

Tidal resonance in the Gulf of Thailand

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**Abstract.** The Gulf of Thailand is dominated by diurnal tides, which indicates that the resonant frequency of the gulf is close to one cycle per day. However, when applied to the gulf, the classic quarter-wavelength resonance theory fails to yield a diurnal resonant frequency. In this study, we first perform a series of numerical experiments showing that the gulf has a strong response near one cycle per day and that the resonance of the South China Sea main area has a critical impact on the resonance of the gulf. In contrast, the Gulf of Thailand has little influence on the resonance of the South China Sea main area. An idealised two-channel model that can reasonably explain the dynamics of the tidal resonance in the Gulf of Thailand is then established in this study. We find that the resonant frequency around one cycle per day in the main area of the South China Sea can be explained with the quarter-wavelength resonance theory, and the large-amplitude response at this frequency in the Gulf of Thailand is basically a passive response of the gulf to the increased amplitude of the wave in the southern portion of the main area of the South China Sea.

1 Introduction

The Gulf of Thailand (GOT) is an arm of the South China Sea (SCS), the largest marginal sea of the western Pacific Ocean (Fig. 1). The width of the GOT is approximately 500 km, and the length of the GOT from the top to the mouth of the gulf, as indicated by the blue line B in Fig. 1, is approximately 660 km. The mean depth in this area is 36 m according to the ETOPO1 depth data set (from the US National Geophysical Center). The mean depth of the SCS from the southern opening of the Taiwan Strait to the cross section at 1.5°N is 1323 m. If the GOT is excluded, the mean depth of the rest of the SCS (herein called the SCS body and abbreviated as SCSB) is 1457 m. Tidal waves propagate into the SCS from the Pacific Ocean through the Luzon Strait (LS) and mainly propagate in the southwest direction towards the Karimata Strait, with two branches that propagate northwestward and enter the Gulf of Tonkin and the GOT. The energy fluxes through the Mindoro and Balabac Straits are negligible (Fang et al., 1999; Zu et al., 2008; Teng et al., 2013). The GOT is dominated by diurnal tides, and the strongest tidal constituent is K<sub>1</sub> (Aungsakul et al., 2011; Wu et al., 2015).

The resonant responses of the GOT to tidal and storm forcing have attracted extensive research interest. However, the previous results have been diverse. Yanagi and Takao (1998) simplified the GOT and Sunda Shelf as an L-shaped basin and concluded that this basin has a resonant frequency near the semi-diurnal tidal frequency. Sirisup and Kitamoto (2012)

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applied a normal mode decomposition solver to the GOT and Sunda Shelf area and obtained four eigenmodes with modal frequencies of 0.42, 1.20, 1.54 and 1.76 d<sup>-1</sup> (cycle per day). Tomkratoke et al. (2015) further studied the characteristics of these modes and concluded that the mode with a frequency of 1.20 d<sup>-1</sup> is the most important. Cui et al. (2015) used a numerical method to estimate the resonant frequencies of the seas adjacent to China, including the SCS and the GOT, and found that the GOT has a major resonant frequency of 1.01 d<sup>-1</sup> and a minor peak response frequency of 0.42 d<sup>-1</sup>. In these studies, except for Yanagi and Takao (1998), no effort was made to establish a theoretical model of the GOT, and the resonant period estimated by Yanagi and Takao (1998) cannot be used to explain the resonance of the diurnal tides.

The GOT is a semi-enclosed gulf with an amphidromic point in the basin for each K<sub>1</sub> and O<sub>1</sub> constituent. Wu et al. (2013) reproduced the tidal system well with superimposed incident and reflected Kelvin waves and a series of Poincare modes. This result raises the question of whether the quarter-wavelength resonant theory can explain the tidal resonance in the gulf, as is the case with other areas (Miles and Munk, 1961; Garrett, 1972; Sutherland et al., 2005). According to quarter-wavelength theory, because the distance from the head of the gulf to the mouth is approximately 660 km and the mean depth is approximately 36 m, the resonant frequency should be 0.61 d<sup>-1</sup>, which is much lower than the estimates by Cui et al. (2015) and Tomkratoke et al. (2015). Thus, it is clear that the tidal resonance phenomenon in the GOT cannot be reasonably explained by the quarter-wavelength theory.

According to the theories of Garrett (1972) and Miles and Munk (1961), tidal oscillations are limited to a specific area. In contrast, Godin (1993) proposed that tides are a global phenomenon that cannot be separated into independent subdomains. The GOT is an auxiliary area of the SCS and is connected to the SCSB. We thus believe that Godin's theory is applicable to the GOT. In this paper, by considering the bathymetry of the SCSB in numerical experiments and theoretical analyses, we investigate the reasons for the GOT to have a strong response around the frequency of one cycle per day and how the physical properties of the SCSB primarily determine the resonances of both the SCSB and the GOT.

## 2 The numerical model

### 2.1 Governing equations and model configuration

In this paper, we use the Princeton Ocean Model (POM) for numerical investigation, but we partially modify its code to meet the needs of the present study. This study is limited to the main mechanism of diurnal tidal resonance; accordingly, the elimination of tidal forces and nonlinear terms and the linearisation of bottom friction in the control equation will not affect the problem we are studying, and the two-dimensional model effectively suits our purpose as shown in a number of previous studies (e.g., Garrett, 1972; Godin, 1993; Webb, 2014; Cui et al., 2015). The general forms of the equation of continuity and the equation of motion used in this study are as follows:

$$\frac{\partial \tilde{\zeta}}{\partial t} = -\frac{1}{R \cos \varphi} \left[ \frac{\partial (H \tilde{u})}{\partial \lambda} + \frac{\partial (H \tilde{v} \cos \varphi)}{\partial \varphi} \right], \quad (1)$$

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$$\frac{\partial \tilde{u}}{\partial t} = 2\Omega \tilde{v} \sin \phi - \frac{g}{R \cos \phi} \frac{\partial \tilde{\zeta}}{\partial \lambda} - \frac{\tau \tilde{u}}{H}, \quad (2)$$

$$\frac{\partial \tilde{v}}{\partial t} = -2\Omega \tilde{u} \sin \phi - \frac{g}{R} \frac{\partial \tilde{\zeta}}{\partial \phi} - \frac{\tau \tilde{v}}{H}, \quad (3)$$

where  $t$  denotes time;  $\lambda$  and  $\phi$ , respectively, refer to the east longitude and north latitude;  $\tilde{\zeta}$  is the surface height above the undisturbed sea level;  $\tilde{u}$  and  $\tilde{v}$  represent the east and north components of the fluid velocity, respectively;  $R$  indicates the Earth's radius;  $\Omega$  refers to the angular speed of the Earth's rotation;  $g$  is the gravitational acceleration;  $H$  denotes the undisturbed water depth; and  $\tau$  represents the linearised bottom friction coefficient.

The computational domain selected is in the range of 99-131 °E and of 1.5-42 °N. The northern and eastern open boundaries are located far beyond the area of the SCS to prevent the numerical values at the open boundaries from influencing the results in the study area. The southern open boundary is set along a latitudinal section of 1.5 °N, which meets the southernmost tip of the Malay Peninsula. The grid resolution is 1/12 °. The water depths are basically taken from the ETOPO1 data set and are modified using depth data extracted from navigational charts.

