Responses of estuarine circulation to the morphological evolution in a convergent, microtidal estuary

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Abstract:

The Huangmaohai Estuary (HE) is a funnel-shaped microtidal estuary in the west of the Pearl River Delta (PRD) in southern China. Since China's reform and opening up in 1978, extensive human activities have occurred and greatly changed the estuary's topography, and modified its hydrodynamics. In this study, we examined the morphological evolution by analyzing remote sensing data with ArcGIS tools and studied the responses of hydrodynamics to the changes in topography from 1977 to 2010 by using the Delft3d model. We took the changes in estuarine circulation during neap tides in dry seasons as an example. The results show that human reclamation caused a narrowing of the estuary, and channel dredging deepened the estuary. These human activities changed both the longitudinal and lateral estuarine circulations. The longitudinal circulation was observed to increase with the deepening and narrowing of the estuary. The lateral circulation experienced changes in both the magnitude and pattern. The momentum balance analysis shows that when the depth and width changed simultaneously, the longitudinal estuarine circulation was modulated by both the

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channel deepening and width reduction, in which the friction, pressure gradient force, and advection terms were altered. The analysis of the longitudinal vortex dynamics indicates that the changes in the vertical shear of the longitudinal flow, lateral salinity gradient, and vertical mixing were responsible for the change in the lateral circulation. The changes in water depth are the dominant factor affecting lateral circulation intensity. This study has implications for sediment transport and morphological evolution in estuaries heavily impacted by human interventions.

Keywords: Estuarine circulation, Morphological evolution, Huangmaohai Estuary

1. Introduction

Estuarine circulation, the tidally averaged flow in estuaries including both the longitudinal and lateral circulations, is the main driving force for the transport of sediment, pollutants, and other materials, and also one of the primary factors affecting the ecological environment of estuaries (Kjerfve et al., 1981). Estuarine circulation is influenced by many factors (Geyer and Maccready, 2014), such as sea-level fluctuations (Wilson and Filadelfo, 1986), river discharge, tides (Pritchard, 1952), and winds (Scully et al., 2005; Waterhouse et al., 2013; Geyer and Maccready, 2014; Salles et al., 2015; Chen et al., 2020a). Topography in an estuary has a significant effect on the pattern and intensity of the estuarine circulation (Fischer, 1976; Dyer, 1977). Human activities may change the estuarine topography, leading to changes in the estuarine circulation and associated material transport. Therefore, a study of the estuarine circulation and its response to human activities is essential for integrated management of the development of estuarine resources, and the maintenance of the estuary's ecological health.

Channel deepening by dredging and sand mining is a common practice in the development and maintenance of navigable channels ~~and resource utilization~~ in estuaries. Generally speaking, channel deepening can increase the longitudinal

estuarine circulation by decreasing the bottom friction and increasing the baroclinic forcing which is proportional to the water depth (Amin, 1983; Chernetsky et al., 2010; Winterwerp, 2011). On the other hand, the increase in water depth can also increase the salt intrusion and decrease the horizontal density gradient, thus reducing the baroclinic force. Channel deepening also affects the estuarine circulation in other ways, such as increasing the Stokes transport and the associated compensating return flow (Amin, 1983), altering the nonlinear tidal rectification (Li and O'Donnell, 1997), and tidal asymmetry in mixing between flood and ebb tides (tidal straining) (Simpson, 1990). Therefore, the effect of channel deepening is an intricate balance between these reinforcing and/or competing effects. Chant et al. (2018) demonstrated that a relatively small (15%) increase in water depth can result in a double exchange flow. They attributed this increase to the increase in horizontal salinity gradient and/or a reduction in vertical mixing, but they did not give a clear distinction about how these two effects work together and which is dominant.

Change in estuary width is another aspect of topographic change in estuaries and is mainly caused by reclamation and utilization of salt marshes, construction of coastal protection structures along the estuarine banks. Change in estuary width generates a change in the estuarine convergence, and therefore a change in the estuarine circulation. Burchard et al. (2014) concluded that an increase in the estuarine convergence results in an enhancement or reduction of the longitudinal estuarine circulation as increased estuarine convergence can reduce or even reverse the straining-induced circulation, though the advection-induced circulation is increased. Changes in estuarine width can also modify the lateral circulation and feedback to the generation of the longitudinal estuarine circulation through the change in lateral advection (Lacy et al., 2003; Lerczak and Rockwell Geyer, 2004; Scully et al., 2009; Burchard et al., 2010; Burchard et al., 2014). Lerczak and Rockwell Geyer (2004) suggested that lateral effects on the longitudinal estuarine circulation would be stronger in narrower estuaries given a constant lateral salinity gradient. Schulz et al. (2015) investigated the impact of the depth-to-width ratio of the estuarine cross-section on the longitudinal estuarine

circulation and found that the longitudinal estuarine circulation exhibits a distinct maximum in medium-wide channels. They diagnosed the mechanisms for such a phenomenon and attributed it to the sensitivities of the straining- and advection-induced circulations on the changes in depth-to-width ratio.

As revealed by Lerczak and Geyer (2004) and other researchers (Chen et al., 2020b), lateral processes play important roles in the generation of the longitudinal estuarine circulation. ~~The lateral circulation can modify the longitudinal estuarine circulation by the lateral redistribution of the longitudinal current in a direct way (Lerczak and Geyer, 2004), and change the longitudinal pressure gradient force and the friction in an indirect way.~~ In estuaries, the pattern and intensity of lateral circulation are controlled by three processes (Li et al., 2014): vertical shear of the longitudinal current affecting the tilting of planetary vorticity, lateral salinity gradient (baroclinicity), and diffusion. The longitudinal estuarine circulation can affect the lateral circulation through all the mentioned three factors. Therefore, the interaction between the longitudinal and lateral processes is fully nonlinear and quite complex. Though these interactions have been discussed in detail (Scully et al., 2009; Li et al., 2017), several questions remain open: How does the longitudinal estuarine circulation affect the intensity and vortex structure of the lateral circulation? Does a decreased/increased lateral circulation necessarily lead to a weakened/strengthened longitudinal circulation? These questions become complicated in an estuary where both width and depth vary. Previous studies showed that the narrowing and deepening of the Yangtze River Estuary resulted in an enhanced longitudinal estuarine circulation (Zhu, 2018), which changed from transversely sheared to vertically sheared. The estuarine stratification was also found to be strengthened, along with an increase in the intensity of lateral circulation. Zhu et al. (2015) investigated the influences of channel deepening and widening on the tidal and nontidal circulations of Tampa Bay, USA, and found that the nontidal circulation was strengthened by these human interventions. However, how does the estuarine circulation respond to both narrowing and deepening/shallowing of the estuary? What happens when the narrowing rate is much larger or smaller than the

deepening rate in an estuary? Here the narrowing rate is the ratio of the difference of cross-section widths between two consecutive years divided by the width in the earlier year. Similarly, the deepening rate is the ratio of the difference of water depth in the cross-section between the two consecutive years divided by the earlier year's depth.

Here we try to address the above questions by studying the changes in the estuarine circulation ~~via using the historical topographic data obtained~~ from 1977 to 2010 in the Huangmaohai Estuary (HE)~~. The HE is~~, a microtidal estuary in the southwest of the Pearl River Delta (PRD), ~~and~~ which experienced different stages of topographic changes under human activities ~~from 1977 to 2010, which can be grouped into two scenarios~~: narrowing and deepening (1977-1994, and 2003-2010), and narrowing and shallowing (1994-2003). ~~These two scenarios of topographic changes caused different responses of the estuarine circulation, and t~~ Thus, it provided a good opportunity to study the effect of human activities induced morphological evolution on the estuarine circulation.

In this study, we used a state-of-the-art three-dimensional baroclinic model (Delft 3d) to simulate the changes in hydrodynamics in the HE in different years and examined the changes in intensities of the longitudinal and lateral estuarine circulations, followed by an analysis of the mechanisms for these changes by conducting diagnostic analyses of the momentum balance. The structure of the rest of the paper is as follows. Section 2 introduces the study area and numeral model ~~(including model setting and validation)~~. Section 3 presents the results of morphological evolution and changes in the estuarine circulation. Then, the mechanisms for the changes in estuarine circulation are investigated using the momentum and vortex balance equations in Section 4. Finally, the conclusions are presented in Section 5. ~~For the sake of conciseness, we append a supplement in the appendix about the model validation for water level, current, and salinity.~~

2. Study area and methodology

2.1 Study area

The HE is located in the west of the PRD in southern China and exhibits a distinctly convergent geometry, with a latitude ranging from 21°50′ to 22°13′ N and a longitude ranging from 113°00′ to 113°51′ E (Fig. 1). The estuary is composed of a bay (Huangmao Bay) and a tidal river. The bay is trumpet-shaped with an area of 409 km^2. It has a complex bathymetry comprising of two channels and three shoals, namely the West Channel and East Channel, the West Shoal, Middle Shoal, and East Shoal. In recent decades, the West Channel is observed to shrink and almost disappear now (Jia et al., 2012). The width of the bay is 30 km at the estuary mouth and decreases to 1.8 km at the head. The mean water depth of the bay is 4.5 m (Gong et al., 2014). The bay is connected to the upstream river catchment by two constrictions (Yamen and Hutiaomen Outlets). Several islands, namely Dajin Island, Hebao Island, and Gaolan Island, are scattered at the estuary's mouth~~. The estuary mouth is divided into three entrances: the West Entrance between the Dajin Island and the western shore; the Central Entrance between the Dajin Island and the Hebao Island, where the West Channel passes through; and the East Entrance between the Hebao Island and the Gaolan Island, where the East Channel goes through~~ (shown in Fig. 1b).

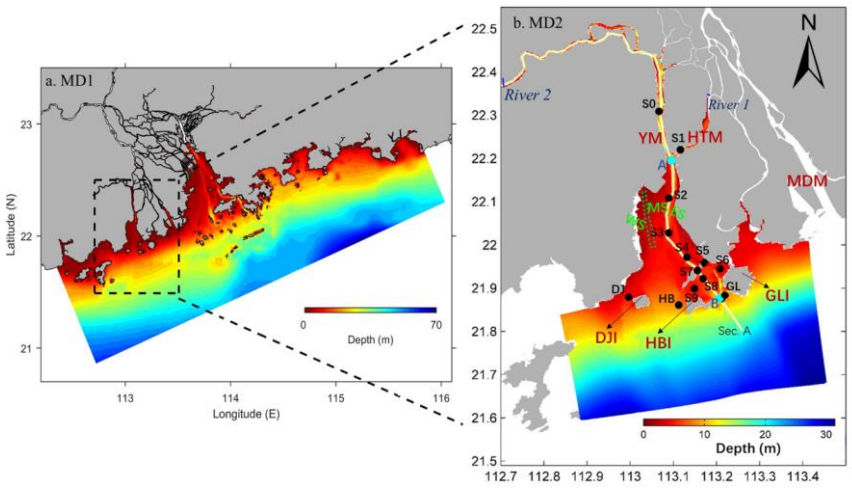


Fig. 1. The study area (Huangmaohai estuary) and observation stations. Major topographic features and domains of the nested modeling system over (a) the PRD and (b) the HE and its adjacent waters. YM = Yamen; HTM = Hutiaomen; MDM = Modaomen; DJI = Dajing Island; GLI = Gaolan Island; HBI = Hebao Island. The black dots (S0–S9, DJ, HB, and GL) in the MD2 domain are stations of field deployments in March 2010. The solid lines represent the along-channel transect (Section A (AB)), which lies in the East Channel. The green dotted lines represent the West Channel in 1977. Three shoals are shown in (b): West Shoal (WS), Middle Shoal (MS), and East Shoal (ES).

The HE has a subtropical monsoon climate, with the precipitation in the wet season (from May to September) being high. Approximately 80% of the river discharge occurs during the wet season, with an average discharge of 200.23 m^3/s. The tides in the HE are mixed semidiurnal with dominant semi-diurnal constituents and smaller diurnal constituents. ~~The tides show obvious asymmetry in terms of tidal duration, velocity, and current acceleration between floods and ebbs (Gong et al., 2016).~~ The tidal range is approximately 1.5 m at the mouth and experiences an initial increase from the mouth towards the head owing to a strong convergence of the bay width. Further landward in the tidal river beyond the bay head, the tidal range decreases by the overwhelming bottom friction (Gong et al., 2012). The tidal current velocity ranges from 0.5 m/s to 1.5 m/s (Huang, 2011), and is higher in deep channels than on shallow shoals. The tidal

currents are generally rectilinear in deep channels but become more rotary in shallow shoals.

