



The Zone of Influence: Matching sea level variability from coastal altimetry and tide gauges for vertical land motion estimation

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Abstract.

Vertical land motion (VLM) at the coast is a substantial contributor to relative sea level change. In this work, we present a refined method for its determination, which is based on the combination of absolute satellite altimetry (SAT) sea level measurements and relative sea level changes recorded by tide gauges (TG). These measurements complement VLM estimates from GNSS (Global Navigation Satellite System) by increasing their spatial coverage. Trend estimates from SAT and TG combination are particularly sensitive to the quality and resolution of applied altimetry data as well as to the coupling procedure of altimetry and tide gauges. Hence, a multi-mission, dedicated coastal along-track altimetry dataset is coupled with high-frequency tide gauge measurements at 58 stations. To improve the coupling-procedure, a so-called 'Zone of Influence' is defined to identify coherent zones of sea level variability on the basis of relative levels of comparability between tide gauge and altimetry observations. Selecting 20% of the most representative absolute sea level observations in a 300 km radius around the tide gauges results in the best VLM-estimates in terms of accuracies and uncertainties. At this threshold, VLM_{SAT-TG} estimates have median formal uncertainties of 0.59 mm/year. Validation against GNSS VLM estimates yields a root-mean-square ($RMS_{\Delta VLM}$) of VLM_{SAT-TG} and VLM_{GNSS} differences of 1.28 mm/year, demonstrating the level of accuracy of our approach. Compared to a reference 250 km radius selection, the 300 km Zone of Influence improves trend accuracies by 12% and uncertainties by 28%. With progressing record lengths, the spatial scales of coastal sea level trend coherency increase. Therefore the relevance of the ZOI for improving VLM_{SAT-TG} accuracies decreases. Further individual Zone of Influence adaptations offer the prospect of bringing the accuracy of the estimates below 1 mm/year.

1 Introduction

Coastal vertical land motion (VLM) significantly contributes to relative sea level change (SLC). VLM is in many places of the same order of magnitude (1-10 mm/yr) as the sea level rise itself and displays significant spatial variations (Santamaría-Gómez et al., 2012). Consequently, VLM affects coastal impacts of climate-sensitive processes and can regionally accounts for large fractions of the observed and projected coastal SLC signal (Wöppelmann and Marcos, 2016; Slangen et al., 2014). Thus, the accurate estimation of VLM is vital, not only to disentangle climatic and geodynamic SLC signatures, but also to obtain more robust estimates of past and future relative SLC and their associated uncertainties (Church et al., 2013; Santamaría-Gómez



et al., 2017a). In this work, we present a novel approach of VLM estimation using coastal satellite altimetry, tide gauges and the Global Navigation Satellite System (GNSS).

VLM is caused by the superimposition of natural processes and anthropogenic influences in the Earth System and operate on manifold spatial and temporal scales (Pugh and Woodworth, 2014). Mechanisms such as the Glacial Isostatic Adjustment (GIA), the postglacial rebound of the Earth to changing ice and water load, cause distinct large-scale VLM, which can be assumed to be uniform on centennial timescales (Peltier, 2014). Recent acceleration of land ice mass loss was shown to additionally enhance deformation rates, posing new challenges for sea-level studies due to its time-varying signal (Riva et al., 2017). Surface mass changes are also caused by terrestrial freshwater storage changes and can have small-scale effects on VLM. Groundwater pumping for instance, contributes not only to local small-scale VLM and gravity changes, but also modifies sea level rise in distant areas (e.g. Wada et al. (2012); Veit and Conrad (2016)). Other small-scale VLM effects such as erosion or tectonic movements can be locally confined to several kilometers with more subtle, not necessarily linear temporal behaviour (Brooks et al., 2007; Kolker et al., 2011; Poitevin et al., 2019).

In response to the substantial impact on relative sea level and the large spectrum of VLM sources, several strategies have been developed to estimate VLM. The ability to capture the diversity of VLM processes, however, strongly depends on the method and geodetic technique used in the VLM estimation. Furthermore, the coverage and associated accuracies of VLM estimates differ across the methods. Given that global absolute sea level trends range in the order of 1 to 3 mm/yr, one prerequisite for VLM estimation is that associated trend uncertainties should be at least one order of magnitude lower than those subtle signals (Wöppelmann and Marcos, 2016). Hence, dense and accurate VLM estimates are required to complement modelled or measured rates of absolute sea level rates, which is ultimately crucial for coastal planning. Improving the reliability of VLM estimates and their associated uncertainties is thus one major concern of this study. In the following, we briefly contrast the three major approaches of deriving coastal VLM globally.

1.1 Estimating Coastal Vertical Land Motions

The majority of global sea-level-studies utilized geodynamic GIA-models to correct, for example, tide gauge records for secular land motion trends or to extrapolate future relative SLC based on climate-projections (e.g. Church and White (2011); Hay et al. (1990); Carson et al. (2015)). GIA still represents the only long-term geological process for which VLM can be modeled on a global scale. However, one caveat is that GIA-VLM models were shown to be still biased by imperfect assumptions of ice history and the Earth's structure (King et al., 2012) and are thus model-dependent (Jevrejeva et al., 2014). Another foreseeable disadvantage is that the sole application of GIA-models neglects other sources of VLM (e.g. tectonics, erosion or anthropogenic impacts, Wöppelmann and Marcos (2016)). This led, for instance, to discrepancies in estimated rates of historical global mean sea level (GMSL) change, when comparing model-based solutions against measurements from GNSS (Hamlington et al., 2016).

For more than a decade, these direct geodetic estimates (GNSS, such as GPS, GLONASS or GALILEO) have been exploited to determine vertical velocities (Wöppelmann et al., 2007; Snay et al., 2007; Mazzotti et al., 2008). GNSS measurements denote the most precise source of VLM detection and are well established in local to global scale studies (e.g. Bouin (2010); Fenoglio



et al. (2012); Santamaría-Gómez et al. (2017b)). Wöppelmann and Marcos (2016) identified considerable low formal errors of GNSS-VLM rates (0.21 mm/year) when auto-correlation was taken into account. Santamaría-Gómez et al. (2012) estimated a precision of 0.6 mm/yr of GNSS-based VLM (from at least three years of continuous data), by comparing 36 globally distributed co-located GNSS velocity estimates. Thus, because of its considerable accuracy, vertical GNSS velocities frequently served as benchmark estimates for many sea-level applications, e.g. for GIA-model evaluation or local VLM-corrections of TG records (Sánchez L., 2009; Sanli and Blewitt, 2001).

For the latter use a necessary working hypothesis is that GNSS-VLM represents the same movements as experienced at the tide gauge (Wöppelmann and Marcos, 2016). Because VLM is shown to potentially possess high spatial variability even on small scales (tens of kilometers), GNSS-stations should be ideally very close to the tide gauge. This requirement, however, reduces the number of available co-located stations (130 GNSS stations within a 1 km range of GLOSS (Global Sea Level Observing System) tide gauges, Wöppelmann et al. (2019)) and thus confine the global coastal coverage to mostly Europe, Japan and North America.

To extend the number of VLM estimates, several studies advanced the application of combining satellite altimetry (SAT) and tide gauge (TG) observations (Cazenave et al., 1999; Nerem and Mitchum, 2003; Kuo et al., 2004; Pfeffer and Allemand, 2016; Wöppelmann and Marcos, 2016; Kleinherenbrink et al., 2018). The principle of this approach is to subtract the absolute SLC gathered by the altimeter from relative SLC observations at the tide gauge. Optimally, the differenced time series (SAT minus TG) yields the vertical displacement of the tide gauge with respect to the reference of the altimeter, when no instrumental drifts are present. Due to the availability of global and continuous absolute sea level measurements, this method not only provides a complementary source to GNSS measurements, but also improves the geographical distribution of the data, as virtually every valid TG is usable.

While all of these three sources of information, GIA-models, GNSS and 'satellite altimetry minus tide gauge' (SAT-TG) techniques have individual merits, synergetic applications are valuable to further substantiate VLM estimates. GNSS-observations are necessary to validate both GIA-models and the SAT-TG approach (Santamaría-Gómez et al., 2012; Wöppelmann and Marcos, 2016; Kleinherenbrink et al., 2018). Recent studies combined all three approaches to reconstruct GMSL (Dangendorf et al., 2017), or to densify the estimation of contemporary rates of vertical land motions (Pfeffer et al., 2017) or relative sea level change (Hawkins et al., 2019). Any advancement in these individual approaches, therefore, supports developments of the others and improves the global assessment of coastal VLM estimates.

In this study, we focus on enhancing the application of SAT-TG difference for VLM detection. Our investigations not only carry on the latest progress of the method, but also gain a new perspective on sea level trend and uncertainty detection in coastal zones. The next section recapitulates the latest state of VLM_{SAT-TG} estimation on which we base our innovations.

1.2 Progress in VLM estimation by satellite altimetry and tide gauge difference

The combination of SAT and TG observations for VLM determination was steadily improved over the last two decades and is elaborated in the latest review by Wöppelmann and Marcos (2016), hereinafter WM16. WM16 investigated performances of different gridded and along-track altimetry products (e.g. AVISO (Archiving, Validation, and Interpretation of Satellite



Oceanographic data) and GSFC (Goddard Space Flight Center). They combined sea-level anomalies (SLAs) as 1° -radius averages with monthly-mean tide gauge records from PSMSL (Permanent Service for Mean Sea Level). Among all datasets, the gridded AVISO product revealed the best correlations and residuals between altimetry and tide gauge records. Also the most precise VLM estimates were achieved, with median formal uncertainties of 0.8 mm/year. Validation against GNSS-based trends from ULR5 (Université de La Rochelle, Institut Géographique National analysis) at 113 colocated stations resulted in an $\text{RMS}_{\Delta\text{VLM}}$ of 1.47 mm/year of $\text{VLM}_{\text{SAT-TG}}$ and VLM_{GNSS} trend differences, providing the highest accuracies among the datasets.

Notwithstanding the weaker performance of the along-track product (from GSFC) achieved in WM16, Kleinherenbrink et al. (2018) made great progress in using along-track altimetry (Topex, Jason1 and 2, from the Radar Altimeter Database, RADS) to estimate VLM. Their approach aimed to overcome the spatial downsampling and associated loss of information in gridded products such as AVISO. They also advanced the procedure of combining altimetry and tide gauge data. Instead of taking 1° -averages around the tide gauges, they selected altimetry data according to different absolute correlation thresholds and implemented correlation-weighting of time series. Generally, the thresholding strategy functioned as a filter to remove stations of low comparability: With varying correlations between 0.0 and 0.7, they obtained $\text{RMS}_{\Delta\text{VLM}}$ errors from 2.1 to 1.20 mm/year (at 155 stations), which significantly improved WM16's results. For a consistent set of stations, they found a slight sensitivity of the $\text{RMS}_{\Delta\text{VLM}}$ to variations of the prescribed minimum correlation, however, with insignificant improvements of a few percent. Because they derived GNSS vertical velocities from the Nevada Geodetic Laboratory (NGL) database by taking the median of available estimates within a 50 km range to the tide gauge, they increased the number at which $\text{VLM}_{\text{SAT-TG}}$ -trends could be validated to 155.

