



Air-sea momentum flux climatologies: A review of drag relation for parameterization choice on wind stress in the North Atlantic and the European Arctic

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1 Abstract

2 In this paper we have chosen to check the differences between the relevant or most commonly
3 used parameterizations for drag coefficient (C_D) for the momentum transfer values, especially
4 in the North Atlantic (NA) and the European Arctic (EA). As is well known, the exact equation
5 in the North equation that describes the connection between the drag coefficient and wind
6 speed depends on the author. We studied monthly values of air-sea momentum flux resulting
7 from the choice of different drag coefficient parameterizations, adapted them to momentum
8 flux (wind stress) calculations using SAR wind fields, sea-ice masks, as well as integrating
9 procedures. We calculated monthly momentum flux averages on a $1^\circ \times 1^\circ$ degree grid and
10 derive average values for the North Atlantic and the European Arctic. We compared the
11 resulting spreads in momentum flux to global values and values in the tropics, an area of
12 prevailing low winds. We show that the choice of drag coefficient parameterization can lead
13 to significant differences in resultant momentum flux (or wind stress) values. We found that
14 the spread of results stemming from the choice of drag coefficient parameterization was 14 %
15 in the Arctic, the North Atlantic and globally, but it was higher (19 %) in the tropics. On
16 monthly time scales, the differences were larger at up to 29 % in the North Atlantic and 36 %
17 in the European Arctic (in months of low winds) and even 50 % locally (the area west of
18 Spitsbergen). When we chose the oldest parameterization (e.g. Wu, 1969 (W69)) values of
19 momentum flux were largest for all months, in compare to values from the two newest
20 parameterizations (Large and Yeager, 2004 (LY04) and Andreas, 2012 (A12)), in both
21 regions with high and low winds and C_D values were consistently higher for all wind speeds.
22 For global data not much seasonal change was noted due to the fact that the strongest winds are
23 in autumn and winter as these seasons are inverse by six months for the northern and southern
24 hemispheres. The situation was more complicated when we considered results from the North
25 Atlantic, as the seasonal variation in wind speed is clearly marked out there. With high winter
26 winds, the A12 parameterization was no longer the one that produces the smallest wind stress.
27 In this region, in summer, the highest wind stress values were produced by the NCEP/NCAR
28 reanalysis, where in C_D has a constant value. However, for low summer winds, it is the
29 lowermost outlier. As the A12 parameterization behaves so distinctly differently with low
30 winds, we showed seasonal results for the tropical ocean. The sequence of values for the
31 parameterization was similar to that of the global ocean, but with visible differences between
32 NCEP/NCAR, A12 and LY04 parameterizations. Because parameterization is supported with
33 the largest experimental data set observations of very low (or even negative) momentum flux



34 values for developed swell and low winds, our results suggest that most circulation models
35 overestimate momentum flux.

36 1. Introduction

37 Wind stress acts at the air-sea interface influence on wind-wave interaction, including
38 wind-driven surface waves, turbulence in upper and deep layers, drift currents, and the main
39 ocean currents (Zilitinkiewicz et al., 1978). The ocean surface mixed layer is a region where
40 kinematic forcing affects the exchange of horizontal momentum and controls transport from
41 the surface to depths (Gerbi et al., 2008, Bigdeli et al., 2017). Any attempt to properly model
42 the momentum flux from one fluid to another as the drag force per unit area at the sea surface
43 (surface shear stress, τ) must take into account other physical processes responsible for
44 generating turbulence such as boundary stress, boundary buoyancy flux, and wave breaking
45 (Rieder et al., 1994, Jones and Toba, 2001). Over the past fifty years, as the entirety of flux
46 data has increased many fold, multiple empirical formulas have been developed to express the
47 ocean surface momentum flux as a relationship between non-dimensional drag coefficient
48 (C_D), wind speed (U_{10}), and surface roughness (z_0) (Wu 1969, 1982; Bunker, 1976; Garratt,
49 1977; Large and Pond, 1981; Trenberth et al., 1989; Yelland and Taylor, 1996, Donelan et al.,
50 1997; Kukulka et al., 2007; Andreas et al., 2012). These formulas can be divided into two
51 groups. One group of theories gives the C_D at level z in terms of wind speed and possibly one
52 or more sea-state parameters (for example, Geernaert et al., 1987, Yelland and Taylor, 1996,
53 Enriquez and Friehe, 1997), while the second group provides formulas for roughness length z_0
54 in terms of atmospheric and sea-state parameters (for example, Wu, 1969, Donelan et al.,
55 1997, Andreas et al., 2012). It is well known that the drag coefficient is not a constant,
56 because surface roughness changes with sea state, and that it is an increasing function of wind
57 speed for moderate wind speeds in the marine atmospheric boundary layer (Foreman and
58 Emeis, 2010). On the other hand, many researchers have recently shown that results for the
59 drag coefficient are underestimated at moderate wind speeds and overestimated at high wind
60 speeds (Jarosz et al., 2007, Sahlée et al., 2012, Peng and Li, 2015, Brodeau et al., 2017).

61 In this paper we chose to check the differences between the relevant or most
62 commonly used parameterizations for drag coefficient (C_D) for momentum transfer values,
63 especially in the North Atlantic (NA) and the European Arctic (EA). As is widely known, the
64 exact equation that describes the connection between the drag coefficient and wind speed
65 depends on the author (Geernaert, 1990). Our intention here is not to re-invent or formulate a
66 new drag parameterization for the NA or the EA, but to revisit the existing definition of drag
67 parameterization, and, using satellite data, to investigate how existing formulas accommodate
68 the environment in the North. We concentrated on wind speed parameterizations, because
69 wind speed is a parameter that is available in every atmospheric circulation model. Therefore,
70 it is used in all air-sea flux parameterizations, and presently it is used even when sea state
71 provides a closer physical coupling to the drag coefficient (for review see Geernaert et al.,
72 1986).