Since the 1980s, human activities have been intense in the HE ~~estuary~~. A hydroelectric power project upstream of the estuary, channel dredging, sand mining, and construction of Gaolan Island levees have led to great changes in the HE's topography. Also, the HE has rich tidal flat resources and endured frequent reclamation activities. From 1965 to 2003, a total of 142.29 km^2 tidal flat was reclaimed, with an average reclamation rate of 3.74 km^2/a, and the reclamation rate continuously but gradually increased during that period. After 2003, the reclamation rate slowed down. In terms of channel dredging, the Yamen Waterway Project was conducted in 1997 to deepen the channel between S0 and S3 in Fig. 1b (Luo, 2010). In April 2005, the Yamen Channel regulation project was implemented to alleviate the serious siltation in the channel, with the channel being dredged to a depth of about 6 m.

In the following, we chose 1977, 1994, 2003, and 2010 as the representative years to study the typical scenarios of bathymetric changes in the HE.

2.2 Remote sensing and topographic data

Remote sensing data were used for coastline extraction and included Landsat Multi-Spectral Scanner (MSS) data, Landsat Thematic Mapper (TM) data, and Landsat Operational Land Imager (OLI) data. A total of ~~142G data of~~ 66 images (Table 1) ~~covering the PRD during cloudless days in multiple years (from 1973 to 2018)~~ were downloaded from http://www.gscloud.cn/. These data were firstly processed by geometric (with ~~the~~ errors ~~were shown to be~~ less than 0.5 pixels (Ai et al., 2019)) and atmospheric corrections by the ENVI 5.3 software. ~~Subsequently, they were compared with topographic data for further geometric corrections. The errors were shown to be less than 0.5 pixels (Ai et al., 2019).~~ The topography data inside the HE were derived from nautical charts (1977, 1994, 2003, and 2010), published by the Navigation Safety Guarantee Bureau. The filling and excavation toolbox of ArcGIS was used to calculate

the difference between the volumes in two consecutive periods by superimposing the corresponding Digital Elevation Models (DEM). ~~This method is actually to decompose three-dimensional space entities into many cuboids, then calculate the differences of area and volume of each cuboid between two consecutive years, and classify the cuboids into different categories based on the siltation thickness.~~ We thus obtained the average siltation rates of the study area over different years (Figs. 2a-c).

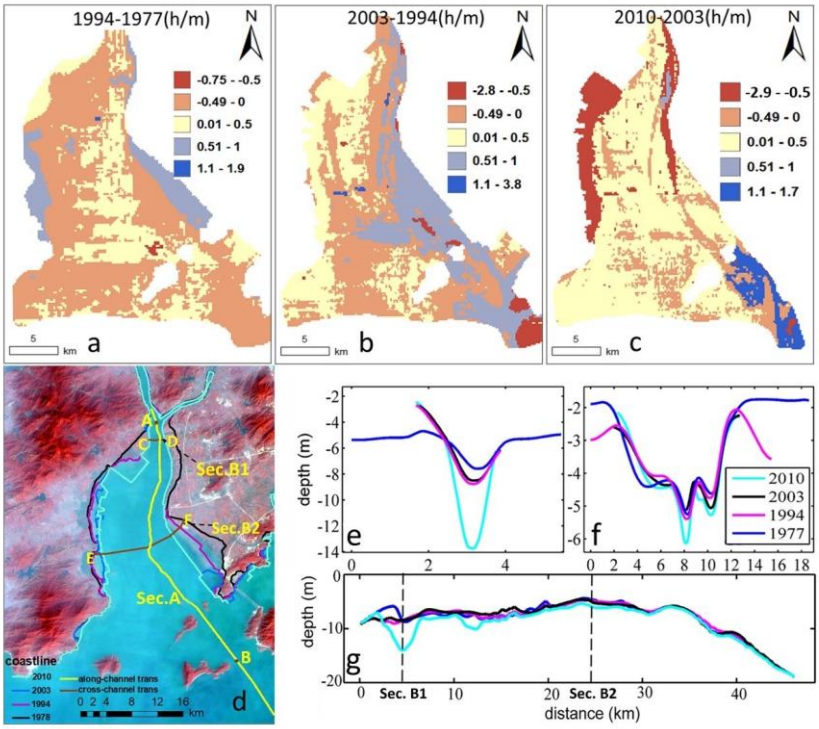


Fig. 2. (a-c) Water depth difference between two consecutive years ((a)1994-1977; (b)2003-1994; (c)2010-2003), where the positive value indicates "deepening" and the negative one indicates "siltation", (d) Shorelines of 1977-2010 and locations of two cross-sections (AB: Sec. A; CD: Sec. B1; EF: Sec. B2); (e, f, and g) The bathymetric evolutions at Sections B1, B2, and A in 1977, 1994, 2003, and 2010.

Table 1. Data of remote sensing images

Time	Satellite	Image sensor	Resolution/m	Path/Row	Memory space
1973,1978	Landsat3	MSS	78	122/45	142G
1986-2011	Landsat5	TM	30		
2012	Landsat7	ETM	30		
2013-2018	Landsat8	OLR	30		

2.3 Numerical model setting up and validation

The numerical model Delft3d, a fully three-dimensional hydrodynamic water quality model (Lesser et al., 2004), was used to simulate the hydrodynamics in the HE. ~~The Delft3d model is a fully three-dimensional hydrodynamic water quality model, and can accurately simulate large-scale flow, water quality, and morphological evolution (Lesser et al., 2004).~~ ~~The~~ Its algorithm ~~of the Delft3d model~~ can guarantee the conservation of mass, momentum, and energy. The model grid consisted of a nesting grid system, with the MD1 (parent model, Fig. 1a) covering the whole PRD, and the MD2 (child model) covering the HE. For the MD2 model, a curvilinear orthogonal grid ~~an orthogonal Cartesian horizontal grid~~ of 269*620 was established, with the horizontal resolution ranging from 85 m in the channel to 324 m at the ocean boundary. Vertically, the grid was discretized into 10 layers of σ coordinate. The model system used here is the same as the one in Chen et al. (2020a). Briefly, the open boundary conditions of the MD1 model included atmospheric forcing at the water surface, river discharge at the upstream boundary, tidal and non-tidal water elevations and currents, a constant salinity of 34 psu at the open ocean boundary. The results from the MD1 were interpolated to provide ocean boundary conditions for the MD2 model.

As mentioned above, the hydrodynamics in the HE experiences distinct seasonal variation. The estuarine circulation during the wet season has been extensively studied before (Chen et al., 2020a; Chen et al., 2020b). Here we choose the dry season to investigate the changes in the estuarine circulation caused by topographic changes in

different years. We conducted a series of numerical experiments using the bathymetry data in 1977, 1994, 2003, and 2010. The simulation time was chosen to be from 00:00 on March 1 to 23:00 on March 31 in the dry season, when observation data were available in 2010. Field measurements were carried out at 14 mooring stations on March 17th 17:00 to 18th 22:00, 2010. The measured variables included vertical profiles of current, temperature, and salinity. ~~In these surveys, ADCP was utilized to measure the vertical profile of current with a vertical resolution of 0.3 m and a time resolution of 5 min, and CTD was used to measure the vertical profiles of salinity and temperature every hour. Hourly data were obtained after post-processing of the raw data and used for model validation here.~~ In all the four scenarios, two upstream boundaries were specified (Fig. 1b): at River 2 by specifying real-time water level data from the MD1 model from 00:00 on March 1, 2010, to 23:00 on March 31, 2010, with a time interval of 1 hour; At River 1 by specifying a constant river discharge of 100 ms^{-2}. The choice of this constant value was based on ~~the~~ previous simulation experiences (Chen et al., 2020a; Chen et al., 2020b). The salinities at the river inflow boundaries were set to be 0 psu. The only changing condition of the four scenarios was the topography (Table 2), so the effect of topographic change can be ~~identified~~ distinguished. The measured data from 14 stations in 2010 were used to validate the model. ~~The validation included water level, current direction and magnitude, and salinity (Figs. A. 1-4).~~

Table 2. Coastline, bathymetries, salinity, flow, and tidal boundary in the four model scenarios.

Scenario	Coastline	Bathymetries	The salinity of the open sea	Flow	Tidal boundary
1977/03	1977	1977	2010/03	2010/03	2010/03
1994/03	1994	1994	2010/03	2010/03	2010/03
2003/03	2003	2003	2010/03	2010/03	2010/03
2010/03	2010	2010	2010/03	2010/03	2010/03

In this study, the Willmott skill score (SK) was used to evaluate whether the model result is consistent with the observed data (Willmott, 1981). The SK is defined as:

$$SK = 1 - \frac{\sum_{i=1}^{n}(O_i - M_i)^2}{\sum_{i=1}^{n}(|M_i - \bar{O}| + |O_i - \bar{O}|)^2}, \quad (1)$$

where n is the number of the observed data, M and O are model simulation results and observations, respectively, and $\bar{o}$ is the average value of the observation data. SK is used to measure the consistency between the model results and the observations, with a value between 0 and 1. The larger the value is, the more consistent the simulation results are with the observed data.

Firstly, the water level of the MD2 model was validated ~~(Fig. A. 1)~~. The SKs of the four observed stations are all above 0.86, indicating that the water level simulation is reasonable. Secondly, the modeled current directions showed good performance except for the surface layer at Stations DJ and S0 ~~(Fig. A. 2)~~, almost all the SKs are greater than 0.7 (Table 3). The simulation of current speed ~~(Fig. A. 3)~~ is worse than that of the current direction, but the SKs at most stations are above 0.6, showing a good performance. ~~We note that the SK (less than 0.4) at Station S3 is significantly lower than other stations, mostly because the station was located near the null point (the convergence point between seaward and landward bottom residual flows) and the current speed was quite small.~~ Lastly, the trends of observed and simulated salinities are consistent ~~(Fig. A. 4)~~, and almost all the SKs of salinity validation are above 0.5, especially in S1-S3, showing a good performance of the salinity simulation.

Table 3. Skill scores by comparison of modeled results with observations.

Stations	Current direction			Current speed			Salinity		
	Sur	Mid	Bot	Sur	Mid	Bot	Sur	Mid	Bot
S0	0.18	0.96	0.96	0.77	0.88	0.86	0.32	0.35	0.35
S1	0.94	0.99	0.99	0.65	0.66	0.61	0.94	0.94	0.90
S2	0.78	0.79	0.71	0.83	0.84	0.84	0.84	0.85	0.85
S3	0.87	0.98	0.95	0.34	0.38	0.39	0.92	0.79	0.77
S4	0.84	0.94	0.94	0.53	0.55	0.53	0.77	0.64	0.54
S5	0.86	0.92	0.93	0.66	0.71	0.72	0.37	0.25	0.26
S6	0.79	0.90	0.88	0.68	0.75	0.74	0.15	0.20	0.25
S7	0.82	0.85	0.96	0.74	0.79	0.83	0.86	0.66	0.56
S8	0.84	0.89	0.89	0.59	0.62	0.66	0.82	0.77	0.72
S9	0.80	0.74	0.77	0.54	0.46	0.41	0.59	0.50	0.52
DJ	0.61	0.77	0.77	0.38	0.47	0.51	0.66	0.47	0.37

GL	0.89	0.91	0.93	0.50	0.51	0.49	0.37	0.43	0.41
HB	0.71	0.89	0.89	0.60	0.56	0.56	0.57	0.54	0.53

As a whole, the simulation of surface currents is worse than that in other layers, since winds and waves were not included in our MD2 model simulations, in which the surface flow is more susceptible to these forcings. The specified river flow at River 2 was constant, which may deviate from the real-time data (not available), leading to a poor salinity reproduction at upstream stations. In short, the water level and current are well-validated. The simulation of salinity is generally good, except for some deviations at upstream stations. It shows that the model can reasonably simulate the hydrodynamic processes in the area, and can be used for the following hydrodynamics study in the HE.

