



Observation System Simulation Experiments in the Atlantic 1 Ocean for enhanced surface ocean pCO_2 reconstructions. 2

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11 Abstract. To derive an optimal observation system for surface ocean pCO_2 in the Atlantic Ocean and the Atlantic 12 13 sector of the Southern Ocean eleven Observation System Simulation Experiments (OSSEs) were completed. Each OSSE is a Feed-Forward Neural Network (FFNN) that is based on a different data distribution and provides ocean 14 15 surface pCO_2 for the period 2008-2010 with a 5 day time interval. Based on the geographical and time positions from three observational platforms, volunteering observing ships (VOS), Argo floats and OceanSITES moorings, 16 17 pseudo-observations were constructed using the outputs from an online-coupled physical-biogeochemical global ocean model with 0.25° nominal resolution. The aim of this work was to find an optimal spatial distribution of 18 observations to supplement the widely used Surface Ocean CO2 Atlas (SOCAT) and to improve the accuracy of 19 ocean surface pCO_2 reconstructions. OSSEs showed that the additional data from mooring stations and an 20 21 22 23 improved coverage of the Southern Hemisphere with biogeochemical ARGO floats corresponding to least 25% of the density of active floats (2008-2010) (OSSE 10) would significantly improve the pCO₂ reconstruction and reduce the bias of derived estimates of sea-air CO₂ fluxes by 74% compared to ocean model outputs.

24 Introduction 1

25 26 27 28 29 30 31 32 33 34 35 36 37 38 The ocean is a major sink of anthropogenic CO₂ (Ciais et al., 2013; Friedlingstein et al., 2020). For the period 2010-2019 the ocean uptake was 2.5 ± 0.6 GtC/yr with a strong intensification (from 1.9 to 3.1 GtC/yr) along with the increase of CO₂ emissions (Friedlingstein et al., 2020). The ocean carbon sink estimate is derived from Global Ocean Biogeochemical Models (Hauck et al., 2020) and data-based reconstructions of surface ocean partial pressures of carbon dioxide (pCO₂). The data-based reconstructions rely on the interpolation of surface ocean pCO_2 - derived from measurements of surface ocean CO₂ fugacity - by a variety of methods (e.g. Watson et al., 2020; Gregor et al., 2019; Denvil-Sommer et al., 2019; Bittig et al., 2018; Landschützer et al., 2013, 2016; Rödenbeck et al., 2014, 2015; Fay et al., 2014; Zeng et al., 2014; Nakaoka et al., 2013; Schuster et al., 2013; Takahashi et al., 2002, 2009). These methods provide converging estimates of the global ocean carbon sink and its variability at seasonal and interannual time scales (Rödenbeck et al., 2015; Denvil-Sommer et al., 2019). They are, however, sensitive to the observation coverage in space and time which contributes to inconsistent results over regions with sparse data (Denvil-Sommer et al., 2019; Rödenbeck et al., 2015) and to persistent uncertainties at global scale (Gregor et al., 2019; Hauck et al., 2020).

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40 The majority of observations contributing to the Surface Ocean CO₂ Atlas (SOCAT) (Bakker et al., 2016) are still 41 42 43 obtained by underway sampling systems on board of volunteering observing ships. The data density is not homogenous, with Southern latitudes being less well sampled in space and also in time. Sparse data coverage and the lack of observations covering the full seasonal cycle challenge mapping methods and result in noisy 44 reconstructions of surface ocean pCO₂ and disagreements between different models (Denvil-Sommer et al., 2019, 45 Rödenbeck et al., 2015). The ship-based sampling effort is progressively complemented by autonomous observing 46 platforms, such as biogeochemical ARGO floats equipped with pH sensors. The expansion of the observing system 47 to autonomous platforms is of particular relevance in regions that are undersampled either because of the presence 48 of fewer regular shipping lines (e.g., South Atlantic) or because adverse weather conditions prevent a year around 49 sampling (e.g., Southern Ocean). The benefits of combining ship-based measurements of pCO_2 and data from





50 biogeochemical ARGO floats was recently demonstrated for the assessment of Southern Ocean CO₂ fluxes (Bushinsky et al., 2019).

51 52 53 54 55 56 57 58 59 This study extended the scope to the Atlantic basin, including the Atlantic sector of the Southern Ocean. It explored design options for a future augmented Atlantic scale observing system which would optimally combine data streams from various platforms and contribute to reduce the bias in reconstructed surface ocean pCO_2 fields and sea-air CO2 fluxes. A series of Observation System Simulation Experiments (OSSEs) were carried out in a perfect model framework using output from an online-coupled physical-biogeochemical global ocean model at 1/4° nominal resolution. Since all fields used by the FFNN are produced by the same model run and thus internally consistent, the comparison between reconstructed and modelled pCO_2 distributions allows to assess the theoretical 60 skill for each experiment. Starting from measurements extracted from the SOCAT database, the goal was to 61 identify how and where the new data from biogeochemical ARGO floats can improve surface ocean pCO2 62 reconstructions and how to optimally integrate them with other existing platforms. Pseudo-observations were 63 obtained by sub-sampling model output at sites of real-word observations. Surface ocean pCO2 was reconstructed 64 from these pseudo-observations at basin scale by applying a non-linear feed forward neural network (FFNN) 65 (Bishop, 1995; Rumelhart et al., 1986). The choice of the FFNN for our experiments was motivated by its overall 66 performance reported in Denvil-Sommer et al. (2019). The architecture of the FFNN method was adapted to the 67 current problem and differs from the one presented in Denvil-Sommer et al. (2019).

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69 The remainder of the article is structured into Section 2 presenting the model output, the observing systems and 70 observations as well as the design experiments, and the description of the statistical model. Results are presented and discussed in Section 3. Section 4 is dedicated to the conclusion and the presentation of perspectives.

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2 Data and methods

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75 76 77 78 79 Here we present the ensemble of observing systems that either already perform measurements to estimate pCO_2 or have the possibility to be equipped with new sensors to provide biogeochemical measurements (Williams et al., 2017). These datasets provide information on geographical, as well as time positions and hence on the distribution of pCO_2 measurements. In this section we also describe the ocean model output and how we use it in the OSSEs. As mentioned in the introduction the data from the model co-localized with real positions of observing-systems 80 are called *pseudo-observations*.

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2.1 Data

83 84 a) Observing systems

85 Three observing systems were selected for the study: (1) volunteering observing ships providing in situ 86 measurements of surface ocean CO2 fugacity (fCO2), (2) moorings (OceanSITES), and (3) profilers (Argo). These 87 88 observations form the dataset of geographical and time positions for our experiments. Surface ocean measurements of fCO₂ from multiple platforms are converted to pCO₂ and compiled in the SOCAT database (Bakker et al., 2016). 89 Moorings are not routinely equipped with sensors of CO₂ fugacity, though, we used their geographical positions **9**0 to identify possible locations for additional measurements. Biogeochemical ARGO floats are increasingly 91 equipped with pH sensors allowing computing pCO2 from pH and SST- based alkalinity. For the design 92 93 94 experiments, we considered distributions of physical ARGO floats (2008-2011) from Gasparin et al. (2019) and supposed that they were equipped with pCO_2 sensors.