## 2.2 Simulation of the K<sub>1</sub> tide

To examine the applicability of the modified POM model to the study area, the model is first used to simulate the K<sub>1</sub> tide in the SCS and its neighbouring area. The amplitudes and phase-lags along the open boundary are taken from the global tidal model TPX09, which is based on satellite altimeter observations (Egbert and Erofeeva, 2002). The model-produced K<sub>1</sub> tidal system is shown in Figure 2a, and a comparison of the model results with observations at 31 tidal gauge stations is shown in Table 1. The locations of these tidal stations are shown in Figure 1, from which it can be seen that the stations are basically evenly distributed along the coast of the SCSB and GOT.

From Table 1, we can see that the deviations in amplitudes are mostly within 0.05 m, while those in phase-lags are mostly within 20 °. Considering that the governing equations are greatly simplified, the linearised bottom friction is used to replace the more accurate quadratic form, the agreement between model results and observations can be regarded as satisfactory. Therefore, the modified model is applicable to the SCS and GOT tidal study.

To show the characteristics of the wave propagation process, we calculate the tidal energy flux density distribution, as given in Figure 2b. One can see that the K<sub>1</sub> tidal wave mainly enters the SCS through the LS and spreads southward, partially moves to the GOT, and partially exits the SCS through the Karimata Strait. Figure 2a shows that the K<sub>1</sub> tidal amplitudes are large in the Gulf of Tonkin and that there is an amphidromic point at the mouth of the gulf caused by one-quarter wavelength resonance (Fang et al., 1999). In the GOT, there is also an amphidromic point, but away from the mouth section, indicating that the amplified K<sub>1</sub> tide cannot be attributed to the quarter-wavelength resonance.

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### 3 Numerical methods for estimating the resonant frequency

#### 3.1 Open boundary condition

The open boundary condition for the tidal resonant study can be written in the following form:

$$\tilde{\zeta}(i, j, t) = \sum_{n=N_1}^{N_2} \tilde{Z}_n(i, j) \cos[2\pi f_n t - \tilde{\theta}_n(i, j)], \quad (4)$$

- 5 where  $(i, j)$  are grid points on the open boundary;  $f_n = n\Delta f$  refers to the frequency of the  $n$ -th wave of interest, with  $\Delta f$  referring to the spectrum resolution; and for  $n = N_1, N_1 + 1, \dots, N_2$ ,  $\tilde{Z}_n$  and  $\tilde{\theta}_n$  represent the amplitude and phase lag of the  $n$ -th wave, respectively. In this study we choose  $\Delta f = 1/1024 \text{ h}^{-1}$  for the following two reasons: First, the value 1024 is equal to  $2^{10}$ , enabling us to efficiently calculate spectra from model-produced time series by using a fast Fourier transform (FFT). Second, because the minimum frequency difference between the main tidal constituents ( $Q_1$ ,  $O_1$ ,  $K_1$ ,  $N_2$ ,  $M_2$ , and  $S_2$ ) is equal to  $1.51 \times 10^{-3} \text{ h}^{-1}$ , the resolution of  $\Delta f = 1/1024 \text{ h}^{-1}$  is sufficient for separating these constituents.
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#### 3.2 Numerical model of the seas adjacent to China

Through the simulation of the  $K_1$  tide, it is shown that the modified model can be applied to tidal study. The model setting is consistent with the setting of the simulation of the  $K_1$  tide except that the water level values at the open boundaries are changed as follows. The amplitudes  $\tilde{Z}_n$  at the open boundaries are specified as a constant, 2 cm; the phase-lags  $\tilde{\theta}_n$  are

- 15 given as random numbers that are evenly distributed in the interval  $(0, 2\pi)$  and generated using a normal random number generator. The purpose of using random phase lags is to avoid all or some of the waves to have the same phase at a certain time, which can lead to simultaneous unreasonably high or low sea levels. The selected  $N_1$  and  $N_2$  values are 1 and 107, respectively. Thus, the frequencies of the waves studied range from  $1/1024$ - $107/1024 \text{ h}^{-1}$  or  $0.0234$ - $2.5078 \text{ d}^{-1}$ . The corresponding periods range from  $10$ - $1024 \text{ h}$  (approximately  $0.4$ - $42.7$  days), which covers all main tidal constituents.

- 20 In the last cycle of 1024 hours, the hourly results at each grid point are preserved, and FFT analysis is performed to yield amplitude  $Z_n$  and phase lag  $\theta_n$ . The amplitude ratio is defined as follows:

$$G_n = Z_n / \tilde{Z}_n, \quad (5)$$

and the phase lag difference is given by the following equation:

$$\psi_n = \theta_n - \tilde{\theta}_n. \quad (6)$$

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According to Munk and Cartwright (1966),  $Ge^{-i\psi}$  is the admittance. Specifically, as Munk and Cartwright (1966) stated,  $G_n$  is the amplitude response and represents the amplification factor of the  $n$ -th wave in response to forcing. In the present study, we call  $G_n$  and  $\psi_n$  the amplitude gain and phase change, respectively, in accordance with Sutherland et al. (2005) and Roos et al. (2011).

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#### 5 **4. Influence of resonance in the main area of the South China Sea on the Gulf of Thailand**

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Cui et al. (2015) revealed that both the SCS and GOT have strong response peaks around one cycle per day and suggested that the resonance of the SCS could be explained by one-quarter wavelength resonance theory, but the authors did not provide the reasons for the strong response of the GOT around this frequency. As an arm of the SCS, the tidal energy of the GOT comes mainly from the SCSB (Figure 2b), so we speculate that the strong response of the GOT around one cycle per day may be related to the SCS resonance.

To examine the influence of SCSB resonance on GOT, we conduct six numerical experiments: Exp. 1 to Exp. 6. In Exp. 1, we use real bottom topography. In Exp. 2, we artificially make the depths in the SCSB equal to half of the real depths and retain the depths in the GOT. In Exp. 3, the depths in the SCSB are artificially doubled and the depths in the GOT remain unchanged. In Exp. 4 and 5, we change the water depths of the GOT by factors of 1/2 and 2, respectively, and the SCSB depths remain unchanged. In Exp. 6, the mouth boundary of the GOT (indicated by the blue line B in Fig. 1) is artificially closed and the SCSB retains the real depths. The results of these six experiments are shown in Figure 3, in which the area-mean values of the top 20% amplitude gains are used to represent the response of the corresponding area. The resonant frequencies corresponding to peak responses are listed in Table 2.

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Table 2 and Figure 3 show that when real water depths are used, the resonant frequency of the SCSB appears at  $0.99 \text{ d}^{-1}$  while that of the GOT is  $1.01 \text{ d}^{-1}$ . The resonant frequencies of these two areas are basically the same, and both are very close to that of the diurnal tide  $K_1$ , whose frequency is equal to  $1.00 \text{ d}^{-1}$  (or more precisely,  $1.0027 \text{ d}^{-1}$ ). The spatial patterns of the amplitude gain and phase change for the frequency  $0.99 \text{ d}^{-1}$  are displayed in Figure 4a, with corresponding energy flux density vectors shown in Figure 4b (the corresponding figures for  $1.01 \text{ d}^{-1}$  are almost the same and are thus not shown). We can find that the patterns shown in Figure 4 are quite similar to the simulated  $K_1$  patterns shown in Figure 2. Minor differences are caused by the use of different open boundary conditions.

