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3 Preface: Developments in the Science and History of Tides

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15 Abstract

16  
17 This special issue marks the 100<sup>th</sup> anniversary of the founding of the Liverpool Tidal Institute (LTI), one  
18 of a number of important scientific developments in 1919. The preface gives a brief history of how the  
19 LTI came about and the roles of its first two Directors, Joseph Proudman and Arthur Doodson. It also  
20 gives a short overview of the research on tides at the LTI through the years. Summaries are given of  
21 the 26 papers in the special issue. It will be seen that the topics of many of them could be thought of  
22 as providing a continuation of the research first undertaken at the LTI. Altogether, they provide an  
23 interesting snapshot of work on tides now being made by groups around the world.

24  
25 Keywords: ocean and earth tides; history of tidal science

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28 1. Introduction

29  
30 The idea for this special issue on tides came about when we realised that the 100<sup>th</sup> anniversary of the  
31 founding of the Liverpool Tidal Institute (LTI) was coming up in 2019, and we thought that a special  
32 issue of a journal would be one good way of celebrating it. The year following the end of the First  
33 World War saw the establishment of a number of organisations which have had a lasting importance  
34 for geophysical research. Notably, the International Union of Geodesy and Geophysics (IUGG) was  
35 founded in that year (Ismail-Zadeh and Joselyn, 2019). In addition, as examples at a national level, the  
36 American Geophysical Union (AGU) and American Meteorological Society (AMS) were established in  
37 the same year (McEntee, 2018; McFarquhar, 2020).

38  
39 The suggestion for a special institute in the UK dedicated to research on tides can be said to have  
40 arisen from a report written in 1916 for the British Association for the Advancement of Science (BAAS)  
41 by Sir Horace Lamb, Professor of Applied Mathematics at Manchester, and Joseph Proudman, a  
42 lecturer in Applied Mathematics at Liverpool (Figure 1). The proposal was accepted by Liverpool  
43 University and funding was obtained from Sir Alfred and Charles Booth of the Booth Shipping Line in  
44 order to ‘prosecute continuously scientific research into all aspects of knowledge of the tides’  
45 (Doodson, 1924; Cartwright, 1980, 1999). These are the basic facts, although Carlsson-Hyslop (2020)  
46 has described how the founding of the LTI came about only after a considerable amount of prior  
47 discussion and argument between the various stakeholders in academia (including Liverpool  
48 University and the BAAS), industry (including the Mersey Docks and Harbour Board) and the Navy  
49 (Admiralty).

51 The first LTI office was set up in March 1919 in the George Holt Building (then the Physics building) on  
52 the Liverpool University campus.<sup>1</sup> Proudman became its Honorary (unpaid) Director while Arthur  
53 Doodson was recruited as its Secretary. Proudman continued with his other university responsibilities  
54 and was promoted to Professor of Applied Mathematics. Meanwhile, in that same year, Liverpool  
55 University established the first university Oceanography department in the UK.

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57 However, space was short at the university after the war, and during the 1920s the LTI relocated across  
58 the River Mersey to Bidston Observatory in the Wirral where there was more room for research and  
59 where Doodson took up residence in 1929, now as Associate Director (Nature, 1928). Proudman  
60 transferred from Applied Mathematics to be Professor of Oceanography in 1933, a position which he  
61 held until retirement in 1954, having handed over as Director of the LTI to Doodson in 1945. By then,  
62 the LTI had become an acknowledged centre of expertise for research into ocean and earth tides, and  
63 it was to further extend its reputation in the following years into research on storm surges, sea level  
64 changes (Permanent Service for Mean Sea Level), and the measurement and modelling of coastal and  
65 shelf processes. The LTI underwent many name changes through the years, most notably being  
66 renamed as the Proudman Oceanographic Laboratory twice in 1987 and 2000, and became a  
67 component of the present National Oceanography Centre in 2010.

68

69 Proudman and Doodson both became Fellows of the Royal Society. Proudman was particularly expert  
70 on the dynamical theories of tides, and he played a major role in international collaboration in  
71 oceanography, being Secretary and then President of the International Association of Physical  
72 Oceanography (IAPO, Smythe-Wright et al., 2019). Doodson was superb at simplifying large numerical  
73 calculations in the days before digital computers. One topic in which he excelled was tidal prediction,  
74 from both a theoretical foundation (his development of the tidal potential, Doodson, 1921) and in  
75 practical application (the construction and use of tidal prediction machines (TPMs), see below). These  
76 topics and other historical aspects of work at the LTI will be mentioned briefly. Excellent biographies  
77 of Proudman and Doodson can be found in Cartwright and Ursell (1976) and Proudman (1968)  
78 respectively.

