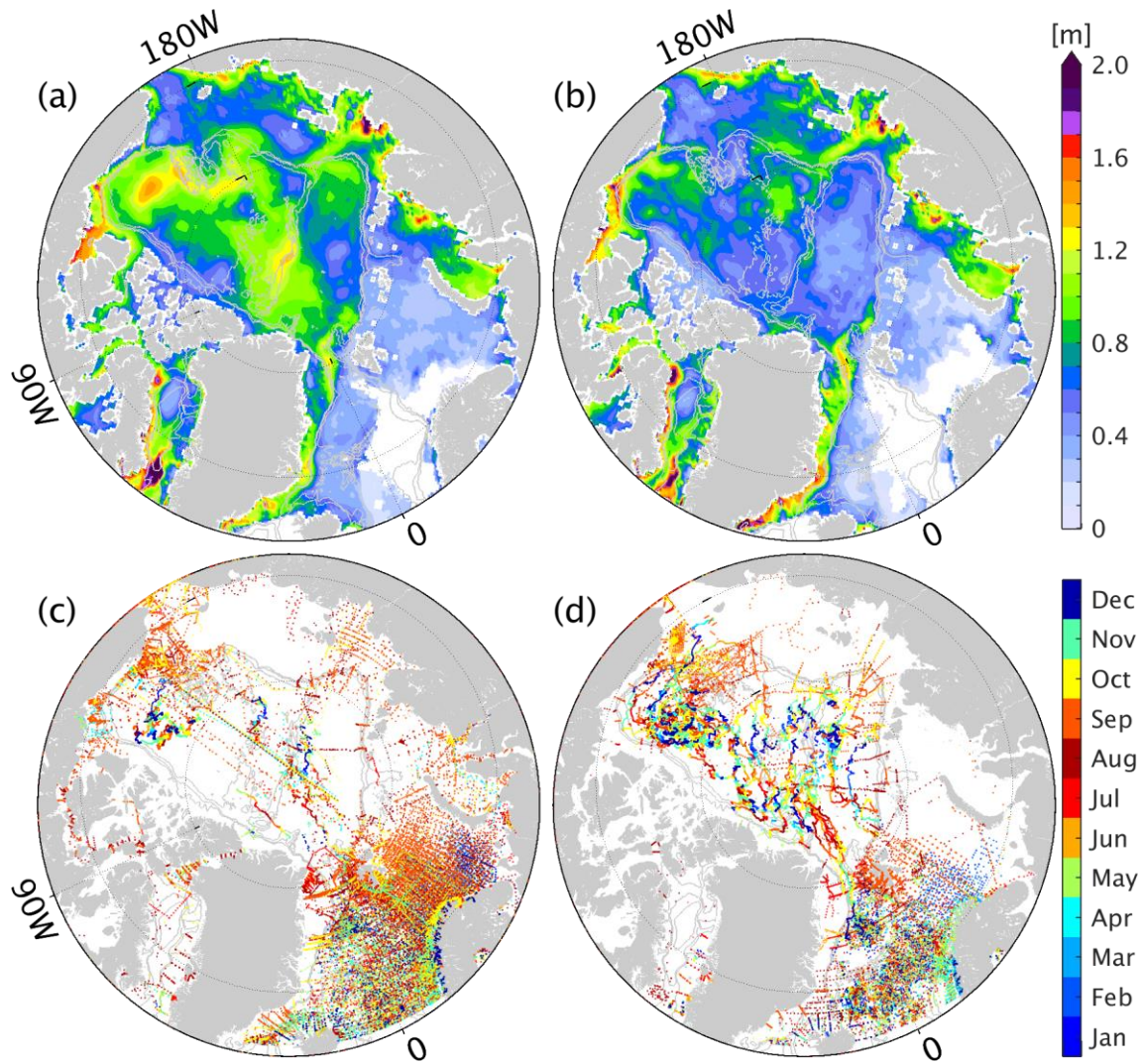
399 In-situ profilers measure salinity directly, but they are limited by sea ice and distributed unevenly in time
 400 and space. Over the past decades, the endeavor of polar expeditions and the evolving measurement techniques
 401 (e.g., ITP) have generated a large number of hydrographic data in the central Arctic and subarctic seas (e.g.,
 402 Behrendt et al., 2018). Using historical hydrographic observations and objective mapping techniques, previous
 403 studies (e.g., Haine et al., 2015; Polyakov et al., 2008; Rabe et al., 2014; Rabe et al., 2011) have explored Arctic
 404 freshwater content changes and the mechanisms on multi-year periods. However, the interpolated products suf-
 405 fer from high uncertainties at timescales shorter than multi-year periods (e.g., Fig. 4 in the supplement of Rabe