Based on Kleinherenbrink et al. (2018) and WM16, we identify two essential factors which are vital for the quality of trend estimation by SAT-TG difference. Advancements with respect to both factors not only potentially led to improved VLM estimates in Kleinherenbrink et al. (2018), but also motivate for further innovations:

- 1 **Data quality:** In coastal regions accuracy of altimetry measurements is affected by the local departure of the radar signal from the known ocean response (due to inhomogeneities of the illuminated area) and by the inaccuracy of the standard routinely applied corrections and tidal models. Developments for the solution of both issues led to rapid improvements in the recent years by e.g. application of coastal-retracking and advanced geophysical corrections (e.g. Cipollini et al. (2017); Passaro et al. (2014); Fernandes et al. (2015)). Dedicated coastal altimetry datasets (e.g. COASTALT, ALES, PISTACH) might thus outperform previously applied products (e.g. AVISO), which do not yet benefit from these implementations.
- 2 **Data selection:** Next to issues concerning data quality, the second factor defining trend uncertainties is the sensitivity of $\text{VLM}_{\text{SAT-TG}}$ estimates to the spatial selection of altimeter data in the vicinity of the tide gauge. WM16 showed, that averaging SLA in a radius of 1° around the tide gauge resulted in higher correlations than using the best correlated or the closest grid point to the tide gauge. Kleinherenbrink et al. (2018) found a small influence of variations of absolute correlation thresholds on the trend estimates. Therefore, considering the diversity of processes, which drive coastal sea



level variability, such as waves, winds or coastal and bathymetric properties, an advanced adaptation of the choice of altimetry SLA might improve representation of the signal captured by the tide gauge.

130 These reasons motivate for further improvements of both components, quality of the data and practise of combining altimetry and tide gauge data. We aim to understand how dedicated along-track coastal altimetry can outperform standard-gridded products. We also seek to generalize an optimal selection of SLA's, underpinned by the local dynamical features of measured sea level variability.

135 In this work, we present a new approach of combining SAT and TG observations to improve VLM estimates. In contrast to previous attempts, we exploit TG and SAT data at the highest available temporal and spatial scale for globally distributed stations. We couple advanced coastal altimetry data with high-frequent tide gauge records from the Global Extreme Sea Level Analysis (GESLA). Implementation of these high-frequent tide gauge records constitutes a further innovation for VLM estimation. SO far such data has only been applied in local studies (Idžanović et al., 2019) and monthly tide gauge data were commonly exploited in this regard. We show that precision and accuracy of the trend estimates can be optimized, when using refined spatial selection criteria of altimetry sea level anomalies. With this approach we identify coherent zones of sea level
140 variability, which best represent the coastal in situ measurements. Our method is generally transferable to analysis of coastal sea level trend determination.

Sections 2 and 3 describe the individual datasets, applied processing steps and the optimization of combining altimetry and tide gauge data. Section 4 presents performance of trend estimates, i.e. estimated uncertainties and validation against GNSS data (in this study all GNSS data are based on the Global Positioning System (GPS)). Finally, we contrast our results
145 and methods with previous work and discuss the impact of the interconnection of time and space-scales on the evolution of coherency of sea level in coastal regions (section 5).

2 Data

We use different altimetry products, in order to assess the impact of special coastal products on associated VLM_{SAT-TG} trend estimates. We compare the coast-dedicated retracker ALES (Adaptive Leading Edge Subwaveform retracker, Passaro et al.
150 (2014)) along-track product against the interpolated AVISO dataset (sections 2.1 and 2.2). Altimetry data are combined with tide gauge observations from the monthly mean PSMSL and the high frequent GESLA data base, which are described in sections 2.3 and 2.4. We develop a new coupling strategy of high-rate altimetry and tide gauge records in section 3.2.

2.1 Coastal along-track altimetry - ALES

The coastal altimetry product is constructed from 1-Hz multi-mission altimetry measurements processed by DGFI-TUM
155 (OpenADB, <https://openadb.dgfi.tum.de>). We combine data from the missions ERS-2, Envisat, Saral, Jason1-Jason3 and its extended missions, which provide continuous altimetry time series of 23 years (1995-2018). The SGDR data are re-processed with the ALES retracker (Passaro et al., 2014) and an improved sea state bias correction scheme (Passaro et al., 2018). The geophysical corrections are summarized in Table 1. They are consistent with those incorporated in the latest development of



Table 1. Applied models and geophysical corrections for estimating sea level anomalies.

Parameter	Model	reference
Range and Sea State Bias	ALES	(Passaro et al., 2014)
Inverse barometer	DAC-ERA	(Carrère et al., 2016)
Wet troposphere	GPD+	(Fernandes et al., 2015)
Dry troposphere	VMF3	(Landskron and Böhm, 2018)
Ionosphere	NIC09	(Scharroo and Smith, 2010)
Ocean and Load tide	FES2014	(Carrère et al., 2015)
Solid Earth and Pole tide	IERS 2010	(Petit and Luzum, 2010)
Mean Sea surface	DTU18MSS	(Andersen et al., 2018)

the empirical ocean tide model (EOT19p) by Piccioni et al. (2019). If available, the Dynamic Atmospheric Correction consists of the ECMWF ERA-Interim reanalysis (DAC-ERA, Carrère et al. (2016)). This product especially reduces along-track sea level errors in the earlier missions (in this study ERS-2). Because this product is unavailable for the very recent missions, we implement the DAC (Carrère and Lyard, 2003) based on ECMWF for the last cycles of Jason-2 (and its extended mission) and the full Jason-3 and Saral missions. To reduce radial errors in the different missions, the tailored coastal altimetry product is cross-calibrated using the multi-mission crossover analysis (MMXO) global calibration (Bosch and Savcenko, 2007; Bosch et al., 2014).

We map all altimetry records on 1-Hz nominal tracks consistent with the CTOH nominal paths (Center for Topographic studies of the Ocean and Hydrosphere, www.ctoh.legos.obs-mip.fr) of the individual missions, using nearest-neighbour interpolation. Then, we scan the data for outliers along the tracks, to hinder spurious extreme values to propagate in time series. This scheme features:

- Absolute thresholds: Any absolute SLA exceeding ± 2 m is excluded.
- Running median test: If the absolute difference of the data and its running median (centered, over 20 points) is greater than ± 12 cm, data are excluded.
- Consecutive difference test: Outliers are detected when the difference of consecutive points exceeds ± 8 cm. The test identifies the outliers according to the differences of the other neighbouring values

The absolute thresholds (± 12 cm, ± 8 cm) correspond to $2\text{-}\sigma$ of the median running variability and $2\text{-}\sigma$ of absolute consecutive differences based on the analysis of different tracks of Jason-2 and ERS-2.

SLAs along the same track and cycle are then averaged over predefined areas as described in sections 2.5 and 2.6. We built a time series by considering all averaged SLAs from the along-track multi-mission dataset for the study period. To check for outliers in each SLA time series, we exclude values exceeding absolute values of $\pm 3\text{-}\sigma$ of the data. This cleaned 1 Hz coastal altimeter dataset is hereinafter called ALES and used for the combination with the TG-datasets described in section 3.1.



2.2 Gridded altimetry data - AVISO

The gridded Ssalto/Duacs altimeter product was produced and distributed by the Copernicus Marine Environment Monitoring Service (CMEMS, <http://marine.copernicus.eu>) and is hereinafter called AVISO as it was previously distributed by CNES AVISO+. We use monthly sea level anomalies, which are resolved on a 0.25° Cartesian grid and cover the period from 1992-
185 2019. The product already includes the DAC (Carrère and Lyard, 2003) comprising the dynamical barotropic ocean response to atmospheric forcing (modelled with MOG2D-G), as well as the inverse barometer (IB) response. Consistent with the along-track dataset ALES, FES2014 (Carrère et al., 2015) is implemented to correct for tidal signals. Other corrections and pre-processing steps are documented by CMEMS.

2.3 Monthly tide gauge data - PSMSL

190 We use monthly mean tide gauge data from the datum controlled PSMSL (Holgate et al., 2013) database. PSMSL constitutes the primary source of tide gauge data for most of sea-level research, or for the assessment of long-term trends of VLM based on SAT and TGs. The service undertakes quality control of the data including checks for consistency of the annual cycle, outlier detection or intercomparisons with neighbouring stations, which enhances the reliability of the data. Among all available stations, we select those which contain at least 180 months (15 years) of valid measurements during the altimetric era (1993
195 - present), resulting in a total number of 627 stations. We apply the same monthly-averaged DAC-correction as used for the AVISO data (Carrère and Lyard, 2003). To match the DAC-correction with the tide gauge records, we select among the 9-closest grid-points of the solution, the one which results in the highest variance reduction.

2.4 High frequent tide gauge data - GESLA

In addition to monthly-mean PSMSL TG-data, we exploit the GESLA dataset (Woodworth et al., 2016), which contains a large
200 global collection of high-frequency TG records with sampling rates ranging from hours down to 6 minutes. The latest version GESLA 2 contains in total 1355 station records and was assembled from a variety of international and national databanks (e.g. UHSLC (University of Hawaii Sea Level Center) and GLOSS) or independent sources. It thus also shares many stations with the monthly PSMSL database, the preferred dataset for VLM_{SAT-TG} computation. Unfortunately, at this time, GESLA holds only data until 2015. Therefore, we also restrict the considered period for all dataset combinations (see section 3.1) to before
205 2015. As for the PSMSL data, we select stations with at least 180 months of valid data.

In contrast to PSMSL data used in WM16, GESLA tide gauges feature no rigorous outlier rejection by default in except that of the primary data providers (Woodworth et al., 2016). Extreme values from strong signals like tsunamis or station shifts and other irregularities are still present in the data. Some of those issues are addressed on the GESLA-webpage, however, for the sake of long-term trend evaluation, we perform a further global outlier analysis. Therefore, we check all tide gauge
210 time series manually for irregularities: Station shifts from seasonal to interannual timescales are either handled by dismissing certain sections of the time series or completely excluding the tide gauge from the analysis. Single extreme events from hourly to monthly timescales are only excluded, when they deviate from the measurements by several meters, because we want to



maintain as much data as possible. If such events are present, we flag any values beyond the upper/lower 0.999 quantiles of a fitted normal distribution of the data. Occasionally we apply this quantile-outlier exclusion recursively.

215 To obtain a uniform temporal resolution, we resample this outlier-free tide gauge set to hourly records by cubic interpolation. The records are then corrected for the tidal signal as well as for the ocean response to atmospheric wind and pressure forcing. The tidal variability is suppressed by using a 40-h loess (locally estimated scatterplot smoothing) filter (Cleveland et al., 1988) as in Saraceno et al. (2008). In accordance with PSMSL-tide gauge data, we implement the same Dynamic Atmospheric Correction (Carrère and Lyard, 2003). This solution features a 6h sampling frequency, which is therefore down-sampled to
 220 hourly anomalies by cubic interpolation. For the global dataset, we obtain a mean variance reduction of 37.8% and a mean correlation of 0.6. As in WM16 and Ponte (2006), we find a distinct latitude dependence of correlations and variance reduction, with decreasing performance in low-latitude regions. We note, that the total variance reduction, which we apply on the high-rate tide gauge data is naturally less than in WM16, who corrected monthly mean, detrended and deseasoned data.