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<sup>1</sup> This is another link between Liverpool University and the shipping companies, George Holt being the co-founder of the Lamport and Holt Line and the brother of Alfred Holt, co-founder of the Blue Funnel Line. Alfred Holt's daughter was Jane Herdman after whom the Geology building on the campus is named. She was married to Sir William Herdman, Professor of Natural History, who became the first Professor of Oceanography.



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81

82 Figure 1. Joseph Proudman CBE, FRS (1888-1975) photographed in 1931 by Walter Stoneman. ©  
83 National Portrait Gallery, London.

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## 85 2. The Special Issue

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87 A special issue such as this was ideally suited to the European Geosciences Union (EGU) family of  
88 journals published by Copernicus. Tides occur in the ocean, solid earth and atmosphere, with each of  
89 those areas of research being served by one or more journals. However, Copernicus provides a good  
90 mechanism for papers to appear in their individual journals and be linked together eventually to  
91 provide an overall special issue.

92

93 The Executive Editors of five journals agreed to be involved in the special issue, the largest number to  
94 have taken part in a special issue so far. However, in the event, papers contributed to the issue were  
95 published in only three journals: History of Geo- and Space Sciences, Solid Earth and, in particular,  
96 Ocean Science. These three journals cover more than adequately most of the research into tides which  
97 was undertaken at the LTI, and also a great deal of the tidal research which is being conducted today.  
98 Potential authors were invited to address virtually any aspect of research into ocean or earth tides  
99 including the history of that research. As examples, the former could possibly include the present  
100 accuracy of coastal, regional and global tide models, tidal dissipation and its role in geophysics,  
101 internal tides and their role in mixing the ocean and in the global ocean circulation, secular changes in  
102 tides, and new techniques for measuring tides and analysing the data. The special issue opened for  
103 submissions on 1 January 2018, and stayed open through 2019 to take advantage of new findings

104 presented at the AGU, EGU and IUGG conferences in that year. It closed finally to new submissions in  
105 the middle of 2020 having received and accepted 26 papers across the three journals.

106

107 To complement the special issue, a number of special sessions on tides were held at international  
108 conferences. These included presentations on tides at the EGU General Assembly in Vienna in April  
109 2019 and the IUGG General Assembly in Montreal in July 2019. Events were also held locally to mark  
110 the LTI anniversary, including a large meeting for the public at the Merseyside Maritime Museum in  
111 May 2019 (Woodworth, 2020b) and in talks to Liverpool history groups.

112

## 113 2.1 History of Tidal Science in the Special Issue

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115 One of the first papers in the special issue was concerned with the tidal data obtained by James Cook  
116 during his remarkable voyage to Tahiti to observe the Transit of Venus followed by the first landings  
117 by Europeans in New Zealand and Australia (Woodworth and Rowe, 2018). This paper marked yet  
118 another anniversary in 2019, in this case being 250 years since Cook's arrival at Tahiti. The paper  
119 discusses how puzzled Cook was by diurnal inequality in the tide along the Queensland coast, a factor  
120 which led to the near-sinking of the *Endeavour*, and diurnal inequality was later to be an important  
121 aspect of tidal research in the 19<sup>th</sup> century.

122

123 Agnew (2020) discusses how tidal fluctuations in gravity played an important role in the accuracy of  
124 timing measurements using pendulum clocks, which were up until the 1940s the best timekeepers  
125 available. The paper shows that the best pendulum clocks were able to detect tides long before the  
126 advent of measurements by gravimeters or Global Navigation Satellite System (GNSS) technology. This  
127 particular aspect of pendulum clocks does not appear to have been addressed at the LTI. However,  
128 good timing was certainly one of the LTI's general interests, as it had been in Liverpool since the middle  
129 of the 19<sup>th</sup> century, first by the astronomer John Hartnup of the Liverpool Observatory at Waterloo  
130 Dock and then at Bidston Observatory. <sup>2</sup> Recent papers (not in the special issue) discuss how timing  
131 formed an important aspect of local scientific research and services over many years. These include  
132 the famous time transfer experiments between Liverpool and Boston; the provision of a chronometer  
133 calibration service for seafarers; and through the time control of the Liverpool One O'Clock Gun and  
134 time balls (Schmidt and Dearden, 2019, 2020; Thomas and Thomas, 2020a,b).