406 et al., 2014), indicating observational gaps on resolving the seasonal to interannual freshwater content changes.
 407 Besides, spatial observational gaps are observed (e.g., Fig. 7 in Rabe et al., 2011) but not explored yet. This
 408 section examines how existing hydrographic observations could help reveal Arctic freshwater content changes
 409 and identify observational gaps in time and space. Based on the spatiotemporal distribution of profiles compiled
 410 by Behrendt et al. (2018) and an ensemble optimal interpolation (EnOI) scheme (Evensen, 2003;Lyu et al.,
 411 2014), we test to what extent the generated synthetic profiles could help to reconstruct the "true" state (here the
 412 ATLARC08km simulation) during the periods 1992 to 2012. Details of the EnOI scheme are given in Appendix
 413 A.



414
 415 Figure 13. Mean freshwater inventory (in meter) in the Canadian Basin (enclosed by the black line in the top
 416 subplot) from the background state, the "truth", and the optimal interpolation reconstructed state (see legend).

417 As shown in Fig. 13, the sparse in-situ profiles help bring the freshwater inventory in the background state
 418 close to the "truth" state. However, it was not until 2007 that the reconstructed state reproduces the seasonal to
 419 inter-annual freshwater inventory variability in the Canadian Basin, benefiting from the increasing number of
 420 research activities and international collaborations. We further examined RMS errors of freshwater inventory
 421 from 1992-2006 (Fig. 14a), 2007-2012 (Fig. 14b), and the corresponding profile locations (Fig. 14c and d). The
 422 lack of in-situ profiles in the Arctic shelves (Figs. 14c and d) and in the deep basin from 1992-2006 (Fig. 14c)
 423 results in pronounced errors. The ITP profiles (trajectories in Fig. 14d) enhanced the capability to observe the
 424 Arctic freshwater changes in the deep basin and the winter season, significantly reducing freshwater inventory
 425 uncertainties (Fig. 14b). Additionally, high errors remain in regions with high variability (e.g., EGC/WGC), in
 426 the Laptev Sea and the Alaskan coast, extending from the coasts to the deep basin, underlining the observing
 427 requirements.



428

429 Figure 14. Root mean square errors of freshwater inventory (in meter) between the reconstructed state and the
 430 "truth" from (a) 1992-2006 and (b) 2007-2012. Panels (c) and (d) are the corresponding profile locations in
 431 different months (color bar).

432

433

The above results highlight that the increase of hydrographic observations has enhanced our ability to re-
 434 construct the changes in Arctic freshwater content since 2007. A lack of hydrographic observations in the
 435 coastal areas results in significant errors in the marginal seas, which require extensive international collabora-
 436 tions.

437 6 Summary and conclusions

438 Sea level variability reflects changes in ocean dynamics, atmospheric forcing, and terrestrial runoff pro-
 439 cesses (Stammer et al., 2013). In particular, sea level observations have been applied to infer freshwater content
 440 changes (Armitage et al., 2016; Giles et al., 2012; Proshutinsky et al., 2019) in the central Arctic Ocean. To com-
 441 plement our understanding of the Arctic sea level variability and its mechanisms, we use two high-resolution
 442 ATLARC model simulations to investigate the Arctic sea level variability at different timescales and the relation
 443 with bottom pressure and thermo/halosteric effects, identifying critical observational gaps that need to be filled.

444 Both the model simulations and mooring observations reveal very high-frequency bottom pressure varia-
445 tions. The model simulations confirm that the bottom pressure anomaly is equivalent to sea level anomaly in
446 most areas of the Arctic Ocean at periods <30 days, reflecting the barotropic nature of this high-frequency vari-
447 ability. Correlation analyses show that the high-frequency sea level variability is caused by wind-driven Ekman
448 transport and propagations of these barotropic signals.