3. Results

3.1 Morphological evolution

Morphological changes between 1977, 1994, 2003, and 2010 are shown in Figs. 2a-c. ~~According to the pattern of erosion and siltation in the two consecutive years,~~ Figure 2a shows that most areas in the HE experienced siltation from 1977 to 1994~~., The~~ but the East Channel was deepened by about 0-0.5 m. In the middle of the bay, the nearshore areas were under erosion, and the erosion thickness at the eastern shore was twice that at the western shore. In other areas, the siltation thickness was between 0 and 0.5 m. From 1994 to 2003, erosion occurred in the West Shoal, East Channel, East Shoal, and Middle Shoal. Siltation of 0.01-0.5 m happened in the rest of the area, which accounted for most of the HE, so the HE became shallower in 2003. In 2003, siltation in the East Channel was serious and the water depth there became only 2m (Li, 2019). From 2003 to 2010, the West Shoal became significantly shallower with a siltation thickness of about 0.5-1m. The East Shoal almost disappeared, and its relict area endured siltation of 1.1-1.7 m, which was mainly due to the construction of coastal

protection works. Strong erosion occurred in other areas, especially in the upper bay with a deepening of more than 4m, and the overall water depth of the HE became greater in 2010. ~~Relevant research shows that the East Channel had been under erosion from 2005 on and the largest water depth reached 7.4 m in 2006 (Luo, 2010).~~

~~We further take the morphological change of the East Channel as an example. The East Channel experienced continuous erosion before 1977. From 1977 to 2003, the channel was under siltation, particularly at the river mouth bar (between the upper bay and the entrances, see Gong et al. (2014), whereas at the upper bay (from the head to the null point of the East Channel, here the null point means the convergence point at which the upstream seaward flow meets the downstream landward bottom flow) and at the inter-island sections, the channel was under erosion. In 2003, siltation in the East Channel was serious and the water depth there became only 2m (Li, 2019). From 2005 on, the East Channel had been under erosion and the largest water depth reached 7.4 m in 2006 (Luo, 2010).~~

Overall, the water depth of the HE changed considerably from 1977 to 2010. It first experienced erosion, then underwent siltation, and followed by erosion again.

Figure 2d shows the changes of coastlines for the four representative years. To calculate the rate of geometry convergence, the DSAS tool (Version 5.0) in Arcmap 10.3 was used to calculate the end-point rates for cross-shore transects. A more detailed procedure is in Zhang et al. (2019). We chose one longitudinal section along the channel in the estuary and two cross-sections (in Fig. 2d) along the channel for analysis. The longitudinal section (Sec. A) extends from the bay head (point A in Fig. 1b) to the estuary mouth (point B in Fig. 1b), spanning a distance of 50 km. Sec. B1 is located at about 4 km downstream from the bayhead, where the water depth changes sharply in the lateral (or longitudinal) direction (see Fig. 2e). Sec. B2 is approximately 24km downstream from the bayhead and near the null point in the middle of the estuary (see Fig. 2f), and the width of the estuary varied dramatically here (see Fig. 2e). At Sec. A, the water depth near the point of Sec. B1 endured a great change in 2010 due to channel dredging (Fig. 2g). In other periods, the water depth along its course endured gradual

deepening. At Sec. B1, the bathymetric change is featured by an increase in water depth and negligible change in width over time. At Sec. B2, both the water depth and width experienced changes from 1977 to 2010, with the depth increased and width decreased (Fig. 2f). The above three sections clearly depict the topographic changes of the estuary in different years.

3.2 C~~c~~hanges in the vertically averaged flow and salinity

Here we present the changes in the tidally and vertically averaged flow and salinity during neap tides ~~in different years~~ in Fig. 3. In 1977 (Fig. 3a), the current speed was generally small, except at the inter-island sections and in the channel. The vertically averaged flow was seaward in the upper bay and the right part of the lower bay (looking landward). It became landward at the left part of the lower bay. ~~The 10 psu isohaline intruded into the upper bay at a latitude of 22.1 to 22.15°N.~~ In 1994 (Fig. 3b), the current speed was increased in the channel, particularly near Sec.B1. The overall flow pattern was almost similar to that in 1977. ~~The salt intrusion was increased, as the 10 psu isohaline intruded to a latitude of 22.15°N.~~ In 2003 (Fig. 3c), the flow pattern still kept unchanged when compared to that in previous ~~periods~~yeas. The current speed was decreased relative to that in 1994. ~~However, the salt intrusion became aggravated as the 10 psu isohaline had reached the bayhead at the Yamen Outlet.~~ In 2010 (Fig. 3d), the seaward flow became more dominant in the upper bay, and more biased southwestward. The seaward flow in the channel was greater than in 2003. The 10 psu isohaline kept moving upstream over time, ~~The salt intrusion was more serious than in 2003, as~~ and ~~the 10 psu isohaline~~ reached beyond the bayhead and entered into the tidal river of the estuary in 2010.

Overall, we observed that the tidally and vertically averaged flow during neap tides experienced an increase-decrease-increase by the topographic changes, whereas the saltwater consistently intruded ~~further into the estuary~~more landward.

As a supplement, we present the horizontal distributions of tidally averaged surface and bottom circulation and salinity during neap tides for different years in the appendix (Figs. A. ~~5~~ 1 and ~~6~~ 2). Over the study period, the enhancement of salt intrusion was stronger for the bottom layer and weaker for the surface layer, whereas the increase in residual flow was stronger in the surface layer and weaker in the bottom layer.

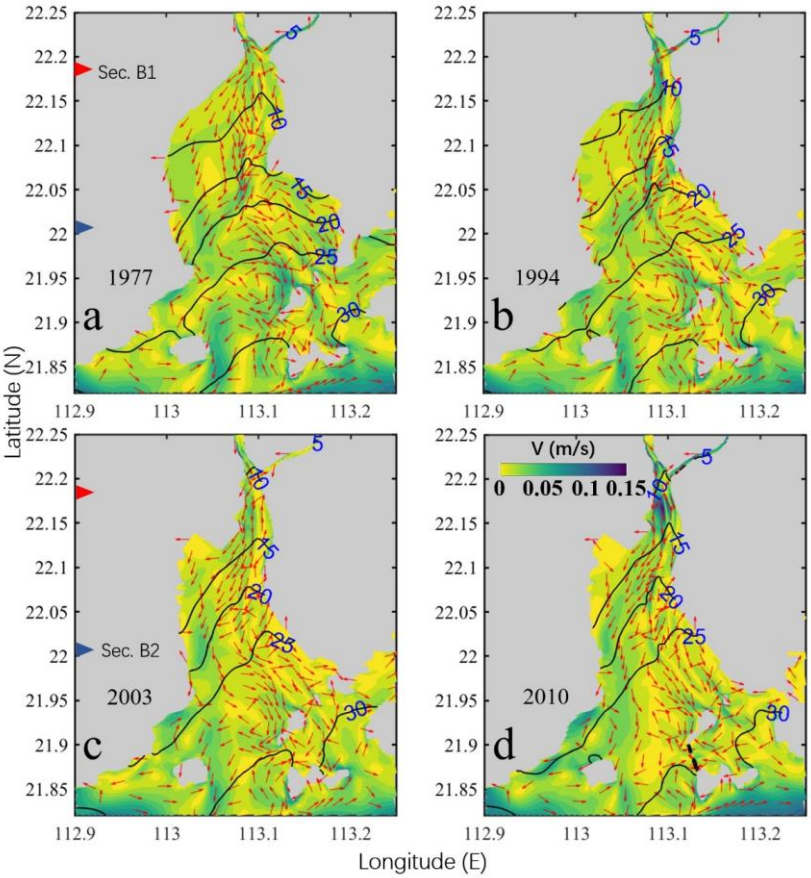


Fig. 3. Patterns of the vertical-averaged horizontal circulation during neap tide in 1977(a1), 1994(a2), 2003(a3), and 2004(a4). The magnitude of the current is represented by the color shading, while the current direction is shown by the arrows. The salinity is depicted by the contour lines. The red and blue triangles depict the positions of two cross-sections (Sec.B1 and Sec.B2).

3.3 Changes in the estuarine circulation

Figures 4 a-d ~~present the longitudinal estuarine circulation and the distributions of salinity isolines during the neap tide in the longitudinal section (Sec. A in Fig. 1b) in different years. The results~~ show that the upper part of the estuary (upstream of the null point) was highly stratified, and the lower part of the estuary (downstream of the null point) was well mixed. The classical exchange flow structure ~~of "a landward residual flow near the bottom and a seaward residual flow near the surface"~~ was more distinct upstream of the null point. Over time, the surface seaward flow became stronger and more concentrated with the narrowing of the estuary, particularly in 2010. It extended more downstream to near the estuary mouth with the narrowing of the estuary, as evidenced by the extent of the seaward flow of 0.2 m/s. Concomitantly, the bottom landward flow was strengthened and concentrated with the increase in depth. It should be noted that the greatly enhanced estuarine circulation between 3 to 8 km in 2010 (Fig. 4d) could be induced by the intratidal fluctuation of the halocline in response to the large topography change there(Geyer and Nepf, 1996; Chen et al., 2012; Wang et al., 2015)

We also present the changes in the surface and bottom current horizontally. Figs. 4e1-g1 show that when the estuary deepened (1977-1994 and 2003-2010), the surface current ~~speed~~ velocity increased in the channel, and when the estuary shoaled (1994-2003), the surface current velocity in the channel decreased. The changes in the bottom current showed a similar trend (Figs. 4e2-g2), except at the upper part of the channel from 1977 to 1994, in which the width was considerably ~~narrowed~~ decreased.

Along with the change in the longitudinal estuarine circulation, the salt intrusion at Sec. A did not change significantly from 1977 to 1994, but increased from 2003 on, particularly in 2010, when the isohaline of 15 psu reached Sec.B1, whose salinities were less than 12 psu in previous years (Figs. 4a-d). The salt intrusions at the surface and bottom gradually increased with the estuary narrowing (Figs. 4e1-g2).

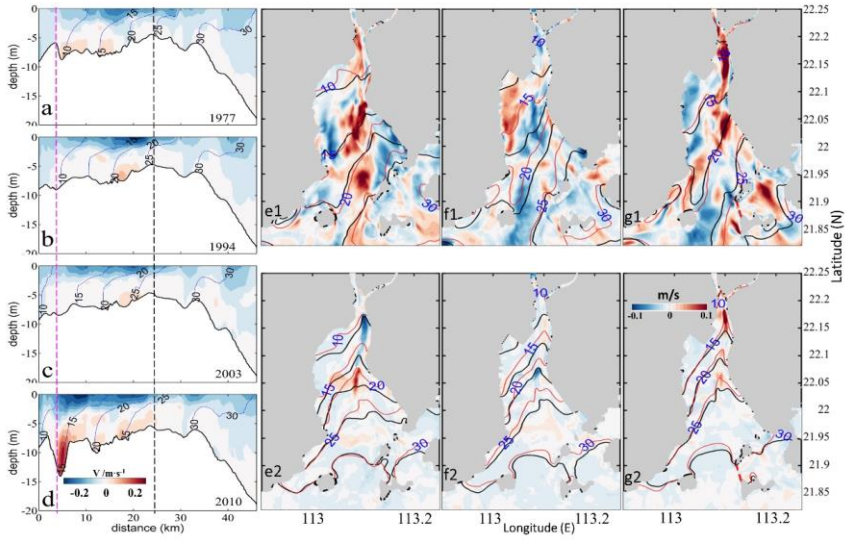


Fig. 4. The patterns of the estuarine circulation during the neap tide in March 1977(a), 1994(b), 2003(c), and 2010(d). The thin lines are the isolines of salinity in a-d. The pink and black dotted lines represent the locations of Secs. B1 and B2, respectively. The starting point of the X-axis is Point A in Fig. 1b. Surface current differences from 1977 to 1994(e1), from 1994 to 2003(f1), and from 2003 to 2010(g1); Bottom current differences from 1977 to 1994(e2), from 1994 to 2003(f2), and from 2003 to 2010(g2). The red and black lines represent the isolines of salinity in the later year and the earlier year.

To analyze the changes of lateral circulation in the estuary, we show the structure and intensity of the lateral circulation at the two cross-sections (Figs. 5 and 6).