135

136 Other historical topics are addressed by Carlsson-Hyslop (2020) who, as mentioned above, provides  
137 many details of the complicated discussions which resulted in the founding of the LTI. One topic  
138 mentioned in that paper concerns the importance of the provision of tidal predictions to its overall  
139 finances. The use of TPMs became essential to such work, as discussed by Woodworth (2020a), and  
140 the LTI, under the direction of Doodson, became a world leader in the design and operation of TPMs.

141

142 Finally, a reminder that tidal measurements have a long history in many other countries is provided  
143 by Raicich (2020) who discusses recording at Trieste since 1782. This paper is an example of what has  
144 become known as 'data archaeology', whereby the information contained in sometimes vulnerable  
145 paper records is being converted into computer form so that the important data can be used in studies  
146 of long-term climate change.

147

## 148 2.2 Tidal Science at the LTI

149

150 The history of a branch of science can often be marked by the introduction of new technologies which  
151 have revolutionised and reinvigorated the research. Tidal science, and sea-level science in general,  
152 provides a good example. In the following, we mention some of the research areas at the LTI which

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<sup>2</sup> A good summary of the history of research at first the Liverpool Observatory and then at Bidston Observatory, marking the centenary of the founding of the former, was provided by Doodson in LOTI (1945).

153 involved tides and sea levels and which benefitted from new technology. This provides one way of  
154 relating the LTI's history to the research papers contained in the special issue. The areas include:

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- 156 • Tidal Prediction

157

158 Woodworth (2020a) explains how it became possible to determine tidal harmonic constants from a  
159 set of tide gauge data. In principle, these constants could be used to provide tidal predictions by means  
160 of tedious hand computations. However, the technological leap provided by Kelvin's invention of the  
161 TPM, a type of analogue computer, speeded up the determination of predictions considerably.  
162 Between the 1870s and 1960s, over 30 TPMs were constructed around the world, of which the  
163 majority were made in the UK. Only three of them were used for tidal prediction at the LTI itself.  
164 However, there were more for which Doodson played a major role in their design or supervised closely  
165 their manufacture. Of course, TPMs were superseded by another technological leap, the advent of  
166 digital computers in the 1960s.

167

- 168 • Storm Surge Modelling

169

170 Proudman (1968) remarked that towards the end of Doodson's tenure as LTI Director he strenuously  
171 opposed the use of modern digital computers, claiming that they would increase the cost of providing  
172 tidal predictions to harbour authorities. That reservation is understandable given Doodson's lifetime  
173 involvement with the TPMs and the fact that they were still a source of income. It was left to his  
174 successor Jack Rossiter to introduce modern computers to the LTI.

175

176 The study of 'meteorological effects on the tides' (i.e. storm surges) had been included in the LTI's  
177 terms of reference since its founding. However, the study was given impetus by the major floods of  
178 1953 (Wolf and Flather, 2005). Attempts were made by Shizuro Ishiguro at the National Institute of  
179 Oceanography (NIO) in the UK (in the south of England, not then associated with the LTI) to predict  
180 surges using electronic analogue computers (Kennard, 2016; Wolf, 2017). However, the work became  
181 much easier once advances in technology had led to the availability of powerful digital computers. In  
182 turn, this enabled the development of numerical storm surge models. Work at the LTI was led by  
183 Norman Heaps and Roger Flather (e.g. Heaps, 1983), with their models adopted for operational use  
184 by the Meteorological Office and Environment Agency for flood warning around the coast of the  
185 United Kingdom and control of the Thames Barrier.