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From Figures 3a and 3b, we can see that the peak amplitude gains in the GOT and SCSB are reduced when the depths of the SCSB are changed to half of the real depths. This reduction in amplitude gain occurs because friction increases as depth decreases (see Eqs. (2) and (3)). Moreover, the amplitude peak frequencies in the GOT and SCSB both change to  $0.75 \text{ d}^{-1}$  (Figure 3a-b and Table 2), indicating that the resonant frequency in the GOT is determined by that of the SCSB. When the depths of the SCSB are doubled, the amplitude peak frequencies of the SCSB and GOT are increased to  $1.49$  and  $1.50$ , respectively (Figure 3a-b and Table 2), again indicating that the peak frequency of the GOT is determined by that of the

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SCSB. It is worth noting that when the depths in the SCSB are artificially changed by factors of 1/2 and 2, the resonant frequencies are roughly changed by factors of  $\sqrt{1/2}$  and  $\sqrt{2}$ , respectively. This indirectly indicates that the quarter-wavelength resonance theory is applicable to the SCSB.

In Exp. 3, there is another weaker peak in the SCSB at the frequency of approximately  $1.15 \text{ d}^{-1}$  (Fig. 3a). The peak frequency response may also have an effect on the GOT (Fig. 4b, Exp. 3), which results in a plateau peak of GOT between  $0.5 \text{ d}^{-1}$  and  $1.2 \text{ d}^{-1}$ . This may be due to the deepening of the SCSB, resulting in discontinuity of topographic data at the junction with the GOT. Moreover, the amplitude gains in the GOT are significantly increased by increasing the depth, which results in reduced friction (see Eqs. (2) and (3)).

Experiments 1-3 suggest that the peak response frequency of the GOT is strongly affected by the SCSB. Here, we conduct further experiments (Exps. 4-6) to investigate whether the GOT can also influence the resonance of the SCSB. From the results of Exps. 4-5 (Table 2, Figures 3c-d), it can be seen that changing the depths of the GOT has little effect on the peak response frequencies of the SCSB and GOT. That is, the resonant frequencies of both areas are still close to one cycle per day.

In Exp. 6, the mouth boundary of the GOT (indicated by the blue line B in Figure 1) is artificially closed. The results of this experiment show that the GOT has a small influence on the response of the SCSB, as shown in Fig. 3c. When boundary B is closed, the resonant frequency of the SCSB becomes slightly higher than the frequency of the  $K_1$  tide, and the response amplitude of the SCSB in the vicinity of the resonant frequency is slightly reduced. As indicated by Arbic et al. (2009), when a shallow basin is connected to a deep basin, the impact of the shallow basin on the tidal response in the deep basin is determined by the depth ratio, width ratio, and length ratio of these two basins, as well as the friction in the shallow basin. In the present case, the depth and width ratios of the GOT against the SCSB are small, and tides in the GOT are strongly damped, so the impact of the GOT on the SCSB is not significant. In addition, there is a weak response peak at the frequency  $0.45 \text{ d}^{-1}$  in the GOT (Exp. 1 in Figure 3b). Since the GOT has a length of 660 km and a mean depth of 36 m, the quarter-wavelength theory gives a resonant frequency of  $0.61 \text{ d}^{-1}$ . It seems that the peak at  $0.45 \text{ d}^{-1}$  is associated with the local regional resonance.

In summary, the resonant periods or frequencies change when the depth of the SCSB varies, and the trends in the two sea areas are consistent (Figure 3). The resonant frequency decreases when the SCSB is shallower and increases when the SCSB is deeper. Additionally, the resonant frequencies of the SCSB and GOT remain almost identical (Table 2). The experimental results show that the SCSB has a critical impact on the tidal resonance of the GOT and that the GOT is not an independent sea area in terms of tidal resonance.

## 5 A theoretical model

The quarter-wavelength resonant theory is based on the wave behaviour in a single channel. As discussed above, this theory does not explain the enhanced tides around one cycle per day in the GOT. Here, we establish a two-channel model and

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examine its applicability to the SCSB-GOT system. Tidal waves from the Pacific Ocean propagate through the LS, pass the SCSB and finally enter the GOT. The tidal waves in the Karimata Strait are very weak (Figure 2a and Wei et al., 2016) and are not able to propagate into the GOT. Thus, the tidal energy in the GOT is mainly from the SCSB. Therefore, we use a two-channel model to represent the SCSB-GOT system, as shown in Fig. 5. This model is quite similar to Webb's (2011) 1-

5 D model, except that we add a forcing at the entrance of the deep channel. In the figure,  $H_1$  is the depth of channel 1 (the deep channel),  $H_2$  is the depth of channel 2 (the shallow channel), and  $L_1$  and  $L_2$  are the lengths of channels 1 and 2, respectively. The tidal waves enter channel 1 through the opening at  $x = L_1$ , enter channel 2 through the junction point at  $x = 0$ , and finally reach the top of channel 2 at  $x = -L_2$ . The equations governing the tidal motion in channels can be expressed as follows:

$$10 \quad \begin{cases} \frac{\partial \tilde{u}_m}{\partial t} = -g \frac{\partial \tilde{\zeta}_m}{\partial x} - \gamma_m \tilde{u}_m \\ \frac{\partial \tilde{\zeta}_m}{\partial t} = -H_m \frac{\partial \tilde{u}_m}{\partial x} \end{cases}, \quad (7)$$

where  $\tilde{\zeta}_m(x, t)$  and  $\tilde{u}_m(x, t)$  represent the elevation and velocity, respectively;  $H_m$  is the depth;  $\gamma_m$  is the friction parameter (equivalent to  $\tau/H$  in Eqs. (2) and (3));  $g$  is the acceleration due to gravity; and  $m=1, 2$  represents the different channel segments. Here,  $\tilde{u}_m(x, t)$  and  $\tilde{\zeta}_m(x, t)$  can be expressed in the forms of  $u_m(x, t) = \text{Re}(u_m(x) e^{-i\omega t})$  and  $\zeta_m(x, t) = \text{Re}(\zeta_m(x) e^{-i\omega t})$ , respectively, where  $\omega$  is the angular frequency,  $t$  is time, and  $\zeta_m(x)$  and  $u_m(x)$  represent the complex amplitudes of the elevation and velocity, respectively. By eliminating the common factor  $e^{-i\omega t}$ , Eq.

(7) can be reduced to ordinary differential equations as follows:

$$\begin{cases} -i\omega u_m = -g \frac{d\zeta_m}{dx} - \gamma_m u_m \\ -i\omega \zeta_m = -H_m \frac{du_m}{dx} \end{cases}. \quad (8)$$

The boundary and matching conditions are as follows:

$$\zeta_1(L_1) = a_0, \quad \zeta_1(0) = \zeta_2(0),$$

$$H_1 u_1(0) = H_2 u_2(0), \text{ and}$$

$$u_2(-L_2) = 0.$$

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From the governing equations and boundary/matching conditions, the complex amplitudes of the elevations of the two channels can be obtained as follows (see the appendix for a detailed derivation):

$$\zeta_1(x) = a_0 R_0 Q(x), \text{ and} \quad (12)$$

$$\zeta_2(x) = a_0 R_0 \cos \beta_2 (x + L_2). \quad (13)$$

5 When the denominator of  $R_0$  reaches its minimum, the amplitudes of the two-sea area become the largest and resonance occurs. The condition is as follows (see expression of  $R_0$  in Appendix (Eq. A10)):

$$|\cos \beta_1 L_1 \cos \beta_2 L_2 - r \frac{p_1}{p_2} \sin \beta_1 L_1 \sin \beta_2 L_2| = \min, \quad (14)$$

where  $r = \sqrt{H_2/H_1}$ .

