

# 1    **Better Baltic Sea wave forecasts: Improving resolution or 2    introducing ensembles?**

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6    **Abstract.** The performance of short-range operational forecasts of significant wave height in the Baltic Sea  
7    is evaluated. Forecasts produced by a base configuration are inter-compared with forecasts from two  
8    improved configurations: one with improved horizontal and spectral resolution and one with ensembles  
9    representing uncertainties in the physics of the forcing wind field and the initial conditions of this field.  
10   Both the improved forecast classes represent an almost equal increase in computational costs. The inter-  
11   comparison therefore addresses the question: would more computer resources most favorably be spent on  
12   enhancing the spatial and spectral resolution or, alternatively, on introducing ensembles? The inter-  
13   comparison is based on comparisons with hourly observations of significant wave height from seven  
14   observation sites in the Baltic Sea during the three-year period 2015-2017. We conclude that for most wave  
15   measurement sites, the introduction of ensembles enhances the overall performance of the forecasts,  
16   whereas increasing the horizontal and spectral resolution does not. These sites represent offshore  
17   conditions, well exposed from all directions with a large distance to the nearest coast and with a large  
18   water depth. Therefore, the detailed shoreline and bathymetry is also *a priori* not expected to have any  
19   impact. Only at one site do we find that increasing the horizontal and spectral resolution significantly  
20   improved the forecasts. This site is situated in nearshore conditions, close to land, with a nearby island and  
21   therefore shielded from many directions. This study therefore concludes that to improve wave forecasts in  
22   offshore areas, ensembles should be introduced. For near shore areas, the study suggests that additional  
23   computational resources should be used to increase the resolution.

24

## 25    **1 Introduction**

26   Severe wave conditions affect ship navigation, offshore activities and risk management in coastal areas.  
27   Therefore, reliable forecasts of wave conditions are important for ship routing and planning purposes when  
28   constructing, maintaining and operating offshore facilities, such as wind farms and oil installations.

29   Waves are generated by energy transfer from surface winds that act on the sea. The energy transfer is  
30   determined by the *fetch* (the distance, over which the wind acts), and by the *duration* of the wind. For *deep*  
31   *water waves*, defined as the wave height being much smaller than the water depth, dissipation of the wave  
32   energy mainly occurs through internal processes, e.g. whitecapping.. For *shallow water waves*, defined as  
33   the wave height being comparable to the water depth, dissipation through bottom friction and through  
34   wave breaking over a shallow and sloping sea bed becomes important. Shallow water waves may also be  
35   refracted over a varying bathymetry Therefore, a correct and detailed description of the bathymetry is  
36   important for correctly forecasting waves in coastal areas and other shallow sea areas. Other factors with a

37 potential effect on the development of waves include nonlinear wave-wave interaction, ocean currents,  
38 time-varying water depth due to variations in sea level, and sea ice coverage.

39 The Baltic Sea is connected to the world ocean through the Danish waters with shallow and narrow Straits  
40 (see Figure 1), and this allows virtually no external wave energy to be propagated into the area. The Baltic  
41 Sea consists of a number of basins with depths exceeding 100 m, separated by sills and water areas with  
42 more moderate water depths. Between Finland and Sweden lies an archipelago with complicated  
43 bathymetry on very small spatial scales. The wind is in general westerly over the area, and the most  
44 prominent cause for severe wind and wave conditions is low pressure systems passing eastward over  
45 central Scandinavia. Winter ice occurs in the northern and eastern parts of the Baltic Sea. There is no  
46 noticeable tidal amplitude or permanent current systems.

47 Short-term forecasting of surface waves is done by a wave model, forced with forecasted wind from an  
48 atmospheric numerical weather prediction (NWP) model. The equations of the NWP model are discretized  
49 on a horizontal grid with a certain spatial resolution, which influences the maximum spatial resolution of  
50 the wave model. The available computer resources limit the horizontal grid spacing, that can be afforded.

51 Over time, technical development has increased available computational resources, which traditionally  
52 have been used to increase the horizontal spatial resolution of the NWP and wave models. This allows for  
53 an improved description and forecasting of the synoptic and mesoscale atmospheric systems, including the  
54 details of the associated wind field. In addition, a more detailed description of the bathymetry improves the  
55 correct description of dissipation and refraction of waves, as argued above. Additional computer resources  
56 may also be used to improve the spectral resolution in the wave model. This includes the directional  
57 resolution and the number of frequencies included.

58 Increasing computer resources have also made ensemble NWP possible. The purpose of ensemble  
59 forecasts is to improve forecast skill by taking both the initial error of the forecast and the uncertainty of  
60 the model physics into account. Furthermore, ensemble forecast allows for probabilistic forecasts,  
61 identified as a priority for operational oceanography (She et al., 2016), and allows for quantifying forecast  
62 uncertainty. Ensemble wave forecast systems have been implemented at global scale (Alves et al., 2013;  
63 Cao et al., 2009; Saetra and Bidlot, 2002) and more regionally in the Norwegian Sea (Carrasco and Saetra,  
64 2008), and in the German Bight and Western Baltic (Behrens, 2015).

65 From the above discussion it is evident that additional computer resources can be used in different ways to  
66 change the wave forecast setup, in order to increase the forecast quality. The purpose of the present study  
67 is to investigate the effect on the forecast quality of increasing the horizontal resolution and the spectral  
68 resolution vs. introducing ensemble forecasts. This will be done by verifying the DMI operational  
69 forecasting of wave conditions in the Baltic Sea in different configurations against available observations of  
70 significant wave height.

71 Increasing the horizontal resolution of the NWP-system may also lead to improved wind forecasts, due to in  
72 particular better descriptions of processes in extratropical cyclones. In these cases, where the wind field is  
73 strong and varying on a small spatial scale, wave forecasts may also be improved by running the wave  
74 model in a similarly high resolution.

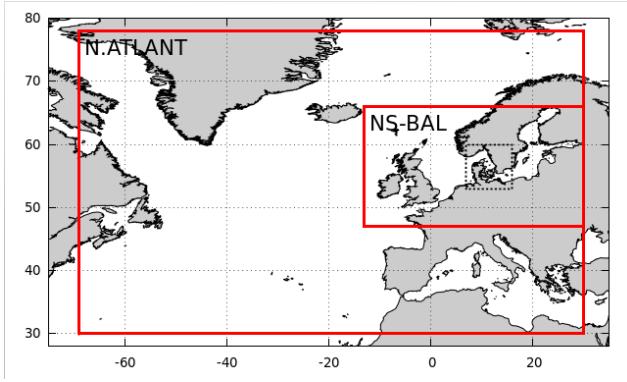
75 This paper is arranged as follows. Section 2 describes the model and setup, Section 3 describes the  
76 observations used and the verification methodology is described in Section 4. Verification of DMI-HIRLAM  
77 wind forecasts is in Section 5, whilst verification of the significant wave height (SWH) is presented in  
78 Section 6. Results of the verification are discussed in Section 7 and conclusions made in Section 8.