3 Methods

225 3.1 Dataset combinations

To understand the sensitivity of the VLM estimations on (1) quality and resolution of the data and (2) the selection procedure, we analyse the performances of four different dataset combinations: ALES-PSMSL-250km, ALES-GESLA-250km, AVISO-PSMSL-250km and ALES-GESLA-ZOI.

The first three combinations are constructed to compare the performances of the along-track (ALES) against the gridded
 230 altimetry product (AVISO) combined with monthly tide gauge observations. With ALES-GESLA-250km we also investigate the possible advantage of using the GESLA high rate tide gauge product. For all these experimental sets, SLA time series are merged or averaged within a 250 km radius around the tide gauges, which is thus a selection procedure independent of the actual comparability of SLAs.

To produce the ALES-GESLA-250km dataset, we derive differences of the merged, non-uniformly sampled SLAs and the
 235 hourly-sampled GESLA tide gauge records, by cubic interpolation of the latter. We down-sample these high-rate differenced time series to monthly means. For ALES-PSMSL-250km on the other hand, we first compute monthly-means from SLAs and subsequently subtract these monthly SLAs from the monthly-sampled relative SLAs from PSMSL. Finally, we directly compute the differenced SAT-TG time series from the averaged monthly AVISO and the PSMSL data, which yields the AVISO-PSMSL-250km dataset.

240 Using these combinations, we investigate the mere changes from matching along-track data at high or at low frequency (ALES-GESLA-250km and ALES-PSMSL-250km), or using monthly gridded data (AVISO-PSMSL-250km). Here, 'high-frequency' refers to daily time scales of variability and 'low-frequency' to monthly time scales. The dataset ALES-GESLA-ZOI incorporates further SLA-selection-schemes, which are explained in the following section.



3.2 The Zone of Influence

We aim to develop a new SLA-selection scheme, which accounts for the observed coherency of sea level variability. However, due to the diversity of the underlying physical mechanisms and their complex interplay with the coast, the spatial coherency of sea level dynamics is highly variable in coastal regions (Woodworth et al., 2019). Coastally trapped waves, for instance, were argued to establish long-range correlations along the continental slopes (Hughes and Meredith, 2006) and to mediate the influence of the open ocean (Hughes et al., 2019) on the coast. While some signals, such as interannual modes of climate variability, generate high spatial coherence, other local features, such as the presence of a coastal current, can significantly modify the sea level variability within few kms of the coast, as shown in the case of the seasonal signal of the Norwegian Coastal Current in Passaro et al. (2015). Accordingly, the capability of compare TG-based sea level variability with altimetry, utterly depends on which time and length scales are resolved by the data.

The key concept of our approach is to capture the extent to which coastal altimetry measurements are similar to the in situ tide gauge observations. To do so, we extend the methodology proposed by Santamaría-Gómez et al. (2014), who looked for the altimetry grid point mostly correlated with the tide gauge, and Kleinherenbrink et al. (2018), who considered a larger set of points based on absolute thresholds of correlation. In contrast to these previous studies, we assess the influence of using relative thresholds of comparability on both the accuracy and the uncertainty of the trends.

We exploit combinations of along-track ALES data and high-frequent GESLA records, to identify regions of sea level variability that show maximum coherency with tide gauge observations, which we hereinafter call the Zone of Influence (ZOI). With this approach, our objective is to decrease noise of the differenced, high-frequent VLM_{SAT-TG} time series using the ZOI to hone trends and uncertainties estimates.

To define the ZOI, we investigate different statistical criteria S , which provide a measure of similarity of sea level variability between TG and SAT observations. Here, we use the Pearson correlation coefficient, the RMS_{SAT-TG} as well as as the amplitude of the residual annual cycle between both TG and SAT records. We compute each of those measures for every point of the 1 Hz along-track data (ALES) in combination with the TG records from GESLA. As for ALES-GESLA-250km, tide gauge data are interpolated onto the time step of the altimetry records. Correlations and RMS_{SAT-TG} are computed from the detrended TG and SAT time series. The amplitude of the residual annual cycle is obtained from the remaining seasonal signal of the difference of the time series (SAT-TG). We acquire a dataset, holding information of the performance of multi-mission along-track data in the vicinity of every GESLA TG.

To confine the ZOI, we select sub-sets of the data containing the best-performing statistics (i.e. highest correlation, lowest RMS_{SAT-TG} or residual annual cycle) above the X th-percentile according to the distribution of the statistic S in a 300 km radius around the tide gauges. Every sub-set (X, S) represents an individual ZOI, in which we average SLAs in accordance with the steps involved in the aforementioned 250 km-radius-selection (ALES-GESLA-250km, section 3.1). The high-rate SLA time series (ALES) are then again subtracted from GESLA, providing the ALES-GESLA-ZOI dataset for VLM estimation (section 3.3).



Note that in contrast to the 250 km selection, we extend the range in which SLAs are taken into account to 300 km to define the ZOI. The previous 250 km selection is, as in Kleinherenbrink et al. (2018), based on the space auto-correlation scales of SLAs, which reflect characteristic eddy length scales (Stammer and Böning, 1992; Ducet et al., 2000). These scales decrease towards higher latitudes with changing internal Rossby radius. However, several studies found much larger correlation length scales of SLAs, in particular along shorelines (Calafat et al., 2018; Hughes and Meredith, 2006). Other mechanisms than mesoscale eddy activity were investigated to account for these coherent changes. One example is given by Calafat et al. (2018), who analysed the driving factors of sea-level variability at the south-eastern coast of the US. Using altimetry and three different ocean-models, they found coherent changes of the annual amplitude of SLAs over length scales of thousands of kilometers along the coast from the Yucatan Peninsula to Cape Hatteras. While the annual cycle signal itself was dominated by steric changes, with likewise large-scale correlations at the continental slope, changes of the annual amplitude were argued to be dominated by boundary waves exerted by incident Rossby waves. Because we similarly find correlations beyond the 250 km length-scale, in particular along elongated coastal regions (Figure 1 a and b), we justify the larger 300 km radius.

We identify coherent zones of sea-level variability represented by different selection-criteria in Figure 1. The statistics S are computed based on individual along-track SLA time series (ALES) and GESLA tide gauges. We show different maps of these along-track statistics for (a) the Australian Coast, (b) Californian Coast and (c) Chichijima island (Japan). The contour in the first column exemplifies the extend of a ZOIs, which represents a sub-set of 20% of the best correlated data.

The obtained coherent structures reveal notable dependencies on the local bathymetric and coastal properties. Figure 1 (a), for instance, shows far-reaching alongshore correlations, which is supported by all of the analysed selection criteria. In this example, the separation of the region of the coastal shelf-sea dynamics from region of offshore variability is in good agreement with the underlying bathymetric gradients. Kurapov et al. (2016) found similarly pronounced SLA coherency along for the Californian coast, as shown in Figure 1b). Based on model data and tide gauge observations, they explained the large-scale along-shore correlation pattern in part with the propagation of coastal trapped waves. In other locations such as in Chichijima island (see Figure 1c), coastal and bathymetric control of SL is reduced and different structures of coherency evolve. Consequently, the ZOI can strongly vary in shape depending on the local coastal features and drivers of coastal variability.

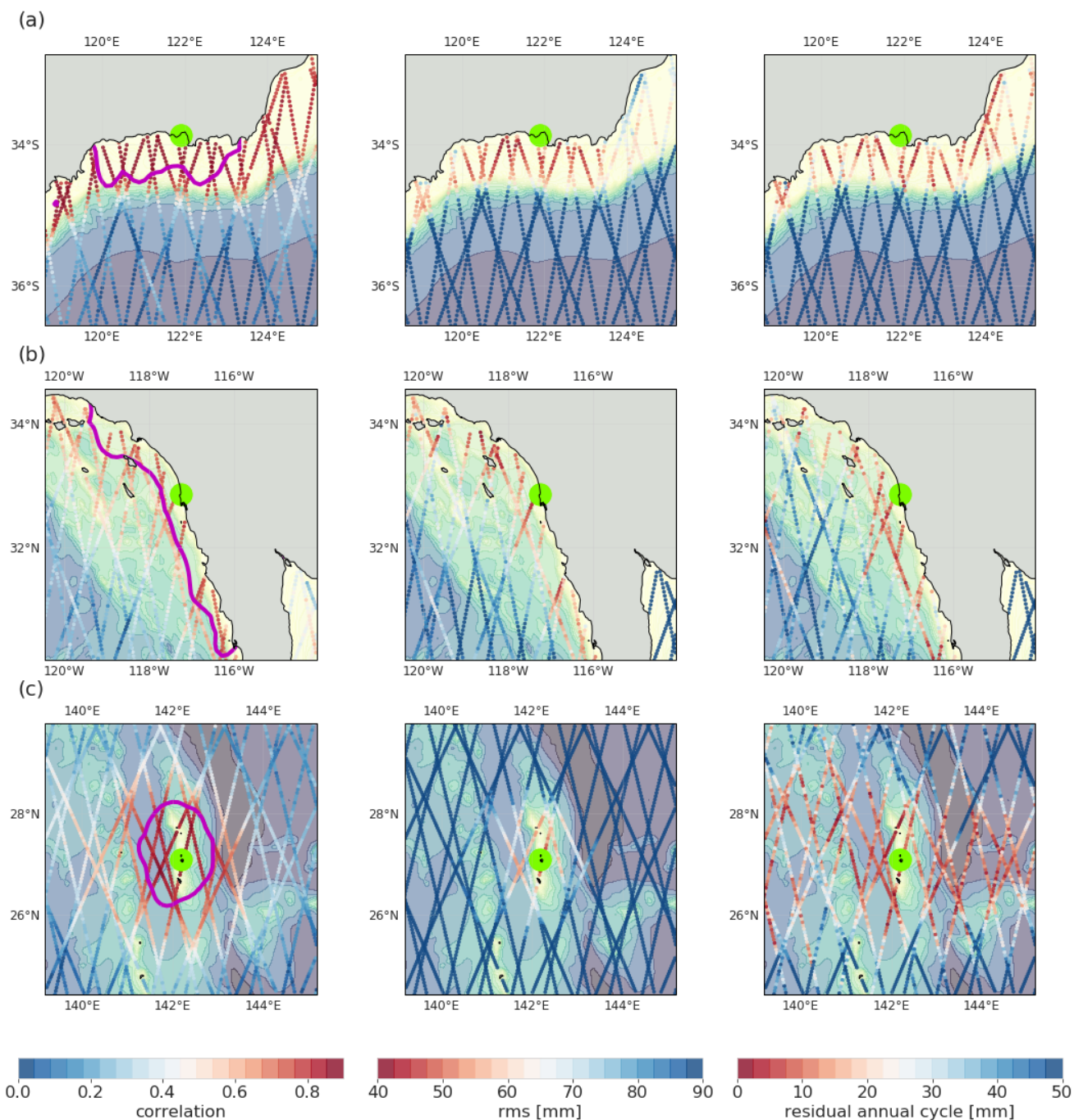


Figure 1. Zone of Influence: Different coherent zones of sea level variability are identified by different statistical criteria S . The columns show correlations, RMS_{SAT-TG} and the residual annual cycle from left to right. The metrics are computed on every point of the 1 Hz along-track product, comparing the performance of altimetry measurements with the tide gauges, highlighted in green (center). (a) shows the South-Coast of Western Australia, (b) the western coast of North America (tide gauge in San Diego) and (c) Chichijima island (Japan). The 'color' contour in the first column indicates a Zone of Influence built from 20% of the best-correlated SLAs within a 300 km radius. The underlying contours denote the underlying bathymetry.