Based on the configurations of the SCSB and GOT, we take  $L_1 = 2600$  km,  $L_2 = 660$  km,  $H_1 = 1457$  m,

10  $H_2 = 36$  m, and  $\gamma_m = \frac{0.0001}{H_m}$ . By substituting these values into (12) and (13), we can obtain the solutions of these

equations. The amplitude gains at locations  $x=0$  and  $-L_2$  are functions of  $\omega$  or functions of the frequency  $f$  ( $f = \omega/2\pi$ ) and can be used to represent the response properties of channels 1 and 2, respectively. The results are shown with red curves in Figure 6. For comparison, we also calculate the corresponding functions in the absence of friction, as shown by the blue curves in Figure 6. From these curves, the resonant frequencies can be readily obtained, as given in Table

15 3.

Figure 6a displays the response function at  $x = -L_2$ , which represents the response of channel 2. This figure shows that the results in the presence of friction are more realistic than those in the absence of friction. The former case has a maximum peak at a frequency of  $1.040 \text{ d}^{-1}$ . The corresponding resonant period is 23.08 h, and this value is similar to the result of the numerical experiment involving the natural basin (Table 2, Exp. 1). The secondary response peak appears at a frequency of  $0.558 \text{ d}^{-1}$ , which is also fairly consistent with the results for the natural basin, as shown in Fig. 3b (red curve). The third peak is very small and appears at a frequency of  $1.848 \text{ d}^{-1}$ . If we carefully examine the red curve in Fig. 3b, we can also find a small peak near a frequency of  $1.9 \text{ d}^{-1}$ . The response function is worse when friction is neglected than when friction is retained, but the obtained resonant frequencies are almost unchanged, as shown by the blue curve in Figure 6a. Figure 6b shows the response function at  $x = 0$ , which represents the response of channel 1. The red curve has only one peak at a frequency of  $1.040 \text{ d}^{-1}$ , which is also similar to the results of the numerical experiment applied to the natural basin (Table 2, Exp. 1). When the friction is neglected, the frequency of the main peak is unchanged. In addition, there are two other peaks that are very narrow, indicating that these two peaks are relatively insignificant.

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$$R_0 = \frac{1}{\cos \beta_1 L_1 \cos \beta_2 L_2 - r \frac{p_1}{p_2} \sin \beta_1 L_1 \sin \beta_2 L_2},$$

and " " (13) .

$$Q(x) = \cos \beta_1 x \cos \beta_2 L_2 - r \frac{p_1}{p_2} \sin \beta_1 x \sin \beta_2 L_2.$$

" " (14) .

In the above equations,  $\beta_m = \beta_m' + i\beta_m''$ ,

$$\beta_m'^2 = \frac{k_m^2 (1 + \sqrt{1 + \gamma_m^2})}{2},$$

$$\beta_m''^2 = \frac{k_m^2 (-1 + \sqrt{1 + \gamma_m^2})}{2}, \quad C_m = \sqrt{g H_m}.$$

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If we apply the quarter-wavelength resonance theory to channel 1, we can obtain resonant frequencies of  $0.99 \text{ d}^{-1}$ . If we apply the quarter-wavelength and three-quarter-wavelength resonance theories to channel 2 we can obtain resonant frequencies of  $0.61$  and  $1.84 \text{ d}^{-1}$ , respectively. Therefore, we can conclude that the major peaks around the frequency of  $1.04 \text{ d}^{-1}$  in Figure 6 are caused by resonance in channel 1. This indicates that channel 1 plays a determinative role in the two-channel system. Similarly, we can also conclude that the secondary and third peaks around the frequencies of  $0.55$  and  $1.85 \text{ d}^{-1}$  in Figure 6 are caused by resonances in channel 2, associated with the quarter-wavelength and three-quarter-wavelength resonances. Although the frequencies of the peaks shown in Figure 6 correspond well with those estimated based on the quarter-wavelength and three-quarter-wavelength theories, there are small discrepancies. This is due to the connection of the two channels. In fact, the resonant frequencies of the two-channel system also depend on the depth ratio of two channels, as shown in Eq. (14). In comparison to channel 2, the secondary, especially the third peak, in channel 1 is much more less significant. This can be explained as follows: The tidal incident wave from the channel 1 partially enters channel 2 across the steep topography at  $x = 0$ , and here, the rest of the wave is reflected. The reflected wave is superimposed with the incident wave, and tidal resonance occurs around the frequency of  $1.04 \text{ d}^{-1}$ . That is, the steep topography at  $x = 0$  acts as a wall for channel 1, which causes the quarter-wavelength resonance to occur in the channel. Furthermore, the steep topography can also block most energy of the wave in channel 2 from entering channel 1. Therefore, the relatively large amplitudes in channel 2 at frequencies around  $0.55 \text{ d}^{-1}$  and  $1.85 \text{ d}^{-1}$  are not obvious in channel 1 under the action of friction.

Figure 7 displays the amplitude gains along the channels when channel 2 is in a resonant state. In this figure, the solution in presence/absence of friction is shown in panel a/b. The figure shows that when the forcing frequency is equal to  $1.040 \text{ d}^{-1}$ , which is the major resonant frequency, the amplitude gain gradually increases from the mouth towards the head in channel 1. In channel 2, the amplitude gain decreases first and reaches a trough before increasing again towards the head. The trough corresponds with the amphidromic zone of the diurnal tides in the GOT (see Figure 2a or the cotidal charts in Wu et al., 2015). For a frequency of  $0.558 \text{ d}^{-1}$ , the amplitude gain is nearly constant in channel 1 and increases with a relatively high rate towards the head in channel 2. For a frequency of  $1.848 \text{ d}^{-1}$ , the amplitude gain is also nearly constant in channel 1, and in channel 2, there are two antinodes and one node. This result is similar to the distribution of semi-diurnal tides in the GOT. When friction is neglected, the basic characteristics are the same, but the amplitude gain significantly increases.

## 6 Conclusions

The GOT is dominated by diurnal tides, indicating that the response near the diurnal tide frequency in the GOT is stronger than that at other frequencies. However, when applied to the GOT, the classical quarter-wavelength resonant theory fails to yield a diurnal resonant period. Changing the water depths in the SCSB in our numerical experiments further shows that the resonance of the SCSB has a critical impact on the resonance of the GOT. An idealised two-channel model that can reasonably explain the resonance in the GOT is established. Through the numerical experiments and two-channel model, we found that the resonant frequency around one cycle per day in the South China Sea main area can be explained with the

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quarter-wavelength resonance theory, and the large-amplitude response at this frequency in the GOT is basically a passive response of the gulf to the increased amplitude of the wave in the southern portion of the main area of the South China Sea. However, there are still some problems that require further exploration, such as the effects of the length, width, depth, Coriolis force and friction of the SCSB on the GOT, which will be the focus of subsequent studies.

5 **Code availability**

In this paper, we use the Princeton Ocean Model (POM), which is available online at <http://www.ccpo.odu.edu/POMWEB/>.