## 79 **2 Model and setup**

80 The DMI operational wave forecasting system DMI-WAM uses the 3rd generation spectral wave  
81 model WAM Cycle4.5.1 (Günther et al., 1992), with one minor change of source term functions. To speed  
82 up wave growth from calm sea, the spectral energy has a lower limit corresponding to a wave height of 7  
83 cm. It is forced by the regional NWP model DMI-HIRLAM and the global NWP model ECMWF-GLM. WAM  
84 solves the spectral wave equation, and calculates the wave energy as a function of position, time, wave  
85 period and direction. Derived variables, such as the significant wave height (SWH), are calculated as  
86 suitable integrals of the wave energy spectrum.

87 The DMI-WAM model system forecasts waves in a larger area than the Baltic Sea and therefore has a setup  
88 with two nested spatial domains of different geographical extent (see Figure 1): North Atlantic (NA) and  
89 North Sea/Baltic Sea (NSB), of which forecast results from the NSB-domain are analyzed in this study. The  
90 NA domain uses the JONSWAP wave spectrum for fully developed wind-sea (Hasselmann et al., 1973) along  
91 open model boundaries, while the NSB domain use modeled wave spectra from the NA domain at its open  
92 boundaries (one-way nesting).

93



94

95 **Figure 1 Nesting of domains in DMI-WAM. Outer frame is North Atlantic (NA) domain, inner frame is the North Sea/Baltic  
96 Sea(NSB)-domain. Dotted frame is the Transition Area. Only data from the NSB-domain are analyzed in this study.**

97 The wave energy is discretized into a number of wave directions and frequencies. To facilitate wave growth  
98 from calm sea, a lower limit is applied to the spectral energy. The resulting surface roughness  
99 parameterizes the effect of capillary waves, and corresponds to a minimum significant wave height of 7 cm.

100 The energy source is the surface wind. The sink terms are wave energy dissipation through wave breaking  
101 (white capping), wave breaking in shallow areas, and friction against the sea bed. Depth-induced wave  
102 breaking (Battjes and Janssen, 1978) is used in the NSB domain only, since in the NA domain, the depth  
103 maps are not detailed enough for activation of this effect. The wave energy is redistributed spatially by

104 wave propagation and depth refraction, and spectrally by non-linear wave-wave interaction. Interaction  
105 with ocean currents and effects due to varying sea level caused by tides or storms are not incorporated.  
106 In addition to a land mask, we have a time-varying ice mask. Below ice 30% concentration, sea ice is  
107 assumed to have no effect. Above 30% ice concentration, no wave energy is generated or propagated, i.e.  
108 the effect is like that of land. The applied sea ice concentrations originate from OSISAF  
109 (<http://osisaf.met.no/p/ice/>) with a frequency of 24 hours and around 25 km true horizontal resolution,  
110 gridded to ~10 km horizontal resolution and interpolated to the WAM-grid. The ice cover is initialized every  
111 day at 00z, and kept constant throughout each forecast run.  
112 The surface wind forcing is provided by different atmospheric models for the two domains. For the NA  
113 domain, wind is provided by the ECMWF-HRES global weather forecast every 3 hours. For the NSB domain,  
114 the surface wind is provided every hour by DMI-HIRLAM. Setup details are summarized in Table 1  
115

116 **Table 1 Specifications of DMI-WAM nested setup.**

Domain	North Atlantic	North Sea/Baltic Sea
Longitude	69W-30E	13W-30E
Latitude	30N-78N	47N-66N
Atmospheric forcing	ECMWF-HRES	<i>DMI-HIRLAM</i>
Boundary condition	JONSWAP	One-way nested
Depth-induced wave breaking	No	Yes

117  
118 Each forecast run is initialized using the sea state at analysis time, calculated by the previous run as a six  
119 hour forecast. The operational DMI-WAM suite is run four times a day to 48 h forecast range. This is also  
120 true for the North Atlantic domain, even when new forcing is available twice per day only. This is for  
121 practical reasons, since the North Atlantic domain is very cheap to run. Spatial fields of forecasted SWH and  
122 other variables are output in hourly time resolution.  
123 Historically, three different configurations of the DMI-WAM setup have been used, and data from these for  
124 the period 2015-2017 is the basis for the present verification. In the old LOW configuration, the horizontal  
125 resolution is around 50 km in the NA domain and around 10 km in the NSB domain. The wave energy is  
126 resolved in 24 directions and at 32 frequencies, corresponding to wave periods between 1.25-23.94 s and  
127 wave lengths between 2.4-895 m (in deep water). Bathymetry is ETOPO (Amante and Eakins, 2009) in the  
128 NA domain, and the Baltic bathymetry from IOW (<https://www.io-warnemuende.de/topography-of-the-baltic-sea.html>) supplemented by depth data from the Danish Geodata Agency (DGA) in the NSB domain.  
129 More recently, an ensemble configuration (LOWENS) has been introduced with characteristics identical to  
130 LOW, but using a parallel run of 11 ensemble members forced with perturbed atmospheric fields (initial  
131 conditions and physics). Finally, in the recently introduced HIGH configuration, the horizontal resolution is  
132 around 25 km in the NA domain and around 5 km in the NSB domain. The wave energy is resolved in 36  
133 directions and 35 frequencies, corresponding to wave periods between 0.94-23.94 s, and wave lengths  
134 between 1.37-895 m (in deep water). Bathymetry is RTopo (Schaffer et al., 2016).

136 All configurations are forced by winds from ECMWF-HRES in the NA domain and DMI-HIRLAM in the NSB  
 137 domain. In the NSB domain, the LOW and HIGH are forced by the S03 version (3 km horizontal resolution),  
 138 while LOWENS is forced by the S05 version (5 km horizontal resolution). The S03 and S05 versions of DMI-  
 139 HIRLAM were used operationally by DMI as deterministic and ensemble weather forecast models in the  
 140 2015-17 period. While the better resolution of S03 might have an impact on forecasts where orographic  
 141 effects matter, the impact on wind forecasts over sea is expected to be insignificant. The DMI-HIRLAM  
 142 winds are interpolated to the WAM grids by bilinear interpolation. To diminish coastal effects, DMI-HIRLAM  
 143 delivers a special *water-wind* to DMI-WAM, in which the surface roughness everywhere is assumed to be  
 144 that of water. This enhances the wind speed in the coastal zone, most important in semi-enclosed areas  
 145 (bays, fjords, etc.). It is basically a way to sharpen the land/sea boundary, reducing influence of land  
 146 roughness on near-shore winds. An overview of the DMI-WAM configurations is provided in Table 2.

