A clustering-based approach to ocean model-data comparison around Antarctica

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Abstract

The Antarctic Continental Shelf Seas (ACSS) are a critical, rapidly-changing element of the Earth system. Analyses of global-scale general circulation model (GCM) simulations, including those available through the Coupled Model Intercomparison Project, Phase 6 (CMIP6), can help reveal the origins of observed changes and predict the future evolution of the ACSS. However, an evaluation of ACSS hydrography in GCMs is vital: previous CMIP ensembles exhibit substantial mean-state biases (reflecting, for example, misplaced water masses) with a wide inter-model spread. Because the ACSS is also a sparsely sampled region, grid-point based model assessments are of limited value. Our goal is to demonstrate the utility of clustering tools for identifying hydrographic regimes that are common to different source fields (model or data), while allowing for biases in other metrics (e.g., water mass core properties) and shifts in region boundaries. We apply K-means clustering to hydrographic metrics based on the stratification from one GCM (Community Earth System Model version 2; CESM2) and one observation-based product (World Ocean Atlas 2018; WOA), focusing on the Amundsen, Bellingshausen, and Ross Seas. When applied to WOA temperature and salinity profiles, clustering identifies “primary” and “mixed” regimes that have physically interpretable bases. For example, meltwater-freshened coastal currents in the Amundsen Sea, and a region of high salinity shelf water formation in the southwestern Ross Sea emerge naturally from the algorithm. Both regions also exhibit clearly differentiated inner- and outer-shelf regimes. The same analysis applied to CESM2 demonstrates that, although mean-state model biases in water mass T-S characteristics can be substantial, using a clustering approach highlights that the relative differences between regimes, and the locations where each regime dominates, are well represented in the model. CESM2 is generally fresher and warmer than WOA and has a limited fresh-water-enriched coastal regimes. Given the sparsity of observations on the ACSS, this technique is a promising tool for the evaluation of a larger model ensemble (e.g., CMIP6) on a circum-Antarctic basis.
1. Introduction

The Antarctic Continental Shelf Seas (ACSS, defined here as the ocean regions adjacent to Antarctica with water depth shallower than 2,500 m) are critical components of the climate system, playing an essential role in ice sheet mass balance, sea ice formation, and ocean circulation (Rignot et al., 2008; Hobbs et al., 2016; Bindoff, Rosenberg and Warner, 2000). ACSS ocean state, and the climate system components that are coupled to it, are changing rapidly. In the Amundsen-Bellingshausen Seas sectors, the atmosphere (Bromwich, et al., 2013) and subsurface ocean (Schmidtko et al., 2014) are warming, the sea ice-free period is rapidly increasing (Stammerjohn et al., 2012), ice shelves are thinning (Rignot et al., 2013; Paolo, Fricker and Padman, 2015; Adusumilli et al., 2020), and the grounded portion of the ice sheet is losing mass at an accelerating rate (Shepherd et al., 2018; Sutterley et al., 2014; Gardner et al., 2018). The Ross Sea has also experienced long-term changes in fresh water content (Jacobs and Giulivi, 2010; Castagno et al., 2019) and an increase in sea ice production and extent (Parkinson, 2019; M. Holland et al., 2017).

Assessing the causes of observed changes in climate and the coastal cryosphere, and their future evolution, requires coupled, global, atmosphere-ocean general circulation models (GCMs). However, recent GCMs exhibit large biases relative to modern observations, and a wide inter-model spread (Agosta, Fettweis and Datta, 2015; Sallée et al., 2013; Rickard and Behrens, 2016; Hosking et al., 2016; Little and Urban, 2016; Barthel et al., 2019). These modern-state biases suggest the potential for large uncertainties in the projected ocean state, including the vertical and horizontal distribution of ocean heat, with significant consequences for the accuracy of projections of the effect of the ACSS on other climate components (e.g., Sallée et al., 2013; Agosta, Fettweis and Datta, 2015). For example, DeConto and Pollard (2016) projected extreme rates of 21st-century ice sheet mass loss from the Pacific sector for a high-emission scenario. However, their projections were forced using a single GCM (CCSM4) that required a +3°C correction to subsurface water temperatures in the Amundsen Sea to match observed hydrography and modern ice shelf melt rates. This significant bias correction indicates an underlying mean-state error (e.g., a misplaced water mass) that casts substantial doubt on the projected future ocean state in that specific model.

The first step toward identifying the physical processes underlying GCM representation errors is assessing the magnitude and spatial distribution of biases. However, such a strategy must account for strong horizontal and vertical gradients in ACSS hydrographic properties (see, e.g., Orsi and Wiederwohl, 2009; Thompson et al., 2018), and the sparseness and variable quality of available observations (e.g., Schmidtko et al., 2014). Strong gradients are
evident in the Amundsen, Bellingshausen, and Ross Seas (ABRS) sector of the ACSS. There, the time-mean ocean
state of the objectively analyzed temperature and salinity field, as represented in the 0.25-degree World Ocean Atlas
version 2018 (WOA hereafter), suggests that the ABRS can be roughly separated into two geographical regions, the
Amundsen-Bellingshausen Seas and the Ross Sea (Figure 1a). In the Ross Sea, dense water formation occurs
locally, through brine rejection from winter sea ice formation in coastal polynyas, resulting in regionally averaged
water well below 0°C at water depths of 100 m to 700 m (Figure 1c). At the same depth range in the Amundsen-
Bellingshausen Seas, water temperatures can reach +1.2°C due to the presence of Circumpolar Deep Water (CDW).