95 96 (1) SOCAT database v5 (Bakker et al., 2016; (https://www.socat.info/index.php/data-access/)): the database provides a good coverage of the Northern Hemisphere. Data for the period 2001-2010 were used, representing 97 ~60% of data in SOCAT database (Fig.1a). We used the synthesis files SOCATv5 with the daily measurements. 98 There are 24 moorings in SOCATv5 that provided CO2 fugacity measurements between 2001 and 2010. These <u>9</u>9 moorings were excluded from OceanSITES data (see below).

100 (2) Argo profilers: We used the network of Argo (Gould et al., 2004) distributions provided by Mercator Ocean 101 (details can be found in Gasparin et al., 2019) for the period 2008-2010. It provides a synthetic homogeneous 102 distribution of 1 profiler per 3°x3° grid box, amounting to 310-360 measurements per day (Fig.1b) based on real 103 trajectories of Argo floats. This synthetic Argo distribution was built based on the time, date and location of Argo 104 profiles during the 2009-2011 period (Gasparin et al., 2019). To provide a homogeneous coverage Gasparin et al. 105 (2019) removed some float trajectories in well-sampled regions, for example the Gulf Stream, or added floats in





106 the low-sampled Tropical and South Atlantic regions. The target for BioGeoChemical Argo (1/4 of ARGO coverage) (Bittig et al., 2018) was derived from this distribution.

(3) OceanSITES: This dataset combines observations from open ocean Eulerian time series stations providing data since 1999 (Fig.1c). We used all available locations of moorings (except moorings included in SOCATv5) and added this information to the period of reconstruction 2008-2010 (http://www.oceansites.org/). It provided 318 additional positions to our data set.

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113For this study, the same set of predictors was used as in Denvil-Sommer et al. (2019) for training the Machine114Learning (ML) algorithm: sea surface salinity (SSS), sea surface temperature (SST), sea surface height (SSH),115mixed layer depth (MLD), chlorophyll a concentration (Chl a) and atmospheric CO2 ($pCO_{2, atm}$). These variables116are known to represent the main physical, chemical and biological drivers of surface ocean pCO_2 (Takahashi et117al., 2009; Landschützer et al., 2013).

118 b) Model output and pseudo-observations

119 Here we used the numerical output from an online-coupled physical-biogeochemical global ocean model, the 120 NEMO/PISCES model, at 5-day resolution. This configuration of the Nucleus for European Modelling of the 121 Ocean (NEMO) framework was implemented on a global tripolar grid. It coupled the ocean general circulation 122 model OPA9 (Madec et al., 1998), the sea ice code LIM2 (Fichefet & Maqueda, 1997), and the biogeochemical 123 model PISCESv1 (Aumont and Bopp, 2006). Information on the simulation is given in Gehlen et al. (2020) and 124 Terhaar et al. (2019). The geographical and time positions identified from the data mentioned before were used to 125 create pseudo-observations by sub-sampling NEMO/PISCES model output at sites of real-word observations. 126 Thus, the positions of SOCAT, Argo floats and mooring stations were chosen over 5 days centred on the 127 128 NEMO/PISCES date and sub-sampled on the model grid. The model grid coordinate closest to the real geographical position was chosen, if several measurements were co-localized at the same grid coordinate and same 129 time step it is counted as one measurement. No Argo floats were added to grid cells if there was already a 130 measurement identified in the SOCAT database. All predictors and target pCO2 were taken from model output at 131 corresponding coordinates. These outputs served as the reference for validation and evaluation of our experiments 132 and for assessing the ML method's accuracy. The simulation covers the period 1958 to 2010, the last 3 years were 133 retained for the design study.

134 2.2 Observational System Simulation Experiences

135 Table 1 summarizes experiments designed for different combinations of observing platforms.

The first test is based on individual sampling data extracted from the SOCAT database. As mentioned before these data provide a good coverage of the Northern Hemisphere. The lesser coverage in the Southern Hemisphere results in a larger dispersion of methods based on these observations only (Denvil-Sommer et al., 2019; Rödenbeck et al., 2015). This has motivated experiments with additional data from Argo profilers limited to the Southern Hemisphere. An experiment based on the full physical ARGO network was included to evaluate the method for a high spatial and temporal coverage (an optimal, yet unrealistic case).

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We have tested combinations of SOCAT data and (1) total Argo data, (2) Argo only in the Southern Hemisphere, and (3) 25% or (4) 10% of the initial (total) Argo distribution. Finally, these experiments were repeated with additional mooring data. It is worth noting (Table 1) that OSSE 4 is closest to the target of the BGC-Argo program with a BGC-Argo density corresponding to 25% of the existing Argo distribution. However, we decided to choose OSSE 3 as a benchmark against which to evaluate individual experiments. This experiment has a high data density and provides additional information on a potential future BGC-Argo network.

149 2.3 Method

150 We used a Feed-Forward Neural Network (FFNN) based on Denvil-Sommer et al. (2019) to reconstruct surface 151 ocean pCO_2 over the Atlantic Ocean. Compared to the previous study we skipped the first step consisting of the 152 reconstruction of the pCO_2 climatology. The reconstruction covered January 2008 to December 2010 with a 5-day 153 frequency and the spatial resolution of the tripolar ORCA025 model grid (nominal 1/4° resolution). The approach 154 consisted in a method that reconstructs the non-linear relationships between the target pCO_2 and predictors 155 responsible for pCO_2 variability: 156 $pCO_2 n =$

$pCO_{2,n} = f(SSS_n, SST_n, SSH_n, Chl_n, MLD_n, pCO_{2,atm,n}, (1)$ $SSS_{anom,n}, SSH_{anom,n}, Chl_{anom,n}, MLD_{anom,n}, pCO_{2,atm,anom,n} lat_n, long_{1,n}, long_{2,n})$





160 As previously (Denvil-Sommer et al., 2019), we use Keras, a high-level neural network Python library ("Keras: 161 the Python Deep Learning library", Chollet, 2015; https://keras.io) to construct and train the FFNN models. We 162 first identified an optimal configuration (number and size of hidden layers, the activation functions etc.) of the 163 FFNN model. Based on our earlier work (Denvil-Sommer et al., 2019), a hyperbolic tangent was chosen as an 164 activation function for neurons in hidden layers, and a linear function was chosen for the output layer. As an 165 optimization algorithm, the mini-batch gradient descent or "RMSprop" was used (adaptive learning rates for each 166 weight, Chollet, 2015; Hinton et al., 2012).

167 The numbers of hidden layers and parameters depend on the number of data used for training. In this work, the 168 FFNN was applied separately for each month (one model for January, one model for February, etc.). A sub-set of 169 50% of data were used for training. 25% participated in the evaluation of the model during the training algorithm, 170 and 25% were used to validate the model after training. These data were chosen regularly in time and space. Tables 171 S1 presents the numbers of training data for each month and each OSSE. To adjust the number of FFNN parameters we followed the empirical rule that suggests using a factor 10 between the number of data and the number of 172 173 parameters to avoid overfitting (Amari et al., 1997). The FFNNs for all OSSEs except OSSE 2 have four layers 174 (two hidden layers) with 1116 parameters in total. The OSSE 2 which is based on Argo data for the period 2008-175 2010, has significantly less data for training and thus, the FFNN for the OSSE 2 is different: 3 layers (one hidden 176 layer) with 541 total parameters.

177 It is worth noting that all data have to be normalized before their use in the FFNN as exemplified for SSS:

178
$$SSS_n = \frac{SSS - \overline{SSS}}{STD(SSS)} \quad (2)$$

179 SSS is the total mean of variable SSS, STD(SSS) is standard deviation of SSS.

180 Normalization is required to rank all predictors in the same scale, and it allows to avoid the possible influence of 181 one predictor with strong variability (Kallache et al., 2011).