At Sec. B1 (Fig. 5), with the increase of water depth, the salinity difference between the surface and bottom increased, along with an increase in the bottom salinity~~, which is more than 14 psu in 2010~~. For the lateral circulation, there was no distinct gyre structure in 1977~~, but a pair of opposite vortices started to develop at the position of 3.5km~~. In 1994, the lateral flow was dominated by an eastward flow. In 2003, a clockwise vortex was developed over the West Shoal (0.5-1 km). Meanwhile, an anticlockwise circulation with smaller vortex intensity was developed in the region of 1-2km from the western shore. Another clockwise circulation was developed over the East Shoal. When the estuary became deepened in 2010, the distribution of the lateral

circulation was similar to that in 1977, but the vortex intensity increased significantly to about 2-4 times that of 1977.

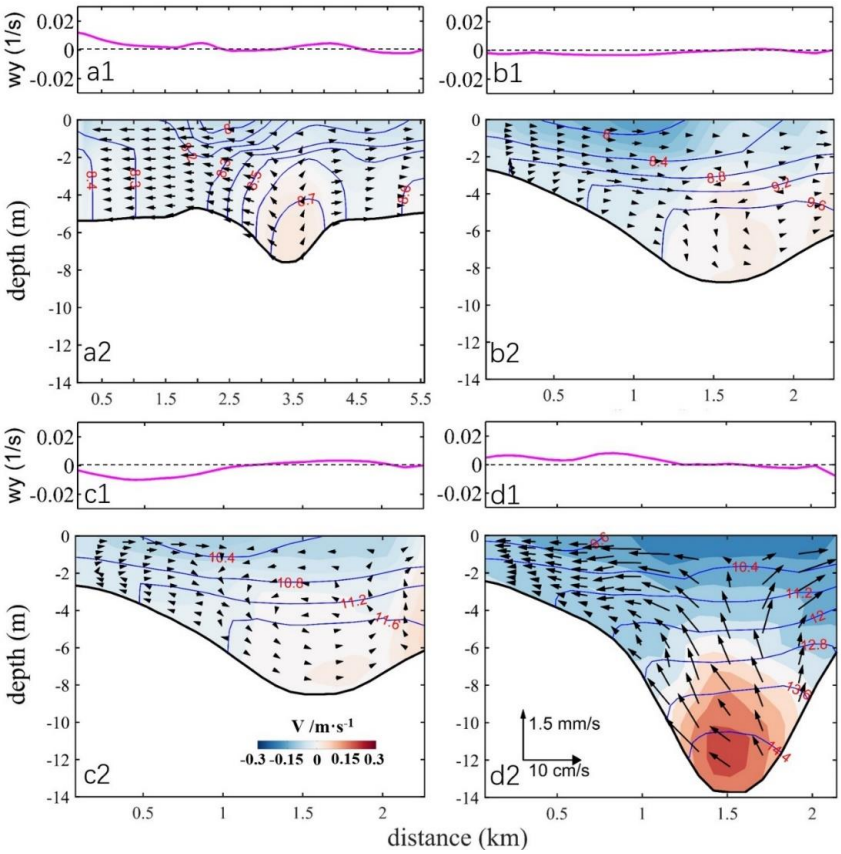
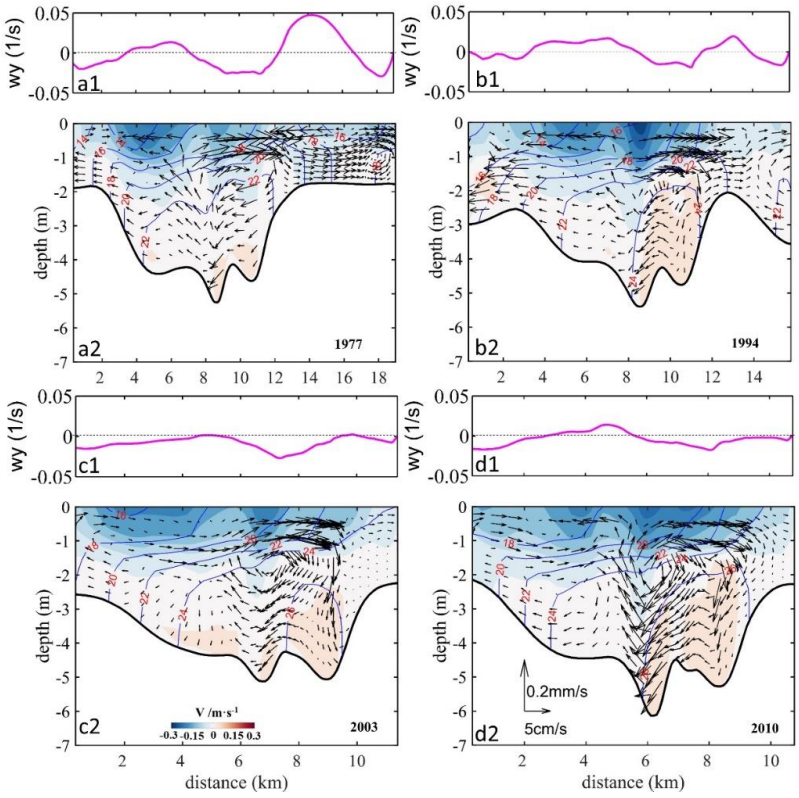


Fig. 5. The lateral circulation and isohalines (blue lines) at Sec. B1 in 1977(a2), 1994(b2), 2003(c2), and 2010(d2). The starting point of the X-axis is Point C in Fig. 2d. w_y is the longitudinal vorticity at Sec. B1 in 1977(a1), 1994(a2), 2003(a3), and 2010(a4).

Figure 6 shows the changes in lateral circulation at Sec. B2. With the decrease of estuary width, the salinity increased in the cross-section over the years. There developed a clockwise circulation at the right of the deep channel in 1977 and 1994. This clockwise vortex was seen to move westward from 2003 on. The spatial extent of the clockwise circulation in the deep channel increased significantly over time. Clockwise vortices developed over the East Shore from 1977 to 2010, but their intensity

455 became weaker since 2003. In 1977 and 1994, the distance between the deep channel
456 and the East Shore was greater than 2 km ~~that~~ which was sufficient ~~enough~~ for
457 accommodating ~~developing~~ clockwise vortices~~, and the accommodation space was~~
458 ~~enough for the clockwise vortices to develop sufficiently~~. From 2003 on, the
459 accommodation space at the East Shore became limited and restricted the full
460 development of the clockwise vortex. Over the West Shoal, the lateral circulation
461 pattern showed an anticlockwise circulation in 1977 and 1994. However, since 2003,
462 the lateral circulation over the West Shoal began to develop a two-cell pattern, with an
463 anticlockwise gyre at the surface and a clockwise one near the bottom. The clockwise
464 cell developed well in 2010.



465
466 Fig. 6. The distribution of lateral circulation and isohalines (blue lines) at Sec.B2 in 1977(a2),
467 1994(b2), 2003(c2), and 2010(d2). The starting point of the X-axis is Point E in Fig. 2d. w_y
468 is the longitudinal vorticity at Sec. B2 in 1977(a1), 1994(a2), 2003(a3), and 2010(a4).

As a whole, over the study period, the longitudinal estuarine circulation continued to increase, whereas the lateral circulation experienced varying changes at different cross-sections. At the upstream cross-section (B1), when the estuary narrowed, the original pattern of two-cell vortices with opposite polarity was disrupted. However, it was amplified in 2010 when the water depth was increased. At the cross-section in the middle of the estuary (B2), a similar two-cell pattern was developed. However, in 2003 and 2010, the single cell at the West Shoal was split into two cells: an anticlockwise cell at the surface and a clockwise cell at the lower part.

3.4 Relationship between the cChanges in the intensity of estuarine circulation and the changes in topography

To further quantitatively identify the influence of topographic changes on the estuarine circulation, we calculated the changes in the intensity of estuarine circulations in the longitudinal and lateral directions. The magnitude of estuarine circulation in the longitudinal section was used to represent the intensity of the longitudinal estuarine circulation (Chen and Sanford, 2009). The method was to subtract the subtidal longitudinal velocity of the bottom layer from that on the surface layer. The magnitude of the vorticity in the cross-sections was used to represent the intensity of the lateral circulation (Becherer et al. 2015), and is expressed as:

$$w_y = \partial w/\partial x - \partial u/\partial z \quad (2)$$

where, w_y is the longitudinal vorticity in the cross-sections. w and u are the currents in the vertical and lateral directions, respectively. $\partial w/\partial x$ is much smaller and can be ignored, therefore, the formula (2) for calculating the intensity of lateral circulation can be simplified as:

$$w_y = -\partial u/\partial z \quad (3)$$

when w_y is positive, the lateral circulation is an anticlockwise vortex, conversely, when w_y is negative, the lateral circulation is a clockwise vortex.

The results of the averaged intensity of estuarine circulation along Sec.A ~~the longitudinal section~~ and the averaged intensity of vorticity at the cross-sections are listed in Table 4.

Table 4. The changes of width and depth (the maximum depth), area (cross-section area), w-to-d, narrowing rate, deepening rate, and the intensity of circulations (w-to-d: width-to-depth ratio; narrowing rate: the ratio of the difference of cross-section widths between two years divided by the width in the earlier year; deepening rate: the ratio of the difference of water depth in the cross-section between the corresponding two years divided by the earlier depth. The positive narrowing rate indicates that the estuary is narrowed; the positive deepening rate indicates that the estuary is deepened.)

		time	1977/03	1994/03	2003/03	2010/03
Sec.B1	width (km)		5.56	2.25	2.26	2.14
	depth (m)		7.58	8.76	8.50	13.73
	w-to-d		734	257	266	156
	area (km^2)		0.0468	0.0213	0.0207	0.0256
	narrowing rate		\	59.50%	-0.44%	5.30%
	deepening rate		\	15.58%	-2.95%	61.47%
Sec.B2	width (km)		18.97	15.77	11.40	10.76
	depth (m)		5.25	5.40	5.12	6.13
	w-to-d		3610	2920	2230	1760
	area (km^2)		0.0849	0.303	0.0647	0.0646
	narrowing rate		\	16.87%	27.71%	5.61%
	deepening rate		\	2.86%	-5.19%	19.73%
circulation intensity	longitudinal	Sec. A	0.0274	0.0428	0.0483	0.0594
	lateral	Sec. B1	0.0111	0.0146	0.0130	0.0278
		Sec. B2	0.0493	0.0460	0.0465	0.0425

Table 4 indicates that the longitudinal estuarine circulation intensity increased with the estuary narrowing, and reached the largest in 2010, which was 0.0594 m/s.

The lateral circulation intensity varied in different cross-sections. For Sec.B1, it increased gradually when the estuary deepened (from 1994 to 2010). When the deepening rate reached the maximum (61.47%) in 2010, the lateral circulation intensity reached the maximum as well. The intensity of lateral circulation increased when the estuary deepened and narrowed (from 1977 to 1994, and from 2003 to 2010), but it decreased when the estuary shallowed and narrowed (from 1994 to 2003). For Sec.B2,

the intensity of lateral circulation decreased when the estuary deepened and narrowed (from 1977 to 1994, and from 2003 to 2010). However, this trend was altered when the estuary entered into the "narrowing and shallowing period", with the deepening rate being -5.19%. ~~The lateral circulation intensity increased in 2003. The change in the lateral circulation intensity~~ It indicates that changes in water depth were the dominant factors affecting the lateral circulation intensity.

