1 Reviewer 1

1.1 Major Comments

- 1. Accuracy. The novelty of the carbon-based methodology described here is that it can be used to derive estimates of excess and redistributed heat (extended to salt) for both model outputs and realworld observations. This latter application will enable ocean temperature time series observations to be deconvolved into that driven by ocean circulation and that caused by uptake of atmospheric anthropogenic heat, something that is simply not possible using PAT. We demonstrate the merits of the approach in a model context as it first allows us to look at global patterns of excess heat, something which is well studied, and also avoids problems associated with observational data sets, namely problems with temporal and spatial resolution, and the lack of a PAT. The reviewer is correct to request better characterisation of the validity of our outputs and given the constraints of our model runs we have given further explanation. Unfortunately due to the setup of our model (simulations were primarily motivated for study mechanisms of carbon uptake) no PAT was included, meaning it is not possible to directly validate our outputs against such an experiment. While this is not optimal we have however now performed a cross validation with the method of Bronselaer Zanna, 2020, who approximated the excess heat field with the anthropogenic carbon field, and were able to validate their approach directly against fixed circulation ocean heat uptake experiments and a PAT (section 3.1, lines 263-343). We show that our results strongly agree, and that the differences between the two methods closely resemble the differences between their method and their fixed circulation heat uptake; we are able to explain this in terms of subduction of carbon through the mixed layer base, indicating differences are likely due to a relaxation of the assumption of a global mean alpha value. This is described in (section 3.1, lines 327-336). As the key motivation of this study is to produce a technique which allows us to estimate excess heat observationally, rather than to model it, this necessitates the use of an alternative methodology to PAT / fixing ocean circulation. We feel we have now better explained how we go about validating its outputs.
- 2. Consistency. We think the Winton et al. paper cited by the reviewer is in fact Winton et al. 2012: "Connecting Changing Ocean Circulation with Changing Climate", which looked at the patterns of heat and carbon storage under freely evolving and fixed preindustrial ocean circulation experiments. In this paper it is shown that a substantial fraction of redistribution heat transport is compensated for by changes in surface fluxes (around 1/3), indicating that redistribution heat transport is a driver of surface heat uptake from low to high latitude. Following this, the reviewer is correct to question the impact of flux and circulation perturbations on our outputs. Our ocean only simulations have an AMOC strength that is approximately 50% weaker than that in HadGEM2-ES (8Sv as compared to 15Sv at 26N in the control simulation; text amended at section 3.2 lines 397-404) to include discussion of this). This would imply that a possible bias in surface heat fluxes associated with redistribution exists due to inconsistency with the forcings. However, we find realistic heat transports by the AMOC in our simulations (when compared to observations - see revised section 3.2 lines 400-402), as well as an AMOC decline in our simulation that is proportional to AMOC decline in HadGEM2-ES, with AMOC strength being approximately half that of HadGEM2-ES at all times in our simulation (section 3.2 lines 402-404). Therefore, although there are likely to be inconsistencies in the forcing and the circulation response, comparisons of the AMOC decline between the ocean-only model and HadGEM2-ES are due to a systematic bias rather than a bias which varies over the course of the runs. Similar such biases resulting from inconsistencies in forcings and sea surface temperatures also exist in FAFMIP type experiments, and are not unique to this study. However, there will still be an excess component of temperature and salinity as a result of surface forcing, and a redistributed component due to changes in circulation; these will be internally consistent within the ocean-only model run, even if the surface forcings are somewhat inconsistent with the atmospheric forcing. In summary, in this study we are looking to describe the utility of using a new method based on carbon data to reconstruct excess and redistributed heat. While the reviewer is correct that the use of an ocean model forced by a coupled model introduces biases, due to the lack of a feedback from the ocean model on the coupled model's atmosphere the existence of these biases does not undermine the demonstration of the method. The text has been amended to account for this discussion (section 3.2 lines 398-400).