In addition to these stark contrasts in regional mean temperature (and salinity), there is also significant
spatial variability within each region of the ABRS, and across the continental shelf break. For example, Figure 1
indicates a high standard deviation in ocean temperature on the continental shelf with water depth shallower than
700 m (0.5°C in the Amundsen-Bellingshausen Seas and 1.4°C in the Ross Sea). Much of this variability is
attributable to the lateral temperature gradient from the subsurface layer of CDW over the continental slope to the
modified (cooled) water masses inshore. In the alongshore direction, vertical profiles of water properties in the
Amundsen-Bellingshausen Seas are similar, with cold and fresh water overlying relatively warm and salty water. In
the Ross Sea, water properties are different on its southwestern and eastern sides, mainly distinguished by their
salinity (Figure 1d).

The sparseness of measurements on the ACSS also aggravates errors associated with gridded observational
products. Coastal regions, in particular, are subject to substantial errors. Sun et al. (2019) showed that salinity biases
between WOA objective analysis and the World Ocean Database increase toward coastlines. The gridded objective
analysis field neglects the dynamical processes governing water mass modifications and circulations induced by
complex continental shelf bathymetry (Dunn and Ridgway, 2002; Schmidtko, Johnson and Lyman, 2013). In
sparsely sampled regions, grid-point based comparisons (e.g., Little and Urban, 2016) are thus of limited utility, and
may underestimate uncertainty in the reference (observational) product. We suggest that it is often more meaningful
to assess GCMs using a regionally averaged approach.

Previous model-data comparisons on the ACSS have employed strategies such as averaging over a-priori
defined regions (e.g., Barthel et al., 2019). Such methods are ill-equipped to assess model biases resulting from
misplaced water masses. An alternative method is objective clustering, which can be used to identify regions of
similar hydrographic metrics. For example, Hjelmervik and Hjelmervik (2013) demonstrated the application of a
clustering-based approach using Argo profiles to segregate the North Atlantic into groups with similar vertical $T$ and $S$ profiles separated by fronts.

The results of clustering analyses are dependent on the metrics chosen for the analysis. For example, metrics could be chosen as the layer thicknesses of water masses defined by $T$, $S$ and neutral density. Schmidtko et al. (2014) partitioned water masses in the Southern Ocean into Winter Water (WW), CDW, and Antarctic Shelf Bottom Water (ASBW) using only temperature. However, their metrics of subsurface water temperature maxima and minima are ineffective on the continental shelf, where temperature profiles are often complex and show strong lateral variability in water properties (Figure 1d). Sallée et al. (2013) proposed a method to use potential vorticity evaluated from density profiles and the local salinity minimum at 30°S to distinguish vertical water masses in the Southern Ocean.

On the ACSS, however, the hydrographic structure is complicated not only by the variability of primary water masses but also by transport, mixing, and strong and highly localized interactions between the atmosphere, ocean, sea ice and ice shelves. Each of these processes is sensitive to vertical and horizontal density gradients and gradients in bathymetry. Metrics that capture the importance of stratification concurrently with dominant water mass characteristics provide the best test of whether a model is representing the principal dynamical processes governing hydrographic variability in the ACSS. Here, we develop new metrics targeted at ACSS hydrography and assess the utility of a clustering-based approach for model-data comparison.

2. **Methods**

In this paper, we identify hydrographic regimes and their $T$-$S$ properties using metrics derived from three-dimensional grids of measured and modeled temperature and salinity (section 2.1) using a K-means clustering method (section 2.2). We then apply a clustering algorithm based on data density to exclude outliers (2.3) from the resulting “groups”.

2.1 **Data and processing**

We use decadal-mean, objectively analyzed $T$ and $S$ fields from WOA for 1995-2004, with 0.25-degree resolution in both latitude and longitude. The data sources, quality controls, and processing procedures of the WOA are detailed in Locarnini et al. (2019) for temperature and Zweng et al. (2019) for salinity. This study focuses on the
domain from the west of Cape Adare (163°E) on the western side of the Ross Sea to the southern end of Alexander Island (76°W), at depths between 0 and 2,500 m. The landward limit of the study domain is the Antarctic coast and the ice shelf edges as identified in Figure 1a.

We compare the Community Earth System Model version 2 (CESM2; Danabasoglu et al., 2019) to WOA for the same period and domain. The time-mean model salinity and temperature fields over the 1995-2004 period are calculated from the monthly output of the Coupled Model Intercomparison Project Phase 6 (CMIP6) historical simulation (experiment tag r1i1p1f) (Eyring et al., 2016) at the native ocean model resolution (roughly 1 degree in longitude and 0.5 degree in latitude). CESM2 uses the CICE5 (Hunke et al., 2015) sea ice model; however, dynamic and thermodynamic interactions with land ice are not represented (Danabasoglu et al., 2019). The CMIP6 forcing data is described in Eyring et al. (2016) and can be download from input4MIPs CoG (https://esgf-node.llnl.gov/search/input4MIPs).