In general, the relationship between the longitudinal estuarine circulation intensity and the estuary width showed a monotonic decrease, while that between the longitudinal estuarine circulation intensity and the water depth is a monotonic increase, but the lateral circulation intensity seemed to have no simple linear relationship with the topographic change~~, including changes in the estuary width, water depth, and cross-section area.~~

4. Discussion

4.1 Contribution of momentum terms to the variation of the longitudinal estuarine circulation

To explain the change in the longitudinal estuarine circulation intensity, we conducted a diagnostic study by examining the changes in terms of the momentum balance equations. We calculated each term of the momentum equation in the longitudinal direction in the tidally averaged timescale:

$$\underbrace{\frac{\partial v}{\partial t}}_{local\ acceleration} = \underbrace{fu}_{coriolis} \underbrace{-g\frac{\partial \eta}{\partial y}}_{barotropic\ presssure} \underbrace{-\frac{gz}{\rho_0}\frac{\partial \rho}{\partial y}}_{baroclinic\ pressure} \underbrace{-\left(u\frac{\partial v}{\partial x}+v\frac{\partial v}{\partial y}+w\frac{\partial v}{\partial z}\right)}_{advection} \underbrace{+\frac{\partial}{\partial z}\left(A_v\frac{\partial v}{\partial z}\right)}_{vertical\ friction}, \quad (4)$$

By comparing the changes in each term and linking them with the characteristics of morphological evolution, we ~~try~~ effort to explain the response of the longitudinal estuarine circulation to bathymetric change in the perspective of momentum balance. Though the change in an individual momentum term in Eq. 4 can not represent the change in the longitudinal estuarine circulation as a whole, it can reflect the change in the corresponding component for the estuarine circulation (Cheng, 2013). For example,

548 an increase or decrease in the baroclinic pressure gradient force can reflect the change
549 in the gravitational circulation, and the change in the advection term is representative
550 of the change in tidal rectification. In the following, we present ~~both~~ the vertically
551 averaged ~~and depth-dependent~~ values for these different terms along the longitudinal
552 section in different years. It should be noted that the friction term consists of a
553 component of the tidally mean eddy viscosity multiplied by the tidally mean vertical
554 current shear, and a component of the correlation between eddy viscosity and vertical
555 current shear, which is referred to as the tidal straining (Simpson et al., 1990).
556 Figure 7 shows that during the neap tide, the baroclinic pressure gradient force
557 was balanced by barotropic gradient force, friction, and advection term in each year.
558 This is different from the classic estuarine momentum balance (Pritchard, 1956) but
559 consistent with the recent understanding of estuarine physics (Geyer and MacCready,
560 2014). The Coriolis force is quite small as both the latitude of the HE and the residual
561 current are small. The high value of the baroclinic term was observed to shift upstream
562 over time. As the baroclinic term is the multiplication of the salinity gradient and water
563 depth, the changes in this term over years can be induced by the change in water depth
564 and/or the salinity gradient. It can be seen from Fig. 4 that in the north of the null point,
565 the salt intrusion gradually moved towards the bayhead with the estuary narrowing,
566 thus increasing the salinity gradient there. In the meantime, the upstream water depth
567 was increased due to channel dredging, particularly in 2010. Therefore, the increase of
568 the baroclinic force term was caused by both the increases in water depth and salinity
569 gradient. Although the barotropic term contributed a lot to the momentum balance, it
570 did not change obviously with the morphological evolution. The advection term at the
571 upstream section (B1) increased slightly with the estuary narrowing, especially in the
572 deepening part of the channel in 2010. The friction term at the upstream section (B1)
573 was the largest in 2010, because the salt intrusion increased the vertical shear of the
574 longitudinal current there. Nevertheless, the increase in friction term was much smaller
575 than that of the baroclinic term. Chant et al. (2018) attributed the increase in exchange
576 flow to the increase in horizontal salinity gradient and/or a reduction in vertical mixing

by deepening, but in our case, the increase in baroclinic term was dominant and the change in vertical mixing even posed a reversed effect.

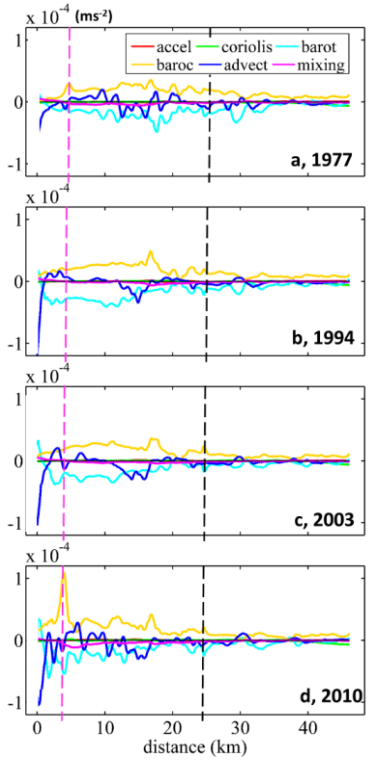


Fig. 7. Patterns of the longitudinal momentum terms during neap tide at Sec. A in 1977(a), 1994(b), 2003(c), and 2010(d). The starting point of the X-axis is Point A in Fig. 1b. "accel" in legend: local acceleration term; "barot" in legend: the barotropic gradient force term; "baroc" in legend: the baroclinic gradient force.

~~In Fig.8, we present the distribution of each momentum term in the longitudinal section and its change with the morphological evolution. Among them, the distribution patterns in 1994 and 2003 were very similar. The area of maximum bottom landward pressure gradient force was shifted to the upper bay. The magnitudes of the bottom pressure gradient force in 1994 and 2003 were greater than that in 1977, but less than that in 2010. The advection term alternated between positive and negative along Sec. A, and was increased in the upper part of Sec. A in 2010. The friction term generally~~

shows a pattern of positive in the upper part and negative in the lower part of the water column, opposite to the estuarine circulation. In the region where the seaward flow was dominant in the whole water column (around 30 km), the friction was positive near the bottom. It can be seen that near Sec. B1, the friction at the bottom increased in 2010, showing an increase in the bottom landward flow.

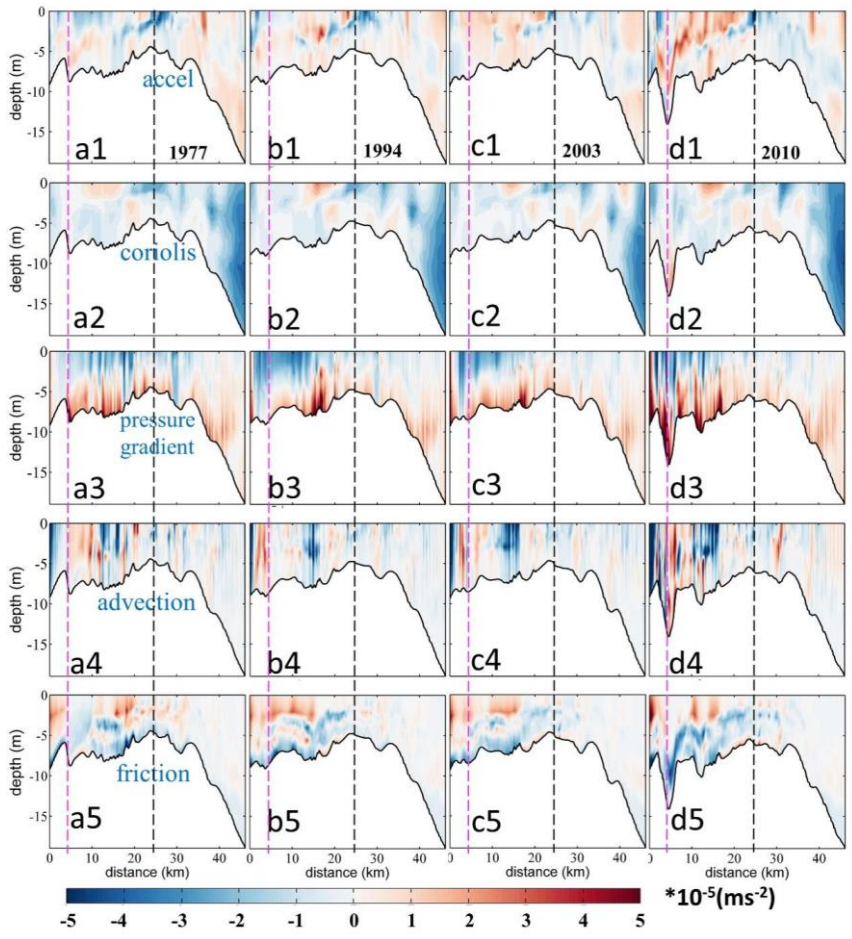


Fig. 8. Patterns of the longitudinal momentum terms during neap tide at Sec. A. (a1-d1): The local acceleration term. (a2-d2): The Coriolis term. (a3-d3): The pressure gradient force term. (a4-d4): The advection term. (a5-d5): The friction (vertical mixing term). 1977, 1994, 2003, and 2010 cases are in the first, second, third, and fourth columns, respectively. The pink and black dotted lines represent the location of Sec.B1 and Sec.B2, respectively. The starting point

~~of the X-axis is Point A in Fig. 1b. For viewing purposes, the acceleration term is multiplied by 10.~~

To further identify the changes in different terms, the advection term was divided into lateral (X-direction), longitudinal (Y-direction), and vertical (Z-direction) advection terms (Fig. ~~9~~8). ~~The~~ It is worth noting that the sum of the advection terms in X and Z directions represents the effect of the lateral circulation. ~~The lateral and longitudinal advection terms are collectively referred to as the horizontal advection term.~~

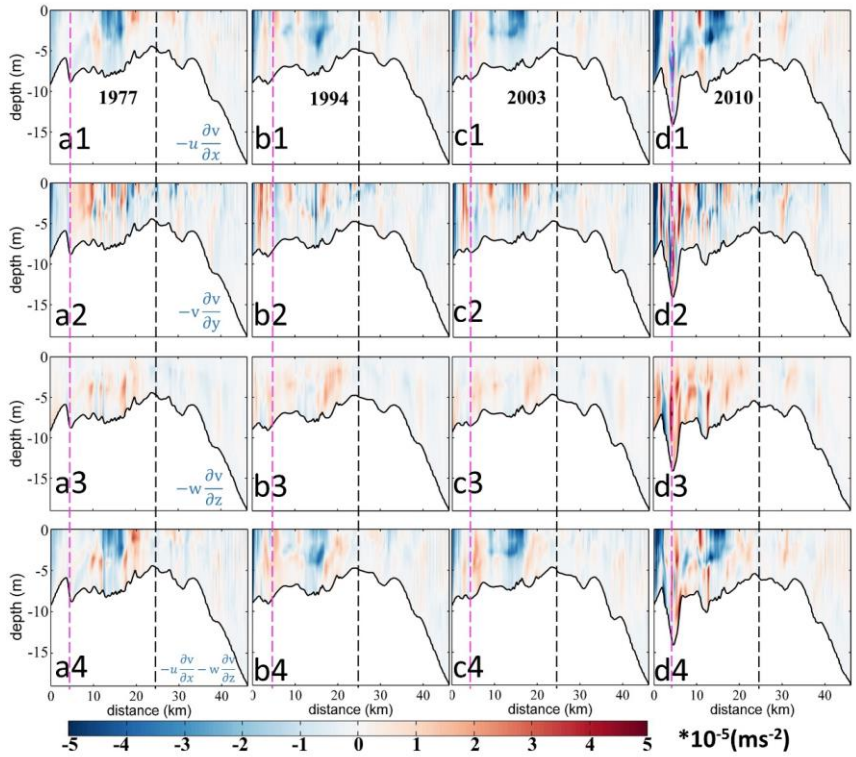


Fig. ~~9~~8. Patterns of the longitudinal momentum terms during neap tide at Sec. A. (a1-d1): The advection in the X direction, $-u\frac{\partial v}{\partial x}$. (a2-d2): The advection in the Y direction, $-v\frac{\partial v}{\partial y}$. (a3-d3): The advection in the Z direction, $-w\frac{\partial v}{\partial z}$. (a4-d4): The sum of the advection terms in X and Z directions. 1977, 1994, 2003, and 2010 cases are in the first, second, third, and fourth columns,

respectively. The pink and black dotted lines represent the location of Sec.B1 and Sec.B2, respectively. The starting point of the X-axis is Point A in Fig. 1b.

From Fig. ~~9~~8, in 2010, the advection terms in all directions increased significantly. Generally, the lateral and vertical advection competes against each other, and their additive effect is to generate a circulation similar to the gravitational circulation. This effect was the strongest in 2010 (Figs. ~~9a4~~ 8a4-d4). The longitudinal advection increased in the upper part of the channel in 2010 (Figs. ~~9a2~~8a2-d2), following the deepening and narrowing of the estuary. In the middle of the longitudinal section, it induced a seaward flow at the surface and a landward flow at the bottom, whereas at the upper part, it generates a uniformly landward flow.

~~Therefore, the maximum longitudinal estuarine circulation in 2010 was caused by the increase in the pressure gradient force and the advection term, especially the baroclinic pressure gradient force. The largest variation of the advection and pressure gradient terms occurred in the period of topography narrowing and deepening.~~

Overall, from 1977 to 2010, the baroclinic force, the friction, and the advection terms were seen to increase along the Sec. A. The maximum longitudinal estuarine circulation in 2010 was caused by the increase in the pressure gradient force and the advection term, especially the baroclinic pressure gradient force. We will further discuss the effects of these changes on estuarine circulation.