3. Representativeness. Models vary in their circulation response to climate change forcings (as well as their uptake of excess heat) that manifest themselves in a range of different temperature changes in various locations in response to increasing radiative forcing. We recognise that we present the outputs of only one model, and we agree with the reviewer that this therefore does not represent the full spread of potential scenarios (for example of AMOC decline) that models predict - we acknowledge this in the revised section 4 lines 516-519, 579-580. However, we don't feel it impacts the utility of the method that we present, or its possible wide application. While we feel applying our decomposition for a range of CMIP5 models is outside of the remit of this particular study, following the reviewer's excellent suggestion we have however subsequently compared the circulation changes in our model with those of HadGEM2-ES, and of HadGEM2-ES with a range of other CMIP5 models, as well as the representation of the AMOC in HadGEM2-ES with observations (section 3.2 lines 397-405).

Minor comments

- 1. We agree that further clarification is necessary for the lines highlighted. Additional context and explanation has now been added (lines 43-48).
- 2. A number of techniques for estimating anthropogenic carbon from observations have been derived. These are based either on the inorganic carbon system (C*, TrOCA, phi) or using measurements of transient tracers as proxies of anthropogenic carbon invasion (TTD), and have been used to quantify oceanic anthropogenic carbon accumulation (Khatiwla et al (2013), and its decadal variability (Gruber et al, 2019). As anthropogenic carbon is closely analogous to excess carbon (Williams et al 2021), we thus have better estimates of excess carbon observationally than excess heat. We have amended the text at lines 59-70 to better explain this.
- 3. The reviewer makes a good point, we have now significantly expanded the experimental specification in the revised draft, with details of all these included (section 2.1, lines 106-140).
- 4. Thank you for highlighting this error, this has now been fixed
- 5. As detailed above when addressing major comment 1 (accuracy) we have now completely rewritten this section (section 2.2, lines 142-260) to make it clearer how our estimation technique works in the revised draft, removing details about how velocity perturbations project into temperature-carbon space, and focussing on how the redistribution of temperature and carbon are linked. We have also cross validated our decomposition against an alternative carbon-based proxy method.
- 6. We thank the reviewer for this suggestion. We have added observational global excess heat uptake from Zanna et al 2019 to Figure 1b. For excess salinity, the signal is dominated by changes in airsea freshwater fluxes (evaporation-precipitation) rather than ice melt so comparison to observational ice-melt budgets will not be as useful/powerful as hoped. However, we have adapted the text at lines 351-353 to consider this.
- 7. The reviewer makes an interesting point. However, although global mean redistributed temperature is constrained to be zero, this is not the case locally or regionally. We therefore think that comparing the scale of positive only and negative only regions is useful, as it is a measure of the degree to which excess and redistributed temperature contribute to local temperature changes.
- 8. We have adapted the revised draft (lines lines 391-393) to clarify that the AMOC does declines continually throughout the COU run, with the decline not slowing.
- 9. We have reworded the text to make this aspect clearer (lines 444-451). Rather than proportionality existing between the excess and redistributed pools and SST anomalies, it is the rate of change in the redistributed heat pool that is proportional to SST change/AMOC change.
- 10. We have removed this discussion from the revised draft, as we have decided that it is too speculative and ambiguous.

11. While our model setup does includes sea ice it does not include ice sheets. This means that unfortunately it is not possible to directly examine the relationship between excess salinity changes and glacial inputs in our model. Following this and as mentioned in point 6 above, the excess salinity signal is dominated by changes in air-sea freshwater fluxes (evaporation-precipitation) so comparison to observational ice-melt budgets will not be as useful/powerful as hoped. References to previous studies finding nontrivial ice sheet loss in the early 20th century was to highlight the different emergence timescales of excess heat and excess salinity. We have amended the text to improve clarity regarding this (lines 371-377, 534-454), and to better describe the model setup (lines 106-140). We have also additionally cited Hetzinger et al. 2019 and Wadhams Munk, 2004 as further support (line 535-537), as Hetzinger et al. reconstructed sea ice decline using an algal proxy and found decline in the Arctic started by the early 1910s. Wadhams Munk calculated a 20th century mean sea ice decline equivalent to a global mean salinity change of 104 PSU: our simulations give a global mean sea ice decline of 5*10⁻4 PSU over the same period - of the same order of magnitude.