186

- 187 • Sea Level Measurements

188

189 The measurement of the tide, and sea level variations in general, using tide gauges has always been  
190 an LTI interest. In 1933, Doodson together with Chadburns of Liverpool installed instrumentation to  
191 the tide gauge in Birkenhead docks, two miles away, so that data could be transmitted to Bidston  
192 Observatory, an early example of near-real-time data reporting. He also designed a current meter for  
193 use on annual Irish Sea cruises (Proudman, 1968) (Figure 2). Eventually, the LTI became a centre of  
194 expertise for tide gauge technology and was responsible for on-going sea level measurements in both  
195 the UK and abroad. It also became a data centre for tide gauge information, the UK data being quality  
196 controlled by the British Oceanographic Data Centre, and mean sea level information from around the  
197 world being archived by the international Permanent Service for Mean Sea Level (PSMSL,  
198 <https://www.psmsl.org>). The latter had been initiated at Bidston in 1933 with Proudman as its first  
199 Secretary. The PSMSL has become one of the main services of the International Association for the  
200 Physical Sciences of the Oceans (Smythe-Wright et al., 2019), and its data set is used within a wide  
201 range of geophysical research, including the regular scientific assessments of the Intergovernmental  
202 Panel on Climate Change (IPCC).

203

204 Doodson also experimented in the 1930s with a number of Favé pressure gauges with which  
205 measurements of the tide offshore were obtained. However, it was not until the 1960s that the serious  
206 measurement of deep-sea tides using bottom pressure records (BPRs) began in the UK, led by the  
207 group of David Cartwright at the NIO. That small team transferred to Bidston Observatory in 1974  
208 when Cartwright became Assistant Director of the Institute of Oceanographic Sciences (Bidston), as  
209 the LTI was then called. Cartwright's contribution to tidal science in the latter half of the 20<sup>th</sup> century  
210 was immense, and he raised the intellectual level of the Institute's contribution enormously. The team  
211 became the world leaders in the measurement of tides at depths down to 5000m (Figure 3). The same  
212 instruments were also used for ocean transport measurements during the World Ocean Circulation  
213 Experiment (WOCE) (Spencer and Vassie, 1997). Cartwright's own interests in sea level measurements  
214 were to be extended later into the use of satellite altimeter data, mostly in studies of tides, in  
215 collaboration with US and UK researchers. Cartwright became the third Fellow of the Royal Society  
216 associated with the LTI. A detailed biography may be found in Webb (2017).

217

218 • Earth Tides

219

220 Bidston Observatory has two levels of basements cut into the sandstone of Bidston Hill. In 1909, a  
221 horizontal pendulum seismometer was installed by John Milne, specifically to study the tidal loading  
222 of the solid Earth. This showed clearly the tilt in the north-south direction due to loading by the tide  
223 in the adjacent Irish Sea (Milne, 1910).

224

225 After measurements using different instruments over many years by different groups, it was  
226 concluded that tilt measurements were overly sensitive to local geology (Baker, 1980), and gravity  
227 measurements took their place, the Bidston research group being equipped with LaCoste and  
228 Romberg Earth Tide meters. These were used at many locations in the UK and abroad, and the  
229 measurements by the Bidston group were shown to be particularly accurate due to their unique  
230 electrostatic feedback mechanism and the careful recalibration of the gravimeters on the Hannover  
231 gravity baseline in Germany. From the mid-1980s onwards, superconducting gravimeters were  
232 deployed at a number of sites around the world (but not in the UK), with calibrations mainly provided  
233 by new Micro-g LaCoste FG5 absolute gravity meters (see below). The results from these  
234 superconducting gravimeters are in close agreement with the earlier results of the Bidston group's  
235 LaCoste and Romberg Earth Tide gravimeters (Baker and Bos, 2003).

236

237 The development of GNSS technology in the 1990s, of which the Global Positioning System (GPS) is  
238 the most well-known, enabled the vertical variations of the loading tide to be measured in an global  
239 reference frame for the first time (and also its smaller horizontal components). The LTI group was  
240 among the first to demonstrate the capabilities of GNSS in this way and it is now the main technique  
241 for tidal loading studies. The result of all this body of work has been to demonstrate which ocean tide  
242 models are more accurate than others, through computation of their corresponding loading tide  
243 distributions, followed by comparison of those distributions to the gravimeter or GNSS data. In  
244 addition, one learns a considerable amount concerning the physical properties of the solid Earth (Bos  
245 et al., 2015). For an authoritative history of this part of the LTI's research, the reader is referred to the  
246 unpublished article by Baker (2016).