**Data availability**

The ETOPO1 data (doi: 10.7289/V5C8276M) are available online at <https://www.ngdc.noaa.gov/mgg/global/>.  
[The tidal data at the open boundaries are available online at ftp://ftp.oce.orst.edu/dist/tides](ftp://ftp.oce.orst.edu/dist/tides).

10 **Appendix: the analytical solution to the tidal wave equation for the two-channel model**

In this appendix, we [provide](#) a detailed derivation process for the solution of the two-channel model presented in Section [5](#).  
The following symbols [are](#) used in the derivation:

$i$  : imaginary units

$t$  : time

15  $\omega$  : angular velocity

$g$  : gravitational acceleration

$\gamma$  : frictional coefficient

$\tilde{\zeta}(x,t)$  : water level

$\zeta(x)$  : complex amplitude of the water level

20  $\tilde{u}(x,t)$  :  $x$ -direction current velocity

$u(x)$  : complex amplitude of the  $x$ -direction current velocity

$k$  : wavenumber

$H$  : water depth

$L$  : length of the channel

25  $m=1,2$  : different channel segments

The governing equation for tidal motion has the form [\(see Eq. \(8\) of the text\)](#):

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$$\begin{cases} -i\omega u_m = -g \frac{d\zeta_m}{dx} - \gamma_m u_m \\ -i\omega \zeta_m = -H_m \frac{du_m}{dx} \end{cases} \quad (A1)$$

Substituting the first equation into the second one, we obtain

$$\frac{d^2 \zeta_m}{dx^2} + \beta_m^2 \zeta_m = 0, \quad (A2)$$

where

$$\beta_m^2 = k_m^2 (1 + i\mu_m) \quad (A3)$$

In which  $\mu_m = \frac{\gamma_m}{\omega}$  is a friction parameter and  $k_m = \frac{\omega}{C_m}$  is the wavenumber with  $C_m = \sqrt{gH_m}$  representing the wave velocity.

The solution to Eq. (A2) is

$$\zeta_m(x) = A_m e^{i\beta_m x} + B_m e^{-i\beta_m x}, \quad (A4)$$

where  $\beta_m$  can be expressed in the form

$$\beta_m = \beta_m' + i\beta_m'' \quad (\beta_m', \beta_m'' \text{ are real numbers}). \quad (A5)$$

$$\beta_m'^2 = \frac{k_m^2 (1 + \sqrt{1 + \mu_m^2})}{2}, \text{ and} \quad (A6)$$

$$\beta_m''^2 = \frac{k_m^2 (-1 + \sqrt{1 + \mu_m^2})}{2}. \quad (A7)$$

We can obtain the following solution of  $u_m(x)$  from Eqs. (A1) and (A4):

$$u_m(x) = \sqrt{\frac{g}{H_m}} (1 + i\mu_m)^{-\frac{1}{2}} (A_m e^{i\beta_m x} - B_m e^{-i\beta_m x}). \quad (A8)$$

Substituting the open boundary and matching conditions of the two channels (see Eqs. (9) to (11) in the text) into Eqs. (A4) and (A8), we obtain

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$$\begin{cases} \frac{\partial \tilde{u}_m}{\partial t} = -g \frac{\partial \zeta_m}{\partial x} - \gamma_m \tilde{u}_m \\ \frac{\partial \zeta_m}{\partial t} = -H_m \frac{\partial \tilde{u}_m}{\partial x} \end{cases}, \dots (A1).$$

where  $\tilde{u}_m(x, t)$  and  $\tilde{\zeta}_m(x, t)$  can be expressed in the following forms: .

$$\tilde{u}_m(x, t) = Re(u_m(x) e^{-i\omega t}), \dots (A2).$$

$$\zeta_m(x, t) = Re(\zeta_m(x) e^{-i\omega t}), \dots (A3).$$

Eq. (A1) can be simplified as follows: .

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$$-i\omega \frac{du_m}{dx} = -g \frac{d^2 \zeta_m}{dx^2} - \gamma_m \frac{du_m}{dx}, \dots (A)$$

5). Therefore, equivalently, .

$$\frac{du_m}{dx} = g \frac{d^2 \zeta_m}{dx^2} (i\omega - \gamma_m)^{-1}, \dots (A6).$$

The second equation in Eq. (4) yields: .

$$\frac{du_m}{dx} = i\omega \zeta_m H_m^{-1}, \dots (A7).$$

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We can obtain the following equations from Eqs. (A10) and (A12) (...

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$$B_2 = \frac{a_0}{2} R_0 e^{-i\beta_2 L_2},$$

where

$$R_0 = \frac{1}{\cos \beta_2 L_2 \cos \beta_1 L_1 - r \frac{p_1}{p_2} \sin \beta_1 L_1 \sin \beta_2 L_2}.$$

We can then obtain the value of  $A_2$ :

$$A_2 = \frac{a_0}{2} e^{i\beta_2 L_2}.$$

Substituting Eqs. (A9) and (A11) into Eq. (A4) gives

$$\zeta_2(x) = a_0 R_0 \cos \beta_2 (x + L_2).$$

We can then obtain the expressions of the coefficients of  $\zeta_1(x)$  as follows:

$$A_1 = \frac{1 + r \frac{p_1}{p_2}}{2} \frac{a_0}{2} R_0 e^{i\beta_2 L_2} + \frac{1 - r \frac{p_1}{p_2}}{2} \frac{a_0}{2} R_0 e^{-i\beta_2 L_2},$$

$$B_1 = \frac{1 - r \frac{p_1}{p_2}}{2} \frac{a_0}{2} R_0 e^{i\beta_2 L_2} + \frac{1 + r \frac{p_1}{p_2}}{2} \frac{a_0}{2} R_0 e^{-i\beta_2 L_2}.$$

Thus,

$$\zeta_1(x) = a_0 R_0 Q(x).$$

$$Q(x) = \cos(\beta_2 L) \cos(\beta_1 x) - r \frac{p_1}{p_2} \sin(\beta_2 L) \sin(\beta_1 x).$$

# Competing interests

15 The authors declare that they have no conflicts of interest.

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Figure captions

**Figure 1:** The South China Sea and its neighbouring area. The contours show the water depth distribution in metres. The blue line B is the mouth cross section of the Gulf of Thailand (GOT). The triangles represent the tidal gauge stations (the full names of these stations are given in Table 1). The inset in the upper-left corner shows the entire model domains (99-131 E, 1.5-42 N).

5 **Figure 2:** Model-produced  $K_1$  tidal system. (a) The distribution of Greenwich phase-lags (in degrees) and amplitudes (colour, in metres). (b) Tidal energy flux density vectors (in  $\text{kW m}^{-1}$ ).

**Figure 3:** Response functions (amplitude gains as a function of frequency) of the South China Sea body (SCSB) (a) and the Gulf of Thailand (GOT) (b) for different bottom topographies. Here, the amplitude gains refer to the area-means of the top 20% values. The definition of the experiments is given in Table 2.

10 **Figure 4:** (a) Distribution of amplitude gain (colour) and phase change (lines in degrees) for the frequency of 0.99 cycle per day; (b) corresponding energy flux density vectors.

**Figure 5:** The two-channel model configuration representing the SCSB-GOT system.

**Figure 6:** Response function at the locations  $x = -L_2$  (a) and  $x = 0$  (b) with and without friction.

**Figure 7:** The amplitude gain as a function of  $x$  for different peak frequencies with friction (a) and without friction (b).