We used the Gibbs SeaWater (GSW) Oceanographic Toolbox of TEOS–10 (McDougall and Barker, 2011) to calculate seawater properties. The absolute salinity ($S_A$) has unit of g/kg, and conservative temperature ($\Theta$) is in °C. All seawater temperatures are referenced to the sea surface.

### 2.2 Prototype-based clustering technique (K-means)

The K-means clustering analysis used in this study is an unsupervised learning technique that classifies data into meaningful groups based on their similarity. In this study, the similarity is defined by two metrics of the water column: 1) salinity at the temperature minimum; and 2) salinity at the temperature maximum. The rationale for these choices is discussed in section 3.1.

The K-means algorithm is initialized by randomly selecting data in N dimensions (here, N=2, for the two specified metrics) for a specified number of groups ($K$). For each group ($k_i$), the Sum of Squared Distance (SSD) of each data point ($\xi$) to the group’s centroid ($c_i$) is calculated:

$$SSD = \sum_{i=1}^{K} \sum_{\xi \in k_i} \text{dist}(c_i, \xi)^2 \quad \text{with} \quad c_i = \frac{1}{m_i} \sum_{\xi \in k_i} \xi$$

Eqn. 1

where dist is the standard distance between data and centroid in N-dimensional Euclidean data space and $m_i$ is the total number of data points in group $k_i$. The algorithm iterates to minimize SSD by adjusting the centroids,
recalculating the distances, and redistributing data points among the groups. The K-means algorithm will have multiple solutions because it is initialized with randomly selected data. We apply the K-means 1,000 times and choose the solution with the lowest SSD for analysis.

The K-means algorithm requires specification of the number of groups ($K$). We use Silhouette scores $s_i(n)$ (Eqn. 2) to assess the appropriate values of $K$.

$$s_i(n) = \frac{b(\xi) - a(\xi)}{\max\{a(\xi), b(\xi)\}}$$

In Eqn. 2, $n$ represents the number of data points in group $k_i$, $a(\xi)$ is the mean dist from a data point $\xi$ to all other data points within the group $k_i$, and $b(\xi)$ is mean dist from $\xi$ to all other data points outside the group $k_i$. Silhouette scores are evaluated for each data point $\xi$ in the group $k_i$ and range between -1 and 1. If $\xi$ lays perfectly at the centroid of group $k_i$, then $s_i(n)$=1.

A rigid interpretation of the Silhouette algorithm would choose the value of $K$ that corresponds to the highest mean value of $s_i(n)$. However, the optimal $K$ value can vary with different clustering evaluation methods (e.g., Elbow method: Thorndike, 1953) and different domains. The selection of $K$ is thus based not only on the results of Silhouette assessment but also on the ability to interpret the groups as representative of different underlying physical processes (see section 3).

2.3 Density-based clustering technique

In subsequent sections, we use a T-S diagram to compare the properties of groups given by the K-means algorithm. We applied a data density-based clustering technique (DBSCAN) (Ester et al., 1996) to define the “core” of a group and to exclude outliers on the T-S diagram. Note that DBSCAN is only used to highlight the core of a given group and facilitate comparisons of water properties between WOA and CESM2.

The T-S core of each hydrographic regime identified by the K-means clustering is determined by the DBSCAN algorithm using two parameters: a radius ($\varepsilon$), and a minimum number of neighboring points (MinPts). The DBSCAN algorithm builds up pools of data by initially choosing a random data point. If the initially chosen data point has less than MinPts within $\varepsilon$, then it is defined as an outlier. If this data point has more than MinPts within $\varepsilon$, then a pool of data is initialized consisting of the initial point and the points within $\varepsilon$ (neighbors). The pool grows by continually clustering neighboring points until these points have fewer than MinPts within $\varepsilon$. The
algorithm continues until all data points are either clustered into pools of data or labeled as outliers. In the current study, we choose MinPts = 10 and $\varepsilon = \sqrt{S^2 + T^2}$. The value of $\varepsilon$ is then selected (Table 1) so that the largest pool of data contains at least 97% of non-outlier points (Table 2). This pool of data constitutes the core of each group.

3 Results

3.1 Defining water column metrics

Our goal in this analysis is to utilize key features of local water columns to identify regions with similar hydrographic properties. Such metrics must be able to capture stratification, and the changes in $T$ and $S$ in both along- and cross-shelf directions. For the ACSS, the metrics must include salinity because it is the dominant factor influencing water column stability and reflects critical processes such as brine input during sea ice formation, and freshwater inputs from melting sea ice and ice shelves. By itself, however, salinity poorly represents the vertical composition of water masses since it increases monotonically with water depth over most of the ACSS (Figure 1); salinity alone is insufficient to identify regimes with sub-surface heat reservoirs that are characteristic of regions with high ice shelf basal melt rates (Rignot et al., 2013; Dinniman et al., 2016; Holland et al., 2020; Adusumilli et al., 2020). The metrics we use in this study – salinity at the vertical temperature minimum and salinity at the vertical temperature maximum – are similar to those used by Timmermans et al. (2014) to segregate surface water from Alaska coastal water in the Central Canada Basin of the Arctic Ocean.