182 Following Denvil-Sommer et al. (2019) we normalized the geographical positions (lat, long) in the following way:

183
$$lat_n = sin(lat * \pi/180)$$

184 $long_{n,1} = sin(long * \pi/180)$

$$long_{n,1} = sin(long * \pi/180)$$

$$long_{n,2} = cos(long * \pi/180)$$

186 A K-fold cross-validation was used to evaluate and validate the FFNN architecture. The cross-validation is based 187 on K=4 different subsamples where 25 % of independent data are chosen for validation. In each of the 4 cases the 188 25% of data are different and there is no overlap. Thereby, each run has 4 outputs. The different architectures of 189 the FFNN were tested and the final one was chosen based on skill assessed by the root-mean-square difference 190 (RMSD), the r^2 and the bias of 4 outputs for each architecture. To ensure a good accuracy of the method and check 191 that there is no overfitting, we compared the RMSD, r² and bias estimated from the validation dataset with those 192 estimated from the training dataset. Denvil-Sommer et al. (2019) provide a detailed description of the model 193 including the accuracy of the ML method and its ability to correctly reproduce the pCO2 variability.

194 2.4 Diagnostics

195 The comparison between OSSEs is done per biome, following Rödenbeck et al. (2015) (Fig. 2, Table 2). Biome 196 8, North Atlantic Ice, has been omitted due to poor data coverage in all OSSEs. It is expected that reconstructions 197 over this region will yield large biases susceptible to interfere with the interpretation of results from individual 198 OSSEs.

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200 In order to simplify the comparison, we used Taylor and Target Diagrams with standard deviation, biases, 201 correlation and normalized RMSD (uRMSD) of the mean of 4 FFNN outputs for each OSSE. Here uRMSD is 202 estimated as:

 $uRMSD = \sqrt{mean(\{ [pCO_{2 OSSE} - \overline{pCO_{2 OSSE}}] - [pCO_{2 NEMO} - \overline{pCO_{2 NEMO}}] \}^2)}$ (3)

204 For each OSSE and each output of the k-fold cross-validation, we estimated a time mean difference between its 205 *p*CO₂ and NEMO *p*CO₂ at each grid point: 206

 $\text{Diff}_{j,i} = \text{mean}_{T}(p\text{CO}_{2 \text{ OSSE } j,i} - p\text{CO}_{2 \text{ NEMO }}) = \frac{1}{T} \sum_{t=1}^{T} (p\text{CO}_{2 \text{ OSSE } j,i,t} - p\text{CO}_{2 \text{ NEMO } t}),$





- 207 where mean_T is a time mean over the period, T is a number of time steps, j is an index of the OSSE and i is an 208 index of output, from 1 to 4.
- 209 Further, the maximum absolute value from 4 outputs maxValuej was estimated for each OSSE: 210
 - $maxValue_j = max_i(abs(Diff_{j,i})),$

211 where maxi is a maximum value on i, the index of output, for each fixed j, the OSSE index. The index i of the 212 213 maximum absolute value of FFNN outputs is called imax.

(4)

- The final mean difference meanD_i was estimated as: 214
 - $meanD_j = sign(Diff_{j,i max}) * maxValue_j,$
- 215 where sign(x) is a function that returns the sign of a value x, -1 or 1.
- 216 The STD of the mean difference Diff_{j,i} is estimated for each OSSE as: 217 (5)
 - $STD_i = std(Diff_{i,i}),$

218 219 where j is fixed, and all outputs of FFNN i are included in the estimation of STD.

220 221 The time series of the mean value from 4 FFNN outputs for pCO_2 were provided per biome, with the maximum and minimum values from these 4 outputs in the form of shadow cloud. Also, the time series of CO₂ sea-air flux 222 are shown in the same way as the ones for $p \in Q_2$. The sea-air CO₂ flux, $fgCO_2$, was calculated after Rödenbeck et 223 al. (2015): 224

 $fgCO_2 = k\rho L(pCO_2 - pCO_{2,atm}), \quad (6)$

225 ρ is seawater density and L is the temperature-dependent solubility (Weiss, 1974). k is the piston velocity estimated 226 as (Wanninkhof, 1992):

227
$$k = \Gamma u^2 (Sc^{CO_2}/Sc^{ref})^{-0.5}.$$

228 The global scaling factor Γ was chosen as in Rödenbeck et al. (2014) with the global mean CO₂ piston velocity 229 equaling 16.5 cm h-1. Sc corresponds to the Schmidt number estimated according to Wanninkhof (1992). The 230 wind speed was computed from 6-hourly NCEP wind speed data (Kalnay et al., 1996). To simplify the 231 interpretation of results the NEMO/PISCES CO2 air-sea flux was also calculated by using formula (6) and NCEP 232 wind speed.

233 3 Results

234 Figure 3 shows the Taylor Diagram (correlation coefficient between reconstructed pCO_2 and model output, and 235 Standard Deviation of reconstructed fields) of 11 OSSEs in the region of 8 biomes (pink) and in each of these 236 biomes separately (color code corresponds to Fig. 2). The target diagrams per biomes for each OSSE are presented 237 on Figure 4. Over regions well-covered with observations (biomes 9, 10, 11) results of different OSSEs lie close 238 to each other. The OSSE 1 (+; Fig. 3a) that is based only on SOCAT data has a lower correlation coefficient over 239 the whole region (0.67, pink) and per biomes (Fig. 3a). Over regions with poor observational coverage the results 240 from OSSE 1 lie at a distance from others. OSSE 1 also shows the largest normalized RMS differences (uRMSD) 241 (Fig. 4), as exemplified for biome 17 with uRMSD of 17.33 μ atm, STD of 21.11 μ atm (compared to 24.03 μ atm 242 estimated from NEMO/PISCES data) and bias of -11.63 µatm (all values in the Fig. 3 and 4 are presented in Tables 243 3 and 4). The OSSE 2 (based on all Argo data, O) and OSSE 3 (combination of Argo and SOCAT data, X) provide 244 comparable results (Fig. 3b and c). OSSE 3 tends to have smaller uRMSD and bias and to lie closer to the STD 245 values from the NEMO/PISCES model (Fig. 4). OSSE 3 is based on the maximum of pseudo-observations for 246 training and represents most likely an unrealistic endmember. However, as mentioned before, OSSE 3 is used as 247 the benchmark to find other OSSEs with similar results and more feasible data coverage.

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249 OSSE 4 (square) and OSSE 5 (rhombus) are based on OSSE 3, the only difference being the number of Argo 250 profiles: OSSE 3, 100%; OSSE 4, 25% and OSSE 5, 10%. The results of OSSEs 4 and 5 are similar to those 251 252 obtained for OSSE 3. The largest difference is observed over biome 17 (Fig. 3, Fig. 4i): correlation coefficients are 0.85 (OSSE 3), 0.77 (OSSE 4), 0.75 (OSSE 5); biases are -0.66 µatm, -2.25 µatm, -4.02 µatm; uRMSDs are 253 10.18 µatm, 11.75 µatm, 11.8 µatm (Tables 3, 4).