Comparing these three examples, we also observe that absolute values of the statistics differ from site to site. Correlations of along-track data near the Australian coastline, for instance, outperform the ones in example Figure 1b. The same holds for $\text{RMS}_{\text{SAT-TG}}$ values. These differences not only indicate different degrees of coherency, but can also stem from regional deviations in the quality of data, i.e. quality of tide gauge records or error sources in the altimetric product, such as tidal adjustments or coastal corrections. Differences can also be caused by coastal properties, e.g. when the tide gauges are located in sheltered areas, which separates the in situ variability from the one measured at distant altimeter tracks. We analyse therefore the use of relative thresholds, to select the SLAs, since setting absolute thresholds as in Kleinherenbrink et al. (2018) might not be applicable in all cases. Figure 1c) also shows that different statistics can determine different extents of the ZOI, considering that rather poorly correlated areas are partially characterised by low residual annual cycle amplitudes.

A correct choice of the ZOI based on a sub-set of high performant SLAs can significantly reduce the SAT-TG residuals as are exemplified in Figure 2. Here, we show three time series of SAT-TG differences for the Australian site (see Figure 1a). The first series (Figure 2a) indicates much lower residual noise, when the time series is constructed from the 20% best SLAs (according to the $\text{RMS}_{\text{SAT-TG}}$). Here, the ALES-GESLA-ZOI residuals outperform those of the other combinations ALES-PSMSL-250km and AVISO-PSMSL-250km, which are still affected by a pronounced annual cycle not related to VLM.

While using relative thresholds can reduce the noise of $\text{VLM}_{\text{SAT-TG}}$ time series for individual stations, we seek to identify a globally optimal ZOI definition and associated criteria and thresholds, which lead to largest improvements of uncertainties and accuracies of $\text{VLM}_{\text{SAT-TG}}$. Therefore, we vary the relative thresholds X between 0.0 and 0.975 (with a stepsize of 0.025), which refers to using 100% and 2.5% of the best performing SLAs according to each criteria. For each threshold and criterion we derive an individual global $\text{VLM}_{\text{SAT-TG}}$ trend and uncertainty dataset. We validate the performance of the trend estimates for a specific ZOI definition in accordance with section 3.4. Optimal parameter X, S are then suggested for the global application (section 4.2).

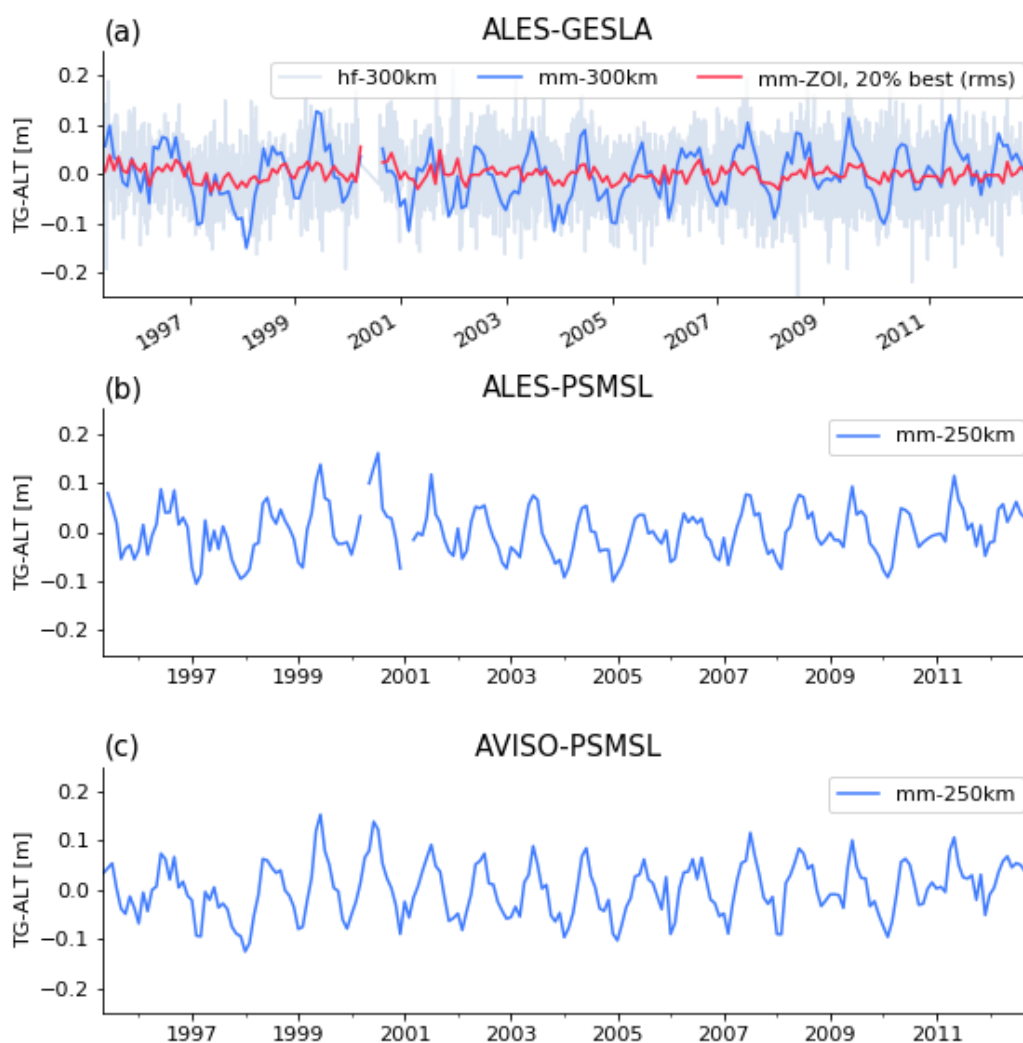


Figure 2. Shown are 'SAT minus TG' time series for different datasets and configurations for the TG in Figure 1a). (a) Monthly mean (mm) time series for ALES-GESLA, when all SLAs are averaged in a 300 km radius (blue) and when SLAs are comprised of the 20% most representative anomalies based on the RMS_{SAT-TG} between altimetry and TG (red). The grey line denotes the underlying high-frequency time series. (b) and (c) Monthly mean differenced time series for ALES-PSMSL and AVISO-PSMSL, which are based on a 250km-radius selection of SLAs.



3.3 Statistical analysis: Trend and uncertainty estimation

We fit the differenced time series to a combination of a deterministic model and stochastic noise models with the Maximum Likelihood Estimation (MLE) method. Parameters of the deterministic model are comprised of a constant offset A and a linear trend B . The annual and semi-annual signals are expressed by harmonic functions with the annual and semi-annual frequencies $\omega_{1,2}$ and amplitudes $C_{1,2}$ and $D_{1,2}$.

$$y(t) = A + Bt + \sum_{i=1}^2 C_i \cos 2\pi t \omega_i + D_i \sin 2\pi t \omega_i \quad (1)$$

When combining altimetry and tide gauges for VLM estimation, several sources can contaminate the differenced time series and inflate the actual 'red'-noise (low-frequency) content in the residuals, which generates auto-correlated signals in the data. Such sources include next to SLA correction or adjustment errors most predominantly sea level dynamics, which do not reflect the tide gauge observations. Therefore, to avoid underestimation of the uncertainties of the parameters, we take into account auto-correlation in the residuals of the detrended and deseasoned time series. We describe the power spectral density of the noise with a combination of a power-law and a white noise model (using the Hector software (Bos and Fernandes, 2019)). The power-law process assumes that time-correlated noise power is proportional to f^κ , which for negative spectral indices κ describes increasing power at lower frequencies f and a white-noise process when $\kappa = 0$ (Agnew, 1992). Gómez et al. (2011) showed that this combination (of power-law and white noise model) represents the best approximation of the noise content for 275 GNSS station position time series. This combination was also implemented in studies concerned with VLM_{SAT-TG} estimation (WM16, Kleinherenbrink et al. (2018); Ballu et al. (2019)). In particular, the spectral index κ can contribute to detect the intrusion of low-frequency signals in the differenced time series. Next to the spectral index κ we estimate the individual fractions of the power-law and white noise models, as well as the total variance σ^2 which scales the amplitude of the noise.

3.4 Validation of VLM_{SAT-TG} with VLM_{GNSS} trends

To validate SAT-TG-based trend estimates, we use the ULR6a GPS solution provided by the GNSS data assembly centre SONEL (Système d'Observation du Niveau des Eaux Littorales, <http://www.sonel.org>). The reanalysis covers 19 years of GNSS data from 1995 to 2014, which are processed within the ITRF2008, consistent with the reference frame of altimetry orbits. The primary coordinates provided by GNSS are geocentric Cartesian coordinates (X, Y, Z, V_x, V_y, V_z). For the comparison with vertical trends inferred from other techniques, they are converted to ellipsoidal coordinates (latitude ϕ , longitude λ and ellipsoidal height h , and V_ϕ, V_λ, V_h). Thus, we compare GNSS ellipsoidal height trends (V_h) with SAT-TG trends. It should be mentioned that, while the altimetry trends refer to the so-called TOPEX/Poseidon, the GNSS vertical trends refer to the GRS80 (Geodetic Reference System, 1980; Moritz (2000)) ellipsoid. Although there is difference of 70 cm between the semi-major axes of both ellipsoids, the GNSS and SAT vertical trends can be compared without degradation of precision, as both ellipsoids are geocentric and have the same orientation with respect to the Earth's body (e.g., the ellipsoid minor axes



coincide with the mean Earth's rotation axis, and the major axes are on the Earth's equatorial plane). We take into account GNSS stations which are closer than 1 km to a tide gauge. With this constraint we aim to avoid potential differential vertical motions between the tide gauge and the GNSS-antenna (WM16).