Along-shelf variations of water properties are evident in salinity at the vertical temperature minimum (Figure 2b). In the Amundsen-Bellingshausen Seas, the depth of minimum temperature (Figure 2c) is commonly above 200 m, where salinity is often less than 34.2 g/kg. In contrast, in the southwestern Ross Sea, the minimum temperature is usually located below 350 m and coincides with much higher salinity (>34.8 g/kg). The northwestern Ross Sea contains a regime with a local temperature minimum at shallower depths approaching the shelf break, but its salinity (between 34.2 to 34.6 g/kg) is higher than near-surface water in the Amundsen-Bellingshausen Seas.

The salinity at the vertical temperature maximum shows pronounced variations in the cross-shelf direction (Figure 2d-f). The maximum water temperature (Figure 2d) is commonly found at depths above 200 m close to the coast and ice shelves (Figure 2f), and deeper toward the shelf break and over the continental slope where the water depth increases. The salinity at the vertical maximal temperature (Figure 2e) shows similar variations in the cross-
shelf direction, with lower salinity (<34.7 g/kg) near the coast and ice shelves and higher salinity (>34.8 g/kg) on the continental shelves and near the shelf break.

### 3.2 Evaluating the optimum number of groups

We used the mean value of Silhouette score $s_i(n)$ in Eqn. 2 to evaluate an appropriate number of groups ($K$) for WOA and CESM2, testing $2 \leq K \leq 13$ (Figure 3). For WOA, the highest value of $s_i$ occurs when $K=3$; for CESM2, $K=6$ has the highest Silhouette score (Figure 3a-b). The spatial distribution of groups 3, 5 and 6 in the ABRS are shown in Figure 3c-h.

When WOA data are clustered into three groups (Figure 3c), the K-means algorithm segregates the water close to the Antarctic coast from the water on the shelf and continental slope. The coastal domains are further distinguished into Amundsen-Bellingshausen coastal waters and Ross coastal waters. By increasing the number of groups to five (Figure 3e), a narrow domain between coastal and shelf waters emerges. In the Ross Sea, waters on the shelf and across the shelf break are segregated into two groups. For $K=6$ (Figure 3g), the southeastern coastal domain of the Ross Sea (orange) is further separated from the narrow domain between coastal and shelf waters in the Amundsen-Bellingshausen Seas, while the locations of the other groups are generally unchanged.

Examining the groups with respect to the two metrics used in the K-means clustering (Figure 4) shows that, when $K=3$, the groups are separated by the perpendicular lines from the incenter of the triangular $T-S$ distributions (Figure 4a). As the total number of groups increases, data points are progressively divided into smaller subsets, with an asymmetry that is influenced by their original distribution in our two-metric parameter space, as well as gaps and discontinuities (Figure 4c and e).

In CESM2, the clusters in the ABRS differ from those for WOA, particularly for $K=3$ and $K=6$. For $K=3$ (Figure 3d), the entire Amundsen-Bellingshausen Seas region is segregated from the Ross Sea, while the southwestern Ross Sea is still recognized as an independent group. For $K=6$, the Amundsen Sea is segregated from the Bellingshausen Sea. With $K=5$ (Figure 3f), CESM2 clustering is qualitatively similar to WOA, with a coastal group emerging in the Amundsen-Bellingshausen Seas; however, its areal extent is much smaller than in WOA. In the Ross Sea, the water on the continental shelf is separated from the water on the continental slope, similar to WOA. CESM2 shows a similar range to WOA in metric space (Figure 4), although with much larger gaps. In particular, CESM2 has substantially fewer data points with intermediate and low salinity (Figure 4b). Increasing $K$ for...
clustering analysis of CESM2 output subdivides high salinity regimes at $T_{\text{max}}$ based on the distribution of salinity at $T_{\text{min}}$ (Figure 4d and f).

Based on the Silhouette scores, the optimum clustering for CESM2 is 6 groups; however, the WOA data have a maximum Silhouette score for $K=3$. Segregating the WOA into 5 or 6 groups is reasonable, as the clustering algorithm continually distinguishes finer differences in the coastal regimes (Figure3e and g). But the segregation of CESM2 into 6 groups (Figure3h) is physically unfair since the water properties below the surface layers are nearly indistinguishable between the Amundsen and Bellingshausen Seas (Figure 1d). Figure 4 also indicates that the segregation of Amundsen-Bellingshausen Seas regions in CESM2 is a result of discontinuities between groups 1 and 5 (Figure 4f). We thus choose to use 5 groups for the rest of the study. Our findings from analyzing the temperature and salinity properties in the following sections further support this decision.

### 3.3 Physical interpretation of WOA groups

Vertical profiles of temperature and salinity are shown for each WOA group in Figure 5. The mean vertical structure of each group is clearly different; furthermore, the standard deviations at each depth within groups are much smaller than those of regional mean profiles (Table 3). With these vertical structures as context, we examine $T$-$S$ properties at all depths from each WOA group in Figure 6. The DBSCAN algorithm is used to identify the “core” of non-outlier data in each group, shown with dark shading in Figure 6.

Group 1, which occupies the inshore regions of the Amundsen-Bellingshausen Seas (Figure 3e), is characterized by weak vertical gradients in both $T$ and $S$ over the ~400 m water column (Figure 5a). The water in this group has relatively low salinity (33.8 to 34.5 g/kg), temperature close to the freezing point (generally lower than -1°C) and low density (26.9 and 27.5 kg/m$^3$) (Figure 6a), which suggests that the water in this regime is strongly influenced by coastal fresh water input (Moffat et al., 2008; Jacobs and Giulivi, 2010; Jourdain et al., 2017).