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## Tables

**Table 1. Comparison between model-produced and observed K<sub>1</sub> tidal amplitudes (m) and phase-lags (degrees refer to Greenwich time).**

No.	Place	E	N	Model		Tidal gauge observation	
				Amp. (m)	Phase-lag °	Amp. (m)	Phase-lag °
<u>1</u>	<u>Makung</u>	<u>119.57 E</u>	<u>23.59 N</u>	<u>0.25</u>	<u>138</u>	<u>0.25</u>	<u>158</u>
<u>2</u>	<u>Hong Kong</u>	<u>114.17 E</u>	<u>22.30 N</u>	<u>0.36</u>	<u>157</u>	<u>0.36</u>	<u>177</u>
<u>3</u>	<u>Hailingshan</u>	<u>111.82 E</u>	<u>21.58 N</u>	<u>0.40</u>	<u>175</u>	<u>0.42</u>	<u>194</u>
<u>4</u>	<u>Naozhou I</u>	<u>110.58 E</u>	<u>20.95 N</u>	<u>0.41</u>	<u>199</u>	<u>0.44</u>	<u>205</u>
<u>5</u>	<u>Basuo</u>	<u>108.62 E</u>	<u>19.10 N</u>	<u>0.60</u>	<u>299</u>	<u>0.54</u>	<u>311</u>
<u>6</u>	<u>Lingshuijiao</u>	<u>110.07 E</u>	<u>18.38 N</u>	<u>0.32</u>	<u>176</u>	<u>0.30</u>	<u>197</u>
<u>7</u>	<u>Quang Khe</u>	<u>106.47 E</u>	<u>17.70 N</u>	<u>0.36</u>	<u>351</u>	<u>0.21</u>	<u>350</u>
<u>8</u>	<u>Qui Nhon</u>	<u>109.22 E</u>	<u>13.75 N</u>	<u>0.34</u>	<u>169</u>	<u>0.34</u>	<u>195</u>
<u>9</u>	<u>Vung Tau</u>	<u>107.07 E</u>	<u>10.33 N</u>	<u>0.58</u>	<u>187</u>	<u>0.61</u>	<u>207</u>
<u>10</u>	<u>Con Dao</u>	<u>106.63 E</u>	<u>8.67 N</u>	<u>0.55</u>	<u>208</u>	<u>0.64</u>	<u>213</u>
<u>11</u>	<u>Kamau River</u>	<u>104.75 E</u>	<u>8.65 N</u>	<u>0.34</u>	<u>257</u>	<u>0.37</u>	<u>245</u>
<u>12</u>	<u>Hatien</u>	<u>104.47 E</u>	<u>10.37 N</u>	<u>0.26</u>	<u>312</u>	<u>0.26</u>	<u>321</u>
<u>13</u>	<u>Kaoh Kong I</u>	<u>103.00 E</u>	<u>11.42 N</u>	<u>0.33</u>	<u>30</u>	<u>0.37</u>	<u>41</u>
<u>14</u>	<u>Chandaburi</u>	<u>102.07 E</u>	<u>12.47 N</u>	<u>0.47</u>	<u>44</u>	<u>0.58</u>	<u>54</u>
<u>15</u>	<u>Satahib bay</u>	<u>100.92 E</u>	<u>12.65 N</u>	<u>0.55</u>	<u>60</u>	<u>0.64</u>	<u>56</u>
<u>16</u>	<u>Ko Raet</u>	<u>99.82 E</u>	<u>11.80 N</u>	<u>0.46</u>	<u>60</u>	<u>0.52</u>	<u>64</u>
<u>17</u>	<u>Tumpat</u>	<u>102.17 E</u>	<u>6.20 N</u>	<u>0.29</u>	<u>236</u>	<u>0.28</u>	<u>231</u>
<u>18</u>	<u>Trengganu</u>	<u>103.13 E</u>	<u>5.35 N</u>	<u>0.47</u>	<u>242</u>	<u>0.52</u>	<u>243</u>
<u>19</u>	<u>Kuantan</u>	<u>103.33 E</u>	<u>3.83 N</u>	<u>0.52</u>	<u>257</u>	<u>0.52</u>	<u>258</u>
<u>20</u>	<u>Pulau Tioman</u>	<u>104.13 E</u>	<u>2.80 N</u>	<u>0.47</u>	<u>272</u>	<u>0.49</u>	<u>265</u>
<u>21</u>	<u>Anamba Is.</u>	<u>106.25 E</u>	<u>3.23 N</u>	<u>0.37</u>	<u>257</u>	<u>0.40</u>	<u>253</u>
<u>22</u>	<u>Pulau Laut</u>	<u>108.00 E</u>	<u>4.75 N</u>	<u>0.37</u>	<u>221</u>	<u>0.36</u>	<u>228</u>
<u>23</u>	<u>Natuna</u>	<u>108.03 E</u>	<u>3.80 N</u>	<u>0.31</u>	<u>235</u>	<u>0.40</u>	<u>235</u>
<u>24</u>	<u>Subi Kechil</u>	<u>108.85 E</u>	<u>3.05 N</u>	<u>0.28</u>	<u>234</u>	<u>0.37</u>	<u>230</u>
<u>25</u>	<u>Tanjong Datu</u>	<u>109.65 E</u>	<u>2.08 N</u>	<u>0.29</u>	<u>207</u>	<u>0.37</u>	<u>215</u>
<u>26</u>	<u>Kota Kinabalu</u>	<u>115.98 E</u>	<u>5.87 N</u>	<u>0.39</u>	<u>175</u>	<u>0.35</u>	<u>194</u>
<u>27</u>	<u>Ulugan bay</u>	<u>118.77 E</u>	<u>10.07 N</u>	<u>0.34</u>	<u>174</u>	<u>0.34</u>	<u>197</u>



<u>28</u>	<u>Lubang I.</u>	<u>120.20 E</u>	<u>13.82 N</u>	<u>0.30</u>	<u>173</u>	<u>0.29</u>	<u>190</u>
<u>29</u>	<u>Santa Cruz</u>	<u>119.90 E</u>	<u>15.77 N</u>	<u>0.28</u>	<u>173</u>	<u>0.26</u>	<u>193</u>
<u>30</u>	<u>San Fernando</u>	<u>120.30 E</u>	<u>16.62 N</u>	<u>0.25</u>	<u>173</u>	<u>0.24</u>	<u>192</u>
<u>31</u>	<u>Yongshujiao</u>	<u>112.88 E</u>	<u>9.55 N</u>	<u>0.35</u>	<u>173</u>	<u>0.35</u>	<u>191</u>

Table 2 ↗ Resonant frequencies and periods obtained from the six experiments.