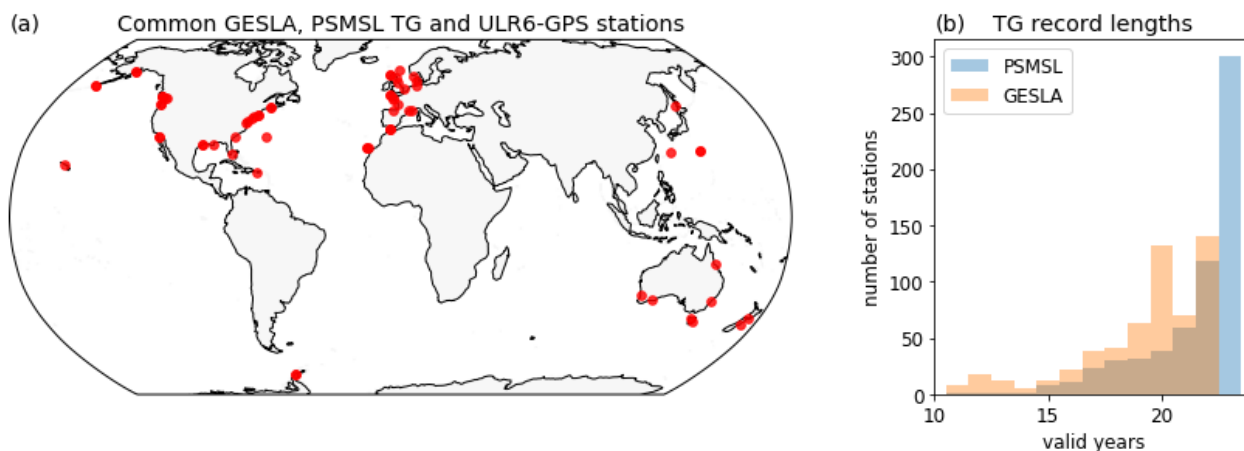


Figure 3. a) Global Distribution of 52 common GESLA, PSMSL and ULR6-GNSS stations, which meet the described requirements. b) Number of all TG stations sorted by the amount of months which contain valid data (here shown in valid years) in the period 1993-2015.

The tide gauge locations and record lengths differ among the presented experimental datasets (section 3.1). Therefore, we define several requirements for the validation of those experimental-datasets, to obtain a consistent set of TG and GNSS validation pairs. In contrast to PSMSL records GESLA-TG observations only last until 2015. Even when PSMSL TG records are limited to before 2015, they still contain more months of valid data than GESLA (see Figure 3b). Hence, we align the time period covered by the PSMSL-TGs to the corresponding GESLA-TGs for all following experimental datasets. Generally, we only take into account SAT-TG time series, when they cover at least 120 months of valid data. Note, that the outlier analysis (section 2.4) or coupling of high-frequent TG data in the ZOI can reduce the length of the SAT-TG time series for GESLA TGs. Taking into account all these requirements, we obtain 52 common GESLA and PSMSL TGs, which provide a neighbouring GNSS station within 1 km distance. These pairs are validated for ALES-PSMSL-250km, ALES-GESLA-250km and AVISO-PSMSL-250km. The ALES-GESLA-ZOI combination includes six more stations. The resulting validation pairs are shown in Figure 3a), where a higher coverage in northerly and midlatitude regions is evident.

We compute the $RMS_{\Delta VLM}$ and the median of the differences (ΔVLM) of VLM_{SAT-TG} and VLM_{GNSS} for a given dataset combination. We analyse also the median of the absolute value of differences ($|\Delta VLM|$). This metric is less prone to extreme deviations and can thus consolidate the evaluation of the dataset performances. We generally assume that GNSS provides a more accurate estimation of the linear component of the VLM with a smaller error than VLM_{SAT-TG} , also despite shorter time span of measurements. Hence, for the purposes of this paper and as done in all studies concerning VLM_{SAT-TG} estimation, we define as measures of accuracy the $RMS_{\Delta VLM}$ and additionally the median of $|\Delta VLM|$. We include the spectral index κ (see



section 3.3) as it helps to understand the level of auto-correlation of the time series. All statistics other than the $\text{RMS}_{\Delta\text{VLM}}$ denote median values (of all $\text{VLM}_{\text{SAT-TG}}$ estimates) for a specific dataset configuration.

375 4 Results

4.1 Comparison of different datasets configurations based on a 250 km average selection

We compare performances of the three datasets which are constructed from 250 km radius SLA averages in Table 2. Validation against GNSS vertical velocities reveals that the gridded combination AVISO-PSMSL-250km slightly outperforms ALES-PSMSL-250km in terms of accuracy. Both the $\text{RMS}_{\Delta\text{VLM}}$ and the median of absolute trend differences are 8% lower for
 380 AVISO-PSMSL-250km. This confirms that, if all the available altimetry data within a wide region are compared against monthly values of TGs, the use of a gridded product outperforms the along-track performances (WM16). Kleinherenbrink et al. (2018) similarly compared an along-track combination of 250km-SLA averages (from RADS) and PSMSL tide gauge data with the AVISO-PSMSL combination from WM16. They found a small $\text{RMS}_{\Delta\text{VLM}}$ reduction of 0.1 mm/year when using the along-track product without any correlation thresholds applied. WM16's trends were however based on 1° radius-averages
 385 of SLAs (in contrast to the 250 km selection), and record lengths were not equalized as in this study.

For both combinations the absolute median bias of trend differences (ALES-PSMSL-250km: -0.51 mm/year AVISO-PSMSL-250km: 0.56 mm/year) exceeds values shown in previous studies [WM16: -0.25 mm/year and, Kleinherenbrink et al. (2018): -0.06 mm/year]. In contrast to these previous estimates, we use different spatial selection scales of SLAs, smaller numbers of TG-GNSS pairs and deviating record lengths, which impedes a direct comparison. Still, the observed $\text{RMS}_{\Delta\text{VLM}}$ of AVISO-
 390 PSMSL-250km (1.50 mm/year) is comparable to WM16 result (1.47 mm/year). In contrast to trend accuracies, the uncertainties are 5% lower for ALES-PSMSL-250km than for AVISO-PSMSL-250km. As in WM16, the spectral index κ of the interpolated gridded product is lower than for the along-track data. Both κ indices (-0.56 and -0.42) also match well those found by WM16 for AVISO (-0.5) and the along-track product (-0.4, GSFC). The larger spectral index (-0.42) is associated with reduced power of the noise at low frequencies and thus indicates reduced contamination of the SLA signal by sea-level variations that do
 395 not represent those measured at the tide gauge. This enhanced comparability is also reflected in the lower trend uncertainties of ALES-PSMSL-250km (0.69 mm/year) compared to AVISO-PSMSL-250km (0.73 mm/year). The differences between the characteristics of the residuals of the datasets can partially be explained by the resolution of the data: Due to the spatial filtering of the data, the gridded solution AVISO incorporates information of SLAs beyond the 250 km radius and thus contains time-correlated SL-signals which stronger deviate from the TG records.

400 In comparison with the low-frequency datasets (ALES-PSMSL-250km and AVISO-PSMSL-250km), the high-rate set-up ALES-GESLA-250km improves the $\text{RMS}_{\Delta\text{VLM}}$. The absolute bias of trend differences decreases more substantially and is with -0.22 mm/year slightly lower than WM16's estimate of 0.25 mm/year. Given the strong improvement in the bias, the ALES-GESLA coupling is further developed based on a better definition of the ZOI in the next section.



Table 2. Statistics of different SAT-TG combinations. ΔVLM refers to the differences of $\text{VLM}_{\text{SAT-TG}}$ and VLM_{GNSS} trends. X denotes the relative level of comparability above which data is included.

X	$\text{RMS}_{\Delta\text{VLM}}$ mm/yr	med. $ \Delta\text{VLM} $ mm/yr	med. ΔVLM mm/yr	med. uncertainties mm/yr	spectral index κ
ALES-PSMSL-250km (52 stations)					
	1.63	1.22	-0.51	0.69	-0.42
AVISO-PSMSL-250km (52 stations)					
	1.50	1.12	0.56	0.73	-0.56
ALES-GESLA-250km (52 stations)					
	1.46	1.13	-0.22	0.79	-0.41
ALES-GESLA-ZOI (best $\text{RMS}_{\text{SAT-TG}}$, 58 stations)					
0	1.52	1.00	-0.46	0.85	-0.47
0.1	1.38	0.88	-0.27	0.87	-0.44
0.2	1.34	0.91	-0.38	0.82	-0.45
0.3	1.31	0.83	-0.41	0.77	-0.47
0.4	1.31	0.84	-0.40	0.77	-0.45
0.5	1.30	0.84	-0.23	0.73	-0.46
0.6	1.30	0.83	-0.30	0.70	-0.49
0.7	1.28	0.83	-0.43	0.67	-0.47
0.8	1.28	0.87	-0.50	0.59	-0.44
0.9	1.51	0.90	-0.44	0.57	-0.43

4.2 The Zone of influence improves VLM estimates

We investigate how the ZOI selection of SLAs fosters quality of SAT-TG VLM estimates. As addressed in section 3.2, we build the ZOI upon different criteria of comparability: $\text{RMS}_{\text{SAT-TG}}$, correlation and the residual annual cycle. First, we focus on the results of using the $\text{RMS}_{\text{SAT-TG}}$ of the detrended differenced time series (Table 2 and Figure 4, ALES-GESLA-ZOI). We observe that the $\text{RMS}_{\Delta\text{VLM}}$, the median of absolute and total differences, as well as trend uncertainties decrease towards higher relative thresholds. The statistics converge to a minimum when the ZOI is restricted to the 30-20% best data. To compare ALES-GESLA-ZOI with the other dataset combinations, we compute the statistics for the same 52 tide gauges used in these configurations (because the shown statistic in Table 2 refer to a larger set of 58 stations). At the 20% thresholds, we obtain similar performances with a $\text{RMS}_{\Delta\text{VLM}}$ of 1.29 mm/year, median uncertainties of 0.57 mm/year and a median of absolute differences ($|\Delta\text{VLM}|$) of 0.86 mm/year. Thus, the improvements of $\text{RMS}_{\Delta\text{VLM}}$ compared to the plain 250km-radius selection (ALES-GESLA-250km) is 12% and 28% for uncertainties. Hence, we find more substantial, nearly linear reductions of trend uncertainties with increasing relative thresholds compared to trend accuracy ($\text{RMS}_{\Delta\text{VLM}}$, Table 2, ALES-GESLA-ZOI). As demonstrated for different time series in Figure 2, selecting e.g. highly correlated SLAs efficiently reduces the noise of the



residuals. Correspondingly, at higher levels of comparability, the variance, which scales the amplitudes of the considered noise models, decreases (not shown).

Because the spectral index (for ALES-GESLA-ZOI) is slightly lower (-0.44 at 20% level) than for ALES-GESLA-250km (-0.41) it cannot account for the uncertainty improvements. Here, the lower κ index reveals an relative increase of power at low frequency (i.e. time scales longer than months). Thus the bulk of improvements we see in uncertainties (comparing ALES-GESLA-ZOI and ALES-GESLA-250km) stems from the reduction of the white noise amplitude in the residuals. This is in turn caused by improvements of the comparability of tide gauge and altimetry measurements at high-frequency (i.e. days). We argue that extending the maximal radius selection from 250 km to 300 km to construct the ZOI (as done for ALES-GESLA-ZOI) increases the low-frequency noise (indicated by κ). However, with this selection we capture more altimetry tracks with similar highly correlated high-frequency signals (see Figure 1), which again contribute to sampling density and reduced white noise. This further substantiates our choice to select SLA within a larger 300 km radius, which is also supported by observed larger-scale coherency of coastal sea level trends (see section 3.2).