4.2 Analysis of the streamwise vorticity balance for the lateral flow

In order to reveal the contribution of the vertical shear of the along-channel flow, the lateral salinity gradient, and the vertical diffusion to changes in the lateral circulation, we examine the changes in terms of the streamwise vorticity transport equation (Li et al., 2014):

$$\frac{dw_y}{dt} = \underbrace{-f\frac{\partial v}{\partial z}}_{tilting\ of\ planetary\ vorticity} \underbrace{-g\beta\frac{\partial S}{\partial x}}_{baroclinicity} \underbrace{+\frac{\partial^2}{\partial z^2}\left(K_V w_y\right)}_{vertical\ diffusion} \underbrace{+\frac{\partial^2}{\partial x^2}\left(K_H w_y\right)}_{horizontal\ diffusion}, \quad (5)$$

In the right side of Eq. 5, the first term represents the tilting of the planetary vorticity by vertical shear in the along-channel flow, the second term is the baroclinicity caused by the lateral salinity gradient, the third is the vertical diffusion, and the fourth is the horizontal diffusion, which is typically two orders of magnitude smaller than the vertical diffusion term. Therefore, we only show the first four terms in Fig. ~~10~~9.

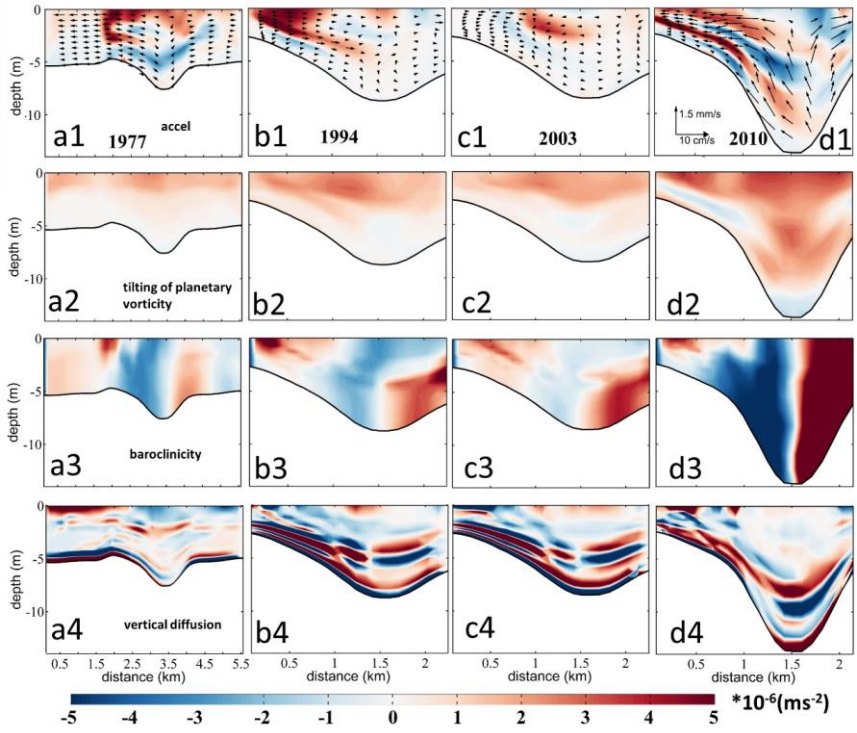


Fig. ~~10~~9. Patterns of the streamwise vorticity equation terms during neap tide at Sec. B1. (a1-d1): The local acceleration term. (a2-d2): The tilting of planetary vorticity term. (a3-d3): The baroclinicity term. (a4-d4): The vertical diffusion term. The cases in 1977, 1994, 2003, and 2010 are in the first, second, third, and fourth columns, respectively. The starting point of the X-axis is Point C in Fig. 2d. For viewing purposes, the acceleration term is multiplied by 5. The block arrows in a1-d1 represent the distribution of lateral circulation.

Figure ~~10~~ 9 shows that the changes of baroclinicity terms caused by the water depth change dominated the changes in the lateral circulation at Sec. B1. The baroclinicity term in the deep channel was generally negative at the left side of the channel, and it

increased significantly in 2010, about 2-3 times the value in 1977. The baroclinicity term with positive values occurred ~~over~~ at the West Shoal over the study period, but the areal extent occupied by the positive values decreased gradually, with its magnitude increased obviously in 1994 when the narrowing rate was the largest. A negative baroclinicity term appeared at the bottom of the West Shoal, indicating that the changes in water depth can lead to changes in the pattern and magnitude of the baroclinicity term, which was mainly caused by the changes in the salt intrusion. The tilting of the planetary vorticity term increased with the estuary narrowing, with the increase ~~of this term~~ in 2010 was greater, which was mostly caused by the depth change. The pattern of the vertical diffusion term changed significantly in 1977 and 1994~~. It changed~~, especially at the surface and the bottom layers of the West Shoal~~: When the width decreased to about 2.5 km, the distribution of vertical diffusion was reversed compared with 1977~~, indicating that it was the changes in width that altered the vertical diffusion term.

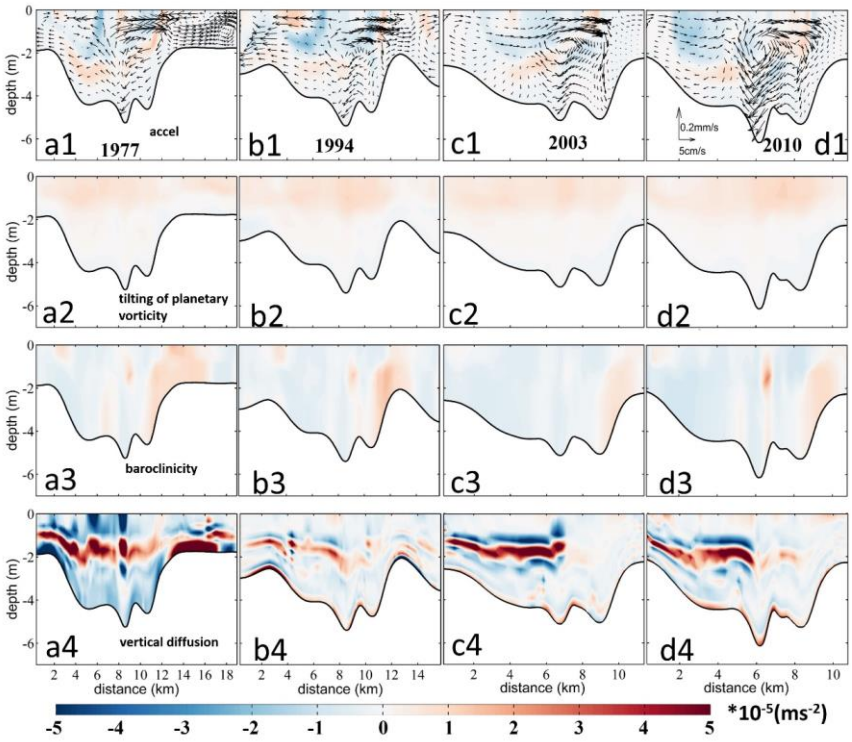


Fig. ~~11~~10. Patterns of the streamwise vorticity equation terms during neap tide at Sec. B2. (a1-d1): The local acceleration term. (a2-d2): The tilting of planetary vorticity term. (a3-d3): The baroclinicity term. (a4-d4): The vertical diffusion term. The cases in 1977, 1994, 2003, and 2010 are in the first, second, third, and fourth columns, respectively. The starting point of the X-axis is Point E in Fig. 2d. For viewing purposes, the acceleration term is multiplied by 5. The block arrows in a1-d1 represent the distribution of lateral circulation.

From Fig. ~~11~~10, the change in the tilting of the planetary vorticity at Sec. B2 was analogous to that at Sec. B1. The baroclinicity term did not change much, because the changes in water depth were smaller in this section ~~than that at Sec. B1~~. The clockwise circulation over the West shoal increased as the estuary deepened in 2010, because the baroclinicity term was larger with the increase of salt intrusion and vertical salinity gradient near Sec. B2. The vertical diffusion of the vorticity was overall negative, indicating its effect in dissipating the vorticity. The vertical diffusion term was larger than the baroclinicity term, especially in the middle water, which was inconsistent with the conclusion that the baroclinicity term is the most important one in the lateral

690 circulation (Li et al., 2014). The reason may be that in our study site, the vertical mixing
691 was strong as the estuary became shallow. However, the existence of a pycnocline
692 greatly weakened the momentum exchange between the upper and lower layers: above
693 the pycnocline, the tilting of the planetary vorticity was dominant; whereas, under the
694 pycnocline, the baroclinic term was dominant. The decrease of the estuary width
695 changed the magnitude and pattern of the vertical diffusion term, ~~, especially when the~~
696 ~~estuary width was less than 15 km,~~ and the area with a large positive value at the bottom
697 of the East Shoal disappeared, ~~and~~ along with the magnitude of the negative value
698 decreased greatly at the easternmost of the section. It indicates that in a shallow estuary,
699 the vertical diffusion term caused by the width change is also important.
700 In Summary, the tilting of the planetary vorticity increased with the decrease of
701 width or with the increase of water depth. The variation of estuary width was
702 responsible for the changes in the vertical diffusion term, and the changes in water depth
703 were responsible for the changes in the baroclinicity term. The increase of the
704 longitudinal estuary circulation can increase the baroclinicity term ~~of~~ at the cross-
705 sections by increasing the salinity gradient near the cross-sections, which mainly
706 occurred in the periods of the estuary deepening. The deepening rate of Sec.B1 was the
707 highest (61%) in 2010, which led to the strongest lateral circulation in 2010. The lateral
708 circulation intensity decreased when the estuary narrowed in 2003 due to the decreased
709 baroclinicity term. In addition, the shallowing was the main reason for the pattern
710 change of the lateral circulation at Sec.B2. At Sec. B2, the narrowing rate was the
711 largest in 2003, and the adjustment of the vertical diffusion term resulted in an increased
712 lateral circulation from 1994 to 2003. The decrease of the clockwise circulation at the
713 East Shoal was mainly related to the adjustment of the vertical diffusion term to the
714 baroclinicity term.
715
716 **4.3 Comparison to theoretical results and other estuaries influenced by human**
717 **interventions**
718

The longitudinal estuarine circulation is generated by the river discharge, Stokes return flow, longitudinal baroclinic pressure force, tidal straining, and advection (Geyer and Maccready, 2014). The HE features a microtidal tidal regime (tidal range less than 1.5 m), and the component generated by the baroclinic pressure gradient, i.e., the gravitational circulation, would be a primary part of the longitudinal estuarine circulation. The convergent geometry makes it susceptible to the residual flow induced by the longitudinal advection (Burchard et al., 2014). However, as seen above, the horizontal advection also plays a role in generating the estuarine circulation.

With channel deepening and width narrowing in the HE, the gravitational circulation was increased by the increased baroclinic pressure gradient force. Based on Geyer's research (2010), the gravitational circulation can be simplified ~~as~~ to: ~~in a straight estuary of rectangular cross-section is scaled as:~~

~~$v_g = a(\beta g s_0 h)^{1/5} U_r^{1/5} U_t^{2/5} = a(\beta g s_0 h)^{1/5} R^{1/5} (wh)^{-1/5} U_t^{2/5}$, (6)~~

~~in which a is a constant, β is the salinity expansion coefficient, g is the gravity acceleration, s_0 is the oceanic salinity, R is the river discharge, w is the width of the cross-section, U_t is the tidal velocity amplitude, h is the water depth, U_r is the outflow velocity associated with the river discharge. Where $u_r = Q_r/A_{cs}$ (Q_r is the freshwater outflow, A_{cs} being the local cross-sectional area of the estuary).~~

~~If we simply assume that the change in tidal current amplitude follows the Green's law $U_t = U_0\sqrt{\frac{w_0 h_0}{wh}}$ (here w_0 and h_0 is the width and depth at the estuary mouth, respectively), then the gravitational circulation becomes:~~

$$v_g = ~~a(\beta g s_0 h)^{1/5} R^{1/5} (wh)^{-1/5} U_0^{2/5} (w_0 h_0)^{1/5} (wh)^{-1/5}~~$$

$$= a_1 (\beta g s_0 R w_0 h_0)^{1/5} U_0^{2/5} w^{-2/5} h^{-1/5}, \quad (~~7~~6)$$

in which w_0 and h_0 is the width and depth at the estuary mouth, respectively.