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255 OSSEs 6 (triangle), 7 (inverted triangle), 8 (pentahedron) were trained on SOCAT data complemented with Argo 256 data in the Southern Hemisphere. In general, the skill scores are lower compared to OSSE 3, especially for OSSE 257 8 (10% of Argo data in the Southern Hemisphere) where results approach those of OSSE 1 (Fig. 3). Large 258 differences are obtained for biomes 12 and 17 (Fig. 3, Fig. 4e and i): in biome 12 and 17, correlation coefficients 259 for OSSE 6, 7, 8 are 0.64/0.86, 0.54/0.8, 0.52/0.66, respectively, compared to 0.79/0.85 for OSSE 3; uRMSDs are





11.46/10.01 µatm, 13.3/11.03 µatm, 13.87/15.16 µatm compared to 8/10.18 µatm for OSSE 3; biases are 3.82/-0.18 µatm, 3.77/-1.8 µatm, 2. 7/-4.12 µatm compared to -0.14/-0.66 µatm for OSSE 3 (Tables 3, 4). Over biome l2 all OSSEs show STD values lower than the one computed for NEMO/PISCES model output (Table 3). This could result from the STD of the mean output being slightly lower than the individual STDs for 4 OSSE FFNN outputs (not shown). However, individual STDs also underestimate the NEMO/PISCES STD which might suggest that the ensemble of predictors do not allow to properly represent the variability over the Equatorial Atlantic.

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267 Reconstruction skill scores are improved by the addition of data from mooring stations to OSSEs 6, 7, and 8 in 268 OSSEs 9 (hexagon), 10 (star) and 11 (triangle centroid) (Fig. 3 and 4, Tables 3 and 4). Over the ensemble of 8 269 biomes the decrease in the number of Argo data goes along with a general decrease of correlation coefficients, 270 0.88 (OSSE 9), 0.85 (OSSE 10), 0.83 (OSSE 11), and an increase of uRMSDs, 8.37 µatm (OSSE 9), 8.71 µatm 271 (OSSE 10), 9.16 µatm (OSSE 11) (Fig. 3, 4a, Tables 3 and 4). Statistics are slightly worse for OSSE 11 compared 272 to OSSEs 9 and 10, which have comparable results. While OSSE 10 shows a smaller correlation coefficient over 273 the whole region compared to OSSE 9, its STD (24.89 µatm) lies closer to the NEMO/PISCES STD (25.34 µatm) 274 and it has a smaller bias (-0.39 μ atm). Similar results are found over other biomes: in biome 12, OSSEs 9 and 10 275 have correlation coefficients close to each other (0.68 and 0.63, respectively) and larger than for OSSEs 6, 7 and 276 8, while for OSSE 11 it is 0.58. The STDs are almost equal (OSSE 9, 12.98 μ atm and OSSE 10, 12.9 μ atm) and 277 uRMSDs have a small difference compared to the one computed for OSSE 3 (8 μ atm) (Tables 3, 4). Thus, the 278 remainder of the discussion will focus on OSSE 10 in comparison to OSSEs 1 and 3. OSSE 10 provides comparable 279 results to OSSE 9 and is in good agreement with OSSE 3 while using less data for training. Figures 3 and 4 are 280 summarized in Supplementary materials (Figure S1).

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282 Figures 5a, b and c present the differences between reconstructed pCO₂ distributions (Fig.5 a - OSSE 1; b - OSSE 283 3; c - OSSE 10) and NEMO/PISCES output. The maximum in absolute value from 4 outputs for each OSSE FFNN 284 is shown (Eq. 4). There is a large improvement in the Southern Hemisphere for OSSEs 3 (Fig. 5b) and 10 (Fig. 285 5c) compared to OSSE 1 (Fig. 5a): the difference varies mostly between -3 and 3 µatm for OSSEs 3 and 10, and 286 between -15 and 15 µatm for OSSE 1 (Fig. 5). However, the average values of the mean over biomes are not 287 always better for OSSE 3 (Table 5): in biome 13, OSSE 1 shows a small positive difference of 0.11 µatm, while 288 for OSSE 3 negative differences of $-0.32 \,\mu$ atm is computed, exceeding 0.11 μ atm in its absolute value. This is due 289 to error compensation by averaging, the reduction of the positive difference in the middle of biome 13 in OSSE 3 290 increases the impact of negative small differences in this region. A large improvement is obtained in biomes 16 291 and 17: from -8.04 µatm for OSSE 1 to -1.89 µatm and -1.91 µatm for OSSEs 3 and 10 in biome 16, and from -292 14.9 µatm for OSSE 1 to -2.05 µatm and -1.55 µatm for OSSEs 3 and 10 in biome 17 (Table 5). Over the whole 293 region, 70°W-30°E 80°S-80°N, OSSE 1 has a mean difference of -6.57 µatm, it is -1.7 µatm and -2.34 µatm for 294OSSEs 3 and 10. The difference between OSSEs 3 and 10 results from the Labrador Sea and Baffin Bay: OSSE 295 10 has fewer data in this region compared to the OSSE 3. However, there is an improvement in OSSE 10 compared 296 to OSSE 1 and 3 in the Greenland Sea (Fig. 5). It results from the addition of mooring data in the Greenland Sea 297 region (Fig. 1c). 298

299 Figures 5d, e and f present the standard deviations (STD) of differences for all 4 outputs for each OSSE FFNN 300 (Fig.5 d – OSSE 1; e – OSSE 3; f – OSSE 10) (Eq. 5). Over most of the Atlantic Ocean STD varies between 0 and 301 10 µatm for OSSEs 3 and 10. In each case there is a strong STD along the coasts and in the Labrador Sea, as well 302 as the Baffin Bay. In general, the mean value of STD tends to decrease (Table 5) from OSSE 1 to OSSEs 3 and 303 10. In the Southern Hemisphere STD reaches up to 30 µatm (Figures 5d, e and f)) when only SOCAT data are 304 used in the FFNN algorithm (OSSE 1). It is significantly reduced in response to the addition of float data in OSSEs 305 3 and 10 with also less spatial variability. The results for other OSSEs are added to the Supplementary material 306 (Table S2, Fig. S2, S3).

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308 Figure 6 shows the correlation between the mean value of 4 OSSEs outputs and NEMO/PISCES pCO2 (a - OSSE 309 1, b - OSSE 3, c - OSSE 10). The additional data from Argo floats and mooring stations increase the correlation 310 coefficient from 0.68 in the case of OSSE 1 (SOCAT data only) to 0.86 and 0.85 in the case of OSSEs 3 and 10 311 (Table 6). A higher correlation was also obtained for these two OSSEs compared to OSSE 1 over the region 312 covering the Greenland Sea, the Norwegian Sea and Barents Sea (mostly biome 9). In the Southern Hemisphere 313 the correlation with NEMO/PISCES pCO2 is also larger when Argo data are included, especially in biomes 16 and 314 17: 0.7 and 0.57 for OSSE 1, 0.83 and 0.85 for OSSE 3, as well as 0.78 and 0.89 for OSSE 10 (Table 6). However, 315 there is a low correlation along the African coasts which is in agreement with our previous results for mean 316 difference and STD (Fig. 5). It reflects the predominantly open ocean data used for this exercise. A well-317 pronounced decrease in correlation is observed for biome 15 (Subtropical seasonally stratified Southern Ocean). 318 Such a decrease can result from the spatial distribution of data or from the predictor data set. We will discuss it





further in the next section. The results for other OSSEs are presented in the Supplementary material (Table S3, 520Fig. S4).