449 The seasonal sea level variability is dominated by volume exchanges with the Pacific and Atlantic Oceans
450 and the redistribution of the water by wind stress. Halosteric effects due to river runoff and ice melt-
451 ing/formation are also pronounced in the marginal seas and seasonal sea ice extent regions. Peralta-Ferriz and
452 Morison (2010) demonstrated that river runoff and EmP drive the seasonal cycle of the Arctic bottom pressure.
453 Although the virtual salt flux parameterization could not mimic the influences of volume input from rivers and
454 surface fluxes, the model simulations still simulate much stronger seasonal mass anomalies than the observa-
455 tions from GRACE. Either volume exchanges with the Pacific and Atlantic Oceans or volume input from river
456 runoff and EmP are large enough to cause the Arctic Ocean's seasonal volume variability. They should work
457 together, resulting in the Arctic seasonal volume variability. We speculate that using river runoff and EmP as
458 volume flux, rather than the virtual salt flux, could likely improve the volume and sea level variability in the
459 marginal seas from April to July since the volume inputs from river runoff could alleviate the negative volume
460 anomalies in the marginal seas caused by wind.

461 At decadal timescales, the model simulations further confirm that the pronounced sea level variability in the
462 central Arctic Ocean, especially in the Canadian Basin, is mainly a halosteric effect. Using the satellite altimet-
463 ric observations and GRACE observations, the method of Giles et al. (2012) could infer the freshwater content
464 changes in the Canadian Basin reasonably at timescales longer than one year since the upper layer (indicated by
465 the 27.9 kg m^{-3} isopycnal in this study) requires time to adjust to sea level changes. Inferring freshwater content
466 changes using a linear relation of freshwater content and steric height (Morison et al., 2012) reveals both the
467 interannual and the seasonal variability of freshwater content. However, caution needs to be taken since the
468 method attributes the thermosteric effects to halosteric effects, resulting in an additional linear trend. In addition,
469 uncertainties in the satellite altimetric and GRACE measurements make the estimation more complicated and
470 introduce significant uncertainties in the steric effects and freshwater content estimation (Ludwigsen and
471 Andersen, 2021).

472 The increasing number of international collaborations and new measurement techniques have generated a
473 large number of profiles. Previous studies have applied different objective mapping methods (Haine et al.,
474 2015;Polyakov et al., 2008;Rabe et al., 2014;Rabe et al., 2011) to reconstruct the Arctic freshwater content
475 changes and budget. However, the interpolated products still show high errors for the annual mean estimate of
476 freshwater content, indicating potential observational gaps in resolving the seasonal freshwater content cycle.
477 We further examined the observational gaps in time and space using monthly output from ATLARC08km.
478 Through reconstructing the salinity with synthetic observations, we note that the in-situ profile system seems to
479 capture the seasonal freshwater variability since the year 2007, encouraging further Arctic data synthesis studies
480 (Behrendt et al., 2018;Cheng and Zhu, 2016;Steele et al., 2001) with more complicated interpolation methods.
481 In addition, international collaborations need to be enhanced to fill in the observational gaps in the marginal seas.

482 Further observing system simulation experiments (e.g., Lyu et al., 2021;Nguyen et al., 2020) should be per-
483 formed in a coordinated fashion to develop an autonomous Arctic observing system (Lee et al., 2019;Sandu et
484 al., 2012) to meet the societal and scientific needs.