Group 2, which is spatially located between the coastal waters (groups 1 and 5) and outer continental shelf waters (groups 3 and 4), represents a narrow domain of mixing (Figure 3e). This regime is characterized by relatively high standard deviations in salinity and temperature at depths between 100 m and 700 m, indicating that the location and shape of the thermocline and halocline above the typical depth of the shelf break vary within this group (Figure 5b). Below 700 m, the range of salinity and temperature are relatively small, due to reduced the limited amount of data at these depths over the relatively narrow continental slope. In the upper ocean, group 2 has a salinity from 33.8 to 34.7 g/kg, temperature -2 to -0.5°C and density 27.1 to 27.8 kg/m$^3$ (Figure 5b and Figure 6b),
lying between the properties of surface waters in groups 1 and 5. In the subsurface, group 2 has a temperature above
-0.5°C and salinity above 34.5 g/kg, which represents modified CDW on the shelf (Carmack, 1970; Orsi and
Wiederwohl, 2009; Emery, 2011).

Group 3, which is found on the outer continental shelf and the continental slope of the Ross Sea (Figure 3e),
shows high standard deviations in temperature above 700 m (Figure 5c), similar to group 2. However, the water in
this regime is generally denser than group 2. The surface water in group 3 is fresher than that of group 5 (Figure5c,
Figure 6c and f), which may result from sea ice melt and/or lateral mixing with fresher shelf water originating in the
Amundsen-Bellingshausen Seas (Assmann, Hellmer and Jacobs, 2005; Porter et al., 2019). The subsurface water
(between 100 and 600 m) of group 3 (Figure 5c and Figure 6c) does not have a clear vertical water mass transition,
and denser water exhibits a wide temperature range (-1.5 to +1.5°C) with relatively high salinity (34.6 to 35 g/kg),
suggestive of mixing between High Salinity Shelf Water (HSSW) and CDW.

Group 4, on the continental shelf of the Amundsen-Bellingshausen Seas and along most of the continental
slope of the ABRS (Figure 3e), exhibits properties consistent with off-shelf Southern Ocean water as noted by
Schmidtko et al. (2014). It has a well-defined vertical temperature structure with limited spatial variability (Figure
5d). In this region, Winter Water (WW) with salinity 33.8-34.5 g/kg, temperature -2 to -0.5°C and density 27 to 27.5
g/m³, overlays CDW (salinity 34.6 to 36.8 g/kg, temperature 0 to +2°C and density 27.8 to 27.9 g/m³), with a mean
profile showing a clear transition between them (Figure 6d).

Group 5, in the southwestern Ross Sea with some extensions to the southeast (Figure 3e), has higher
salinity than other groups (Figure 6). The almost uniform vertical temperature profile (Figure 5e) is identified as
HSSW. It is characterized by salinity 34.3 to 35.1 g/kg, temperature close to the freezing point, and density of 27.5
to 28.1 kg/m³ (Figure 6e), resulting from brine rejection in the polynyas along the coast and Ross Ice Shelf front
(Foster and Carmack, 1976). The surface portion of the waters in group 5 with salinity lower than 34.62 g/kg is often
defined as Low Salinity Shelf Water (LSSW) in the Ross Sea shelf, but we generally refer to group 5 as HSSW
because its volume is much higher than the LSSW (Orsi and Wiederwohl, 2009).

Overall, groups 1 and 5 (Figures 6a and 6e) show relatively homogeneous salinity and temperature, while
group 4 has a pronounced thermocline and halocline at shallow depth. These three groups (1, 4 and 5) represent the
three “primary” ABRS hydrographic regimes. In contrast to these primary regimes, groups 2 and 3 have more
complex vertical structures, more spatial variability in thermocline at depths above about 600 m (roughly the shelf break) and can be considered as “mixed” regimes.

3.4 Assessing groups in CESM2

To identify hydrographic regimes in CESM2, we conduct the same analyses as described for WOA in the previous section, focusing on results for $K=5$ (Figure 3f). The $T$-$S$ properties of each group in CESM2 are shown in Figure 7. CESM2 results are similar to WOA’s in that three primary regimes are present (group 1, coastal fresh-water-enriched; group 4, off-shelf; and group 5, HSSW), but they show differences in their spatial extent (Figure 3e vs. f), volume (Table 4), and $T$-$S$ properties (Figure 8).

As in WOA, HSSW (group 5) of CESM2 is localized in the southwestern Ross Sea, but its eastward extension into the southeastern Ross Sea is missing in CESM2 (Figure 3e and f), resulting in a reduced HSSW volume (Table 4). The coastal fresh water-enriched regime (group 1) is mostly absent in CESM2 and is replaced by the off-shelf regime in the Amundsen Sea.