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322 In Figure 7, time series of pCO_2 for OSSEs 1, 3 and 10 are compared to corresponding NEMO/PISCES model 323 output. For each OSSE, the mean pCO_2 from 4 FFNN outputs is shown, as well as the mean bias (OSSE -324 NEMO/PISCES). Figure 7a and b presents the pCO_2 time series over the period of reconstruction 2008-2010 for 325 OSSE 1, 3, 10 compared to NEMO/PISCES pCO₂ used as reference (black) over all biomes. For OSSE 1 (SOCAT 326 data only) a large difference and an underestimation of reconstructed pCO_2 (blue) compared to NEMO/PISCES 327 pCO_2 (black) are found: the maximum error is up to -10 μ atm (Fig. 7b). To the contrary, OSSEs 3 and 10 show a 328 good agreement with NEMO/PISCES model output. Averages of pCO_2 over the 8 biomes are 372.18 μ atm for 329 OSSE 3, 372.26 µatm for OSSE 10 and 368.39 µatm for OSSE 1, compared to 372.65 µatm for NEMO/PISCES 330 (Table 7). The experiment corresponding to the BGC-Argo distribution target over the entire Atlantic basin, OSSE 331 4 (Fig. S7, S8), has a basin-wide average pCO_2 equal to 371.8 μ atm (Table 7). This corresponds to a larger 332 difference with NEMO/PISCES (-0.84 μ atm) compared to OSSEs 3 and 10.

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334 Panels (c) to (h) of Figure 7 illustrate time series of reconstructed pCO₂ for biomes with varying data coverage. 335 Biome 11, the Subtropical permanently stratified North Atlantic, (Figure 7c and d) is well covered by data. All 336 three OSSEs yield pCO2 reconstructions that are in good accordance with the NEMO/PISCES reference. The 337 amplitude and the phasing of the seasonal cycle are well reproduced. The bias varies within a range of $\pm -5 \mu$ atm 338 for OSSEs 3 and 10. A predominantly negative bias is found for OSSE 1 with values as high as -10 μ atm. The 339 pCO2 averaged over the total biome 11 area for OSSE 10 is close to NEMO/PISCES with, respectively 389.39 340 μatm and 390.11 μatm (Table 7). OSSE 1 yields a biome-averaged pCO₂ equal to 387.11 μatm, while it is 389.39 341 μ atm for the OSSE 3.

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343 Biome 13, the Subtropical permanently stratified South Atlantic, (Figure 7e and f) corresponds to a region with a 344 low data coverage. We observe a large difference between pCO_2 reconstructed by OSSE 1 (blue) and 345 NEMO/PISCES (black). While the phasing of the reconstructed seasonal cycle is satisfying, it is noisy with a 346 systematic overestimation in spring by up to 18 μ atm (Table 7). However, the total averaged pCO₂ over biome 13 347 for OSSE 1 is close to the one of NEMO/PISCES: 391.66 μ atm, respectively 389.54 μ atm. The preceding suggests 348 that while the variability of the predictors (mainly SST) is sufficient to constrain at first order the biome-average 349 pCO_2 and the phasing of the seasonal cycle, an improved coverage by *in situ* observations is needed for a smooth 350 reconstruction of the seasonal cycle's amplitude. Reconstructions are largely improved by the addition of data 351 from Argo floats (OSSE 3) and moorings (OSSE 10). Biases mostly range between -3 and 3 μ atm for these OSSEs. 352 The Southern Ocean Ice biome (biome 17) is characterized by a sparse data coverage and a bias towards the ice-353 free season. The results for biome 17 are presented in Figure 7g and h. OSSE 1 underestimates the pCO₂ in this 354 region over the full seasonal cycle. The biome-wide average is $351.44 \ \mu atm$, $-11.63 \ \mu atm$ below the 355 NEMO/PISCES reference. The reconstruction is much improved for OSSEs 3 and 10, both for the phasing and 356 amplitude of the seasonal cycle, as well as for the biome-wide averages. The latter are 362.42 µatm and 362.87 357 µatm, respectively for OSSE 3 and OSSE 10, compared to 363.08 µatm computed for NEMO/PISCES (Table 7) 358 Results for all OSSEs and for all biomes are included to the Supplementary material (Table S4, Fig. S5 - S10). B59

360 Figure 8 shows the sea-air CO₂ flux time series (negative, uptake of CO₂ by the ocean). Over all biomes in the 361 region 70°W-30°E 80°S-80°N the OSSEs 3 (red) and 10 (green) show a good agreement with NEMO/PISCES 362 $fgCO_2$: the differences vary around zero and mostly do not exceed ± 0.3 Pg/yr (Fig. 8b, d, f and h). The total 363 averaged fgCO₂ for OSSE 3 and 10 are -0.74 Pg/yr compared to -0.7 Pg/yr in NEMO/PISCES, while for OSSE 1 364 it equals -0.99 Pg/yr (Table 8). The mean value over biome 11 is slightly better for OSSE 10 than for OSSE 3 365 compared to NEMO/PISCES: -0.06 Pg/yr (OSSE 10), -0.07 (OSSEs 3) and -0.03 Pg/yr for NEMO/PISCES. The 366 OSSE 1 (blue) shows again a large difference, it overestimates the ocean sink computed by the NEMO/PISCES 367 model mostly during the whole period (Fig. 8b). In the well data-covered biome 11, OSSE 1 also has a tendency 368 to overestimate the sea-air CO_2 flux, (Fig. 8d): the total averaged fgCO_2 is -0.18 Pg/yr for OSSE 1 while it is -0.03 369 Pg/yr in the model. While the phasing and amplitude of the seasonal cycle of sea-air fluxes of CO₂ are well 370 reproduced over biome 13 by OSSEs 3 and 10, the f_{gCO_2} reconstructed by OSSE 1 is noisy with differences with 371 respect to the model reference of up 1 Pg/yr (Fig. 8e). The biome-wide mean sea-air flux of CO₂ is close to zero 372 in NEMO/PISCES: -0.004 Pg/yr. This slight uptake of CO₂ by the ocean in the model reference is not reproduced 373 by the OSSEs which yield a source over biome 13, albeit of variable strength: 0.19 Pg/yr for OSSE 1, 0.05 Pg/yr for OSSE 3 and 0.08 Pg/yr for OSSE 10. Over the Southern Ocean biome 17 (Fig.8g and h) OSSE 1 (blue) 374 375 overestimates fgCO2 by -0.65 g/yr (Table 8). OSSE 10 (green) reproduces the local maxima and minima of the 376 fgCO₂ time series slightly better than OSSE 3, with average differences equaling -0.03 Pg/yr and -0.06 Pg/yr, 377 respectively. Results for all OSSEs and for all biomes can be found in the Supplementary material (Table S5, Fig. 378 S11 - S16).