To understand air-sea interaction, Taylor (1916) parameterized the wind's drag on the sea surface using the bulk aerodynamic formula:

$$\tau = \rho C_{Dz} U_z^2 \quad (1)$$

where (τ) is the drag per unit area of sea surface (also called surface stress or momentum flux), ρ is air density, C_{Dz} is the non-dimensional drag coefficient appropriate for z height, and U_z is the average wind speed at some reference height z above the sea. C_{Dz} is commonly parameterized as a function of mean wind speed (m s^{-1}) for neutral-stability at a 10 m reference height above mean sea level (Jones and Toba, 2001), which is identified as C_{DN10} or C_{D10} (this permits avoiding deviation for the vertical flow from the logarithmic law):

$$C_{DN10} = \frac{\tau}{\rho} U_{10}^2 = \left(\frac{u_*}{U_{10}}\right)^2 \quad (2)$$

where u_* is friction velocity. Alternatively, the neutrally stratified momentum flux can be determined from the logarithmic profile, thus Eq. 1 can be express as:

$$C_{DN10} = [\kappa / \ln(10/z_0)]^2 \quad (3)$$

where z_0 (m) is the aerodynamic roughness length, which is the height, above the surface to define the measure of drag at which wind speed extrapolates to 0 on the logarithmic wind profile (Andreas et al., 2012), and κ is von Kármán constant ($\kappa=0.4$).

At the same time, we can define the value of friction velocity (u_*) as having the dimension of velocity, which is defined by the following equation:

$$\tau = \rho u_*^2 \quad (4)$$

Comparison with bulk formula (1) leads to the equation:

$$u_*^2 = C_{D10} U_{10}^2 \quad (5)$$

Some of the first studies (Wu, 1969, 1982, Garrat, 1977) focused on the relationship between wind stress and sea surface roughness, as proposed by Charnock (1955), and they formulated (for winds below 15 m s^{-1}) the logarithmic dependence of the stress coefficient on wind velocity (measured at a certain height) and the von Kármán constant. Currently common parameterizations of the drag coefficient are a linear function of 10 m wind speed (U_{10}), and the parameters in the equation are determined empirically by fitting observational data to a curve. The general form is expressed as (Guan and Xie, 2004):

$$C_D 10^3 = (a + b U_{10}) \quad (6)$$

Wu (1969), based on data compiled from 12 laboratory studies and 30 oceanic observations, formulated power-law (for breezes and light winds) and linear-law (for strong winds) relationships between the wind-stress coefficient (C_y) and wind velocity (U_{10}) at a certain height y at various sea states. In his study, he used roughness Reynolds numbers to



characterize the boundary layer flow conditions, and he assumed that the sea surface is aerodynamically smooth in the range of $U_{10} < 3 \text{ m s}^{-1}$, transient at wind speed $3 \text{ m s}^{-1} < U_{10} < 7 \text{ m s}^{-1}$, and aerodynamically rough at strong winds $U_{10} > 7 \text{ m s}^{-1}$. He also showed that the wind-stress coefficient and surface roughness increase with wind speed at light winds ($U_{10} < 15 \text{ m s}^{-1}$) and is constant at high winds ($U_{10} > 15 \text{ m s}^{-1}$) with aerodynamically rough flow. Garratt (1977), who assessed the 10 m neutral drag coefficient (C_{DN10}) based on 17 publications, confirmed the previous relationship and simultaneously suggested a linear form of this relationship for light wind. Wu (1980) proposed the linear-law formula for all wind velocities and later (Wu, 1982) extended this even to hurricane wind speeds. All of the preceding results rely heavily on the Monin-Obukhov similarity theory (MOST) in order to eliminate the stability dependence by choosing 10 m as the standard reference height and using data obtained under different experimental conditions (laboratory or field) and data analysis. In 1981, Large and Pond's estimated momentum flux using the direct Reynolds flux method and the dissipation method indicated the linear-law of C_D for wind speed in moderate winds. Their results confirm the assumption that the neutral drag coefficient increases with higher wind speed values and support the theoretical prediction that C_{DN} is independent of the bulk stability parameter (z/L). Trenberth et al. (1989), who considered the uncertainty in C_D from earlier experiments in which there were difficulties in calculations for low frequency (less than 10 days), suggest incorporating a quantity called pseudostress (P), which assumes using an effective drag coefficient and constant air density. Their results were based on data from the European Centre for Medium Range Weather Forecasts (ECMWF) collected over seven years. Yelland and Taylor (1996) presented results obtained from three cruises using the inertial dissipation method in the Southern Ocean and indicate that using the linear-law relationship between the drag coefficient and wind speed (for $U_{10} > 6 \text{ m s}^{-1}$) is better than using friction velocities (u_*) with U_{10} . Fairall et al. (2003) used the COARE algorithm (Coupled Ocean-Atmosphere Response Experiment) globally as a function of ambient conditions. Their results with direct covariance flux measurements showed increases in C_{DN10} values from 1.0×10^{-3} to 2.3×10^{-3} (or to 2.07×10^{-3} if inertial dissipation fluxes were used) with increasing wind speed (from 3 m s^{-1} to 20 m s^{-1}). All of these studies show that coefficients are not identical and vary with wind speed and atmospheric stability.