2 Reviewer 2

- (a) We have now significantly rewritten the text to describe the experimental specification for individual runs in far greater detail (lines 109-124) separating this out into sections for CTR (lines 117-119), COU and RAD (120-124). With regard to the specific questions/points raised by the reviewer: surface heat, momentum, freshwater fluxes and atmospheric chemistry from HadGEM2-ES combined with RCP8.5 atmospheric CO2 concentrations was used to force NEMO, with no restoring used description of this has been included in lines 111-116. Additional references as suggested by the reviewer to make the experimental specification clearer have been added (line 137). To describe the different runs we follow the terminology employed by Schwinger et al. 2014, namely COU, CTR and RAD. Description of each of these have been added to the text (lines 109-110, 117-122) to aid the reader. For the COU simulation, this specifically refers to a coupled climate change run that imposes both physical and biogeochemical change (line 120-122).
 - (b) Following the reviewers recommendations section 2.2 has been completely rewritten to more clearly explain how the decomposition works (lines 142-260) and to show that that it is producing an estimate of how the preindustrial states of temperature and DIC covary. We have removed the confusing formulation about how velocity perturbation project into temperature carbon space and focussed on the key principle of estimating how temperature and DIC covary spatially, adding references as appropriate (lines 142, 144, 200). As detailed in response to Reviewer 1 (Comment 1) the simulations we use here were performed to study mechanisms of carbon fluxes and variability in the carbon cycle. As such, no PAT tracer was included nor fixed circulation experiments were performed, meaning it is not possible to directly validate our outputs against such an experiment. We have now performed a cross validation with the method of Bronselaer Zanna, 2020, who like we said, approximated the excess heat field with the anthropogenic carbon field, and were able to validate their approach directly against fixed circulation ocean heat uptake experiments and a PAT (section 3.1, lines 263-348). We quantify our method against the alternative carbon proxy of Bronselear Zanna 2020 (lines 261-348) and explain the differences between the two methods in terms of oceanographic features. Williams et al. 2021 explained and defined excess and redistributed temperature and DIC in terms of the correlation of the excess and anticorrelation of the redistributed components (lines 86-90). We have amended the text to clarify that our decomposition is a method for specifying the anticorrelation between redistributed components, much as the method of Bronselaer & Zanna 2020 specifies the correlation between the excess components (lines 90-96). In this study natural carbon is defined as that component of the total inorganic carbon signal that would have existed in the absence of an anthopogenically-forced atmospheric CO2 concentration, essentially a preindustrial carbon field (lines 126-136) We define how this is a useful tracer in our technique (lines 95-96, 187-194), qualifying that the choice of natural carbon is not unique (lines 190-194).
 - (c) We have clarified that we use PCA in order to obtain a total least squares regression (rather than an ordinary least squares regression) as this allows the relationship defined to be independent

of the choice of dependent variable (lines 211-215). As described at lines 206-209 decadal data binning is performed in order to eliminate the small effects of model drift and using repeat surface forcing cycles that are misattributed as excess temperature/DIC.