147 Table 2 Details of DMI-WAM configuration used in this study.

	DMI-WAM Horizontal resolution [km]		# wave directions	# wave spectral frequencies	Bathymetry		Atmospheric horizontal resolution [km]		Ensemble members	
	North Atlantic	NSB			North Atlantic	NSB	North Atlantic (ECMWF)	NSB (DMI- HIRLAM)	North Atlantic	NSB
LOW	50	10	24	32	ETOPO	IOW/DGA	16	3	-	-
LOWENS	50	10	24	32	ETOPO	IOW/DGA	16	5	-	11
HIGH	25	5	36	35	RTopo	RTopo	16	3	-	-

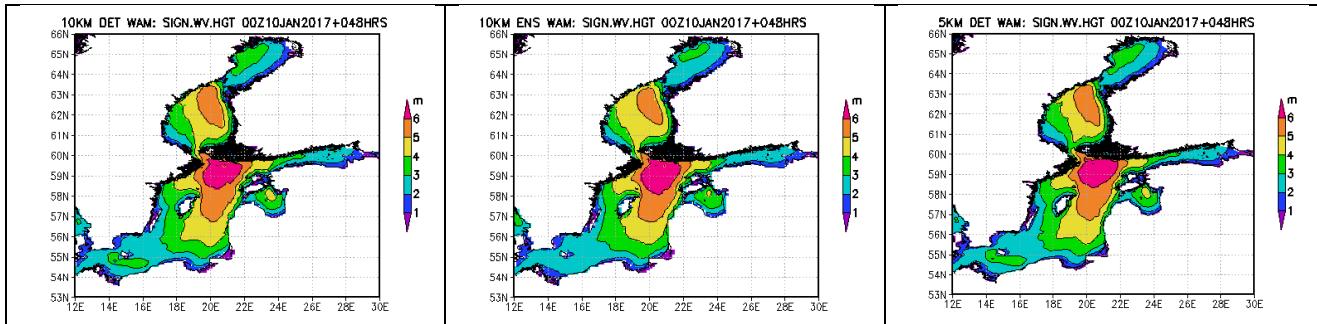
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149 When replacing the LOW forecast configuration with the HIGH configuration, the required computational  
 150 resources for running DMI-WAM are increased by a factor of  $2^2$  (increase in horizontal resolution)  $\times 1.75$   
 151 (effective decrease in time step) = 7 due to higher spatial resolution, and by a factor of 1.5 (increase of  
 152 number of directions)  $\times 35/32$  (increase of number of spectral frequencies) = 1.6. This gives a total factor of  
 153  $7 \times 1.6 \approx 11.5$ . From the LOW to the LOWENS configuration, it is increased by a factor of 11 (number of  
 154 ensemble members). Since these increases in computational effort are very similar, an inter-comparison  
 155 can contribute to answering the question: should additional computer resources be used for increasing the  
 156 spatial and spectral resolution, or for sampling the uncertainty in meteorological conditions using  
 157 ensembles.

158 The LOW and HIGH configurations both produce a class of deterministic forecast, which are also named  
 159 LOW and HIGH, respectively. The LOWENS configuration produces a class of probabilistic forecast, called  
 160 LOWENS. In addition, the ensemble mean defines a class of deterministic forecasts, called LOWENSMEAN.

161 To illustrate differences to be expected among the deterministic forecasts, we show 48 h forecasts of SWH  
 162 valid at the peak of the 'Toini' storm on 10 January 2017.

163



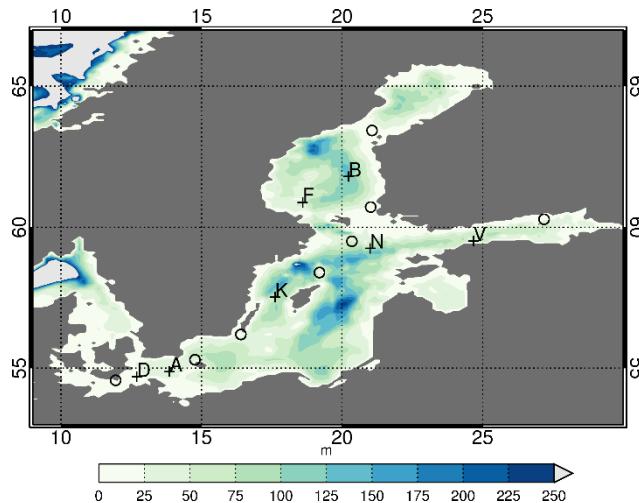
165 **Figure 2 Forecasted (48h) SWH at the peak of 'Toni' storm 10 january 2017 00z for LOW (left), LOWENSMEAN (middle) and HIGH (right) forecasts.**

167 All three forecasts agree in the gross features of the forecasted SWH field. However, there are differences,  
 168 e.g., northeast of the island of Gotland, the area with SWH above 6 m extends further southward in the  
 169 LOWNSMEAN forecast, than in the LOW and HIGH forecasts.

### 170 **3 Observations**

171 Observed series of SWH from wave measurement sites in the Baltic Sea, obtained from the Copernicus  
 172 Marine Environmental Monitoring System (CMEMS) database, are used. None of the series has a  
 173 continuous record over the three-year period 2015 – 2017. Data gaps may be due to malfunction,  
 174 maintenance or withdrawal of the instrument. The latter occur during winter due to the possibility of ice.  
 175 We selected sites with valid observations that covered more than 40% and were distributed reasonably  
 176 throughout the study period. To avoid biases in the verification measures due to under- or  
 177 overrepresentation of particular seasons, we also aimed at having an approximately even coverage  
 178 throughout the year.

179 Figure 3 and Table 3 show the positions and water depths of the wave measurement sites together with  
 180 the bathymetry of the Baltic Sea. Some sites did not observe at the full hour. Observations from these sites  
 181 were ascribed to the nearest full hour, if the time distance between the observation time and the full hour  
 182 was less than 15 min, otherwise not used. All observation series used are shown in Figure S1. The frequency  
 183 of observed SWH in different intervals for each site is given in Table 4



184

185 **Figure 3** Map of the Baltic Sea with bathymetry and positions of wave measurement sites marked with crosses. For details about  
186 sites, see Table 3. Meteorological stations used in the wind verification of DMI-HIRLAM are marked with circles.

187 **Table 3 Details of wave measurement sites.**

Observation site	Lon	Lat	Depth [m]	Model	Actual
A Arkona WR	13.9	54.9	46	45	
B Bothnian Sea	20.2	61.8	118	~120	
D Darsser Sill WR	12.7	54.7	20	21	
F Finngrundet WR	18.6	60.9	56	67	
K Knolls Grund	17.6	57.5	63	90	
N Northern Baltic	21.0	59.2	68	~100	
V Vahemadal	24.7	59.5	18	5	

188

189

190 **Table 4 Observed frequency of SWH in different bins for wave measurement sites.**

SWH [m]	0-1	1-2	2-3	3-4	4-5	>5
Arkona WR	0.47	0.39	0.12	0.01	<0.01	<0.01
Bothnian Sea	0.46	0.38	0.12	0.02	0.01	<0.01
Darsser Sill WR	0.67	0.31	0.02	<0.01	<0.01	<0.01
Finngrundet WR	0.69	0.27	0.04	0.01	<0.01	<0.01
Knolls Grund	0.62	0.31	0.06	0.01	<0.01	<0.01
Northern Baltic	0.39	0.37	0.18	0.05	0.01	<0.01
Vahemadal	0.78	0.20	0.02	<0.01	<0.01	<0.01