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It indicates that the gravitational circulation is inversely related to the water depth and width in the estuary, with a weaker dependence on the water depth. In Chant et al. (2018), the gravitational circulation is completely unrelated to the water depth in their

equation (2), which is $v_g \propto \left(\frac{g' R}{w}\right)^{\frac{1}{3}}$, in which the g' is the reduced gravity acceleration. This seems to contradict the situations occurring in many estuaries, such as in the Coos Bay (Eidam et al., 2020), Tampa Bay (Zhu et al., 2015), Changjiang Estuary (Zhu, 2018), Ems estuary (Van Maren et al., 2015), Hudson Estuary (Ralston and Geyer, 2019), and Newark Bay of the Delaware estuary (Chant et al., 2018). In all these estuaries, the gravitational circulation demonstrated an increase with the deepening of the channel. It suggests that the changes in gravitational circulation vary in different parts of the estuary and the longitudinal salinity gradient may not catch up with the change in water depth in the analytical solution, proposed by Chant et al. (2018) and Ralston and Geyer (2019). In our study site, the salinity gradient at the upstream part of the longitudinal section was increased owing to an enhanced salt intrusion where water depth increased, which led to an increased gravitational circulation in the upstream of the HE (Fig. 4).

The tidal straining-induced estuarine circulation is another important component of longitudinal estuarine circulation. The straining-induced circulation is the covariance of the eddy viscosity and the vertical shear of the longitudinal flow (ESCO) in a tidal cycle and is included in the term of internal friction. Cheng et al. (2010) have indicated that ESCO-induced flow dominates the gravitational circulation in periodically stratified estuaries with strong tides, having the same structure as the gravitational circulation. It has the same order of magnitude in weakly stratified estuaries with moderate tides, and is less important in highly stratified estuaries with weak tides, even with a reversed structure with the gravitational circulation. As indicated by Becherer et al. (2015), the strength of the straining-induced circulation is dependent on the Simpson number (or the horizontal Richardson number). The Simpson number is expressed as:

$$S_i = g\beta \frac{dS}{dy} \frac{h^2}{u_*} , \qquad (8\underline{7})$$

in which u_* is the bottom friction velocity, represented by $u_* = \sqrt{C_d} U_t$, where C_d is the bottom friction coefficient and U_t is the tidal velocity amplitude.

~~When S_t lies in the range of 0.088 to 0.84, the water column stays periodically stratified, and the straining-induced circulation is an important component in the longitudinal estuarine circulation.~~ When S_i is larger than 0.84, the water column is in a persistent stratified situation, and the straining-induced circulation becomes weaker. We calculated the S_i along the longitudinal section in different years and depict them in Fig. ~~12~~11.

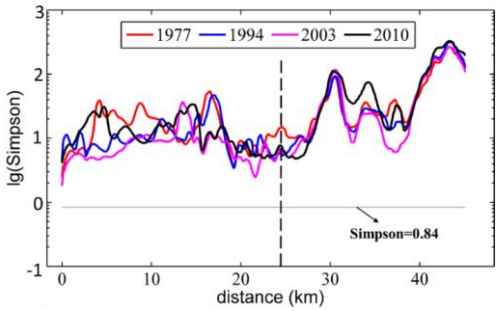

Fig. ~~12~~11. Distribution of the Simpson number in different years along the longitudinal section. The Y-axis represents the logarithmic of the S_i. The black dotted line represents the location of the null point.

It indicates that along the longitudinal section, the S_i number was mostly above the criterion of 0.84, showing that the straining-induced circulation is not significant. The Si number was the smallest in 2003 and the largest in 2010. It indicates that with the narrowing and deepening of the HE, the straining-induced circulation became weaker. This is consistent with Burchard et al. (2014) and Schulz et al. (2015). It indicates that with the human interventions, the straining-induced circulation became less important in the longitudinal estuarine circulation.

For the advection-induced longitudinal estuarine circulation, we noted that the longitudinal and vertical advection terms were smaller than the lateral advection. Based on Cheng and Valle-Levinson (2009), the lateral advection-induced longitudinal circulation is proportional to the ratio of $h/(wK_m)$, where w is the width, and K_m is the eddy viscosity. It shows that in a narrower and deeper estuary, the lateral advection has a larger effect in influencing the longitudinal estuarine circulation. Lerczak and

Geyer (2004) also showed that the effect of the lateral advection on longitudinal circulation is stronger for narrower estuaries. Our results show that with the narrowing and deepening of the estuary, not only the lateral advection but also the longitudinal advection has great influences on the longitudinal estuarine circulation.

4.4 The possible future development of the estuarine circulation and its implications

The pattern of lateral circulation during the dry season in the HE experienced a dramatic change from 2003 to 2010 in the West Shoal at Sec. B2, from an under-developed circulation structure to a complete clockwise vortex in 2010. This transition was associated with the increase in lateral salinity gradient, the increase in longitudinal bottom landward flow, and a decrease of friction by the increased water depth and stratification.

The mechanisms for the lateral circulation during the wet season have been revealed by Chen et al. (2020b), who showed that it was primarily driven by the barotropic process, i.e., the water elevation gradient, and thus by the intensity of the ebb jet. Different from the wet season when the river discharge was higher, the lateral circulation in the dry season was more affected by the baroclinic effect. We speculate that with the narrowing and deepening of the estuary, the lateral circulation even in the wet season will be enhanced with the ebb jet in the deep channel strengthened.

In the HE, the channel underwent siltation, and sediment was carried from the channels to side banks by the lateral circulation, making the estuary overall shallower in 2003. In 2005, dredging of the channel increased the channel depth (Luo, 2010), ~~resulting in a high deepening rate,~~ and increased the longitudinal estuarine circulation, though the lateral circulation decreased slightly by the smaller rate of convergence. If reclamation did not occur as frequently as it did in the last century, and the channel dredging continued, the estuarine circulation of the estuary will in general keep increasing with the increase in water depth, and ~~there exists~~ thus a positive feedback

exists. However, as revealed in Eq. (6) and Eq. (2) in Chant et al. (2018), with the increase in salt intrusion, the longitudinal salinity gradient will decrease, showing negative feedback. Moreover, Schulz et al. (2015) noted that estuarine circulation exhibits a distinct maximum in medium-wide channels by comparing estuarine circulation under different width-to-depth ratios. In our study, as shown in Table 4, the width-to-depth ratio has been decreasing from 1977 to 2010, but the estuarine circulation has been increasing. The difference would be caused by the fact that in our study site, the tidal mixing is not strong enough to generate an effective tidal straining-induced circulation.

The changes in the estuarine circulation have important implications for sediment transport and morphological evolution in the HE. With the increase of longitudinal estuarine circulation, the sediment trapping effect is expected to be enhanced, thus more riverine sediment would be trapped inside the estuary. In the meantime, the change in lateral circulation would decrease the sediment advection from the channel to the West Shoal, which occurred in the wet season and was favorable for the siltation in the West Shoal (Chen et al., 2020b).

In this study, the model used was only driven by river discharge and tides, without considering the effects of winds, waves, and other upstream flows into the estuary. Future work could incorporate the above factors to improve the model's accuracy.

5. Conclusion

This study investigated the morphological evolution of the HE from 1977 to 2010 using ArcGIS and remote sensing. It was noted that the West Channel of the HE disappeared, causing the morphological pattern to change from "two channels and three shoals" gradually to "one channel and two shoals" throughout the years. Due to the reclamation and development of salt marshes along the estuarine banks, the estuary has been experiencing continuous narrowing. Meanwhile, channel dredging has

deepened the estuary over the study period. The intensity of the longitudinal estuarine circulation kept increasing as the estuary width continued to decrease. The trend of the lateral circulation intensity altered when the estuary shollowed (from 1994 to 2003).

The changes in the longitudinal estuarine circulation were dominated by the changes in the baroclinic pressure gradient force and advection. As the estuary was narrowing and deepening, the pressure gradient force and advection term (especially the horizontal advection term) increased, which increased the longitudinal circulation. The change in lateral circulation intensity was mainly caused by the change of the vertical shear of the longitudinal subtidal flow, the lateral salinity gradient, and the vertical dissipation term. The changes in water depth were the dominant factor affecting lateral circulation intensity. The increase of water depth enhanced the longitudinal circulation and the lateral circulation of the upstream cross-section in 2010. The changes in the estuarine circulation have great implications for the sediment transport in the HE, which would be explored in the next step.

Data availability

A total of 142G data of 66 images (Table 1) covering the PRD during cloudless days in multiple years (from 1973 to 2018) were downloaded from http://www.gscloud.cn/.

Author contributions

RuiZhang: Writing - original draft, model runs and analyses. Bo Hong: Writing - review. Lei Zhu: Writing - review. Wenping Gong: Writing - review & editing, Conceptualization, Funding acquisition. Heng Zhang: Visualization, Funding acquisition.

Competing interests

The authors declare that they have no conflict of interest.

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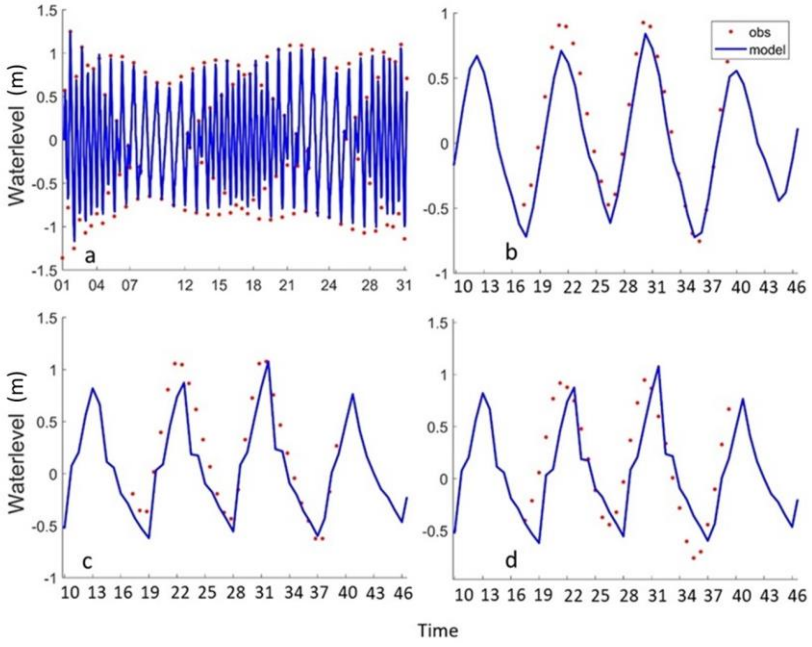
Appendix A



~~Fig. A. 1. Validation of water level of the MD2 model at 4 stations (S6 (a): SK=0.9969, DJ (b): SK=0.9337, S1 (c): SK=0.8652, and GL (d): SK=0.8928) in March 2010. The red dots and blue lines represent observation and simulated results, respectively. The station locations are shown in Fig. 1b. Time in (a) is days from 2010/3/1, in (b-d) is hours from 2010/3/17 00:00.~~

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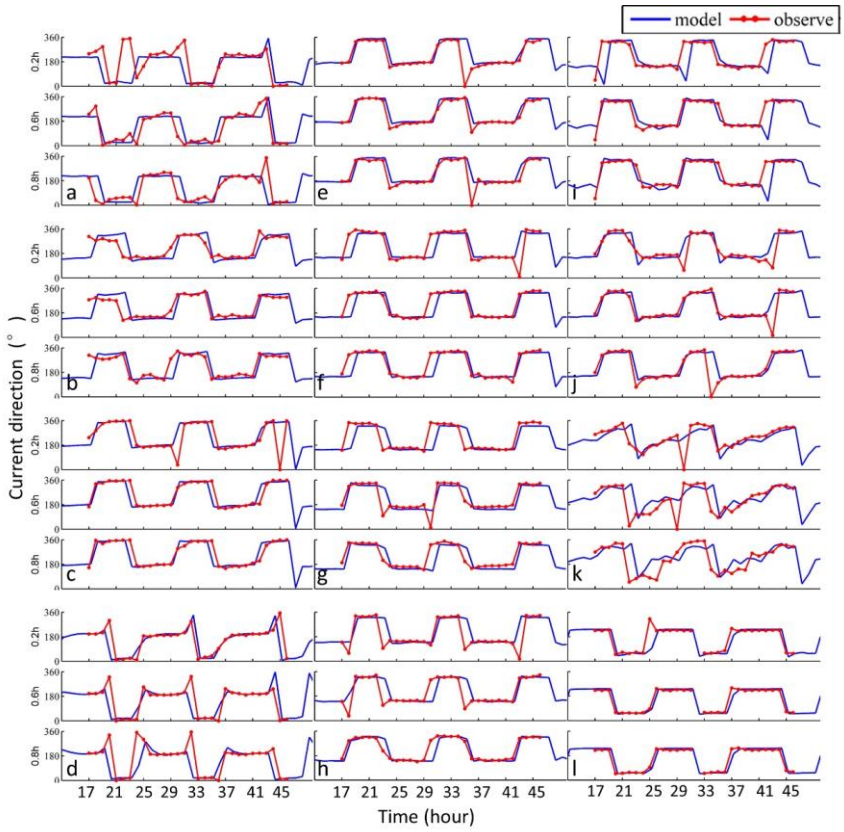

Fig. A. 2. Validation of current direction of the MD2 model at 12 stations (DJ (a), GL (b), HB (c), S2(d), S3(e), S4(f), S5(g), S7(h), S6(i), S8(j), S9(k), and S1(l)) in March 2010. The red and blue lines represent observation and simulation results, respectively. The station locations are shown in Fig. 1b. Time is hours from 2010/3/17 00:00.