- (d) We thank the reviewer for this advice. As well as improving the description and application of the decomposition (detailed above, lines 142-260), we have amended the text to clarify that using local relationships between temperature and natural carbon derived from observations we can deconvolve estimates of excess and redistributed temperature (and by extension salinity) (lines 508-512). Carbon is useful observationally as we have global observations of temperature and carbon dating back to 1990 (GLODAP) that enables the development of the excess/redistributed fields to be tracked with time. We have added text to explain that that the choice of carbon is not unique, though carbon is useful because excess/redistributed carbon and anthropogenic/natural carbon are similar, with reference to Williams et al. 2021 (lines 68-70).
- 2. We thank the reviewer for these constructive suggestions. We have rewritten the methodological derivation section to more effectively describe how and why we define the covariability of the preindustrial states of temperature and carbon (lines 142-260). As detailed in a previous response above, we have removed all descriptions of how velocity perturbations project into temperature-carbon space, as this was an unhelpful formulation which did not make our approach clear. We have removed repetitions, added further references (lines 141, 168, 200). Need a list here of actions taken and line references
 - (a) We recognise the ambiguity relating to our discussion of salinity and lead/lag times. To account for this we have calculated times of emergence of signals of excess heat and salinity from noise for the basins discussed (lines 371-377) which are presented in Figure 6. We have also clarified the text to reflect that the discussion primarily concerns the emergence of signals in excess salinity and excess temperature, rather than lagged correlations (lines 371-377). We have significantly expanded the discussion relating to this (lines 534-543) and included extra citations to relevant literature (Stott et al. 2008, Terray et al. 2012, Pierce et al. 2012, Skliris et al. 2014, line 541).
 - (b) Thank you for this suggestion, this is an excellent point. In the revised draft, we have explicitly calculated the redistribution of heat and salinity in the Atlantic through the Equator (lines 405-420), showing that our method is reliably capturing the redistribution of heat and salinity in response to AMOC changes. We have also added that AMOC is not the only relevant process at play (line 421-426).
 - (c) The original manuscript noted the resemblance of the excess salinity fields to the sea surface salinity changes in Zika et al. 2018 in response to an imposed heat flux, and also in response to water cycle amplification. We agree with the reviewer that there is some ambiguity in the text, so we have removed the reference to imposed water cycle amplification in the revised draft to improve this (line 534).
 - (d) We appreciate the reviewer's position and where appropriate we have maintained axis scales as constant; for example, in Figure 3 (Figure 7 in the revised draft), we have rescaled the plots in terms of mean temperature change in order to improve clarity. In some cases however, due to the different scales of each component and in each ocean basin, keeping axes scales constant would result in a number of important features becoming indiscernible. In these cases (Figures 6, 7, 8, 9) we have pointed out to the reader in the text and caption the different scales used. Specifically for the new Figure 7, we have also rewritten the surrounding text (lines 432-435) to make it clear that relationships are not emerging in every ocean basin, and that it is the North Atlantic that is of interest due to its different behaviour to every other ocean basin (lines 442-451).

In response to minor comments: The manuscript has been fundamentally rewritten to account for the deficiencies identified by the reviewers. We have attempted to identify and remove all redundancies, included additional description and information where this was lacking, and clarified the text where possible. We have added a significant number of references:

Linking results to observations

- Antonov, J. I., Levitus, S., and Boyer, T. P.: Steric sea level variations during 1957–1994: Importance of salinity, Journal of Geophysical Research: Oceans, 107, SRF 14–1–SRF 14–8, https://doi.org/https://doi.org/10.1029/2001JC000964, 2002
- Bopp, L., Lévy, M., Resplandy, L., and Sallée, J. B.: Pathways of anthropogenic carbon subduction in the global ocean, Geophysical Research650Letters, 42, 6416–6423, https://doi.org/https://doi.org/10.1002/2015GL065073, 2015.
- Firing, Y. L., McDonagh, E. L., King, B. A., and Desbruyères, D. G.: Deep temperature variability in Drake Passage, Journal of Geophysical Research: Oceans, 122, 713–725, https://doi.org/https://doi.org/10.1002/2016JC012452, 2017
- Thomas, J., Waugh, D., and Gnanadesikan, A.: Relationship between Ocean Carbon and Heat Multidecadal Variability, Journal of Climate, 31, 1467 1482, https://doi.org/10.1175/JCLI-D-17-0134.1, 2018
- Sabine, C., Feely, R., Gruber, N., Key, R., Lee, K., Bullister, J., Wanninkhof, R., Wong, C., Wallace, D., Tilbrook, B., Millero, F., Peng, T.-H., Kozyr, A., Ono, T., and Rios, A.: The Oceanic Sink for Anthropogenic CO2, Science (New York, N.Y.), 305, 367–71, https://doi.org/10.1126/science.1097403, 2004
- Lauvset, S. K., Key, R. M., Olsen, A., van Heuven, S., Velo, A., Lin, X., Schirnick, C., Kozyr, A., Tanhua, T., Hoppema, M., Jutterström, S., Steinfeldt, R., Jeansson, E., Ishii, M., Perez, F. F., Suzuki, T., and Watelet, S.: A new global interior ocean mapped climatology: the 10×10GLODAP version 2, Earth System Science Data, 8, 325–340, https://doi.org/10.5194/essd-8-325-2016, 2016.