485 **7 Data availability**

486 The data used to create the plots in the paper are available at Pangaea ([https://issues.pangaea.de/browse/PDI-](https://issues.pangaea.de/browse/PDI-22940)
487 [22940](https://issues.pangaea.de/browse/PDI-22940)). To access the results of the two high-resolution ATLARC model simulations, please contact Dr. Nuno
488 Serra at <https://www.ifm.uni-hamburg.de/en/institute/staff/serra.html>. The Beaufort Gyre Exploration Program
489 data were collected and made available by the Woods Hole Oceanographic Institution
490 (<https://www2.whoi.edu/site/beaufortgyre/>) in collaboration with researchers from Fisheries and Oceans Canada
491 at the Institute of Ocean Sciences and were derived from
492 <https://www2.whoi.edu/site/beaufortgyre/data/mooring-data/>. The North Pole Environmental Observatory data
493 were derived from <http://psc.apl.washington.edu/northpole/Mooring.html>. The satellite altimetric and GRACE
494 measurements were retrieved via http://www.cpom.ucl.ac.uk/dynamic_topography and
495 [https://podaac.jpl.nasa.gov/announcements/2021-06-11-GRACE-and-GRACE-FO-L3-Monthly-Ocean-and-](https://podaac.jpl.nasa.gov/announcements/2021-06-11-GRACE-and-GRACE-FO-L3-Monthly-Ocean-and-Land-Mass-Anomaly-RL06-04-Dataset-Release)
496 [Land-Mass-Anomaly-RL06-04-Dataset-Release](https://podaac.jpl.nasa.gov/announcements/2021-06-11-GRACE-and-GRACE-FO-L3-Monthly-Ocean-and-Land-Mass-Anomaly-RL06-04-Dataset-Release). We gratefully acknowledge the Ice-Tethered-Profiler Pro-
497 gram based at the Woods Hole Oceanographic Institution (<https://www.whoi.edu/itp>) and the Unified Database
498 for Arctic and Subarctic Hydrography (<https://doi.pangaea.de/10.1594/PANGAEA.872931>) collected and com-
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500

501 *Author contribution.* G. Lyu performed the analysis and wrote the paper. N. Serra performed the model simula-
502 tions. D. Stammer proposed this study, and M. Zhou provided advice on the analysis.

503 *Competing interests.* The authors declare that they have no conflict of interest.

504

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515 Appendix A

516 An EnOI Scheme

517 We use an EnOI scheme (Cheng and Zhu, 2016) to reconstruct the salinity in the Arctic Ocean using syn-
518 thetic observations. At one grid (denoted by subscript g), the analysis state φ_g^a is a linear combination of a back-
519 ground field φ_g^b and surrounding in-situ observations d :

$$520 \varphi_g^a = \varphi_g^b + K(d - H\varphi_g^b) \cdot e^{-\frac{x^2}{2\sigma^2}} \quad (\text{A1}),$$

521 where H is a transfer matrix that maps model state from model space to observation points. In this study, the
522 background state of salinity φ_g^b is taken as the mean salinity at each grid over the period 1992-2012. K is the
523 Kalman gain, calculated as:

$$524 K = \varphi_g' \varphi_g'^T H^T (H \varphi_g' \varphi_g'^T H^T + \gamma \gamma^T)^{-1} \quad (\text{A2}).$$