Authors of coupled circulation models preferred even simpler parameterizations. The NCEP/ NCAR reanalysis (Kalnay et al., 1996) uses a constant drag coefficient of 1.3×10^{-3} while, for example, the Community Climate System Model version 3 (Collins et al., 2006) uses a single mathematical formula proposed by Large and Yeager (2004) for all wind speeds. Their parameterizations explicitly or implicitly assume that equation (6) is exact. However, Foreman and Emeis (2010) show that friction velocity is proportional to wind speed, but with offset:

$$u_* = aU_{10}^2 + b \quad (7)$$

Andreas et al. (2012), further referred to as A12, updated equation (8) based on available datasets, friction velocity coefficient (u_*) versus neutral-stability wind speed at 10 m (U_{N10}), and sea surface roughness (z_0), to find the best fit for parameters $a = 0.0583$ and $b = -0.243$.



They justify their choice by demonstrating that u^* vs. U_{N10} has smaller experimental uncertainty than C_{DN10} , and that one expression of C_{DN10} for all wind speeds overstates and overestimates results in low and high winds (**Figs. 7 and 8** in A12).

This led directly to a new C_D formulation with much lower values for light winds (4 - 9 m s⁻¹). These low values could explain why the observed momentum flux with light winds and fast traveling swell can even be negative (Grachev and Fairall, 2001; Hanley and Belcher, 2008), and if true, this means that all previous parameterizations overestimate wind stress in basins with prevailing light winds (for example, the tropics).

All the above studies propose different parameterizations (see **Fig. 1**) of the drag coefficient and the function of wind speed, which reflects the difficulties in simultaneously measuring at high sea stress (or friction velocity) and wind speed. The purpose of this study is to show how the choice of C_D parameterization influences the value of the momentum flux from the atmosphere to the ocean with observations based on wind fields in different parts of the ocean, but especially in the NA and the EA seas.

2. Materials and Methods

We calculated monthly and annual mean momentum fluxes using a set of software processing tools called FluxEngine (Shutler et al., 2016), which was created as part of the OceanFlux Greenhouse Gases project funded by the European Space Agency (ESA). Since the toolbox, for now, is designed to calculate only air-sea gas fluxes but it does contain the necessary datasets for other fluxes, we made minor changes in the source code by adding parameterizations for the air-sea drag relationship. For the calculations, we used Earth Observation (EO) wind speed data at 10 m above sea level for 1992-2010 and sea roughness (σ_0 – altimeter backscatter signal in the Ku band) from the GlobWave project (<http://globwave.ifremer.fr/>). GlobWave produced a 20-year time series of global coverage multi-sensor cross-calibrated wave and wind data, which are publicly available at the Ifremer/CERSAT cloud. Satellite scatterometer derived wind fields are at present believed to be at least equally as good as wind products from reanalyses (see, for example, Dukhovskoy et al. 2017) for the area of our interest in the present study. The scatterometer derived wind values are calibrated to the equivalent neutral-stability wind at a reference height of 10 m above the sea surface, and, therefore, are fit for use with the neutral-stability drag coefficient (Chelton and Freilich, 2005). Wave data were collected from six altimeter missions (like Topex/POSEIDON, Jason-1/22, CryoSAT, etc.) and from ESA Synthetic Aperture Radar (SAR) missions (ERS-1/2 and ENVISAT). All data came in netCDF-4 format. The output data is a compilation file that contains data layers, and process indicator layers. The data layers within each output file include statistics of the input datasets (e.g., variance of wind speed, percentage of ice cover), while the process indicator layers include fixed masks as land, open ocean, coastal classification, and ice.

All analyses using the global data contained in the FluxEngine software produced a gridded (1° x 1°) product. The NA was defined as all sea areas in the Atlantic sector north of 30° N, and the EA subset was those sea areas north of 64° N (**Fig. 6**). We also defined the



subset of the EA east of Svalbard (“West Svalbard” between 76° and 80° N and 10° to 16° E), because it is a region that is studied intensively by multiple, annual oceanographic ship deployments (including that of the R/V Oceania, the ship of the institution the authors are affiliated with). FluxEngine treats areas with sea-ice presence in a way that is compatible with Lüpkes et al. (2012) multiplying the water drag coefficient by the ice-free fraction of each grid element. We also define “tropical ocean” as all areas within the Tropics (23° S to 23° N, not show) in order to test the hypothesis that the new A12 parameterization will produce significantly lower wind stress values in the region.

In this study, we calculated air-sea momentum flux average values using seven different drag coefficient parameterizations (C_D). All of them are generated from the vertical wind profile, but they differ in the formulas used.

$$10^3 \cdot C_{D10} = 0.5U_{10}^{0.5} \quad \text{for } 1 \text{ m s}^{-1} < U_{10} < 15 \text{ m s}^{-1} \quad (8)$$

(Wu, 1969)

$$10^3 \cdot C_{DN10} = 0.75 + 0.067U_{10} \quad \text{for } 4 \text{ m s}^{-1} < U < 21 \text{ m s}^{-1} \quad (9)$$

(Garratt, 1977)

$$10^3 \cdot C_{D10} = (0.8 + 0.065U_{10}) \quad \text{for } U_{10} > 1 \text{ m s}^{-1} \quad (10)$$

(Wu, 1982)

$$10^3 \cdot C_{DN10} = 0.29 + \frac{3.1}{U_{10N}} + \frac{7.7}{U_{10N}^2} \quad \text{for } 3 \text{ m s}^{-1} < U_{10N} < 6 \text{ m s}^{-1} \quad (11)$$

$$10^3 \cdot C_{DN10} = 0.60 + 0.070U_{10N} \quad \text{for } 6 \text{ m s}^{-1} < U_{10N} < 26 \text{ m s}^{-1}$$

(Yelland and Taylor, 1996)

$$10^3 \cdot C_D = 1.3 \quad \text{everywhere} \quad (12)$$

(NCEP/NCAR)

$$10^3 \cdot C_{DN10} = \frac{2.7}{U_{10N}} + 0.142 + 0.076U_{10N} \quad \text{everywhere} \quad (13)$$

(Large and Yeager, 2004)

$$C_{DN10} = \frac{u^*}{U_{10N}} = a^2 \left(1 + \frac{b}{a} U_{10N}^2\right) \quad \text{everywhere} \quad (14)$$

where $a = 0.0583$, $b = -0.243$ (Andreas et al., 2012)

where C_{DN10} is the expression of neutral-stability (10-m drag coefficient), C_{D10} is the drag coefficient dependent on surface roughness, U_{10} is the mean wind speed measured at 10 m above the mean sea surface, U_{10N} is the 10-m, neutral-stability wind speed.