Model setup and terminology description

- Couldrey, M. P., Oliver, K. I. C., Yool, A., Halloran, P. R., and Achterberg, E. P.: On which timescales do gas transfer velocities control North Atlantic CO2 flux variability?, Global Biogeochemical Cycles, 30, 787–802, https://doi.org/https://doi.org/10.1002/2015GB005267, 2016
- Schwinger, J., Tjiputra, J. F., Heinze, C., Bopp, L., Christian, J. R., Gehlen, M., Ilyina, T., Jones, C. D., Salas-Mélia, D., Segschneider, J., Séférian, R., and Totterdell, I.: Nonlinearity of ocean carbon cycle feedbacks in CMIP5 earth system models, Journal of Climate, 27,3869–3888, https://doi.org/10.1175/JCLI-D-13-00452.1, 2014.
- Madec, G. and Imbard, M.: A global ocean mesh to overcome the North Pole singularity, Climate Dynamics, 12, 381–388, 1996.
- Madec, G. and Team, 2008.: NEMO ocean engine, https://doi.org/10.5281/zenodo.1464816.
- Martin, T. H. D. T. G. M., Bellouin, N., Collins, W. J., Culverwell, I. D., Halloran, P. R., Hardiman, S. C., Hinton, T. J., Jones, C. D., McDonald, R. E., McLaren, A. J., O'Connor, F. M., Roberts, M. J., Rodriguez, J. M., Woodward, S., Best, M. J., Brooks, M. E., Brown, A. R., Butchart, N., Dearden, C., Derbyshire, S. H., Dharssi, I., Doutriaux-Boucher, M., Edwards, J. M., Falloon, P. D., Gedney, N., Gray, L. J., Hewitt, H. T., Hobson, M., Huddleston, M. R., Hughes, J., Ineson, S., Ingram, W. J., James, P. M., Johns, T. C., Johnson, C. E., Jones, A., Jones, C. P., Joshi, M. M., Keen, A. B., Liddicoat, S., Lock, A. P., Maidens, A. V., Manners, J. C., Milton, S. F., Rae, J. G. L., Ridley, J. K., Sellar, A., Senior, C. A., Totterdell, I. J., Verhoef, A., Vidale, P. L., and Wiltshire, A.: The HadGEM2 family of Met Office Unified Model climate configurations, Geoscientific Model Development, 4, 723–757, https://doi.org/10.5194/gmd-4-723-2011, 2011
- Riahi, K., Rao, S., Krey, V., Cho, C., Chirkov, V., Fischer, G., Kindermann, G., Nakicenovic, N., and Rafaj, P.: RCP 8.5—A scenario of comparatively high greenhouse gas emissions, Climatic Change, 109, 33–57, https://doi.org/10.1007/s10584-011-0149-y, 2011.

• Rodgers, K. B., Ishii, M., Frölicher, T. L., Schlunegger, S., Aumont, O., Toyama, K., and Slater, R. D.: Coupling of Surface Ocean Heat and Carbon Perturbations over the Subtropical Cells under Twenty-First Century Climate Change, Journal of Climate, 33, 10 321 – 10 338, https://doi.org/10.1175/JCLI-D-19-1022.1, 2020.

Method description, context of decomposition methodology

- Gregory, J. M., Bouttes, N., Griffies, S. M., Haak, H., Hurlin, W. J., Jungclaus, J., Kelley, M., Lee, W. G., Marshall, J., Romanou, A., Saenko, O. A., Stammer, D., and Winton, M.: The Flux-Anomaly-Forced Model Intercomparison Project (FAFMIP) contribution to CMIP6: investigation of sea-level and ocean climate change in response to CO2 forcing, Geoscientific Model Development, 9, 3993–4017, https://doi.org/10.5194/gmd-9-3993-2016, 2016
- Katavouta, A., Williams, R. G., Goodwin, P., and Roussenov, V.: Reconciling Atmospheric and Oceanic Views of the Transient Climate Response to Emissions, Geophysical Research Letters, 45, 6205–6214, https://doi.org/https://doi.org/10.1029/2018GL077849, 2018.
- Williams, R. G. and Follows, M. J.: Ocean Dynamics and the Carbon Cycle: Principles and Mechanisms, Cambridge University Press, https://doi.org/10.1017/CBO9780511977817, 2011.
- Williams, R. G., Katavouta, A., and Roussenov, V.: Regional Asymmetries in Ocean Heat and Carbon Storage due to Dynamic Redistribution in Climate Model Projections, Journal of Climate, 34, 3907 3925, https://doi.org/10.1175/JCLI-D-20-0519.1, 2021