Exp	Topography		Resonant frequency /d <sup>-1</sup>		Resonant period /h	
	SCSB	GOT	SCSB	GOT	SCSB	GOT
1	Real <u>depth</u>	Real <u>depth</u>	0.99	1.01	24.36	23.79
2	Hal <u>ved depth</u> ↘	Real <u>depth</u>	0.75	0.75	32.00	32.00
3	Doubled <u>depth</u> ↘	Real <u>depth</u>	1.49	1.50	16.10	16.00
<u>4</u>	<u>Real depth</u>	<u>Halved depth</u>	<u>0.99</u>	<u>1.01</u>	<u>24.36</u>	<u>23.79</u>
<u>5</u>	<u>Real depth</u>	<u>Doubled depth</u>	<u>0.99</u>	<u>1.01</u>	<u>24.36</u>	<u>23.79</u>
<u>6</u>	<u>Real depth</u>	<u>Section-B closed</u>	<u>1.01</u>	<u>=</u>	<u>23.79</u>	<u>=</u>

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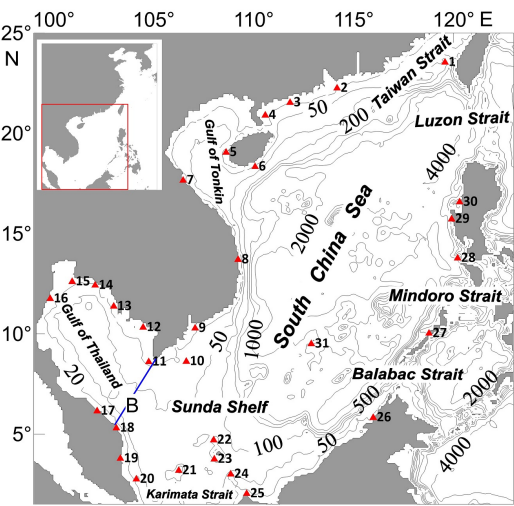
Table 3. The resonant frequencies and corresponding periods at  $x = -L_2$  and  $x = 0$ .

Solution	$x = -L_2$						$x = 0$					
	Peak frequency /d <sup>-1</sup>			Peak period /h			Peak frequency /d <sup>-1</sup>			Peak period /h		
1	0.558	1.040	1.848	43.01	23.08	12.99	-	1.040	-	-	23.08	-
2	0.545	1.044	1.856	44.04	22.99	12.93	0.545	1.044	1.856	44.04	22.99	12.93

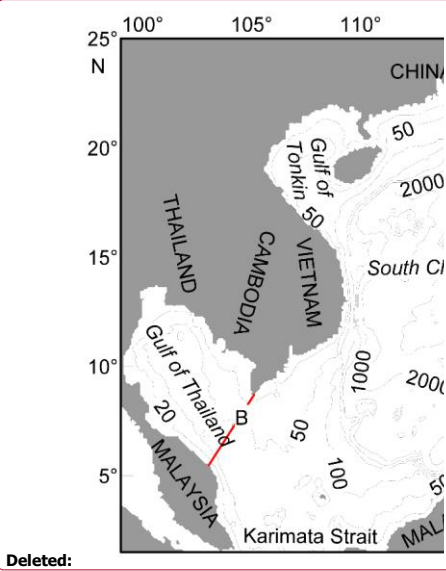
Notes: Solution 1 and 2 are respectively for the cases in the presence and in the absence of friction

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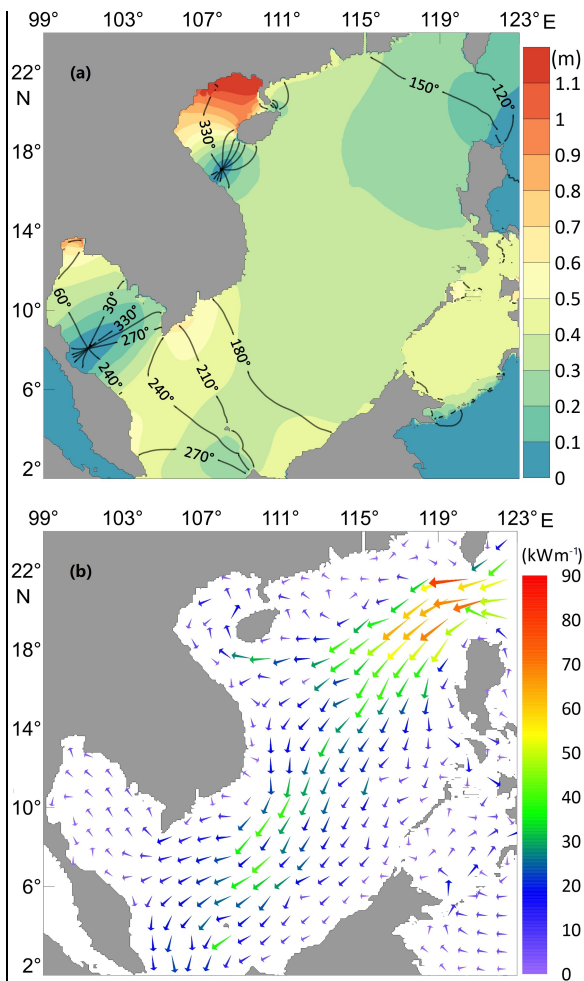
Figures



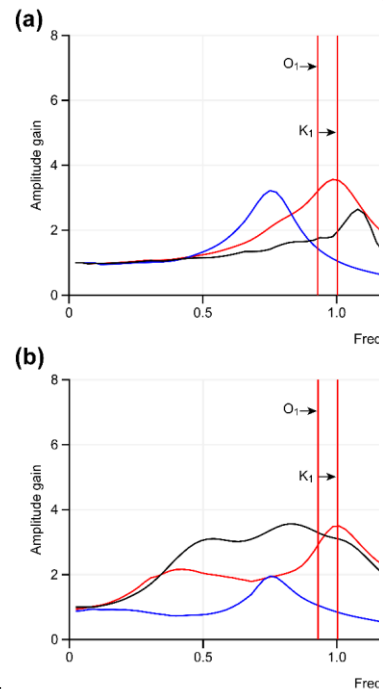
**Figure 1.** The South China Sea and its neighbouring area. The contours show the water depth distribution in metres. The blue line B is the mouth cross section of the Gulf of Thailand (GOT). The triangles represent the tidal gauge stations (the full names of these stations are given in Table 1). The inset in the upper-left corner shows the entire model domains (99-131° E, 1.5-42° N).



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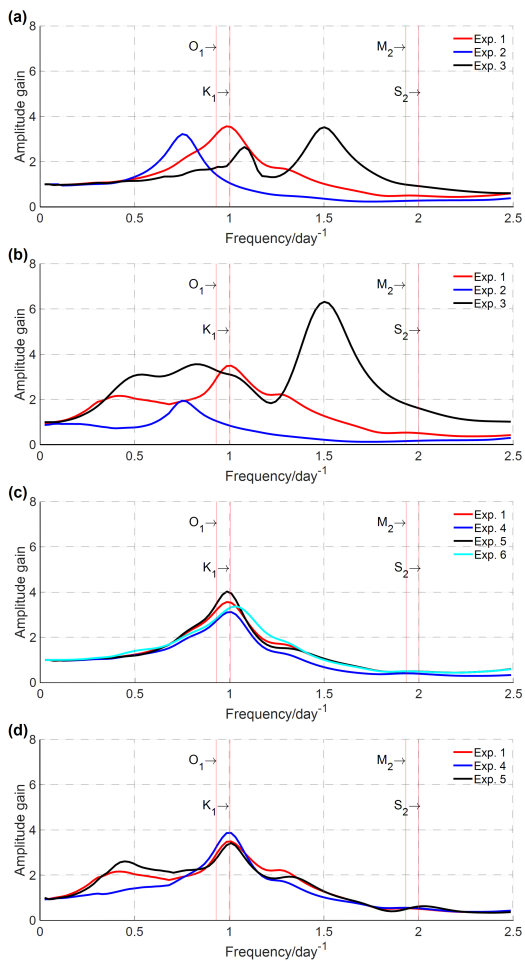
**Figure 2.** Model-produced  $K_1$  tidal system. (a) The distribution of Greenwich phase-lags (in degrees) and amplitudes (colour, in metres). (b) Tidal energy flux density vectors (in  $\text{kW/m}^2$ ).