191

## 192 **4 Verification methodology**

193 In this section, a short overview of the verification procedure will be given. For background and more  
194 details regarding the verification measures, we refer to (Jolliffe and Stephenson, 2003)

195 For each measurement series of SWH, the corresponding forecast series for all forecast classes and for  
 196 forecast range zero to 48 h for the grid point nearest to the position of the wave measurement site was  
 197 extracted from the model output.  
 198 For the deterministic and continuous forecast classes (LOW, LOWENSMEAN and HIGH), we use the  
 199 conventional performance measures *root mean square error* (RMSE), defined as the square root of the time  
 200 average of the sum of squared differences between forecast and observation:

$$RMSE(\tau) = \langle (h_{s,f cst}^\tau - h_{s,obs})^2 \rangle$$

201 the bias

$$BIAS(\tau) = \langle h_{s,f cst}^\tau - h_{s,obs} \rangle,$$

203 and the correlation coefficient

$$CC = \frac{\langle (h_{s,f cst}^\tau - \langle h_{s,f cst}^\tau \rangle)(h_{s,obs} - \langle h_{s,obs} \rangle) \rangle}{\sqrt{\langle (h_{s,f cst}^\tau - \langle h_{s,f cst}^\tau \rangle)^2 \rangle \langle (h_{s,obs} - \langle h_{s,obs} \rangle)^2 \rangle}}$$

204 where  $h_{s,obs}$  is the observed SWH and  $h_{s,f cst}^\tau$  is a corresponding forecast with forecast range  $\tau$ .

205 The RMSE is a positive definite quantitative measure, and smaller values mean a better forecast. The bias  
 206 can take positive and negative values, and a good forecast has a numerically small value. The averaging,  
 207 indicated by  $\langle \cdot \rangle$ , is found based on all available values during the three-year period. Also, the RMSE and  
 208 BIAS as function of  $h_{s,obs}$  will be considered.

209 A framework for verifying probabilistic forecasts is the *continuous ranked probability score* (CRPS), defined  
 210 as

$$CRPS(\tau) = \langle \int [F^\tau(h_s) - H(h_s - h_{s,obs})]^2 dh_s \rangle,$$

212 where  $F^\tau(h_s)$  is the forecasted probability distribution,  $h_{s,obs}$  is the observed value, and  $H(\cdot)$  is the  
 213 Heaviside step function. A small CRPS occurs when the median of the probabilistic forecasts are close to the  
 214 observed values. Also a sharp probabilistic forecast with a small spread favors a small CRPS. This means that  
 215 the best forecast is achieved when CRPS is small. CRPS can be applied to both the probabilistic forecast  
 216 class LOWENS, as well as the deterministic forecast classes, LOW, LOWENSMEAN and HIGH, since these  
 217 can be regarded as probabilistic forecasts with a step probability distribution. For the deterministic forecast  
 218 classes, the CRPS equals the *mean absolute error*.

219 Besides the continuous and probabilistic forecasts, also the binary forecast of the SWH exceeding a  
 220 specified threshold is considered. The performance measure used is the Brier Score, defined as

$$BS(\tau) = \langle (p - x)^2 \rangle,$$

222 where  $p$  is the forecasted probability with forecast range  $\tau$  of exceeding the threshold and  $x$  takes the  
 223 value of 1 or 0 dependent on whether the threshold actually was exceeded or not. The Brier Score is thus a

224 positively definite measure, where values are between zero and one, and the lower the value, the better  
225 the forecast.

## 226 **4.1 Calculation of confidence bands**

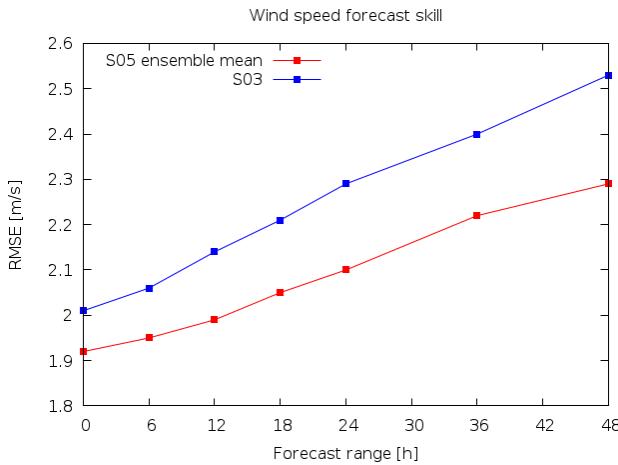
227 All the measures described above are subject to sampling uncertainty; if they had been calculated on data  
228 from another time period than 2015-2017, they would have had different values. To estimate this sampling  
229 uncertainty and thereby obtain confidence bands, we applied a block bootstrapping procedure, where a  
230 large number of resampled series with the same length as the original series (three years) were created. A  
231 blocking length of one month was chosen. This choice takes the atmospheric decorrelation time scale of a  
232 few weeks into account and it allows a large number of different resampled series to be made.

233 Each resampled series is constructed as follows: The resampled series will contain three January months,  
234 and each of these is randomly chosen, with replacement, of the three January months from the original  
235 series. A similar procedure applies for February, etc. In this way, the resampled series are most likely  
236 different but the annual cycle is preserved. Both the observed series and the forecast series are resampled.

237 For each pair of resampled series bootstrapped value of the performance measures are calculated.  
238 Repeating the resampling procedure, we obtain 1000 resampled values of the measures, from which their  
239 approximate statistical distribution and confidence bands can be calculated. As a standard, confidence  
240 bands (5/95%) are calculated by the bootstrap procedure described above and this allows for a quantitative  
241 inter-comparison of the performance measures for the different forecast classes: if the confidence bands  
242 do not overlap then there is a significance difference.

## 243 **5 Verification of the wind forecasts**

244 In order to illustrate the benefit of the meteorological ensemble on wind forecasts the S03 deterministic  
245 and S05 ensemble mean have been verified against available wind observations for eight coastal  
246 meteorological stations around the Baltic Sea (Figure 3). The RMSE of all stations for the period 1 Jan 2015 -  
247 31 Dec 2017 is shown in Figure 4 as a function of forecast range. This reveals that the S05 ensemble mean is  
248 more accurate than S03, especially at the longer forecast ranges. Similar results are found for other  
249 verification scores, such as correlation and hit rate (not shown).