RMS $_{\Delta VLM}$ and trend uncertainties level off at very high thresholds and ultimately increase when only 5% of the data is used (Figure 5a and 5c). We argue that this is closely related to a decrease in sampling-density of the time series included in the selection. Robust trend estimates require a minimum of samples, hence, using a reduced number of along-track data time series, even when they show a maximum degree of comparability, yields on a global average decreased trend accuracies (RMS $_{\Delta VLM}$). Indeed, one would expect the highest comparable (for instance expressed by correlations or RMS) or even the closest altimetry measurement point to result in most accurate VLM $_{SAT-TG}$ trends. This is, however, not the case for this SAT and TG combination on a global average. We thus argue that the optimum threshold identified at about the 80th percentile (of the data sorted by RMS) represents a compromise between data-comparability, as well as sampling-density of altimetry data.

When setting this optimal threshold to 20%, the ALES-GESLA-ZOI set-up outperforms the other investigated configurations. Figure 4 compares the scatter of estimated VLM $_{SAT-TG}$ against GNSS trends of all datasets. For ALES-GESLA-ZOI, we find lower VLM $_{SAT-TG}$ trend uncertainties and reduced spread of the estimates with respect to the bisector (Figure 4). This result proves the importance of using such a refined selection procedure (ZOI), as this approach outstrips the improvements induced by the different altimeter or tide gauge data combinations.

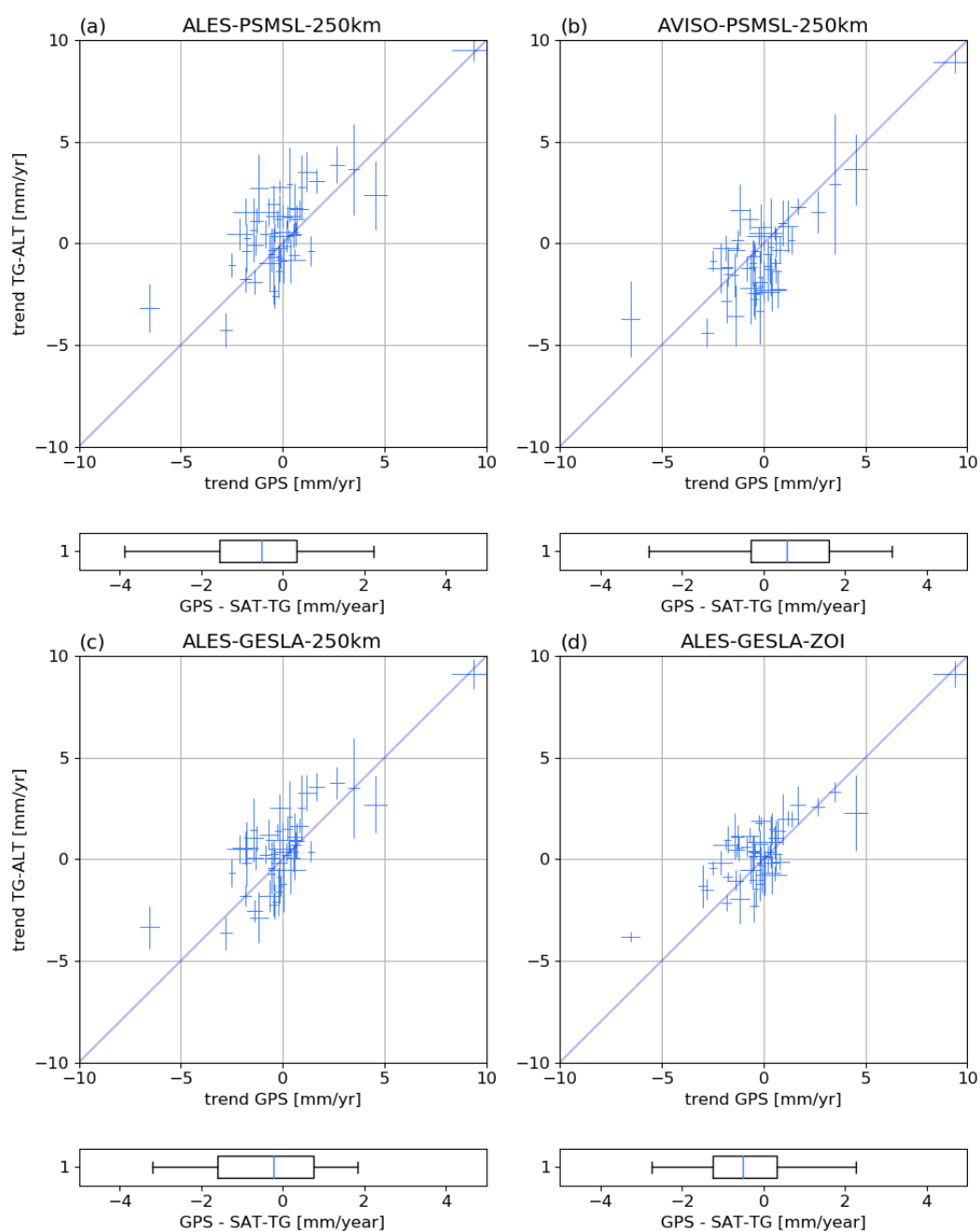


Figure 4. Scatter and boxplots compare estimated SAT-TG trends and GNSS trends, as in WM16 Figure 14. a) ALES-PSMSL-250km b) AVISO-PSMSL-250km c) ALES-GESLA-250km d) ALES-GESLA-ZOI (at 20% threshold based on RMS-criterion). Bars denote trend uncertainties of the individual estimates



Figures 5a and 5c illustrate the influence of applying different criteria on the performance of estimated trends. Generally, increasing relative $\text{RMS}_{\text{SAT-TG}}$ or correlation thresholds yields similar optimal ranges ($\sim 20\%$) for both $\text{RMS}_{\Delta\text{VLM}}$ or uncertainties of $\text{VLM}_{\text{SAT-TG}}$ trends and can thus be interchangeably used. At lower relative threshold levels (20-60%), however, application of the RMS-criterion yields slightly reduced $\text{RMS}_{\Delta\text{VLM}}$ values compared to correlations. Hence, for this set of tide gauges a SLA-selection based on the minimum $\text{RMS}_{\text{SAT-TG}}$ generally provides more accurate trend estimates (in terms of $\text{RMS}_{\Delta\text{VLM}}$). The criterion residual annual cycle only weakly reproduces the improvements provided by the other criteria and is less suited to confine the ZOI. This observation emphasizes the need of matching the data according to the high-frequency comparability (RMS, correlation), because selecting the data based on the residual annual cycle (i.e. low frequency comparability), limits the performance of the estimates (Figure 5c).

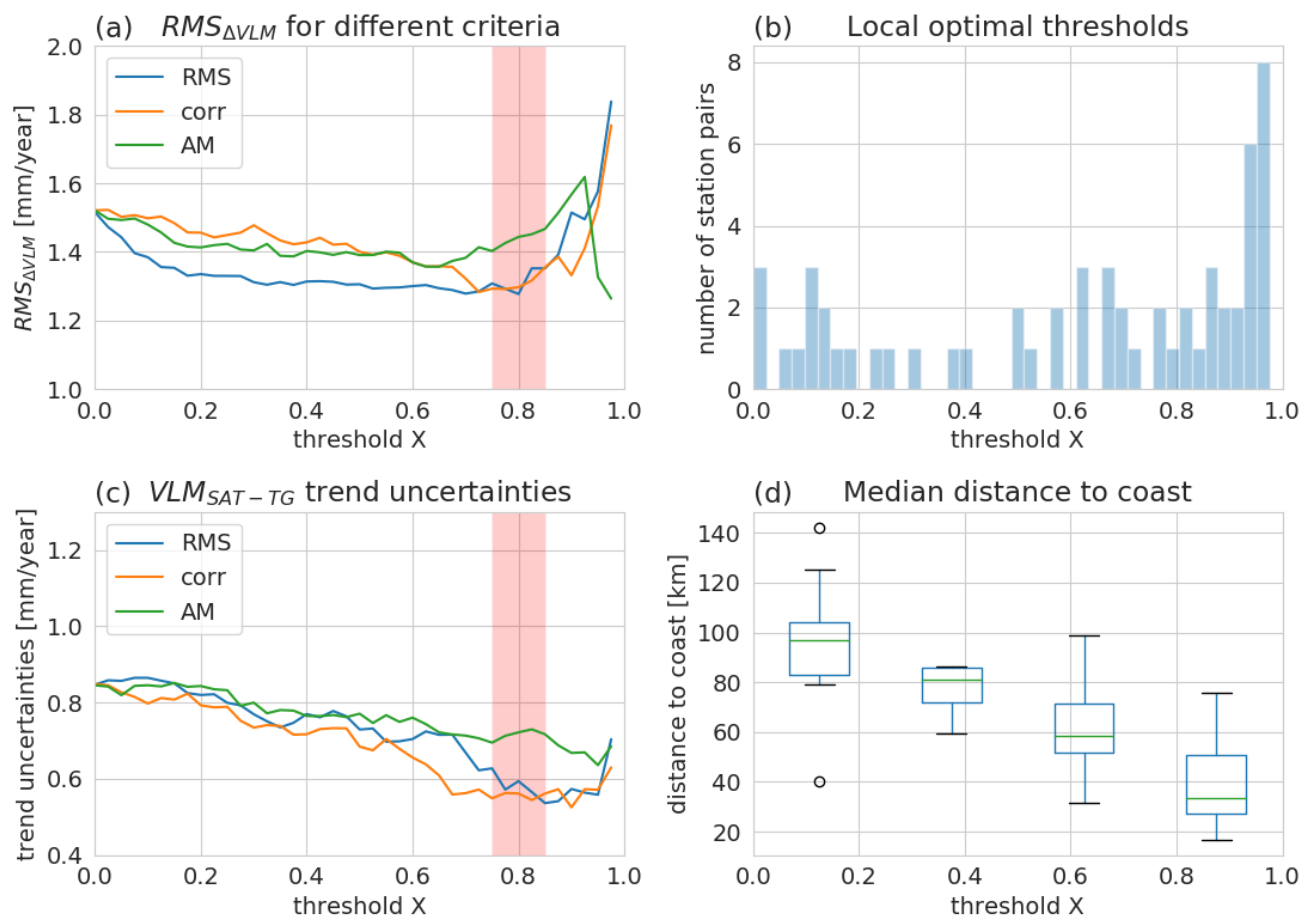


Figure 5. Performance of VLM_{SAT-TG} trend estimates for ALES-GESLA-ZOI. a) $RMS_{\Delta VLM}$ for different relative thresholds (step size 2.5%) and different selection criteria: RMS_{SAT-TG} (blue), correlation (red) and residual annual cycle (green); c) same as (a) but for median uncertainties. b) Distribution of best performing relative thresholds for individual stations. The local optimal threshold is defined at the minimum of the absolute difference of VLM_{SAT-TG} and GNSS trends. d) Boxplot shows the distribution of the mean distances to coast for the individual optimum ZOI's as denoted in b). The distances refer to the distributions within the 0-25%, 25-50%, etc. levels, respectively.