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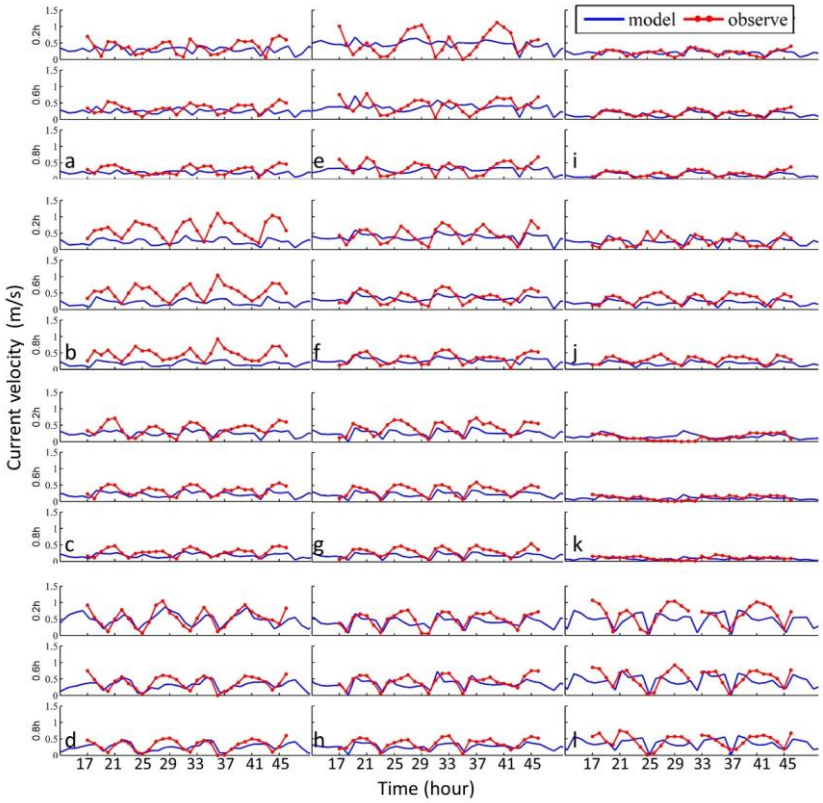

Fig. A. 3. Validation of current velocity of the MD2 model at 12 stations (DJ (a), GL (b), HB (c), S2(d), S3(e), S4(f), S5(g), S7(h), S6(i), S8(j), S9(k),and S1(l)) in March 2010. The red and blue lines represent observed and simulated results, respectively. The station locations are shown in Fig. 1b. Time is hours from 2010/3/17 00:00.

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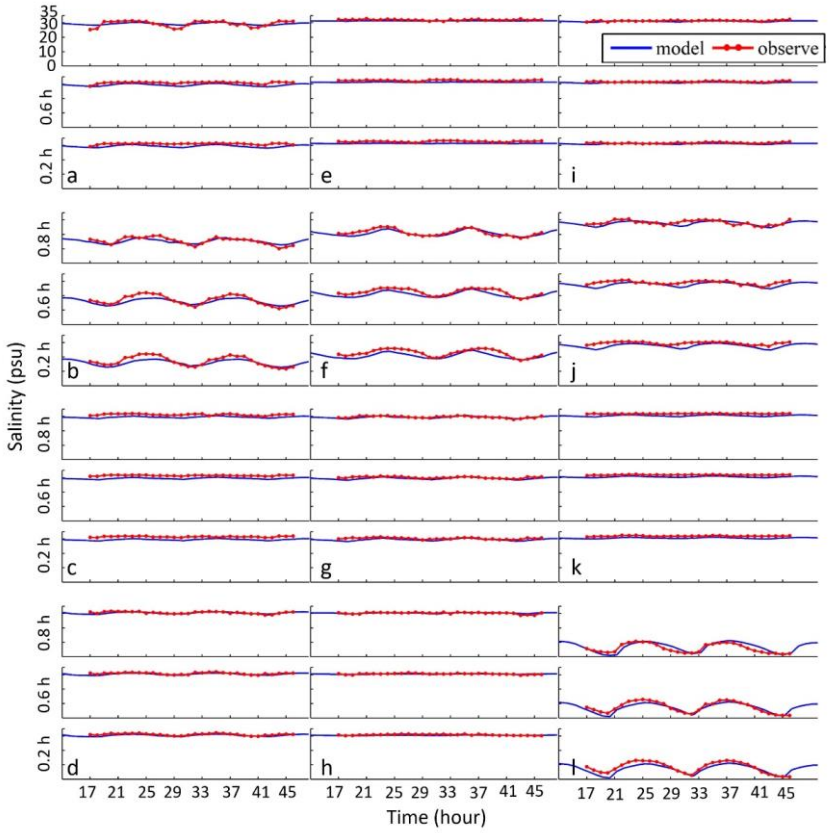

~~Fig. A. 4. Validation of salinity of the MD2 model at 12 stations (DJ (a), GL (b), HB (c), S2(d), S3(e), S4(f), S5(g), S7(h), S6(i), S8(j), S9(k), and S1(l)) in March 2010. The red and blue lines represent observed and simulated results, respectively. The station locations are shown in Fig. 1b. Time is hours from 2010/3/17 00:00.~~

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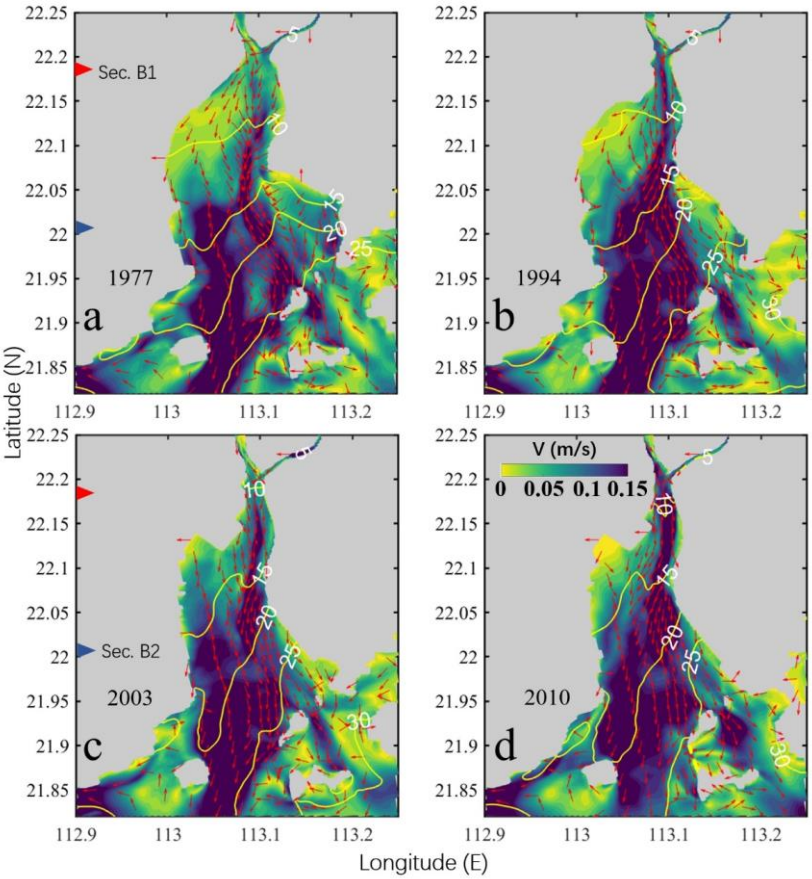

Fig. A. ~~5~~1. Patterns of the horizontal circulation at the surface during neap tide in 1977(a1), 1994(a2), 2003(a3), and 2004(a4). The magnitude of the current is represented by the color shading, while the current direction is shown by the arrows. The salinity is depicted by the contour lines. The red and blue triangles depict the positions of two cross-sections (Sec.B1 and Sec.B2).

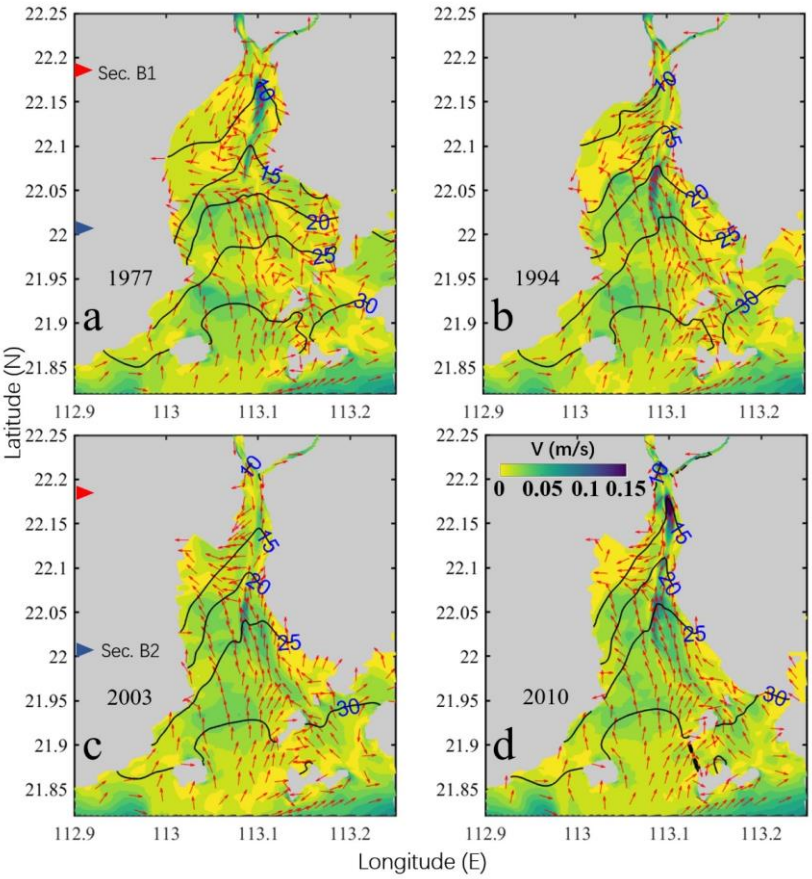

Fig. A. ~~6~~2. Patterns of the horizontal circulation at the bottom during neap tide in 1977(a1), 1994(a2), 2003(a3), and 2004(a4). The magnitude of the current is represented by the color shading, while the current direction is shown by the arrows. The salinity is depicted by the contour lines. The red and blue triangles denote the positions of two cross-sections (Sec.B1 and Sec.B2).

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