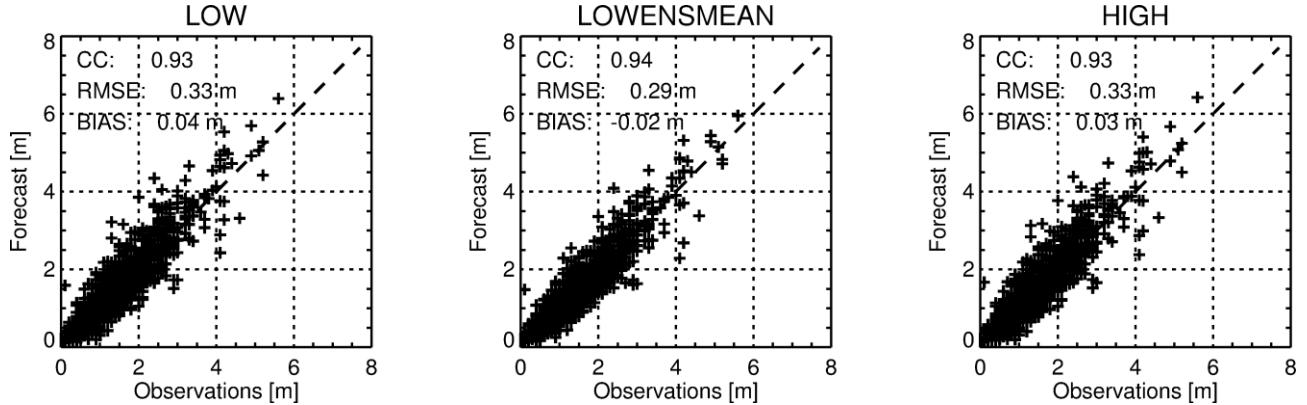
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251 **Figure 4 Verification of wind speed. Average RMSE between model and observations for eight coastal meteorological stations in**  
 252 **the Baltic Sea area.**

254

## 255 6 Verification of forecasted SWH against observations

### 256 6.1 Deterministic measures



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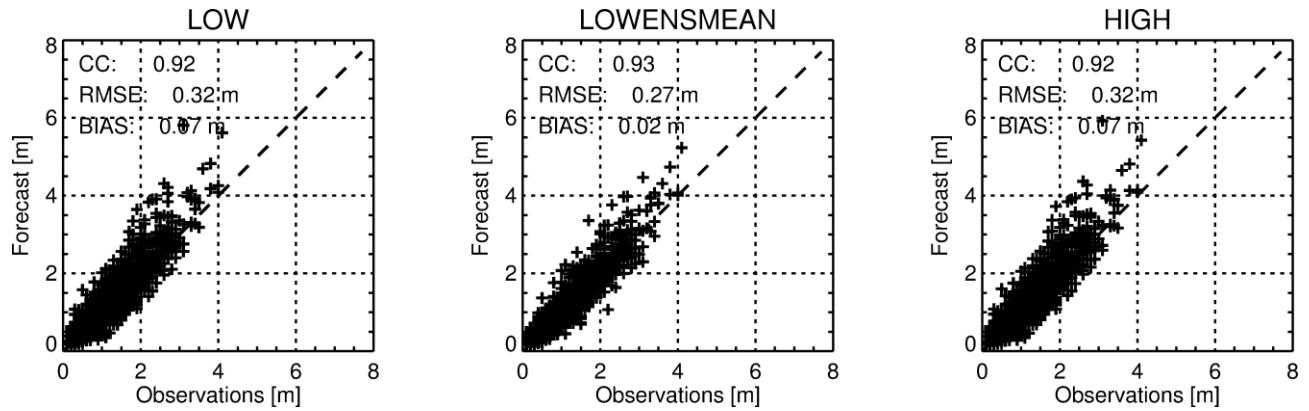
258 **Figure 5 Scatter plot of 24 h forecasts and corresponding observations of significant wave height at site**  
 259 **Bothnian Sea for the LOW, LOWENSMEAN and HIGH forecast classes. Dotted line is the diagonal,**  
 260 **representing a 1:1 agreement between observations and model.**

261

262 To get an idea of the overall quality of the forecasts, Figure 5 shows scatter plots between 24 h forecasted  
 263 and observed SWH for station Bothnian Sea. The points are distributed along the diagonal in all three  
 264 configurations with correlation coefficients above 0.9. The RMSE is 0.33 m for both LOW and HIGH but is  
 265 lower at 0.29 m for the LOWENSMEAN forecasts, which also have the numerically lowest bias. Also for  
 266 other sites, such as Arkona WR (see Figure 6), the RMSE for LOWENSMEAN forecasts is lower than for the  
 267 LOW and HIGH forecasts, and similarly for the bias. However, the scatter plot appears differently for this  
 268 station, because there is a tendency for over-predicting high waves for all three forecast classes.

269

270



271

Figure 6 As Figure 5. Scatter plot of 24 h forecasts and corresponding observations of significant wave height at site Arkona WR for the LOW, LOWENSMEAN and HIGH forecast classes. Dotted line is the diagonal, representing a 1:1 agreement between observations and model.

272

We now turn to the RMSE as function of forecast range, of which plots for all sites can be found in Figure S2. For all sites, the RMSE increases slightly as function of forecast range. All sites except Vahemadal exhibit qualitatively similar behavior: the RMSE for the LOW and HIGH forecasts are almost similar, while it is lower for the LOWENSMEAN forecasts. Thus, for Arkona WR (shown in Figure 7), Bothnian Sea and Darss Sill WR, the RMSE of the LOW and the HIGH forecasts have overlapping confidence bands. The RMSE for LOWENSMEAN gradually diverges to a lower value (around 5 cm) and for large forecast ranges, the confidence bands do not overlap with those for the LOW and HIGH forecast classes. The remaining sites except Vahemadal behave similarly, but with overlapping confidence bands even for the largest forecast ranges.