247

248 • Geodetic Measurements

249

250 Alongside the GNSS measurements for tidal loading studies, the LTI group embarked in the 1990s on  
251 collaborative research, especially with Nottingham University, on using the technique to measure  
252 long-term rates of vertical land movements in the UK. Such GNSS data sets are now used by many  
253 groups around the world in order to remove land movements from time series of relative sea level  
254 measurements provided by tide gauges. This is becoming a well-established technique, although

255 problems remain, such as the stability of the reference frame in which measurements are made  
256 (Wöppelmann and Marcos, 2016). Eventually, the group also acquired two Micro-g LaCoste FG5  
257 absolute gravity meters, which measure small changes in the local acceleration due to gravity that can  
258 be interpreted as equivalent to changes in vertical land movement (e.g. Teferle et al., 2006). However,  
259 although absolute gravity continues to be used by other groups, especially where land movements are  
260 particularly large (e.g. due to Glacial Isostatic Adjustment in Canada), it is no longer used in this role  
261 in the UK.

262

- 263 • Other Research

264

265 The above sub-headings inevitably omit those research topics at the LTI which were not particularly  
266 dependent on technology but which nevertheless had an important connection to tidal science. The  
267 most obvious ones are the many dynamical studies of Proudman, a good summary of which can be  
268 found in Cartwright (1980). They also omit many other aspects of the LTI's work which are less  
269 applicable to the special issue. These include studies of coastal and shelf processes, modelling of water  
270 quality and ecosystems, and investigations into the use of wave and tidal energy. For a more complete  
271 overview of work at the LTI, the reader might consult publications such as Scofield (2006) or its regular  
272 reports through the years.

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Figure 2. Joseph Proudman (right), Arthur Doodson (centre) and R.J. Daniel, a marine biologist from Liverpool University (left), during an Irish Sea cruise in the late 1930s aboard the *Zephyr*. Photograph courtesy of Valerie Gane. Other photographs of Doodson may be found in Carlsson-Hyslop (2020) and Woodworth (2020a).





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Figure 3. David Cartwright, FRS (1926-2015) (left) and colleagues around a 'Mark IV' bottom pressure recorder deployed to measure the tide in over 3000 m of water NE of the Azores in 1980. Others appearing the photograph (left to right): Ken Parry, Ian Vassie, Bev Hughes and Bob Spencer. Photograph courtesy of the National Oceanography Centre.

### 291 2.3 Tidal Science in the Special Issue

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It is possible to make connections in many cases between papers in the special issue and the areas of work at the LTI mentioned above.

296 For example, Woodworth and Hibbert (2018) discuss long period ocean tides (Mf, Mm and Mt) in the  
297 Drake Passage, and how their variation over a nodal cycle compares to expectations from the  
298 equilibrium tide. They were indeed found to vary as expected. However, such a study would have been  
299 impossible without the many years of BPR measurements in that 'choke point' area undertaken for  
300 the WOCE and in the following years.

301  
302 The term 'radiational potential' was introduced by Walter Munk to account for motions of a tidal  
303 nature, which are caused, directly or indirectly, by the Sun's radiation, instead of being of astronomical  
304 tidal origin due to the Moon or Sun. Radiational tides include seasonal and diurnal variations due to

305 varying meteorological forcings. In addition, there are important non-astronomical seasonal variations  
306 in sea level due to steric (density) changes in the ocean. The magnitude of such radiational tidal  
307 contributions was estimated by Cartwright and Tayler (1971), work which came just before  
308 Cartwright's move to the LTI. Williams et al. (2018) take a fresh look at these quasi-tidal variations and  
309 consider how they may be double-counted in storm surge forecasts and also how estimates of Highest  
310 Astronomical Tide might be affected.

311  
312 Third-degree tides represent a much under-studied aspect of tidal research, probably because they  
313 are very small (usually millimetric) at most locations and so are of less interest to people primarily  
314 interested in tidal predictions. Nevertheless, the different spatial pattern of their forcing in the tidal  
315 potential to those of the more familiar second-degree semidiurnal and diurnal tides provides another  
316 way of testing our understanding of the ocean's response to astronomical forcing. Woodworth (2019)  
317 returned to this topic using the global set of tide gauge data in the GESLA-2 data set and a global  
318 numerical model. M1, the largest third-degree tide, was confirmed to have a geographical variation  
319 consistent with the suggestions of Platzman and Cartwright, that it is generated in the ocean as a  
320 consequence of the spatial and temporal overlap of M1 in the tidal potential and one (or at least a  
321 small number of) diurnal ocean normal mode(s). It is remarkable that several of the larger (but still  
322 tiny) third-degree tides have also begun to be mapped reliably by making use of the many years of  
323 precise satellite altimetry (Ray, 2020).