Mismatches between CESM2 and WOA are also evident in the $T$-$S$ properties of these primary regimes. In general, HSSW in CESM2 has a fresh and warm bias relative to WOA (Figure 8d). Combined with its reduced volume relative to WOA, this bias in CESM2 HSSW properties suggests that weak modeled katabatic winds in the southwestern Ross Sea may limit sea ice production and export. Group 4 (the off-shelf regime) exhibits a fresh bias in WW in the upper water column, but the densest off-shelf water in group 4, i.e., CDW, is saltier and warmer (Figure 8c). Sea ice concentrations are biased low in CESM due to positive zonal wind stress biases in the Southern Ocean (Singh et al., 2020). This wind stress bias may, in turn, lead to an overestimate of the upwelling of warm and salty CDW onto the ACSS. The limited extent of the coastal fresh-water-enriched regime (group 1) in CESM2 may result from the absence of basal melt from ice shelves.

The mixed regimes shift geographic location in CESM2. The narrow mixing zone (group 2) between coastal fresh-water-enriched and off-shelf regimes in the Amundsen-Bellingshausen Seas is not evident in CESM2 (Figure 3e and f); the CESM2 is likely too coarse to resolve these mixing fronts. In the Ross Sea, groups are separated into on-shelf (group 2) and off-shelf (group 3) approximately along the 1,000 m isobath (Figure 3f). CESM2 fails to show the path of export of Ross on-shelf water (group 2, Figure 3f) along the northwestern continental slope (Orsi, Johnson and Bullister, 1999), as it is seen in the WOA (group 3, Figure 3e). The core of on-shelf water (group 2) also has less overlap with HSSW (group 5) in the $T$-$S$ diagram in CESM2 (Figure 7f).
compared to WOA (Figure 6f). It is possible that these differences result from the overflow parameterization in CESM2 (Briegleb, Danabasoglu, & Large, 2010). In this parameterization, locations of the on-shore source water at its formation regions and off-shore entrainment, which mixes with the source water to produce the final water mass, are defined, and overflow water is routed to fixed locations. While this parameterization allows transport of HSSW to the Southern Ocean, it is entirely artificial and does not represent on-shelf mixing processes.

3.5 Assessing clustering over the ACSS

As the K-means algorithm is based on purely statistical criteria (centroid and minimized SSD in Eqn. 1) applied to specific metrics, it is valuable to assess whether clustering results are sensitive to different study domains. As a test case, we apply the same algorithm to WOA over the entire circumpolar ACSS where total water depth is less than 2,500 m. The metrics used as input for the K-means analysis, as well as the total number of groups ($K=5$), are unchanged. The use of the uniformly-gridded WOA product, rather than observational data, avoids the possibility that the comparison is biased by regional variations in data density.

The location of five clustered water groups over the entire ACSS is shown in Figure 9a. Within the ABRS domain, the geographic locations of all groups are almost unchanged, indicating the clustering results in the ABRS are insensitive to substantial enlargement of the domain. The region identified as group 5 in the southwestern Ross Sea, which is associated with HSSW formation, remains. Outside the ABRS, the clustering approach identifies water of similar properties to group 5 in the Weddell Sea near the Filchner-Ronne Ice Shelf, the George V Coast near the Mertz Glacier tongue, and Bransfield Strait and south of Trinity Peninsula (regions marked on Figure 9b). The southern Weddell Sea experiences similar conditions to the southwestern Ross Sea, with HSSW formation in winter due to brine rejection from sea ice formation enhanced by katabatic winds and tides driving a narrow but persistent along-ice-front polynya (Nicholls et al., 2009). Along the George V Coast, HSSW is also generated by similar processes acting near the Mertz Glacier ice tongue (Bindoff, Rosenberg and Warner, 2000; Post et al., 2011).

The waters in the subsurface of Bransfield Strait and south of the Trinity Peninsula are also grouped with the HSSW regions, although their surface water is warmer and fresher than that of other HSSW regions around Antarctica. Cook et al. (2016) showed that the regional water properties around the tip of the Antarctica Peninsula, based on the World Ocean Database, are very similar to HSSW. Gordon et al. (2000) also noted that the water properties in the center of Bransfield Strait are similar to HSSW in the Weddell Sea; they inferred that these waters are formed in western Weddell Sea coastal polynyas and flow into Bransfield Strait.
4 Discussion

We have shown that the ABRS can be clustered into different regions based on salinity at the vertical water temperature minimum and maximum. This technique can help identify regions, in model and observational datasets, in which water properties are controlled by similar physical processes. It contrasts with traditional grid point-based comparisons, which do not adequately account for misplaced water masses.

In this study, WOA has been employed to assess CESM2 results. However, the hydrographic regimes identified in WOA may be misleading if they result from interpolation/extrapolation artefacts associated with non-uniform sampling of data in time and space, or if the water column structures are not adequately represented in WOA. One source of uncertainty in WOA arises from differences between true and gridded bathymetry, complicating interpolation and extrapolation of sparsely sampled data into deeper portions of the water column. In Figure 10, we compare the depths of the deepest available data in WOA and CESM2 with water depths in the International Bathymetric Chart of the Southern Ocean (IBCSO, Arndt, et al., 2013). WOA has a clear misrepresentation of the Amundsen-Bellingshausen Seas continental shelf bathymetry (Figure 10b). First, the 1000 m isobath is shifted substantially landward in the Amundsen Sea. Second, deep across-shelf troughs (e.g., in Figure 10a) are not represented in the inner shelf of WOA, which possibly affects the value of salinity at the temperature maximum because the CDW is missing in these regions of the Amundsen-Bellingshausen Seas.