5 Discussion

The integration of the ZOI primarily reduces uncertainties of VLM_{SAT-TG} trend estimates. Over a considerable range of thresholds (80 - 20% of best performing data) trend accuracies do not improve as strongly as the uncertainties decrease. This is in line with Kleinherenbrink et al. (2018), who showed that for a highly correlated sub-set of TGs, increasing absolute correlation thresholds would not significantly reduce the $RMS_{\Delta VLM}$. We thus strive to understand better why trend estimates not always improve when selecting highly comparable (w.r.t. tide gauge) or closely located absolute SLA measurements. This question ultimately leads to the discussion of the importance of identifying the small-scale dynamical components of local sea-level variability, given that long-term absolute sea level trends are large-scale signals.

5.1 Space and time dependencies of coastal sea level trends

The results presented in Figure 5 and Table 2 denote average performances for the globally distributed TG-GNSS station pairs for ALES-GESLA-ZOI and support an optimal threshold at 20%. It is however unclear, whether the described optimum threshold for this 'global' selection also reflects the best choice at every considered coastal site. Therefore, we investigate at which relative levels individual VLM_{SAT-TG} and VLM_{GNSS} trends estimates yield the smallest absolute deviations. Postulating that the actual VLM at the TG location is linear and perfectly detected by the GNSS station, these thresholds denote the 'local' optimal levels.

Figure 5b displays the distribution of local optimal thresholds for TG-GNSS stations for the ALES-GESLA-ZOI dataset. Overall, the optimal levels X are broadly distributed from 0 to 0.975. We find highest concentrations between 0.8-0.975, which slightly exceeds the range of the global optimum. At these high thresholds, the mean distance to coast averaged over all SLA measurements in a ZOI is 33 km. Hence, a large proportion of these SLAs heavily profits from demonstrated coastal advancements of the along-track dataset, which are most pronounced in the last 20 km off the coast (Passaro et al., 2015).

In contrast to these examples, we find very low local optima for some stations (Figure 5b). Here, local VLM_{SAT-TG} and GNSS trend differences do not converge to a minimum when increasing the comparability of SAT and TG observations. Accordingly, in these cases, vertical land motion estimates do not necessarily benefit from high coastal resolution of the data, because a low relative threshold is simultaneously linked to a larger-scale selection of SLAs (Figure 5d). At the lower level ranges, for instance at 0-0.2, SLAs have an average distance of 95 km to the coast. Supposing that the sources of these larger scales of coherency of coastal SL trends would be known, a more advanced adaption to these additional factors would further increase accuracies of VLM estimates. An associated ideal selection of trends, based on optimal individual levels shown in Figure 5d would largely reduce to $RMS_{\Delta VLM}$ to 0.9 mm/year.

To further shed light on the relationships between dynamical-sea-level-based SLA selection and spacial coherence of trends and uncertainties, we show trend and uncertainty maps (Figure 6) in accordance with those in Figure 1 (displaying maps of statistical criteria). Here, we map linear trends and uncertainties onto observed levels of comparability defined by the correlation-criterion. We thus compute these VLM_{SAT-TG} trends over different coastal regions (see further details in the Appendix A). As a result, we observe sharp trend gradients consistent with the degree of comparability: Figure 6a for instance, shows high

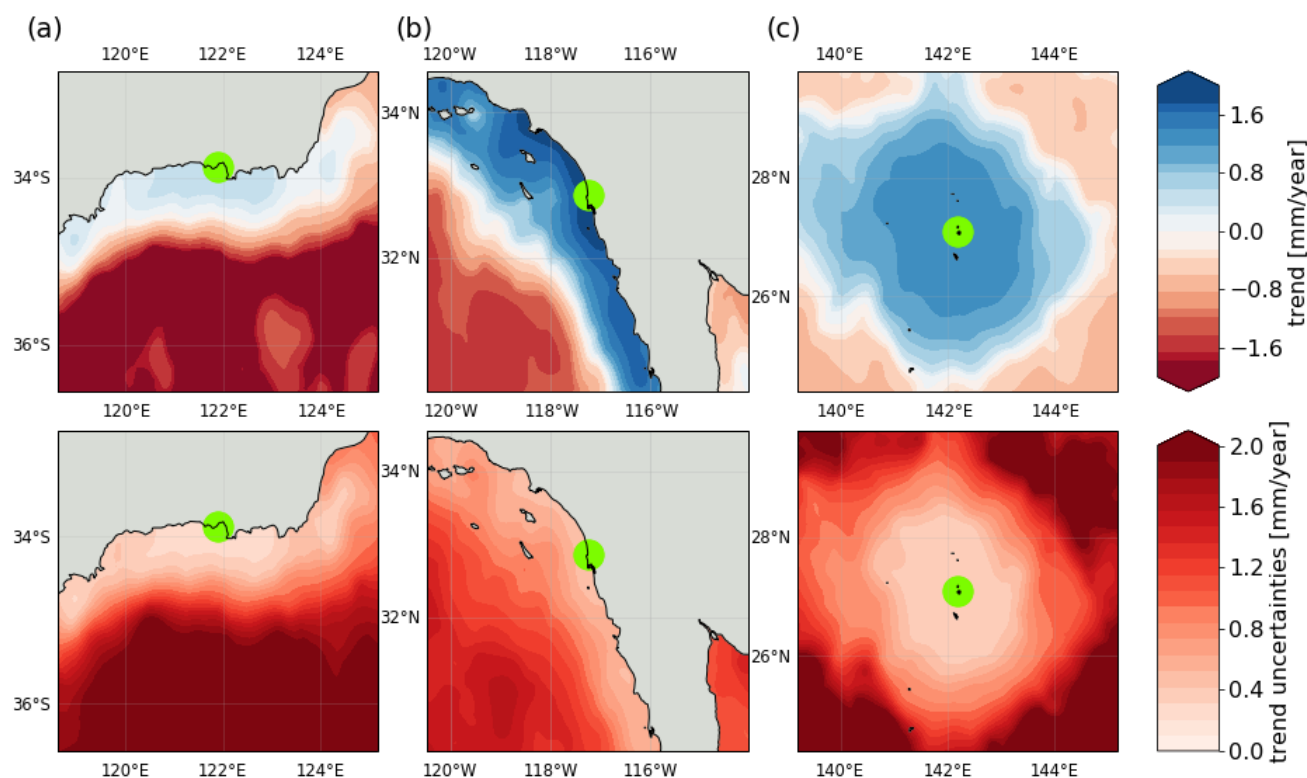


Figure 6. VLM_{SAT-TG} trends (first row) and uncertainties (second row) mapped onto relative correlation levels. The mapping and interpolation method is further elucidated in the Appendix A. We show the same stations (a,b,c) as in Figure 1.

small-scale variability of trends, because trends off the slope-current-region are detached from the trends in the along-shore continental shelf region. Trends in Figure 6a and 6b project onto the far-reaching along-shore correlations as observed in Figure 1 showing consistent signals over several hundreds of kilometers along the coast. Uncertainty maps further pronounce the importance of the application of highly resolved coastal altimetry data (Figure 6 lower row). The use of less comparable SLAs can inflate uncertainties by a factor of three to four. Therefore, for the majority of cases, these results promote using high relative levels of comparability to define the ZOI for trend estimation. However, we also observe that the coherency of trends (highlighted by the strength of absolute trend gradients) can be differently expressed at different coastal regions.

Bathymetric and coastal properties can cause large discrepancies in responses of coastal sea level variability as they modify the character of the impact of large-scale atmospheric forcing or remote variability from the deeper ocean (Woodworth et al., 2019). Hence, an advanced analysis of SL coherency and the role of bathymetry might facilitate further enhancements of trend accuracies based on SAT and TG. We note, that physical origins might, however, not necessarily cause the spread of individual optimal thresholds (Figure 5b). If our assumption, that GNSS-trend estimates perfectly represent the linear trend over the time



span of the altimetry/tide gauge records was not met, the shown individual thresholds would erroneously reflect local optima. Ruling out these sources of error is thus a prerequisite to further study physical explanations for different extents of the ZOI.

Next to site-dependent physical factors, the spatial-scales of trend coherency might also depend on the time span of the observations themselves. Global maps of sea level trends, for example, even when derived from two decades of observations, still show distinct pattern of natural/forced variability and thus shade signals of ocean mass or steric contributions (e.g. Stammer et al. (2012)). Similarly, coastal sea level trends that are computed in the ZOI are affected by local interannual sea level variability on top of the secular trend. Therefore, the importance to adopt the concept of the ZOI for improving trend accuracy might also be influenced by the actual time span covered by the record.

To investigate this time-scale-dependency, we truncate the VLM_{SAT-TG} time series such that we obtain different experimental ALES-GESLA-ZOI sets with maximum record lengths from 10 to 18 years. We repeat the same validation analysis against GNSS trends as in section 4. Figure 7a) encompasses anomalies of the $RMS_{\Delta VLM}$ with respect to the mean $RMS_{\Delta VLM}$ for a dataset of a specific time scale which is given in Figure 7b (red). The same evolution is shown for trend uncertainties in Figure 7c).

Mean $RMS_{\Delta VLM}$ as well as mean uncertainties (which are averaged over all relative thresholds for a specific maximum record length) substantially decrease with increasing record length (Figures 7a and 7c). Both statistics approximately follow the theoretical proportionality of uncertainties and sample size n of $1/\sqrt{n}$ (assuming no serial correlation). The evolution of the $RMS_{\Delta VLM}$ anomaly shows that selecting SLAs in a ZOI at high relative thresholds more substantially reduces the $RMS_{\Delta VLM}$ on shorter time scales (e.g. 10 years) than on longer time scales (Figure 7a, e.g. at 18 years). At long time scales, the $RMS_{\Delta VLM}$ anomalies do not significantly improve between the 80% and 20% thresholds, which we also observe in the previous analysis in Figure 5a. We argue that the transition time scale where the improvements of $RMS_{\Delta VLM}$ flatten (14-16 years), marks when the high-frequent coastal sea level dynamical variability is superseded by dynamics producing large-scale sea level trends. In other words, this is the time scale in which coastal sea level trends start to merge with the offshore trends. The tendency of increasing spatial scales with time is also reflected by the increasing distances to coast of the measurements for an optimal ZOI at a specific time scale (Figure 7b). The time-scale-dependency could explain the mismatch of trend accuracy and uncertainty improvements when using higher levels of comparability. This is also supported by Kleinherenbrink et al. (2018), who showed little sensitivity for SAT-TG combinations which had minimum lengths of 15 years.

The same evaluation for the dependency of uncertainties on time and level of comparability X demonstrates that using the ZOI nearly constantly improves trend uncertainties at any time scale. Hence, even though spatial scales of trend coherency might increase with time, an ideal match of altimetry and tide gauges should be based on a ZOI.