3. Results and Discussion

Using FluxEngine software, we produced monthly gridded global air-sea momentum fluxes data. We calculated average momentum flux values separately for each month for the global ocean, the NA Ocean, and its subsets: the Arctic sector of the NA and the West



220 Spitsbergen area (WS). Some of the parameterizations used were limited to a restricted wind
221 speed domain. We used them for all the global wind speed data to avoid data gaps for winds
222 that were too high or too low for a given parameterization (**Fig. 1**). However, circulation
223 models have the very same constraint and, therefore, the procedure we used emulated using
224 the parameterization in oceanographic and climate modeling.

225 Since wind velocity was used to estimate C_D , **Fig. 1** shows a wide range of empirical
226 formulas and **Fig. 6** shows annual mean wind speed U_{10} (m s^{-1}) in the NA and the EA. The
227 differences between the oldest (eq. 8 - 10) and the newer (eq. 11, 13, 14) parameterizations
228 are distinct (**Fig. 1**). The C_D values from the oldest parameterizations increased linearly with
229 wind speed since the results from newer ones are sinusoidal indicating decreases for winds in
230 the range of 0 - 10 m s^{-1} , after which they began increase. Under weak winds ($< 10 \text{ m s}^{-1}$), the
231 drag coefficient values were significantly lower than under stronger winds ($> 10 \text{ m s}^{-1}$), with
232 greater differences among all used parameterizations. At a wind value of about 15 m s^{-1} , the
233 results from eq. 9, 10, and 14 overlapped providing the same values for the drag coefficient
234 parameterizations. The annual mean wind speed in the NA is 10 m s^{-1} , and in the EA it is 8.5
235 m s^{-1} (**Fig. 6**).

236 **Figure 2** presents maps of the mean boreal winter DJF and summer JJA momentum
237 fluxes for the chosen C_D parameterizations (Wu, 1969 and A12 – the ones with the largest and
238 smallest C_D values). The supplementary materials contain complete maps of annual and
239 seasonal means for all the parameterizations. The zones of the strongest winds are in the
240 extra-tropics in the winter hemisphere (southern for JJA and northern for DJF). The older Wu
241 (1969) parameterization produces higher wind stress values than A12 in both regions with
242 high and low winds and C_D values are consistently higher for all wind speeds except the
243 lowest ones (which, after multiplying by U^2 , produced negligible differences in wind stress
244 for the lowest winds). The average monthly values for each of the studied areas are shown in
245 **Fig. 3**. Generally, this illustrates that the newer the drag coefficient parameterization is, the
246 smaller the calculated momentum flux is. For global data (**Fig. 3a**), not much seasonal change
247 is noted, because the strongest winds are in fall and winter, but these seasons are the opposite
248 in the northern and southern hemispheres. The parameterization with the largest momentum
249 flux values for all months is that of Wu (1969), the oldest one, while the two
250 parameterizations with the lowest values are the newest ones (Large and Yeager, 2004 and
251 A12). For the NA (**Fig. 3b**), with is much more pronounced seasonal wind changes, the
252 situation is more complicated. With high winter winds, the A12 parameterization is no longer
253 the one that produces the smallest wind stress (it is actually in the middle of the seven).
254 However, for low summer winds, it is the lowermost outlier. Actually, in summer, the
255 constant C_D value used by the NCEP/NCAR reanalysis produces the highest wind stress
256 values in the Na. The situation is similar for the EA (a subset of the NA), the wind stress
257 values of which are shown in **Fig. 3c**, and for the WS area (not show). In the Arctic summer,
258 A12 produces the least wind stresses, while all the other parameterizations look very similar
259 qualitatively (even more so in the Arctic than in the whole NA). Because the A12
260 parameterization behaves so distinctly differently with low winds, we also show seasonal
261 results for the tropical ocean (**Fig. 3d**). The seasonal changes are subdued for the whole



tropical ocean with the slight domination of the Southern Hemisphere (the strongest winds are during the boreal summer) with generally lower momentum transfer values (monthly averages in the range of 0.2 to 0.3 N m^{-2} compared to 0.2 to 0.4 N m^{-2} for the NA and 0.2 to 0.5 N m^{-2} for the Arctic). The sequence of values for the parameterization is similar to that of the global ocean, but there are differences. Here the NCEP/NCAR constant parameterization is the second highest (instead of Wu, 1982 for the global ocean) while, unlike in the case of the global ocean, A12 produces visibly lower values than does the Large and Yeager (2004) parameterization.

We compared directly the results of the two parameterizations for the drag air-sea relation that uses different dependencies (**Fig. 4**). For this estimation we chose the two most-recent parameterizations (eq. 13 and 14) that showed the lowest values and change seasonally depending on the area used. This comparison showed that the A12 parameterization demonstrates almost zero sea surface drag for winds in the range of $3 - 5 \text{ m s}^{-1}$, which is compensated for by a certain surplus value for strong winds. As a result, these months with weak winds have significantly lower momentum flux values. This could be at statistical effect of weak wind ocean areas having stable winds with waves traveling in the same direction as the wind at similar speeds. The small drag coefficient values facilitate what Grachev and Fairall (2001) describe as the transfer of momentum from the ocean to the atmosphere at wind speeds of $2 - 4 \text{ m s}^{-1}$, which correspond to the negative drag coefficient value. Such events require specific meteorologist conditions, but this strongly suggests that the average C_D value for similar wind speeds could be close to zero.