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380 The relationship between the average number of Argo floats (5-day period) and the error in $fgCO_2$ estimates (Table 381 8, Table S5) is shown in Figure 9 for all biomes (a), biome 11 (b), biome 13 (c) and biome 17 (d). Figure 9a 382 illustrates how the increase of the number of floats usually yields a reduction in the error of fgCO₂ estimates. 383 Considering the whole region, OSSE 10 provides the best results with less Argo floats (-0.04 PgC/yr and 48 Argo 384 floats). At the biome-scale, the addition of floats does, however, not systematically reduce the error. This holds 385 for biome 11 (Fig. 9b), which is well-covered by observations, but also for biome 13 with a much sparser data-386 coverage (Fig. 9d). For biome 11, OSSE 10 has the best trade-off between error reduction and number of floats. 387 The largest error (0.22 PgC/yr) is obtained for OSSE 2 (only Argo data). It suggests that the period chosen for this 388 study is too short to adequately capture the seasonal variability. This hypothesis is supported by the fact that while 389 OSSE 3 and OSSE 2 share the same number of Argo data, OSSE 3 is further constrained by SOCAT data that 390 cover the period 2001-2010. These additional data from SOCAT introduce the information needed for the 391 reconstruction of the seasonal cycle. For biome 13 (Fig. 9c), the combination of SOCAT data and Argo float data 392 improves estimates of fgCO₂. The errors in OSSE 10 are comparable to OSSE 3 (benchmark), 0.08 PgC/yr (OSSE 393 10) and 0.06 PgC/yr (OSSE 3). The error is even lower for OSSE 11 (0.04 PgC/yr), the experiment with the 394 smallest number of Argo floats (19), than for OSSE 3. Unfortunately, results provided by OSSE 11 are less good 395 over the remainder of the biomes. The tendency for a decrease of $fgCO_2$ error with an increase of the number of 396 Argo floats is confirmed for biome 17 (Fig. 9d). The additional data from mooring stations (OSSE 9, 10 and 11) 397 improve in particular OSSEs with smaller numbers of floats. An error of -0.03 PgC/yr is computed for OSSE 10 398 (49 floats) over biome 17. The results for other biomes can be found in the Supplementary material (Fig. S17).

399 4 Summary and Conclusion

400 The aim of this work was to identify an optimal observational network of pCO_2 over the Atlantic Ocean. The 401 analysis was based on results obtained with a Feed-Forward Neural Network model trained on the SOCAT 402 database. The SOCAT database has a sparse coverage in the Southern Hemisphere. The approach consisted in 403 adding the position of mooring data and Argo trajectories in the Atlantic Ocean to find an optimal distribution and 404 combination of data to reconstruct pCO_2 with a good accuracy. The advantage of the SOCAT database is the long 405 time period covered by its records, which allows to reconstruct the interannual variability with a good accuray. 406 However, its data coverage is biased towards the North Atlantic, which leads to larger reconstruction errors over 407 the South Atlantic by the Neural Network. As a long-term perspective, the inclusion of data from Argo floats will 408 contribute to a more homogenous data distribution and provide a better spatial coverage. The Argo floats and 409 moorings used here do not currently provide pCO_2 measurements, hence only their positions were used to build 410 OSSEs. A series of experiments were performed using outputs from the NEMO/PISCES model. The model 411 simulations were sub-sampled at co-localized sites of observing systems for all predictors (SSS, SST, SSH, CHL, 412 MLD, $pCO_{2, atm}$) used in the FFNN and the target (pCO_{2}) to create pseudo-observations with a 5-day time step. 413 These experiments should be useful for the planning of future deployments of BGC-Argo floats (Biogeochemical-414 Argo Planning Group, 2016) and moorings equipped with the sensors to measure pCO₂ or CO₂ fugacity.

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416 The results suggest that the addition of data from Argo floats could significantly improve the accuracy of FFNN-417 based ocean pCO₂ reconstructions over the Atlantic Ocean and the Atlantic sector of the Southern Ocean compared 418 to the case when only SOCAT data are used (OSSE 1). However, even with an improved coverage over the open 419 ocean, additional observations are required in coastal regions and shelf seas which are not accessible to floats, as 420 well as in regions with a strong seasonal variability of pCO_2 and all predictors. This is exemplified by OSSE 2, 421 the experiment based on all Argo data, which yields high RMSDs in biome 9, the Subpolar seasonally stratified 422 North Atlantic (Fig. 3, Fig.4b, Table 4). The RMSD of 17.1 μ atm reflects the poor coverage of this region by Argo 423 floats (Fig. 1b), in particular the Greenland Sea and the North Sea, with a large part of the latter not suitable for 424 the deployment of floats. The combination of SOCAT data and Argo floats (OSSE 3) improves the reconstruction 425 with a RMSD reduced to 9.59 µatm (Fig. 4b, Table 4).

426 The reduction of the number of Argo data used in our experiments slightly decreases the accuracy (Fig. 3 and 4, 427 Tables 3 and 4). A lower number of Argo data corresponds, however up more realistic distribution of instruments still comparable to OSSE 3. The best 428 and to the target of the global BGC-Argo network. The result 429 compromise between the statistics yielded by the comparison between reconstructed pCO_2 and NEMO/PISCES 430 outputs, as well as the feasibility of a future observation network is found for OSSE 10. In this experiment SOCAT 431 data are combined with simulated mooring data and 25% of the initial distribution of Argo floats placed only in 432 the Southern Hemisphere (around 49 floats with a 5-day sampling period). The use of only SOCAT data results in 433 a correlation coefficient of 0.67 compared to NEMO/PISCES output and a standard deviation of 26.08 µatm (25.34 434 µatm for NEMO/PISCES) over the region of study. While the successful OSSE 10 has a correlation coefficient of 435 0.85 and a standard deviation of 24.89 µatm. These results are close to the unrealistic benchmark case with total





436 and only Argo float distribution over 2008-2010: 0.87 and 23.79µatm. The total pCO₂ over the whole region is 437 also close to NEMO/PISCES, ~370 µatm and ~371 µatm, respectively. The air-sea flux fgCO2 is -0.83 Pg/yr 438 (OSSE) and -0.76 Pg/yr (NEMO). OSSE 10 shows the bias reduction of derived estimates of sea-air CO₂ fluxes 439 by 74% from OSSE 1(fgCO₂ is -1.03 Pg/yr) compared to NEMO/PISCES.

440The OSSE 10 network could be further improved by instrumenting the Baffin Bay, the Labrador Sea, the 441 Norwegian Sea, as well as regions along the coast of Africa (10°N to 20°S), all regions with pronounced biases in 442 all OSSEs, with moorings or gliders along the shelf break and on the continental shelf.

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444 The inclusion of errors from in situ measurements is one of the next steps of this work. It will include the errors 445 for predictor values (SSS, SST, SSH, CHL, MLD, pCO_{2, atm}) that are measured directly or derived from remote 446 sensing (e.g., SST, chlorophyll, SSH), as well as the errors related to the computation of pCO₂ from pH and 447 alkalinity. The new FFNN runs could provide important information on the effect of biases from observational 448 datasets and identify predictors or targets that have large errors and that must be corrected.

449

450 Author contribution:

451 ADS, MG, MV contributed to the development of the methodology and designed the experiments, and ADS 452 carried them out. ADS developed the model code and performed the simulations. ADS prepared the paper with 453 contributions from all coauthors.

454 Acknowledgments:

455 This study was funded by the AtlantOS project (EU Horizon 2020 research and innovation program, grant 456 agreement no. 2014-633211) and GreenGrog PPR (GMMC). At present ADS is under funding from the Royal 457 Society (grant no. RP\R1\191063) at the UEA. MV acknowledges support from the CoCliServ project, which is 458 part of ERA4CS, an ERA-NET initiated by JPI Climate and cofunded by the European Union. Authors thanks 459 Florent Gasparin for his help with reference data of Argo distribution.

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(c) Figure 1: Spatial distribution of data sets used for training (number of measurements per grid points): (a) SOCAT data (5-day time step) for the period 2001-2010; (b) Argo data (5-day time step) for the period 2008-2010; (c) mooring positions modelled for the period 2008-2010 (5-day time step).