5.2 Comparison with previous results

Based on optimal relative thresholds, we estimated an $RMS_{\Delta VLM}$ between SAT-TG and GNSS trends of 1.28 mm/year and a median uncertainty of 0.59 mm/year at 58 sites. Our approach of combining along-track altimetry, high-frequent tide gauge data and a refined SLA selection-scheme improves the performance of VLM estimation compared to using gridded altimetry products and constant spatial SLA averages (WM16: $RMS_{\Delta VLM}$: 1.47 mm/year; uncertainties 0.80 mm/year). Other studies

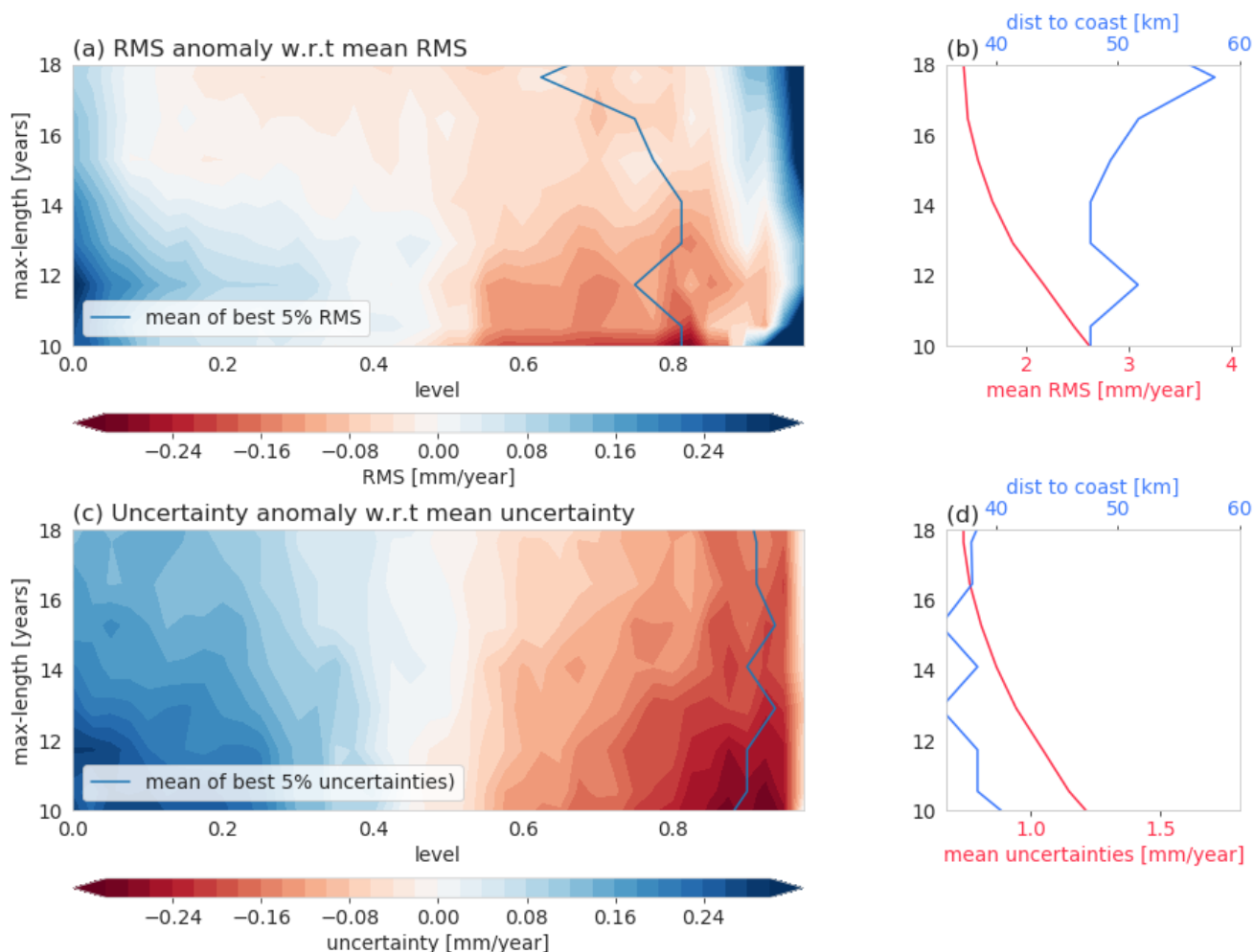


Figure 7. Time and space dependencies of trend uncertainties and accuracies: a) Evolution of the $\text{RMS}_{\Delta\text{VLM}}$ anomaly (SAT-TG vs. GNSS trend) for subsets of ALES-GESLA-ZOI, depending on a relative threshold X (x-axis) and a maximum record length (y-axis). $\text{RMS}_{\Delta\text{VLM}}$ anomaly is defined as the departure from the mean $\text{RMS}_{\Delta\text{VLM}}$ (shown in b) averaged over all thresholds X for a specific maximum record length. In b) we also show in blue the mean distance to coast of the measurements, associated with the average of the best 5% ZOI-levels per time scale, shown in a). c,d) Same as a,b) but for uncertainties.

530 further emphasized the importance of spatial resolution in coastal zones, considering the decreasing temporal and spatial scales of sea level variability in such areas. With the focus on coastal sea level trends, Cipollini et al. (2017) demonstrated that the along-track X-TRACK product contained much more valid data close to the coast than AVISO, not only due to the spatial down-sampling in AVISO, but also to less adapted coastal processing. Here, we tackle both issues by implementing an advanced coastal along-track altimetry product. Because we find that much of the observed high-performing altimetry data has



535 a close vicinity to the coast, our results underpin that along-track data is the best choice for coastal sea level trend estimation, and substantiate the results of Kleinherenbrink et al. (2018).

Accuracies of estimated VLM_{SAT-TG} expressed by $RMS_{\Delta VLM}$ are in the order of Kleinherenbrink et al. (2018)'s result of 1.20 mm/year. These results can, however, not unequivocally compared due to different validation settings. We extend their analysis by investigating a variety of other criteria of comparability and find that the RMS_{SAT-TG} of the differenced VLM_{SAT-TG} time series provides the most robust estimates compared to correlations or residual annual cycle. Our results also propose that increasing the radius of selection denotes another improvement for VLM estimates. Practically, the approach of using absolute thresholds, which was put forward by Kleinherenbrink et al. (2018) almost halved the number of considered stations from 294 to 155, when setting an absolute correlation threshold to 0.7. Applying relative thresholds, facilitates the estimation of trends at lower correlated stations, which would be rejected otherwise. This is crucial, because it was frequently shown, that correlations between altimetry and tide gauges are highly variable across the globe (WM16). Hence, we maintain the main advantage of using tide gauges for VLM estimation: The large global distribution compared to continuous GNSS-measurements.

6 Conclusions

We investigate potential improvements of combining altimetry and tide gauges for coastal vertical land motion estimation. The innovations of our approach are twofold: (1) For the first time, we exploit a global network of high-frequent tide gauge data (GESLA) and dedicated coastal altimetry (ALES) to determine VLM at a variety of co-located GNSS stations. Secondly (2) we define a Zone of influence, to identify coherent zones of coastal SL variability which optimizes the combination of altimetry and tide gauges. We rate improvements of both innovations against various SAT-TG datasets, which are comprised of along-track and gridded altimetry, as well as high (daily) and low-frequent (monthly) tide gauge combinations.

Combining high frequent tide gauge with coastal altimetry data (ALES-GESLA-250km) yields modest improvements of trend accuracies, compared to a monthly gridded or monthly along-track combination, when averaging SLAs in a radius of 250 km. The high spatio-temporal resolution of the data, however, provides the foundation to identify coherent zones of sea level variability. We confine a Zones of Influence by using relative thresholds of comparability based on RMS_{SAT-TG} , correlation and residual annual cycle of the altimetry and tide gauge timeseries. We identify a global optimal threshold, when selecting 20% of the data with the lowest RMS_{SAT-TG} . At this threshold, validation against GNSS velocity estimates (at 58 stations) yields a $RMS_{\Delta VLM}$ of VLM_{SAT-TG} and VLM_{GNSS} differences of 1.28 mm/year with formal uncertainties of VLM_{SAT-TG} trends of 0.59 mm/year. This refined selection method improves trend accuracies by 12% and uncertainties by 28% compared to the 250 km-average selection. The smaller degree of improvements of trend accuracies compared to uncertainties is explained by the increasing space-scales of sea-level trend components with progressing time scales. We show that in many cases, capturing small scale features of coastal sea level variability within few tens of kilometers from the coast is vital for VLM_{SAT-TG} estimation and constantly reduces trend uncertainties of the estimates. We thus promote using relative levels of comparability and coastal dedicated altimetry matched with high-frequency tide gauges to confine ZOIs, increase the number of VLM estimations along the global coastline and decrease their uncertainty.



Data availability. ULR6a GNSS trend estimates are obtained from the data assembly centre SONEL (Système d’Observation du Niveau des Eaux Littorales, <https://www.sonel.org/-Vertical-land-movement-estimate-.html?lang=en>, Gómez et al. (2016)). GESLA tide gauge data are available at <http://www.gesla.org> (Woodworth et al., 2016) and PSMSL data at <https://www.psmsl.org/data/obtaining/> (Holgate et al., 2013). ALES along-track data are processed at DGFI-TUM (<https://www.dgfi.tum.de/en/>) with OpenADB (<https://openadb.dgfi.tum.de>). Averaged DT-MSLA AVISO gridded altimetry data are obtained from <https://www.aviso.altimetry.fr>.

Appendix A: Methods

In Figure 6 we map linear VLM_{SAT-TG} trends and uncertainties onto observed levels of comparability set by the correlation-criterion. First, we group observed SLA time series in 0-20th, 20-40th, 40-60th etc. percentile-ranges, sorted by their correlations with the TG time series. Then, we merge the altimetry time series for each group and calculate their associated VLM_{SAT-TG} trends. The resulting VLM_{SAT-TG} trends are hereinafter defined on the altimetry tracks, categorized by the aforementioned groups of comparability. To better illustrate the different zones of coherency the trends are interpolated onto a regular grid (100x100 nodes i.e. 6km resolution) and thus smoothed as seen in Figure 6. We use linear radial basis functions to interpolate the data.

Author contributions. J.O. and M.P. conceptualized and designed the study. J.O. wrote the manuscript and is the author of the full software code used in this study. M.P. is the author of the ALES retracking algorithm and mentored the work of J.O.; C.S. and D.D. are responsible for the altimetry database organisation and the data structure. L.S. provided assistance in the use of GNSS data. F.S. provided the basic resources making the study possible and coordinates the activities of the institute. All authors read and commented on the final manuscript.

Competing interests. The authors declare that they have no conflict of interest.

Acknowledgements. This work was funded by the Deutsche Forschungsgemeinschaft (DFG) (grand agreement 411072120) and the Technical University of Munich (TUM) in the framework of the Open Access Publishing Program. We thank the data-providers GESLA, PSMSL, SONEL and AVISO for the opportunity to use their products. We thank Ashwita Chouksey and Michael Hart-Davis for their help, as well as two anonymous reviewers for their comments.



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