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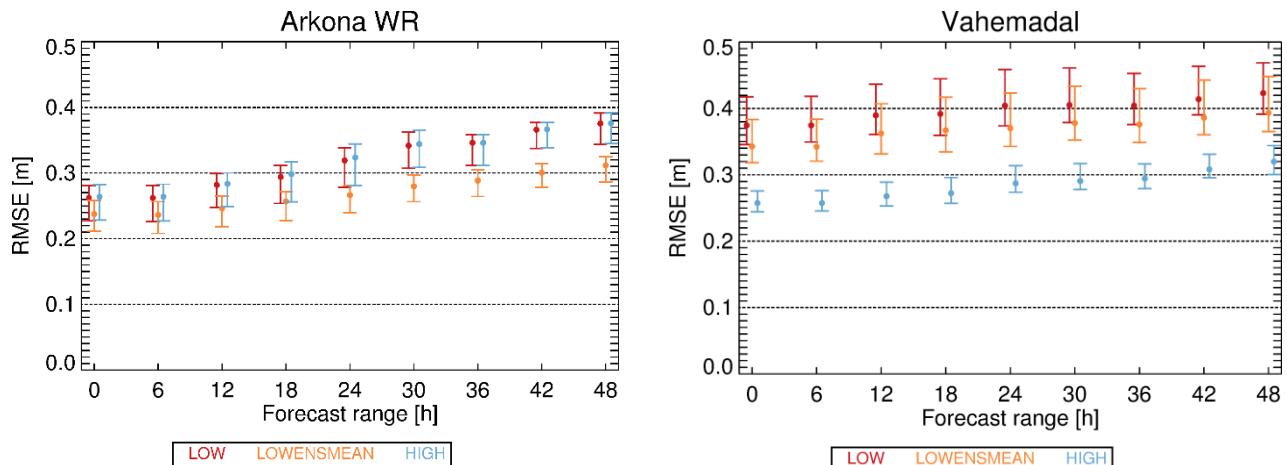
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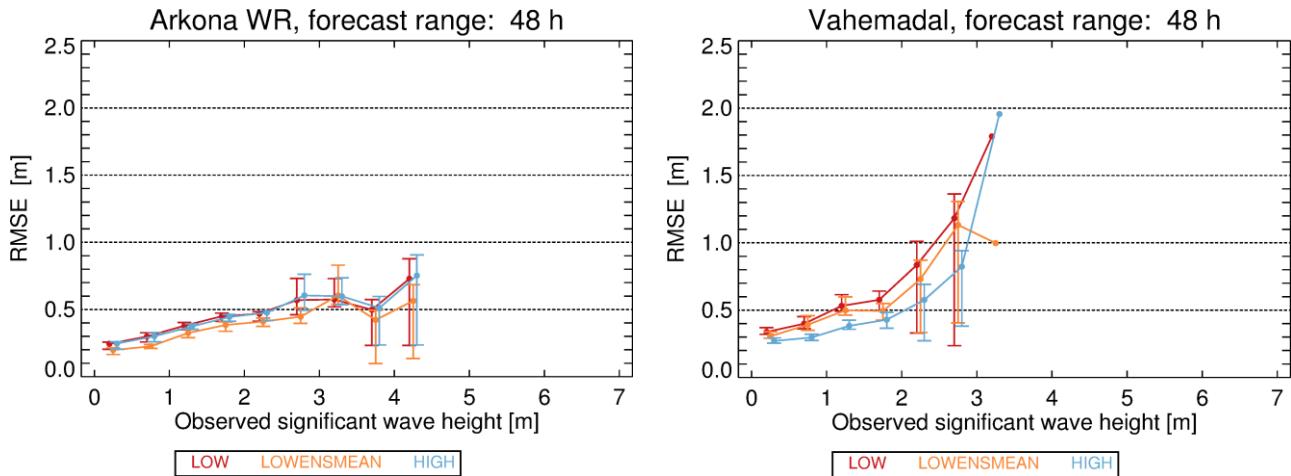
Figure 7 RMSE for selected forecast ranges for Arkona WR (left panel) and Vahemadal (right panel) for LOW, LOWENSMEAN and HIGH forecasts. Error bars show 5/95% confidence bands calculated by bootstrapping.

286

The site Vahemadal (Figure 7) has a different behavior. For this site, the HIGH forecast class has a significantly smaller RMSE and with non-overlapping confidence bands with the RMSE of the LOW and LOWENSMEAN forecasts. This site also has a non-negligible bias of around 12 cm for the HIGH and around 20 cm for the LOW and LOWENSMEAN forecasts; this bias is independent of forecast range (not shown).

291    6.1.1 Performance depending on observed SWH

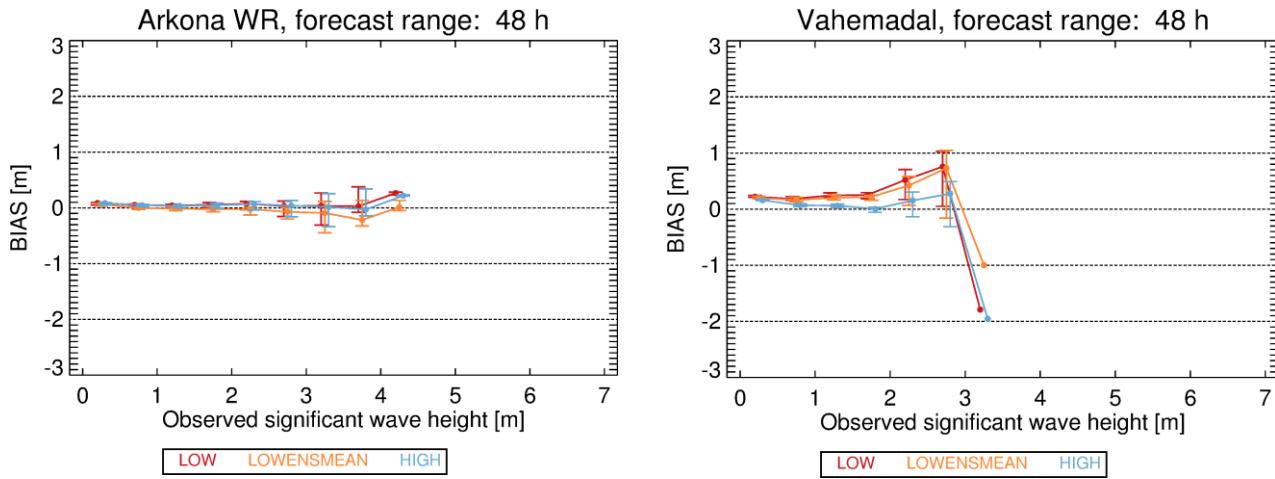
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293    **Figure 8** RMSE as function of SWH for Arkona WR (left panel) and Vahemadal (right panel) for LOW, LOWENSMEAN and HIGH  
294    forecasts and forecast range 48 h. Error bars show 5/95% confidence bands calculated by bootstrapping.

295    The RMSE of the forecasts depends on the magnitude of the SWH. Plots for all sites for the 24 h and 48 h  
296    forecast ranges of RMSE as function of the SWH can be found in Figures S3 and S4. The RMSE for Arkona  
297    WR and Vahemadal as a function of the SWH for the forecast range 48 h is shown in Figure 8. The RMSE  
298    increases as a function of the observed SWH for both sites. For Arkona WR, the LOWENSMEAN forecast  
299    class has the lowest RMSE, although with confidence bands overlapping with the other forecast classes.  
300    This behavior is seen at all sites, except Vahemadal. For Vahemadal, the HIGH forecast class has the lowest  
301    RMSE, and up to a SWH of 2 m, the confidence band is well separated from the confidence bands of the  
302    other forecast classes.

303    Also the bias depends on the SWH. Plots for all sites for 24 and 48 h forecast range of the bias as function of  
304    the SWH are displayed in Figures S5 and S6. For small SWH, the bias is close to zero for most sites. For some  
305    sites, the bias remains close to zero for increasing SWH, as shown for Arkona WR in left panel of Figure 9,  
306    while for others it becomes different from zero for large values of SWH. There is no noticeable different in  
307    the bias of the different forecast classes, except for Vahemadal, shown in right panel of Figure 9, where the  
308    HIGH forecast class has a significantly smaller under-prediction bias than the other forecast classes.