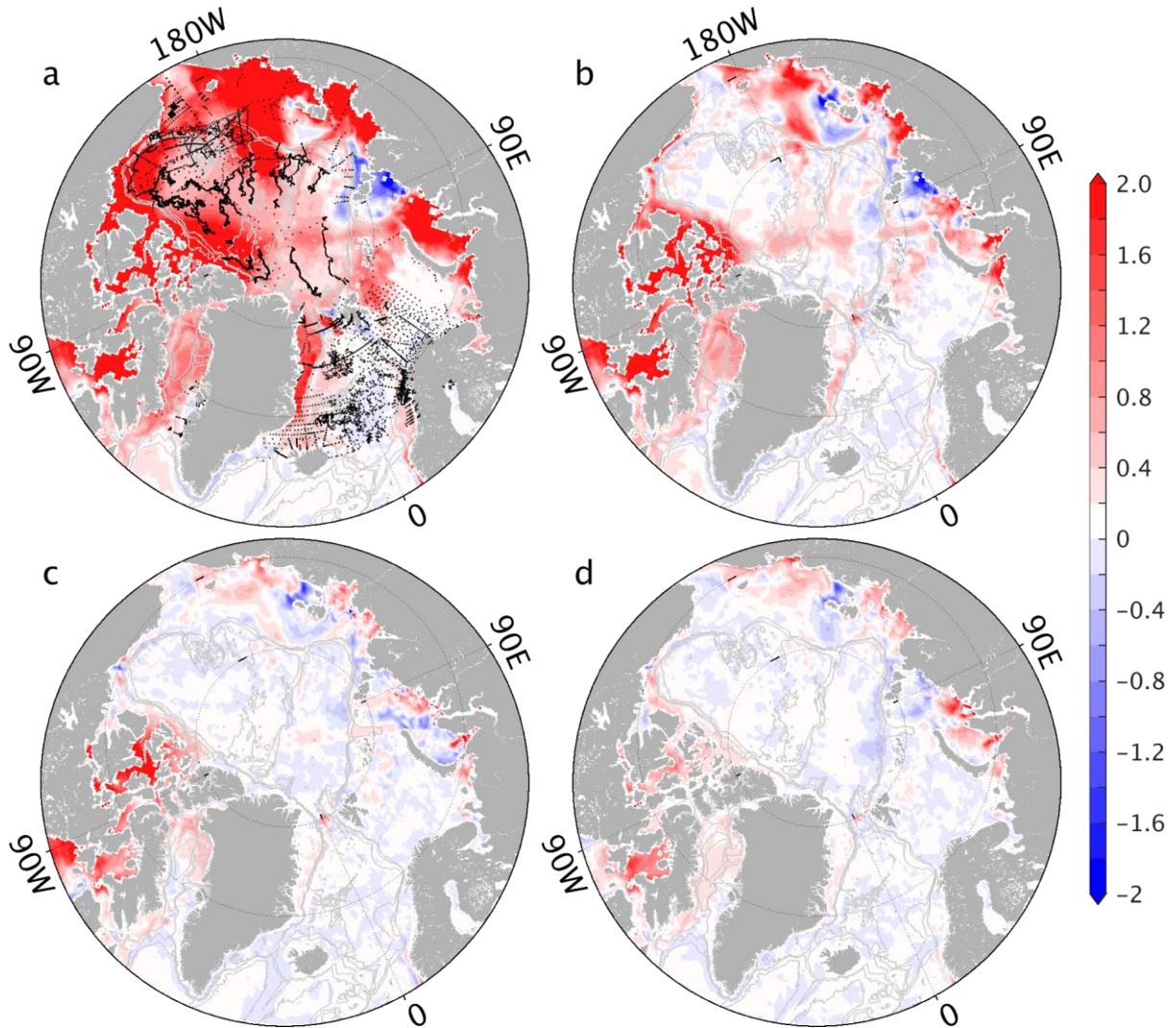
525 The superscript T denotes matrix transposition. In this formulation, we use φ_g' , the salinity deviation from
526 the mean salinity, to compute the error covariance of the background state ($\varphi_g' \varphi_g'^T$). We use monthly data from
527 the year 1992 to 2012 to compute φ_g' , resulting in a total of 252 ensemble members. For simplicity, we assume
528 the representation errors γ only depend on depth, ranging from 0.09 PSU at the surface to 0.02 PSU in the deep
529 ocean, and are not correlated.

530 The use of ensemble members to approximate the background error covariance ($\varphi_g' \varphi_g'^T$) will inevitably
531 introduce long-distance correlations and propagate the observational information incorrectly over a much longer
532 distance. Therefore, we introduce a Gaussian function depending on the distance between observational
533 locations and the model grid (x in Eq. A1) and a decorrelation radius (σ in Eq. A1) to ensure that only
534 observations within the decorrelation radius σ of a model grid point could modify the analysis state.

535 Taking the "true" salinity state from August 1992 and observation locations from 2008 (black dots in Fig.
536 A1a), we test the impacts of the decorrelation radius on the analysis field. The background state is more saline
537 than the truth (Fig. A1a). With a 300 km decorrelation radius (Fig. A1b), the analysis state reduces the errors
538 near the observations while significant errors remain in regions far from observations. Increasing the

539 decorrelation radius to 1000 km, we see that salinity errors in the marginal seas, north pole areas, and the Baffin
540 bay are reduced (Fig. A1c). A 2400 km decorrelation radius further reduces salinity error in the Canadian Arctic
541 Archipelago (Fig. A1d). However, only slight improvements are observed in the central Arctic Ocean, and
542 errors in the Kara Sea are slightly increased. Since we focus on the Arctic freshwater content variability, we use
543 a 1000 km decorrelation radius throughout this study.

544



545

546 Figure A1. Example of sea surface salinity difference between (a) the background and the truth, (b) the analysis
547 with a decorrelation radius of 300 km and the truth, (c) the analysis with a decorrelation radius of 1000 km and
548 the truth, and (d) the analysis with a decorrelation radius of 2400 km and the “truth.” Black dots in panel (a)
549 denote the locations of synthetic observations, sampled using sites of the observations from the year 2008.
550

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