Table 1 and **Fig. 5** present the average air-sea momentum flux values (in N m^{-2}) for all the regions studied and all the parameterizations. All the values are also presented as percentages of A12, which produced the lowest values for each region. A surprising result is the proportionality of all the parameterizations for the global, the NA, and the Arctic regions on annual scales (**Fig. 3** shows that this is not true on monthly scales). The spread of the momentum flux results is 14 % in all three regions, and even flux values themselves are larger in the NA than globally and larger in the Arctic than in the whole of the NA basin. The smaller WS region, with winds that are, on average, weaker than those of the whole Arctic (but stronger than those of the whole NA), had slightly different ratios of the resultant fluxes. For the tropical ocean, which is included for comparison because of its weaker winds, the spread in momentum flux values on an annual scale is 19 %. The spreads are even larger on monthly scales (not shown). The difference between A12 and Wu (1969) and NCEP/NCAR (the two parameterizations producing the largest fluxes on monthly scales) are 27 % and 29 % for the NA (in July), 31 % and 36 % for the Arctic (in June), 42 % and 51 % for the WS region (in July) and 23 % and 22 % for the tropical ocean (in April), respectively. Seasonality in the tropics is weak, therefore, the smallest monthly difference of 16 % (July) is larger than the difference for the global data in any month (the global differences between the parameterizations have practically no seasonality). On the other hand, the smallest monthly differences between the parameterizations in the NA, the Arctic, and the WS regions are all 7 %, in the month of the strongest winds (January).



Because the value of momentum flux is important for ocean circulation, its correct calculation in coupled models is very important, especially in the Arctic, where cold halocline stratification depends on the amount of mixing (Fer, 2009). We show that with the parameterization used in modelling, such as the NCEP/NCAR constant parameterization and Large and Yeager (2004), production stress results differ by about 5 %, on average (both in the Arctic and globally), and the whole range of parameterizations leads to results that differ, on average, by 14 % (more in low wind areas) and much more on monthly scales. One aspect that needs more research is the fact that the newest parameterization, A12, produces less momentum flux than all the previous ones, especially in lower winds (which, by the way, continues the trend of decreasing values throughout the history of the formulas discussed). The A12 parameterization is based on the largest set of measurements of friction velocity as a function of wind speed and utilizes the recently discovered fact that b in equation (8) is not negligible. It also fits the observations that developed swell at low wind velocity has celerity which leads to zero or even negative momentum transfer (Grachev and Fairall, 2001). Therefore the significantly lower A12 results for the tropical ocean (the trade wind region) and months of low winds elsewhere could mean that most momentum transfer calculations are overestimated. This matter needs further study, preferably with new empirical datasets.

4. Conclusions

We show that the choice of drag coefficient parameterization can lead to significant differences in resultant momentum flux (or wind stress) values. The differences between the highest and lowest parameterizations are 14 % in the Arctic, the NA, and globally, and they are higher in low winds areas. The parameterizations generally have a decreasing trend in the resultant momentum flux values, with the most recent (Andreas et al., 2012) producing the lowest wind stress values, especially at low winds, resulting in almost 20 % differences in the tropics. The differences can be much larger on monthly scales, up to 29 % in the NA and 36 % in the EA (in months of low winds) and even 50 % locally in the area west of Spitsbergen. For months with the highest winds, the differences are smaller (about 7 % everywhere), but because the flux values are largest with high winds this discrepancy is also important for air-sea momentum flux values. Since momentum flux is an important parameter in ocean circulation modeling, we believe more research is needed, and the parameterizations used in the models possibly need upgrading.

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471 **Table 1.** Average annual mean values of momentum flux (wind stress) [N m^{-2}] for all the
472 studied regions and parameterizations. In each column the percentage values are normalized
473 to A12, the parameterization that produced the smallest average flux values.

474

475 **Figure 1.** The drag coefficient parameterization used in the study (Eqs. 8-14) as a function of
476 wind speed U_{10} (m s^{-1}).

477

478 **Figure 2.** Maps of momentum flux [N m^{-2}] across the sea surface (wind stress) for boreal
479 winters ((a) and (c)) and summers ((b) and (d)) for Wu (1969) and A12 drag coefficient
480 parameterizations (the two parameterizations with the highest and lowest average values,
481 respectively).

482

483 **Figure 3.** Monthly average momentum flux values [N m^{-2}] for (a) global ocean, (b) North
484 Atlantic, (c) European Arctic, and (d) tropical ocean. The regions are defined in the text.

485

486 **Figure 4.** The drag coefficient values for Large and Yeager (2004) and Andreas et al., (2012)
487 parameterization as a function of wind speed U_{10} (m s^{-1}).

488

489 **Figure 5.** Annual average momentum flux values for (a) European Arctic and (b) Tropical
490 ocean. The vertical solid line is the average of all seven parameterization and the dashed lines
491 are standard deviations for the presented values. Global and the North Atlantic results are not
492 shown because the relative values for different parameterizations are very similar (see Table
493 1), scaling almost identically between the basins.

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495 **Figure 6.** Annual mean wind speed U_{10} (m s^{-1}) in the study area—the North Atlantic and the
496 European Arctic (north of the red line).