It is, therefore, unclear whether groups 1 and 2 are separated from the shelf and continental slope waters of group 4 in WOA (Figure 3e) due to their upper-ocean fresh water enrichment relative to other groups, or if the groups are influenced by under-sampling of hydrography in deep troughs of the Amundsen-Bellingshausen Seas. We note that the bathymetry of CESM2 has similar issues as WOA in the Amundsen-Bellingshausen Seas (Figure 10c). Neither WOA nor CESM2 represents the water in deep troughs below about 300 m in these regions, so the differences in the groups between WOA and CESM2, i.e., the missing group 1 in the Amundsen coast and narrow group 2 in the Bellingshausen Sea, are unlikely to be due to the bathymetric misrepresentation (Figure 3e and f). We suggest, instead, that the mismatch of water properties is likely to be induced by the misrepresentation of fresh water input, or unresolved coastal currents, in CESM2 (Tseng, Bryan and Whitney, 2016; Sun et al., 2017).

We have highlighted a key advantage to assessing models with clustering-based approaches compared to traditional grid point-based methods; the ability to identify geographic displacements of hydrographic regimes and to distinguish these displacements from biases in water mass T-S properties. In addition, this approach minimizes
potential biases introduced during gridding or re-gridding of data and models to a common grid for comparison studies. For example, it is possible to circumvent interpolation-related issues associated with using scattered and/or sparse data. Such datasets might include individual observations, or model output on a native grid. For example, the deepest observational temperature measurements in the World Ocean Database 2018 (WOD), even at a 1-degree resolution, show that observations are available in coastal Amundsen-Bellingshausen Seas troughs that are not present in IBCSO (compare Figure 10d with Figure 10a); see, also, Padman et al. (2010). More broadly, the WOD-based salinity and temperature climatology of Sun et al. (2019) reveals that its use can avoid biases created by spatial interpolation of shelf water with off-shelf water.

The success of this technique at identifying locations and properties of HSSW regimes at other locations on the Antarctic continental shelf suggests that it might be used to evaluate other global and/or regional models on a circum-Antarctic basis. Other metrics might be employed depending on specific research goals. For example, the pycnocline depth, or the mean or maximum temperature below a fixed depth, may be better metrics of subsurface water masses. It will also be interesting to track water masses and their pathways with metrics based on their characteristic properties. However, we note that comparisons of the locations of groups could become complex if the approach is applied to multiple models with substantial biases between their representations of specific water masses.

5 Conclusions

We have demonstrated the utility and sensitivity of a clustering-based approach for assessing hydrographic regimes and their water properties on the Antarctic continental shelf, using the World Ocean Atlas objective analysis product (WOA) and numerical model output from the Community Earth System Model version2 (CESM2). We segregated the waters in the ABRS into 5 physically interpretable groups using the salinity at the minimum and maximum temperature of each water column in the domain. The method identifies High Salinity Shelf Water (HSSW), coastal fresh-water-enriched, and off-shelf hydrographic regimes in observations and the model. Water on the continental shelf and upper continental slope in the ABRS generally show a warm bias in CESM2 compared to WOA. The near-surface ocean in CESM2 is generally fresher than in WOA but lacks a well-defined fresh-water-enriched coastal current. In the subsurface, CESM2 is saltier in regions of Circumpolar Deep Water, but fresher than WOA in HSSW formation regions. Our comparison suggests that mean-state biases of CESM2 on the ACSS result from both local and remote processes, including overestimated zonal winds in the Southern Ocean, unrepresented
thermodynamic interactions with ice shelves, and the inadequate representation of overflows in the Ross Sea. A more specific investigation of coastal processes, Southern Ocean dynamics, and atmospheric forcing will help further identify the cause of these biases.

The clustered hydrographic regimes in the ABRS are largely unchanged when our method is applied to the entire circum-Antarctic Continental Shelf Seas. HSSW-characterized regimes emerge in WOA in the southern Weddell Sea, near Mertz Glacier tongue, and in Bransfield Strait. Future work will focus on applying this approach to a wider range of models (e.g., CMIP6 output and circum-Antarctic simulations) and establishing techniques to work with scattered observational data. Finally, we note that the clustering results for the ACSS based on the WOA decadal data (1995-2004) are consistent with the results based on the most modern WOA decadal data (2005-2017). However, clustering, applied to a variety of metrics, provides the potential to identify more subtle temporal changes in hydrographic fields such as changes in regime extent in the absence of significant changes in water mass characteristics in the ACSS.

Acknowledgments

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References


### Tables and Figures

#### Table 1 The radius $\varepsilon$ used in the DBSCAN for WOA and CESM2

<table>
<thead>
<tr>
<th></th>
<th>Group 1</th>
<th>Group 2</th>
<th>Group 3</th>
<th>Group 4</th>
<th>Group 5</th>
</tr>
</thead>
<tbody>
<tr>
<td>WOA</td>
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<td>0.05</td>
<td>0.04</td>
<td>0.03</td>
<td>0.03</td>
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<tr>
<td>CESM2</td>
<td>0.045</td>
<td>0.04</td>
<td>0.06</td>
<td>0.035</td>
<td>0.04</td>
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</table>