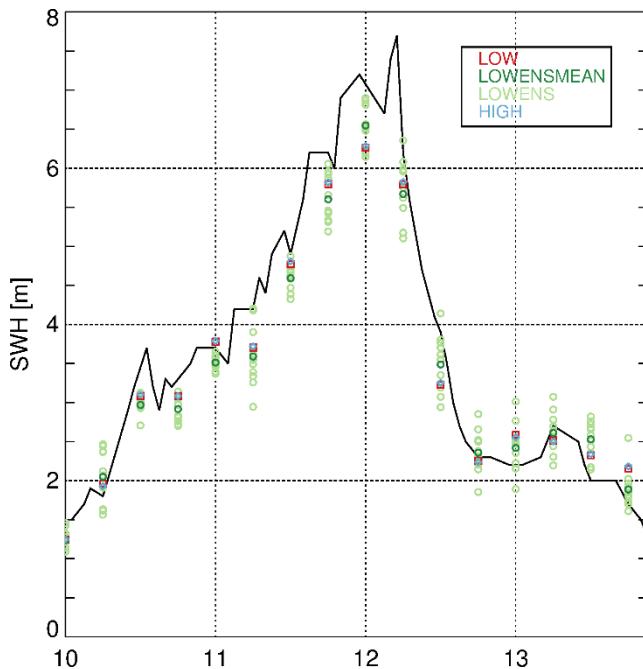


309 Figure 9 Bias as function of SWH for Arkona WR (left panel) and Vahemadal (right panel) for LOW, LOWENSMEAN and HIGH  
 310 forecasts and forecast range 24 h. Error bars show 5/95% confidence bands calculated by bootstrapping.

311 **6.1.2 Forecasts during 'Toni' storm**

312 The Toni storm on 11. January 2017, where a SWH of 8.0 m was recorded at Northern Baltic (Björkqvist et  
 313 al., 2017a), is within our verification period.

314



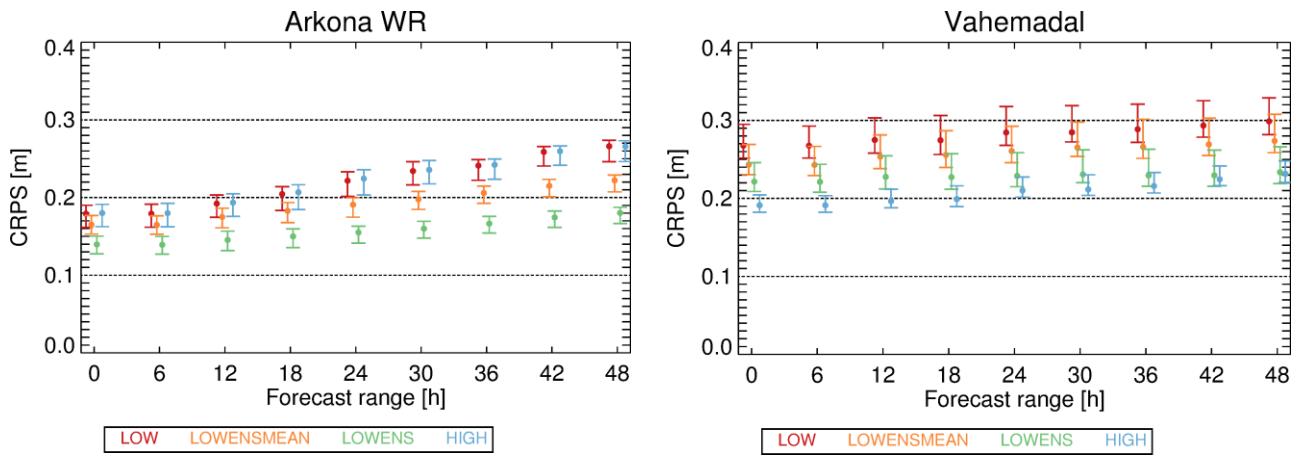
315 Figure 10 Observed SWH for Northern Baltic during, 10-13 January 2017, including the Toni storm. Open circles are 48 h  
 316 forecasts.

317 Figure 10 shows the observed SWH at Northern Baltic during 10-13 January 2017, i.e. including the Toni  
 318 storm, peaking in the early hours of 12 January, together with 48 h forecasts. In this case there is no  
 319 apparent 'best' forecast. Near the peak, LOWENSMEAN performs best, but both before and after, the  
 320 HIGH/LOW performs better. Furthermore, the LOW and HIGH forecasts are very similar in most cases,  
 321 indicating that the higher resolution does not improve the forecasts. Finally, we note that the observations  
 322 generally are within or just a little outside the range of the ensemble forecast.

324 **6.2 Probabilistic metrics**

325 The 11 ensemble members of the LOWENS forecast class defines a statistical distribution function, which is  
 326 a probabilistic forecast of the wave conditions. The deterministic forecast classes LOW, LOWENSMEAN and  
 327 HIGH may be regarded as probabilistic forecasts with probability one for the deterministically forecasted  
 328 future state and probability zero for all other states.

329 As described in Section 4, we use CRPS to describe performance of probabilistic forecasts. CRPS for all sites  
 330 for selected forecast ranges can be found in Figure S7. As typical examples, Figure 11 displays this plot for  
 331 Arkona WR and Vahemadal.



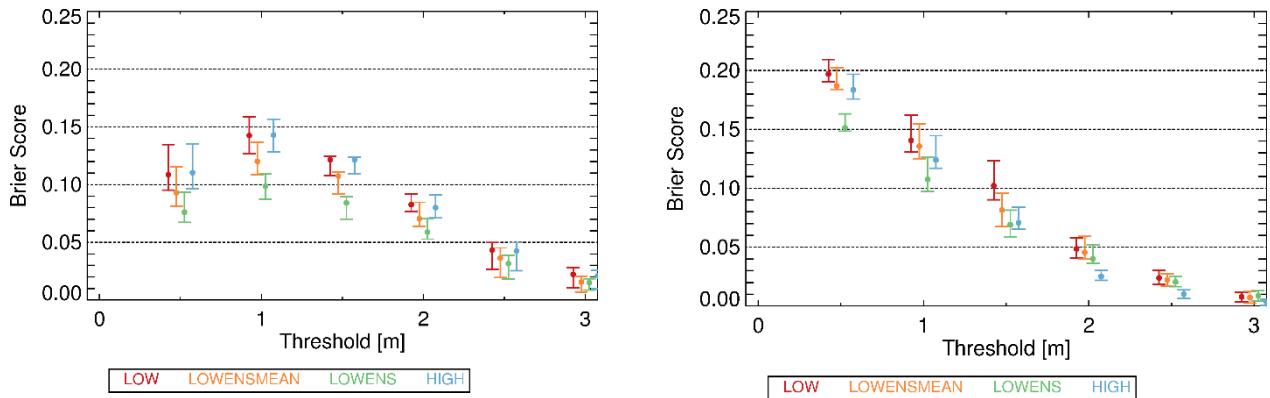
332 **Figure 11** CRPS for selected forecast ranges for Arkona WR (left panel) and Vahemadal (right panel) for LOW, LOWENSMEAN,  
 333 LOWENS and HIGH forecasts. Error bars show 5/95% confidence bands calculated by bootstrapping.