- 592 593 594 Figure 2: Map of biomes (after Rödenbeck et al., 2015; Fay and McKinley, 2014) focused on the region [70°W-30°E] and used for comparison between OSSEs.







 $\begin{array}{c} 595\\ 596\\ 597\\ 598\\ 598\\ (k) - OSSE 11. \end{array}$















Figure 5: Differences between OSSE FFNN outputs and NEMO/PISCES pCO₂ and its standard deviation (STD) in patm: (a), (b), (c) - its maximum in absolute value (maximum bias) from 4 outputs for each OSSE FFNN, Eq. (4); (g), (h) - standard deviation of differences for all 4 outputs for each OSSE FFNN, Eq. (5). (a), (d) – OSSE 1; (b), (e) – OSSE 3; (c), (f) – OSSE 10.



Figure 6: Correlation coefficient between OSSE FFNN outputs and NEMO/PISCES pCO₂: (a) - OSSE 1, (b) - OSSE 3,
 (c) - OSSE 10.







(g) (h) Figure 7: (a), (c), (e) - mean of 4 FFNN outputs for OSSE 1 (blue), 3 (red), 10 (green); shadow is the maximum and minimum values from 4 FFNN outputs for each OSSE. Black curve - NEMO/PISCES pCO_2 . (b), (d), (f) - mean of





- 614 615 616 differences between OSSE 1 (blue), 3 (red), 10 (green) of 4 FFNN outputs and NEMO/PISCES pCO₂; shadow is the
- maximum and minimum values of differences from 4 FFNN outputs for each OSSE. (a), (b) estimates are available over all biomes presented in Figure 2 except biome 8; (c), (d) biome 11; (e), (f) biome 13; (g), (h) biome 17.







618 Figure 8: (a), (c), (e) - mean of sea-air CO₂ flux from 4 FFNN outputs for OSSE 1 (blue), 3 (red), 10 (green); shadow is 619 the maximum and minimum values from 4 FFNN sea-air CO₂ flux estimates for each OSSE. Black curve -





NEMO/PISCES fgCO2. (b), (d), (f) - mean of differences between OSSE 1 (blue), 3 (red), 10 (green) fgCO2 of 4 FFNN outputs and NEMO/PISCES fgCO2; shadow is the maximum and minimum values of differences from 4 FFNN fgCO2 for each OSSE. (a), (b) - estimates are available for all biomes presented in Figure 2 except biome 8; (c), (d) - biome 11; (e), (f) - biome 13; (g), (h) - biome 17.



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Figure 9: Averaged number of Argo profiles per 5-day time step over 2008-2010 versus averaged differences between each OSSE $fgCO_2$ and NEMO $fgCO_2$ (in Pg/yr). (a) - all biomes; (b) - biome 11; (c) - biome 13; (d) - biome 17.

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29 Table 1: Information on Observation System Simulation Experiments.

Data	OSSE number	Period for training	averaged number of Argo floats per 5 days
SOCAT	OSSE 1	2001-2010	0
Argo (3°x3°)	OSSE 2	2008-2010	404
SOCAT + Argo (3°x3°)	OSSE 3	2001-2010 (SOCAT) + 2008-2010 (Argo)	403
SOCAT + Argo 25% (3°x3°)	OSSE 4	2001-2010 (SOCAT) + 2008-2010 (Argo)	101
SOCAT + Argo 10% (3°x3°)	OSSE 5	2001-2010 (SOCAT) + 2008-2010 (Argo)	40
SOCAT + Argo South (3ºx3º)	OSSE 6	2001-2010 (SOCAT) + 2008-2010 (Argo South)	195

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SOCAT + Argo 25% South (3°x3°)	OSSE 7	2001-2010 (SOCAT) + 2008-2010 (Argo South)	48
SOCAT + Argo 10% South (3°x3°)	OSSE 8	2001-2010 (SOCAT) + 2008-2010 (Argo South)	19
SOCAT + Argo S + Moorings	OSSE 9	2001-2010 (SOCAT) + 2008-2010 (Argo South, Moorings)	195
SOCAT + Argo S 25% + Moorings	OSSE 10	2001-2010 (SOCAT) + 2008-2010 (Argo South, Moorings)	48
SOCAT + Argo S 10% + Moorings	OSSE 11	2001-2010 (SOCAT) + 2008-2010 (Argo South, Moorings)	19

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1 Table 2: Biomes from Fay and McKinley (2014) used for time series comparison (Fig. 2).

Number	Name
8	(Omitted) North Atlantic ice
9	Subpolar seasonally stratified North Atlantic
10	Subtropical seasonally stratified North Atlantic
11	Subtropical permanently stratified North Atlantic
12	Equatorial Atlantic
13	Subtropical permanently stratified South Atlantic
15	Subtropical seasonally stratified Southern Ocean
16	Subpolar seasonally stratified Southern Ocean
17	Southern Ocean ice

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Table 3: Correlation coefficient and Standard Deviation (µatm) of 11 OSSEs from Table 2 estimated over 8 Atlantic Ocean biomes and at basin scale; the results are presented in Fig. 3.

Biome OSSE	All biomes	9	10	11	12	13	15	16	17
NEMO STD	25.34	28.17	17.29	19.59	17.89	18.84	15.20	10.79	24.03
OSSE 1	0.67/	0.88/	0.92/	0.89/	0.46/	0.68/	0.31/	0.70/	0.57/
	26.08	27.44	16.67	18.42	12.48	16.11	15.28	11.76	21.11
OSSE 2	0.89/	0.91/	0.96/	0.97/	0.83/	0.92/	0.76/	0.87/	0.90/
	22.82	22.28	17.09	19.14	15.42	18.19	8.89	9.43	19.56
OSSE 3	0.87/	0.93/	0.96/	0.95/	0.79/	0.91/	0.73/	0.83/	0.85/
	23.79	25.78	17.00	19.03	14.33	17.91	11.21	10.55	21.06





OSSE4	0.82/	0.92/	0.95/	0.93/	0.70/	0.88/	0.63/	0.80/	0.77/
	23.99	25.91	17.11	18.31	12.13	17.62	11.62	10.99	21.2
OSSE 5	0.80/	0.92/	0.94/	0.92/	0.65/	0.86/	0.59/	0.75/	0.75/
	24.18	26.48	17.16	18.83	11.39	16.95	11.86	11.3	20.58
OSSE 6	0.85/	0.89/	0.93/	0.91/	0.64/	0.91/	0.72/	0.82/	0.86/
	24.72	27.40	16.66	18.73	12.34	17.51	11.56	10.84	22.41
OSSE 7	0.82/	0.89/	0.93/	0.91/	0.54/	0.88/	0.66/	0.80/	0.80/
	24.48	27.87	16.32	18.19	11.17	17.33	11.71	11.12	20.90
OSSE 8	0.77/	0.89/	0.93/	0.91/	0.52/	0.86/	0.57/	0.79/	0.66/
	25.10	27.90	16.19	18.3	11.66	16.92	11.74	11.17	22.63
OSSE 9	0.88/	0.92/	0.95/	0.94/	0.68/	0.92/	0.72/	0.84/	0.91/
	24.51	28.17	16.11	17.67	12.98	17.84	11.31	10.89	21.63
OSSE 10	0.85/	0.91/	0.94/	0.94/	0.63/	0.88/	0.65/	0.78/	0.89/
	24.89	28.28	17.10	18.41	12.90	17.36	11.35	11.01	22.25
OSSE 11	0.83/	0.91/	0.93/	0.93/	0.58/	0.86/	0.56/	0.74/	0.88/
	24.67	28.39	16.4	18.10	13.20	16.79	11.29	10.96	21.92

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Table 4: Normalised RMS differences and Biases (μatm) of 11 OSSEs from Table 2 estimated over 8 Atlantic Ocean
 biomes and at basin scale; the results are presented in Fig. 4.