324  
325 One result of Cartwright's sabbatical at the Scripps Institution of Oceanography with Walter Munk  
326 during 1963-1965 was the development of the response method of tidal analysis in which tides are  
327 treated as the overall oceanic response to the astronomical forcing by the Moon and Sun (Munk and  
328 Cartwright, 1966). In this special issue, Byun and Hart (2020b) further develop their own response-  
329 type method of analysis with application to a mixed tidal regime around Antarctica. In an earlier paper  
330 in the issue (Byun and Hart, 2020a), the same authors explained their classification scheme for tides  
331 around New Zealand in terms of the relative proportions of the S2, N2, and M2 constituents, N2 being  
332 relatively more important than S2 along some parts of the coast. Their new index provides a useful  
333 addition to the usual Form Factor classification which simply describes the relative importance of  
334 diurnal and semidiurnal components. Tidal analysis is also the topic of the paper by Boesch and Müller-  
335 Navarra (2019) who make use of a technique called the Harmonic Representation of Inequalities  
336 (HROI) method, that combines aspects of harmonic and non-harmonic methods, to reassess long-  
337 period constituents for tidal predictions along the German North Sea coast and its tidally influenced  
338 rivers. The usefulness of tidal predictions arising from tidal analysis in providing information on actual  
339 high tides for use in the international Witness King Tides project (<http://kingtides.net/>) is assessed in  
340 a paper by Hunter (2020).

341  
342 Global tide modelling is represented in the special issue by Lyard et al. (2021) who discuss the  
343 performance of the most recent global tide model of the Toulouse group (FES2014). This model  
344 provides a significant improvement on earlier versions and is one of the most obvious demonstrations  
345 of the value of many years of satellite altimetry. Regional modelling is represented by Medvedev et  
346 al. (2020), who provide a model of the tides of the Caspian Sea, making use of available tide gauge  
347 data around its coast. The importance of bathymetry in the modelling of tides in extensive shallow  
348 water regions is demonstrated by Rasquin et al. (2020), who consider the uncertainties in how tides  
349 might change in the German Bight following a rise in sea level. The importance of bathymetry also  
350 enters into the study of Fofonova et al. (2019) who consider the non-linear aspects of tidal dynamics  
351 in an even smaller part of German-Danish coastal waters.

352  
353 The need for good bathymetric information in tide modelling of coastal waters is also discussed by  
354 Green and Pugh (2020). The authors make use of a large number of short-term tidal measurements  
355 around Bardsey Island off the coast of North Wales to investigate how well the dynamics of tidal  
streams around the island compare to present knowledge derived from satellite altimetry or regional

356 tide models, both having their acknowledged spatial resolution limitations. The set of tide gauge  
357 measurements infers much larger tidal currents than anticipated with important consequences for the  
358 computation of local tidal energetics.

359  
360 There is an agreed need to understand better the reasons for variability in tides on longer timescales  
361 for the whole global coastline (Haigh et al., 2020). A possible connection between long-term changes  
362 in the tide in the North Atlantic and the North Atlantic Oscillation climate index is discussed in this  
363 issue by Pineau-Guillou et al. (2020), while Harker et al. (2019) discuss possible changes to tides  
364 around Australia due to a rise in mean sea level.

365  
366 Tidal loading investigations such as those described above at the LTI are represented in the special  
367 issue by two papers (Wang et al., 2020; Matviichuk et al., 2020). The former paper considers  
368 asthenospheric anelasticity effects on ocean tide loading around the East China Sea using GNSS data  
369 and employing a number of ocean tide models from which loading is computed. The latter paper  
370 investigates the potential improvements in GNSS loading measurements around the UK and western  
371 Europe using GLONASS data in combination with GPS. These two papers demonstrate the present  
372 maturity of using GNSS in tidal loading studies.

373  
374 Internal tides were primarily a regional numerical modelling activity at the LTI (e.g. Xing and Davies,  
375 1999). They are now being modelled worldwide by several groups (e.g. Zaron, 2019b) with important  
376 applications to studies of tidal energy dissipation, vertical heat transfer, ocean mixing and, potentially,  
377 variations in climate. This topic is represented in the special issue by a regional study of the  
378 predictability of Caribbean internal tides by Zaron (2019a), and an accuracy assessment of various  
379 global internal tide models by Carrere et al. (2021). The benefits of technology for the local  
380 measurement of internal tides using gliders and moored acoustic Doppler current profilers is  
381 described by Hall et al. (2019).