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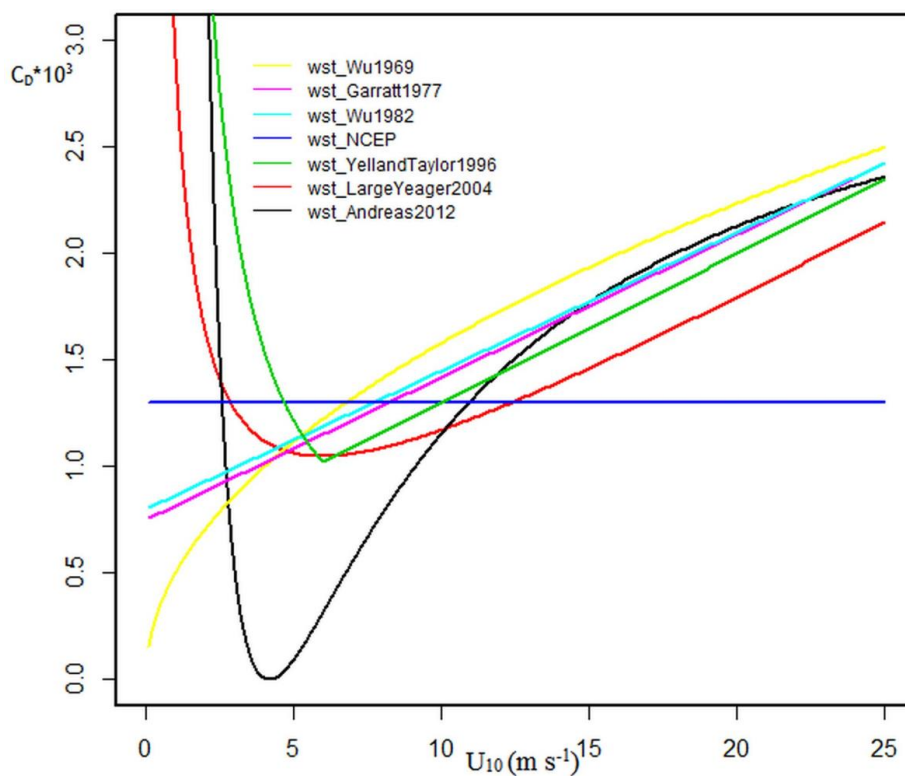


Table 1. Average annual mean values of momentum flux (wind stress) [N m^{-2}] for all the studied regions and parameterizations. In each column the percentage values are normalized to A12, the parameterization that produced the smallest average flux values.

	Global	North Atlantic	Arctic	W. Spitsbergen	Tropics
Wu (1969)	0.322 (114 %)	0.330 (114 %)	0.375 (114 %)	0.360 (114 %)	0.261 (119 %)
Garratt (1977)	0.307 (109 %)	0.316 (109 %)	0.358 (109 %)	0.344 (110 %)	0.251 (115 %)
Wu (1982)	0.311 (110 %)	0.320 (110 %)	0.363 (110 %)	0.349 (111 %)	0.255 (117 %)
NCEP/NCAR	0.303 (107 %)	0.312 (107 %)	0.353 (107 %)	0.341 (108 %)	0.258 (118 %)
Yelland & Taylor (1996)	0.297 (105 %)	0.306 (105 %)	0.348 (106 %)	0.335 (107 %)	0.245 (112 %)
Large & Yeager (2004)	0.285 (101 %)	0.293 (101 %)	0.333 (101 %)	0.320 (102 %)	0.236 (108 %)
Andreas et al., (2012)	0.283 (100 %)	0.290 (100 %)	0.329 (100 %)	0.314 (100 %)	0.219 (100 %)



517 **Figure 1.** The drag coefficient parameterization used in the study (Eqs. 8-14) as a function of
 518 wind speed U_{10} (m s^{-1}).



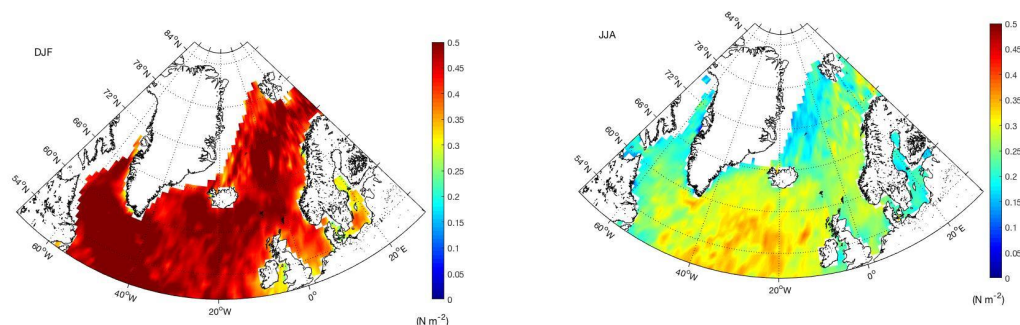
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529 **Figure 2.** Maps of momentum flux [N m^{-2}] across the sea surface (wind stress) for boreal
 530 winters ((a) and (c)) and summers (b) and (d)) for Wu (1969) and A12 drag coefficient
 531 parameterizations (the two parameterizations with the highest and lowest average values,
 532 respectively).
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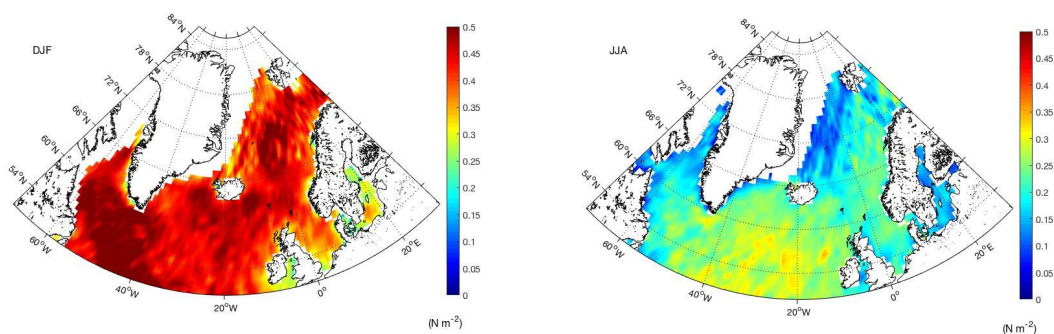
534 (a) Wu, (1969)