Expanding description of motivation/study context

- Gruber, N.: Warming up, turning sour, losing breath: ocean biogeochemistry under global change, Philosophical Transactions of the Royal Society A: Mathematical, Physical and Engineering Sciences, 369, 1980–1996, https://doi.org/10.1098/rsta.2011.0003, 2011
- McKinley, G. A., Fay, A. R., Lovenduski, N. S., and Pilcher, D. J.: Natural Variability and Anthropogenic Trends in the Ocean Carbon Sink, Annual Review of Marine Science, 9, 125–150,

 $https://doi.org/10.1146/annurev-marine-010816-060529, \, pMID: \, 27620831, \, 2017$

 Oschlies, A., Brandt, P., Stramma, L., and Schmidtko, S.: Drivers and mechanisms of ocean deoxygenation, Nature Geoscience, 11, 467–473, https://doi.org/10.1038/s41561-018-0152-2, 2018

Specifically relating to ice

- Hetzinger, S., Halfar, J., Zajacz, Z., and Wisshak, M.: Early start of 20th-century Arctic sea-ice decline recorded in Svalbard coralline algae, Geology, 47, 963–967, https://doi.org/10.1130/G46507.1, 2019
- Wadhams, P. and Munk, W.: Ocean freshening, sea level rising, sea ice melting, Geophysical Research Letters, 31, https://doi.org/https://doi.org/10.1029/2004GL020039, 2004.

Relating to AMOC

- Johns, W. E., Baringer, M. O., Beal, L. M., Cunningham, S. A., Kanzow, T., Bryden, H. L., Hirschi, J. J. M., Marotzke, J., Meinen, C. S., Shaw, B., and Curry, R.: Continuous, Array-Based Estimates of Atlantic Ocean Heat Transport at 26.5°N, Journal of Climate, 24, 2429 –2449, https://doi.org/10.1175/2010JCLI3997.1, 2011.
- Sgubin, G., Swingedouw, D., Drijfhout, S., Hagemann, S., and Robertson, E.: Multimodel analysis on the response of the AMOC under anincrease of radiative forcing and its symmetrical reversal, Climate Dynamics, 45, https://doi.org/10.1007/s00382-014-2391-2, 2014

 Weaver, A. J., Sedláčcek, J., Eby, M., Alexander, K., Crespin, E., Fichefet, T., Philippon-Berthier, G., Joos, F., Kawamiya, M., Matsumoto, K., Steinacher, M., Tachiiri, K., Tokos, K., Yoshimori, M., and Zickfeld, K.: Stability of the Atlantic meridional overturning circulation: A model intercomparison, Geophysical Research Letters, 39, https://doi.org/https://doi.org/10.1029/2012GL053763, 2012.

Relating to salinity

- Skliris, N., Marsh, R., Josey, S. A., Good, S. A., Liu, C., and Allan, R. P.: Salinity changes in the World Ocean since 1950 in relation tochanging surface freshwater fluxes, Climate Dynamics, 43, 709–736, https://doi.org/10.1007/s00382-014-2131-7, 2014.
- Stott, P. A., Sutton, R. T., and Smith, D. M.: Detection and attribution of Atlantic salinity changes, Geophysical Research Letters, 35,https://doi.org/https://doi.org/10.1029/2008GL035874, 2008.
- Terray, L., Corre, L., Cravatte, S., Delcroix, T., Reverdin, G., and Ribes, A.: Near-Surface Salinity as Nature's Rain Gauge to Detect Human Influence on the Tropical Water Cycle, Journal of Climate, 25, 958 977, https://doi.org/10.1175/JCLI-D-10-05025.1, 2012.

Regarding Figure projections, we have reproduced all maps using a Robinson projection, rather than a native grid. Finally, following the reviewer's suggestion we have tried to improve the manuscript with respect to the terminology we use and its specificity, particularly regarding the type of variability we are considering (e.g. spatial/temporal etc) and the exact timescales being considered.