382  
383 The only paper in the issue concerned with the role of the tide in marine biology is that of Petrushevich  
384 et al. (2020) who consider the impact of tidal dynamics on diel vertical migration of zooplankton in  
385 Hudson Bay.

386  
387 In possibly the most charming paper in the special issue, Cooper et al. (2018) discuss the ability to  
388 learn about tidal currents by observing the positions of sea birds (razorbills) resting on the water  
389 surface and thereby functioning as 'drifters of opportunity'. This paper provides a good demonstration  
390 of how a new technology (in this case GNSS tracking) can complement existing techniques for  
391 measuring tidal currents.

392

### 393 3. A Short Forward Look on Tides

394  
395 The availability of precise satellite altimeter data in the early 1990s revolutionised the development  
396 of regional and global tide models (Stammer et al., 2014). These models provide accurate maps of  
397 amplitude and phase lag for the largest constituents of the barotropic tide throughout the global  
398 ocean, and enable a reliable determination of tidal energy budgets (Ray and Egbert, 2017). However,  
399 this encouraging situation is far from complete. For example, there is still a need to know more about  
400 seasonal variability in the tides, including those at high latitudes under ice shelves. Measurements in  
401 polar regions require the use of several different types of *in situ* tide gauge or GNSS instrumentation  
402 as well as altimetry.

403  
404 A particular high priority is to have a better understanding of tides in coastal waters, comparable in  
405 accuracy and completeness to our knowledge of deep-ocean tides. For example, one of the tests of  
406 the Stammer et al. (2014) review was to calculate differences in tidal heights from the eight major

407 constituents in the models and the heights derived using the same constituents obtained from  
408 analyses of in situ (tide gauge) data. The best models showed root-sum-square agreement of  
409 approximately 0.9, 5.0, and 6.5 cm for pelagic (deep ocean), shelf and coastal regions, respectively.  
410 This demonstrated the centimetric accuracy for the best models over most of the deep ocean.  
411 However, the modelled tides were found to be considerably less accurate close to the coast, where  
412 problems remain due to the inherent limitations of spatial and temporal sampling by altimeters,  
413 technical issues to do with land contamination in altimeter and radiometer footprints, and the fact  
414 that coastal tides are larger and more complex than those of the deep ocean with a multiplicity of  
415 shallow-water processes (Ray et al., 2011; Woodworth et al., 2019).

416

417 The need to do better near the coast has resulted in a whole new field of research being created called  
418 'coastal altimetry' (Vignudelli et al., 2019). It has spurred more sophisticated processing (retracking)  
419 of radar returns from existing and past missions, in order to remove as much as possible of the land  
420 contamination from the data. In addition, the altimeters of later missions such as Cryosat-2, Sentinel-  
421 3 or Sentinel-6 are capable of providing measurements closer to the coast (for the global coastline for  
422 the latter, only certain sections of coast for the former). It remains to be seen how well data from  
423 these missions will benefit global tide models in general. Attention is now turning to the next  
424 generation of altimeters for tidal research (e.g. SWOT, Morrow et al., 2019) which will provide  
425 considerably greater information on tidal variations on short spatial scales including in coastal waters.

426

427 Many opportunities for future tidal studies exist for interested researchers, for example in a better  
428 estimation of the global tide through geological history. Such studies are important for a more  
429 complete understanding of topics such as species evolution. The same modelling techniques can be  
430 applied to the study of putative tides on other planets and even exoplanets. In addition, there is much  
431 to be learned how tides contribute to biological variability and to variations in the climate of our planet  
432 through modulation in the strength of the over-turning circulation. There have been recent papers on  
433 all these subjects (too many to list here) but it is clear that much interesting research remains.

434

#### 435 4. Conclusions

436

437 We hope that this special issue has been useful in marking an anniversary of an important institution  
438 in the history of tidal science. The work advanced at the LTI is far from over and continues as part of  
439 the present-day National Oceanography Centre. In addition, we hope that the special issue will also  
440 have been of interest in providing a snapshot of the exciting range of present-day tidal research.

441

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450

451

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