(b) Wu (1969)



536 (c) Andreas, et al., (2012)

(d) Andreas, et al., (2012)



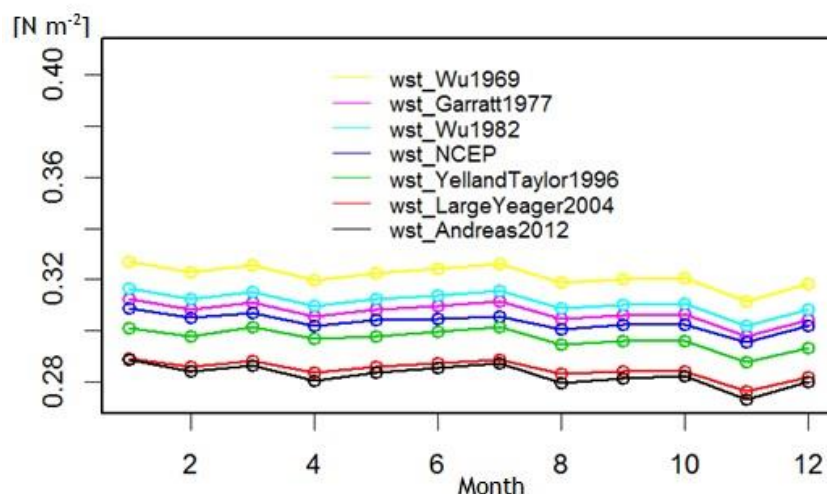
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545 **Figure 3.** Monthly average momentum flux values [N m^{-2}] for (a) global ocean, (b) North
546 Atlantic, (c) European Arctic, and (d) Tropical ocean. The regions are defined in the text.
547 (a)

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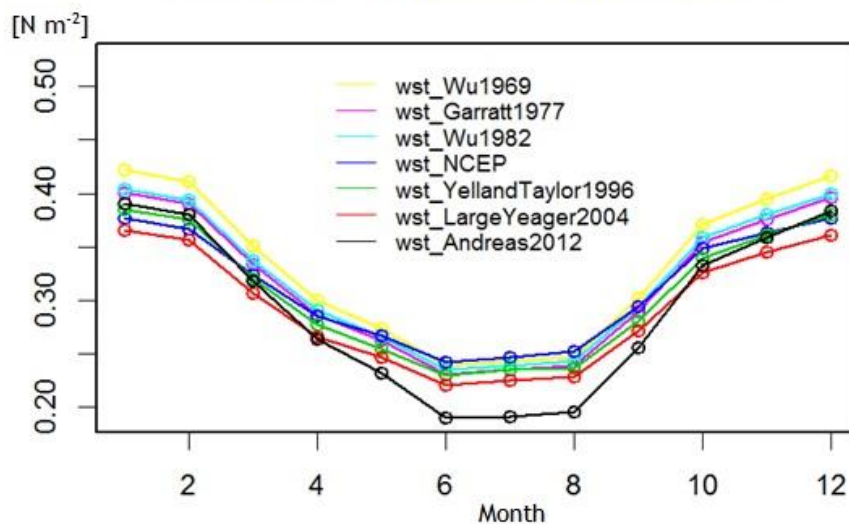
Global ocean mean momentum flux



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569 (b)

North Atlantic mean momentum flux



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574 (c)

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585 (d)

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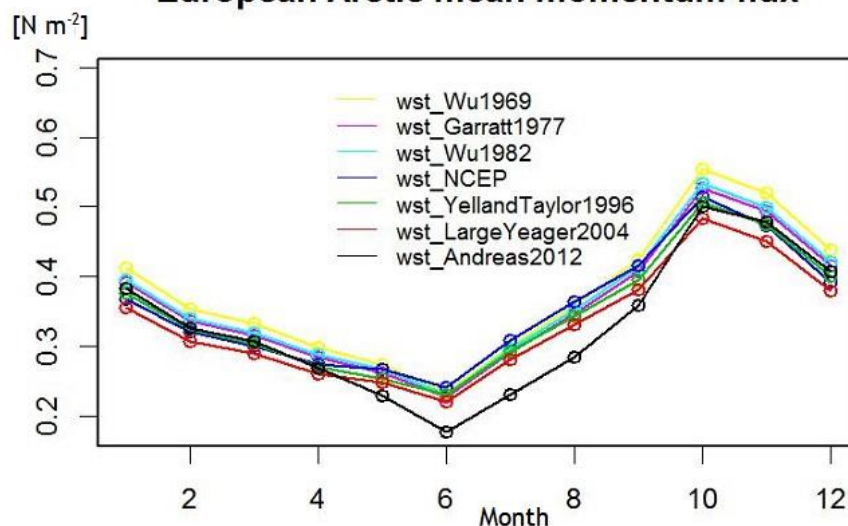
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European Arctic mean momentum flux