#### Table 2 The coverage (%) of the majority group of DBSCAN in the total non-outlier data

<table>
<thead>
<tr>
<th></th>
<th>Group 1</th>
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<th>Group 3</th>
<th>Group 4</th>
<th>Group 5</th>
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</thead>
<tbody>
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<td>WOA</td>
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<td>97.9</td>
<td>99.9</td>
<td>100</td>
<td>100</td>
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<tr>
<td>CESM2</td>
<td>100</td>
<td>97.3</td>
<td>99.5</td>
<td>99.9</td>
<td>99.7</td>
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#### Table 3 The salinity and temperature standard deviation of WOA (at depth of 500 m if not specified)

<table>
<thead>
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<th>Geography</th>
<th>Amundsen &amp; Bellingshausen</th>
<th>Ross</th>
<th>Amundsen &amp; Bellingshausen</th>
<th>Ross</th>
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<tbody>
<tr>
<td>Salinity (g/kg)</td>
<td>0.16</td>
<td>0.11</td>
<td>0.84</td>
<td>1.37</td>
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<tr>
<td>Temperature (°C)</td>
<td>0.10</td>
<td></td>
<td>1.42</td>
<td></td>
</tr>
<tr>
<td>K-means groups</td>
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<td></td>
<td></td>
<td></td>
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<tr>
<td>1</td>
<td>0.10 (200 m)</td>
<td>N/A</td>
<td>0.22 (200 m)</td>
<td>N/A</td>
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<tr>
<td>2</td>
<td>0.07</td>
<td></td>
<td>1.34</td>
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<tr>
<td>3</td>
<td>N/A</td>
<td>0.08</td>
<td>N/A</td>
<td>0.97</td>
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<tr>
<td>4</td>
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<tr>
<td>5</td>
<td>N/A</td>
<td>0.10</td>
<td>N/A</td>
<td>0.17</td>
</tr>
</tbody>
</table>

#### Table 4 The percentage of clustered water in the total ocean volume in the ABRS.

<table>
<thead>
<tr>
<th></th>
<th>Group 1</th>
<th>Group 2</th>
<th>Group 3</th>
<th>Group 4</th>
<th>Group 5</th>
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</thead>
<tbody>
<tr>
<td>WOA</td>
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<td>3.6</td>
<td>21.0</td>
<td>62.1</td>
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<tr>
<td>CESM2</td>
<td>0.3</td>
<td>7.2</td>
<td>33.2</td>
<td>50.4</td>
<td>8.9</td>
</tr>
</tbody>
</table>
Figure 1 (a) the study domain of Amundsen-Bellingshausen Seas and Ross Sea with bathymetry above 2,500 m. The magenta line indicates the 1,000 m IBCSO depth contour. (b) and (c) show geographically averaged decadal (1995-2004) WOA salinity and temperature profiles in the Amundsen-Bellingshausen Seas (orange; corresponding to the orange stippled region in (a)) and the Ross Sea (cyan; corresponding to the cyan stippled region in (a)). Dashed lines indicate ±1 standard deviation of values at each depth in each region. (d) T-S properties of selected water columns (corresponding to colored circles in panel (a)).
Figure 2 Clustering metrics in WOA. Minimum temperature at each grid point (a), and the salinity (b) and water depth at the minimum temperature. d-f) as a-c, but for quantities at the temperature maximum.
Figure 3 K-means clustering evaluation for WOA and CESM. Silhouette analysis is shown in (a) and (b) for WOA and CESM, respectively. The geographic regions corresponding to 3, 5 and 6 groups for WOA, (shown in c, e and g), and for CESM (shown in d, f and h).
Figure 4. ABRS groups in metric space. Each point corresponds to a grid point, with a color corresponding to its group number, for K=3, 5 and 6, for WOA, (shown in a, c and e), and for CESM2 (shown in b, d and f).
Figure 5 Mean (solid lines) WOA salinity (in blue) and temperature (in red) profiles for five groups (from a to e) shown in Figure 3 (e). ±1 standard deviation at each depth is shown with dashed lines.
Figure 6 T-S properties for the five WOA groups (from a to e) shown in Figure 3 (e). The yellow dotted lines show the profile of mean temperature and salinity in each group, and the dark shaded areas are the cores of water property from the density-based clustering results. The cores of all five groups are overlaid on the same plot in (f).
Figure 7 As Figure 6, but for the five groups identified in CESM2 (from a to e) shown in Figure 3 (f).
Figure 8 The core of water properties in WOA (red) and CESM2 (blue). Note that groups 2 and 3 have been combined for CESM2.
Figure 9 (a) WOA-based groups on the entire ACSS (same color code as Figure 3e). (b) Four places are identified as HSSW regime with color codes blue: southwestern Ross Sea; red: Weddell Sea near the Filchner-Ronne Ice Shelf, the George V Coast; cyan: Bransfield Strait and south of Trinity Peninsula; and green: Mertz Glacier tongue. (c) T-S properties of group 5 (HSSW) regions, with their geographic location and color code matched in (b).
Figure 10 Bathymetry between 400 m and 1,000 m of: (a) IBCSO (500 m horizontal resolution), (b) WOA (0.25-degree horizontal resolution), (c) CESM2 (1 x 0.5-degree lon/lat resolution), and (d) the WOD bin-averaged into 1-degree horizontal resolution with all types of instrument with temperature measurements). The magenta line indicates the 1,000m IBCSO depth contour.