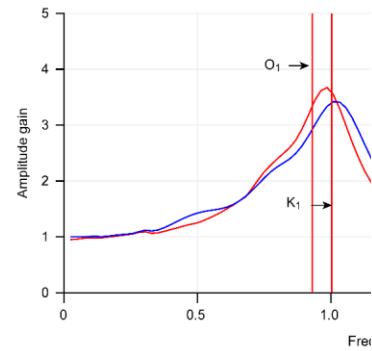
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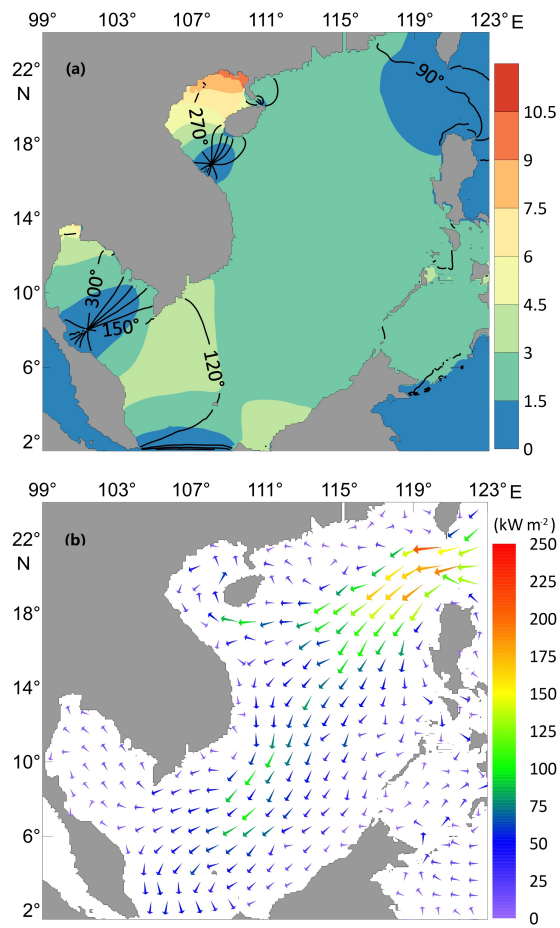


**Figure 3. Response functions (amplitude gains as a function of frequency) of the South China Sea body (SCSB) (a) and the Gulf of Thailand (GOT) (b) for different bottom topographies. Here, the amplitude gains refer to the area-means of the top 20% values. The definition of the experiments is given in Table 2.**

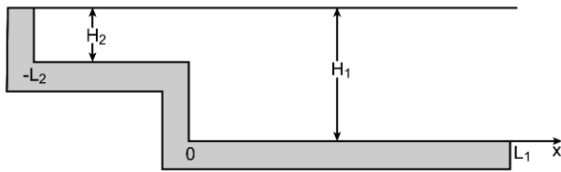


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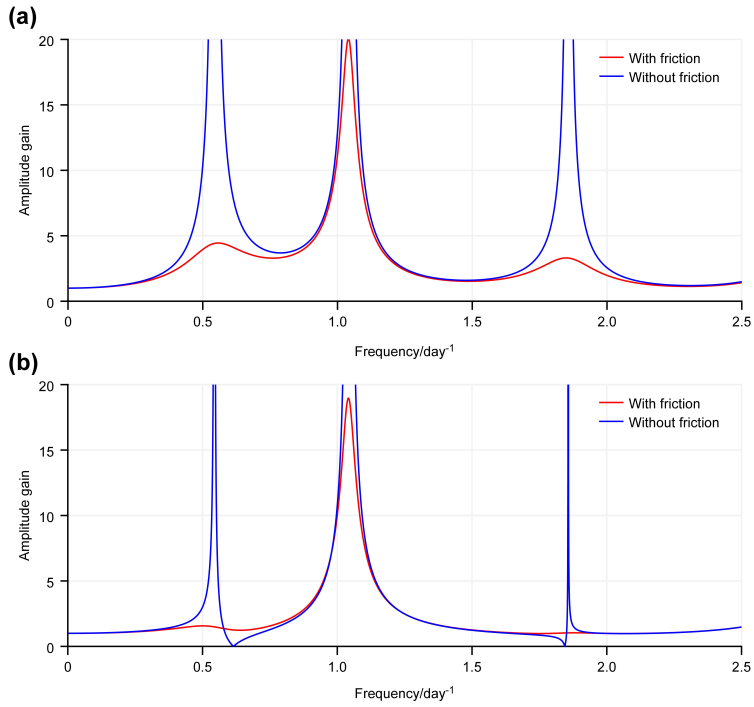
**Figure 4. (a) Distribution of amplitude gain (colour) and phase change (lines in degrees) for the frequency of 0.99 cycle per day; (b) corresponding energy flux density vectors.**



**Figure 5.** The two-channel model configuration representing the SCSB-GOT system.

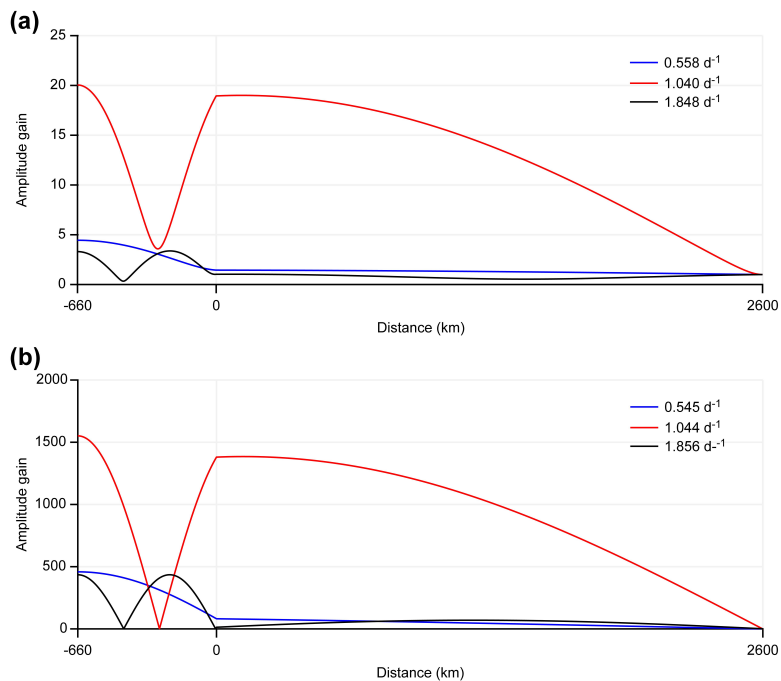
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**Figure 6. Response function at the locations  $x = -L_2$  (a) and  $x = 0$  (b) with and without friction.**

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**Figure 7.** The amplitude gain as a function of  $x$  for different peak frequencies with friction (a) and without friction (b).

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