Tropical Ocean mean momentum flux

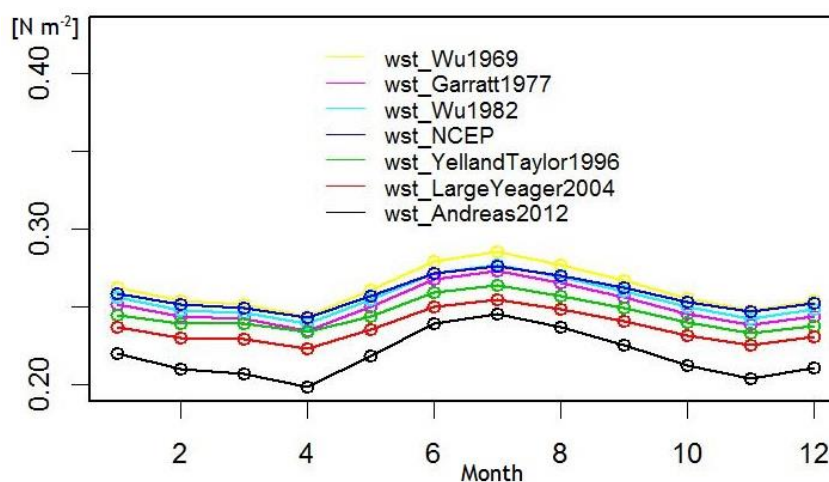




Figure 4. The drag coefficient values for Large and Yeager (2004) and Andreas et al., (2012) parameterization as a function of wind speed U_{10} (m s^{-1}).

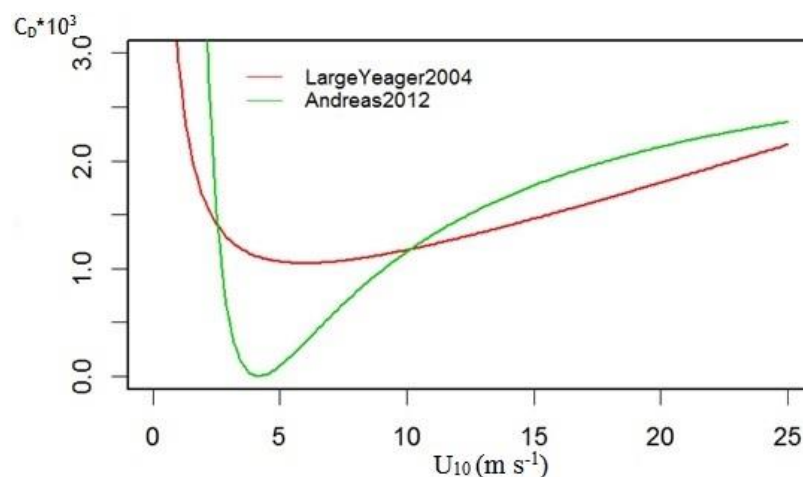
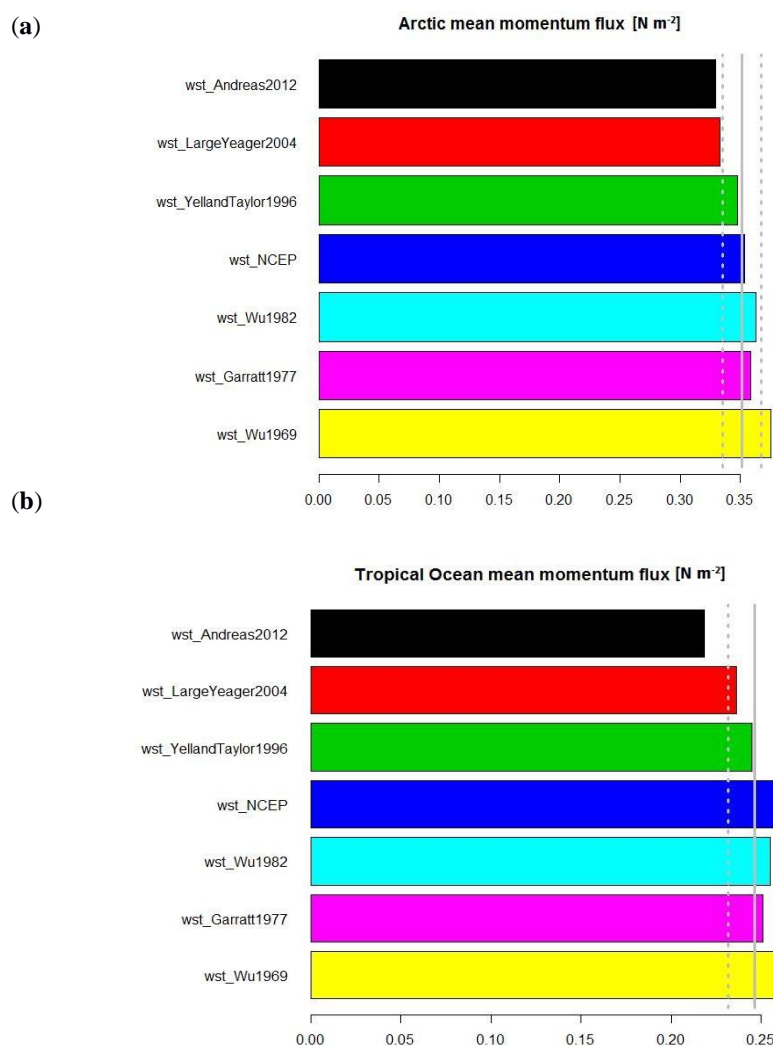




Figure 5. Annual average momentum flux values for (a) European Arctic and (b) Tropical ocean. The vertical solid line is the average of all seven parameterization and the dashed lines are standard deviations for the presented values. Global and the North Atlantic results are not shown because the relative values for different parameterizations are very similar (see Table 1), scaling almost identically between the basins.





655 **Figure 6.** Annual mean wind speed U_{10} (m s^{-1}) in the study area—the North Atlantic and the
 656 European Arctic (north of the red line).
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