Biome OSSE	All biomes	9	10	11	12	13	15	16	17
OSSE 1	14.13/	11.63/	6.32/	6.63/	15.41/	12.5/	15.97/	8.08/	17.33/
	-4.25	-3.26	-0.39	-2.93	0.17	2.12	1.32	-5.41	-11.63
OSSE 2	10.11/	17.10/	4.21/	3.94/	7.26/	4.98/	12.63/	4.31/	10.00/
	0.36	-2.02	0.09	0.19	0.22	0.38	-0.43	-0.21	2.50
OSSE 3	8.32/	9.59/	4.56/	4.24/	8.00/	5.73/	11.87/	4.20/	10.18/
	-0.46	-0.32	-0.30	-0.71	-0.14	0.57	-0.85	-0.97	-0.66
OSSE 4	9.40/	10.08/	5.08/	5.01/	10.41/	6.96/	12.59/	4.87/	11.75/
	-0.84	-0.53	-0.05	-0.88	-0.29	0.85	-0.40	-0.93	-2.25
OSSE 5	9.82/	10.43/	5.50/	5.35/	11.11/	7.93/	12.72/	5.71/	11.80/
	-1.46	-0.83	0.50	-0.98	-0.25	0.85	-0.54	-1.69	-4.02
OSSE 6	9.12/	11.40/	5.93/	6.48/	11.46/	5.75/	12.06/	4.35/	10.01/
	-0.54	-2.57	0.02	-1.86	3.82	0.53	-0.51	-0.56	-0.18
OSSE 7	9.75/	11.79/	6.16/	6.26/	13.30/	6.90/	11.97/	4.90/	11.03/
	-1.22	-2.64	-0.10	-2.68	3.77	0.58	-0.56	-1.68	-1.80
OSSE 8	11.36/	11.62/	6.02/	5.91/	13.87/	7.84/	12.55/	5.42/	15.16/
	-1.89	-2.59	0.49	-2.80	2.70	0.90	-0.89	-2.03	-4.12
OSSE 9	8.37/	10.58/	5.47/	5.13/	11.34/	5.37/	12.18/	4.16/	8.51/
	-0.44	-2.52	-0.001	-1.33	2.91	0.41	-0.88	-0.75	0.37
OSSE 10	8.71/	10.79/	5.54/	4.94/	12.64/	6.82/	12.25/	4.89/	8.61/





	-0.39	-2.35	0.79	-0.71	3.35	1.01	-0.92	-0.90	-0.21
OSSE 11	9.16/	10.85/	5.91/	5.32/	14.28/	7.59/	12.49/	5.13/	9.23/
	-1.18	-3.21	-0.68	-1.97	2.41	0.002	-1.18	-1.56	-0.77

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639Table 5: Differences (Eq. 4) between OSSE FFNN outputs and NEMO/PISCES pCO_2 and its standard deviation (STD)640(Eq. 5) in μ atm.

Biome	Region 70°W- 30°E 80°S- 80°N	All 8 biomes	9	10	11	12	13	15	16	17
OSSE 1	-6.57/	-6.57/	-4.84/	-1.46/	-4.21/	-2.03/	0.11/	-1.35/	-8.04/	-14.90/
	14.49	13.54	10.17	6.98	7.62	13.88	13.88	14.96	8.99	20.83
OSSE 3	-1.70/	-1.50/	-1.36/	-0.90/	-1.48/	-1.49/	-0.32/	-1.93/	-1.89/	-2.05/
	8.12	7.15	7.52	4.62	4.64	7.09	5.58	7.16	4.42	10.59
OSSE	-2.34/	-1.54/	-3.54/	-0.10/	-1.52/	1.93/	-0.04/	-2.15/	-1.91/	-1.55/
10	8.64	7.50	8.59	6.18	5.42	9.38	6.51	8.18	5.21	8.99

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642 Table 6: Correlation coefficient between OSSEs and NEMO/PISCES pCO₂.

Biome	Region 70°W- 30°E 80°S- 80°N	All 8 biomes	9	10	11	12	13	15	16	17
OSSE 1	0.68	0.67	0.88	0.92	0.89	0.46	0.68	0.31	0.70	0.57
OSSE 3	0.86	0.87	0.93	0.96	0.95	0.79	0.91	0.73	0.83	0.85
OSSE 10	0.85	0.85	0.92	0.94	0.94	0.63	0.88	0.65	0.78	0.89

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Table 7: pCO₂ averaged over the region 70°W-30°E 80°S-80°N and biomes from Fig. 2 for the NEMO/PISCES model
 and OSSEs 1, 3 and 10, as well as the corresponding averaged differences between OSSEs and NEMO/PISCES (in μatm).

Biome	Region 70°W- 30°E 80°S- 80°N	All 8 biomes	9	10	11	12	13	15	16	17
NEMO	371.13	372.65	350.36	373.18	390.11	397.18	389.54	376.14	376.99	363.08
OSSE 1	367.09/	368.39/	347.10/	372.78/	387.17/	397.36/	391.66/	377.46/	371.58/	351.44/
	-4.04	-4.25	-3.26	-0.39	-2.93	0.17	2.12	1.32	-5.41	-11.63
OSSE 3	370.62/	372.18/	350.04/	372.88/	389.39/	397.04/	390.10/	375.29/	376.02/	362.42/
	-0.51	-0.46	-0.32	-0.30	-0.71	-0.14	0.57	-0.85	-0.97	-0.66





OSSE	370.14/	372.26/	348.01/	373.98/	389.39/	400.53/	390.55/	375.22/	376.09/	362.87/
10	-0.99	-0.39	-2.35	0.79	-0.71	3.35	1.01	-0.92	-0.90	-0.21

Table 8: fgCO₂ averaged over the region 70°W-30°E 80°S-80°N and biomes from Fig. 2 for the NEMO/PISCES model and OSSEs 1, 3, 4 and 10, as well as the corresponding averaged differences between each OSSEs and NEMO/PISCES

(in Pg/yr).

Biome	Region 70°W- 30°E 80°S- 80°N	All 8 biomes	9	10	11	12	13	15	16	17
NEMO	-0.76	-0.70	-2.34	-1.14	-0.03	0.53	-0.004	-0.74	-0.50	-0.52
OSSE 1	-1.03/	-0.99/	-2.57/	-1.17/	-0.18/	0.42/	0.19/	-0.68/	-1.15/	-1.17/
	-0.26	-0.28	-0.23	-0.03	-0.15	-0.10	0.20	0.06	-0.64	-0.65
OSSE 3	-0.80/	-0.74/	-2.36/	-1.16/	-0.07/	0.49/	0.05/	-0.82/	-0.61/	-0.59/
	-0.04	-0.04	-0.02	-0.02	-0.03	-0.04	0.06	-0.07	-0.10	-0.06
OSSE	-0.83/	-0.74/	-2.50/	-1.09/	-0.06/	0.56/	0.08/	-0.82/	-0.60/	-0.56/
10	-0.06	-0.04	-0.15	0.04	-0.03	0.03	0.08	-0.07	-0.09	-0.03