334 All sites except Vahemadal behave qualitatively as Arkona WR: the LOWENSMEAN forecast class has a  
 335 lower CRPS compared to both the HIGH and LOW classes, although the difference is significant (non-  
 336 overlapping confidence bands) for Arkona WR, Bothnian Sea and Darsser Sill WR only, and only for the  
 337 largest forecast ranges. Furthermore, for all these sites, the LOWENS forecast class has an even lower CRPS,  
 338 with confidence bands separated from those of all other forecasts classes. Again, Vahemadal behaves  
 339 differently; here the HIGH forecast class has the best performance in terms of CRPS. However, for large  
 340 forecast ranges, the LOWENS forecast class tends to perform equally well.

341 **6.3 Binary forecasts**

342 For the probabilistic LOWENS forecast class, a binary forecast can be derived as the probability of exceeding  
 343 a defined threshold of SWH. For the deterministic forecast classes: LOW, LOWENSMEAN and HIGH, this  
 344 probability of exceedance is either zero or one. As described in Section 4, the Brier Score is used as  
 345 performance measure for probabilistic, binary forecasts.

346 The Brier Score as a function of threshold is shown for all sites in Figures S7 and S8. Figure 12 shows the  
 347 Brier Score as a function of threshold for Arkona WR and Vahemadal for 48 h forecast range. For Arkona  
 348 WR, the Brier Score for the LOWENS forecast class is the smallest, however the confidence intervals overlap  
 349 with confidence intervals from the other forecasts above the 2 m threshold. Also the LOWENSMEAN  
 350 forecast class has a low Brier Score. This behavior is common to all sites except Vahemadal. For Vahemadal,  
 351 the Brier Score is smallest for the HIGH forecasts for thresholds above 1 m.



352 **Figure 12** Brier score for Arkona WR (left panel) and Vahemadal (right panel) for binary forecast for forecast range 48 h.

#### 353 **6.4 Rank histogram**

354 Rank histograms serve the purpose of illustrating the reliability of probabilistic ensemble forecasts. It is a  
 355 histogram of the rank of the observation, when the observation and all ensemble members of the  
 356 corresponding forecast are pooled together. If the observations and the ensemble members belong to the  
 357 same distribution, then the rank histogram will be flat, while a U-shaped histogram indicates too small  
 358 variance within the ensemble members. For more discussion, see Jolliffe and Stephenson (2003).

359 Rank histograms for all wave measurement sites for forecast range 24 and 48 h are shown in Figure S10 and  
 360 S11 for forecast range 24 h and 48 h respectively. We note that all histograms show the U-shape, indicating  
 361 an unrealistically small variance within the ensembles. For most sites the U-shape is symmetric, except for  
 362 Vahemadal, where the U-shape is strongly asymmetrical. This corresponds well with the bias mentioned in  
 363 Section 6.1.

## 364 **7 Discussion**

365 Our main finding in the previous section is that for most wave measurement sites included in this study, the  
 366 LOWENSMEAN and the LOWENS forecast classes in many cases have a better performance than the LOW  
 367 and HIGH forecast classes. Only for one site results are different; namely that the HIGH forecast class has  
 368 the superior performance. The conclusions hold, whether based on overall RMSE, CRPS or the Brier score.

369 In the discussion below, it should be mentioned that improving wave forecasts is not the only driving factor  
 370 in reducing the grid size of the wave model. Coupling the wave model with atmosphere or ocean circulation  
 371 models may give a better description of vertical fluxes of heat and momentum (Cavaleri et al., 2012). For  
 372 instance, Alari et al.(2016) documented a significant improvement of modelled sea-surface temperatures  
 373 by the NEMO circulation model in the Baltic Sea when a two-way coupling to the wave model WAM was  
 374 introduced. Introducing such coupling may demand a high horizontal resolution, in atmosphere, wave and  
 375 ocean models, in order to describe the fluxes satisfactorily. Note also that the methodology applied in this  
 376 study is a site-specific verification and inter-comparison of the different forecast families. This is a valid  
 377 approach, since most uses of the wave forecasts are site-specific. However, it must be remembered, that  
 378 the approach has a risk of under-estimating the overall performance due to *double-counting errors* in both  
 379 space and time. We have made no attempt to assess the magnitude of this potential effect.

380

381 **7.1 Comparison with other operational forecast systems**  
382 Multi-year verification results from two operational deterministic wave forecast systems that covers the  
383 region in focus have been published, and can be compared to results from the present study. Both these  
384 systems are based on the third generation WAM; the system described in (Tuomi et al., 2008) has about 22  
385 km horizontal resolution, while the system described in (Tuomi et al., 2017) has 1 naut. mile horizontal  
386 resolution.

387 For certain sites, the RMSE of the 6 hour forecasts of SWH are available for at least one of the  
388 aforementioned forecast systems in addition to the DMI-WAM forecasts; thus comparison of the systems is  
389 possible. All sites have a water depth of more than 46 m and therefore represent offshore conditions.

390 **Table 5 Comparison of RMSE for SWH of 6h forecast runs for selected sites. FIMR values are from (Tuomi et al., 2008) and FMI  
391 values are from (Tuomi et al., 2017)**

	FIMR	FMI	DMI LOW	DMI LOWENSMEAN	DMI HIGH
Horizontal resolution WAM	~ 22 km	1 naut. mile	10 km	10 km	5 km
Horizontal resolution NWP	~ 22 km	2.5 km	3 km	5 km	3 km
Arkona WR	-	0.28	0.26	0.24	0.26
Bothnian Sea	-	0.28	0.25	0.23	0.25
Finngrundet WR	-	0.27	0.24	0.22	0.23
Helsinki Buoy	0.25	0.26	-	-	-
Northern Baltic	0.31	0.26	0.24	0.23	0.24

392  
393 We remind the reader that the cases compared in Table 5 have different wind forcing and probably also  
394 different version of WAM. Therefore the figures cannot be directly compared and differences cannot with  
395 certainty be attributed to differences in horizontal resolution.

396 From Table 5 one can see that for the sites considered, the LOWENSMEAN has the lowest RMSE. This  
397 supports the finding of this study that for offshore conditions there is no reason to improve the resolution  
398 further than that of the LOW configuration. In addition, the results emphasize the value of describing the  
399 uncertainties of in the atmospheric forcing by introducing ensembles, as this leads to a lower RMSE of the  
400 forecasts. This is also in line with our findings in the previous section.

401 Test runs of a few months duration of deterministic and ensemble wave forecasts of SWH for the Baltic Sea  
402 (Behrens, 2015) also show slight improvement of ensemble mean forecasts, compared to deterministic  
403 forecasts, and thus support our findings.

404

405 **7.2 Limitations of the study**

406 **7.2.1 Length of verification period**

407 Operational centers typically renew their computer installations every 5-6 years with about an order of  
408 magnitude increase in performance. At DMI, a new installation was introduced early 2016, allowing the  
409 HIGH and LOWENS configurations to replace the LOW configuration. Presently (mid-2018) the system is  
410 mid-term upgraded and this makes it appropriate to do the inter-comparison now as a guidance for any  
411 changes in the operational setup.

412 For this reason, the operational forecasts performed on the present system, supplemented by delayed-  
413 mode forecasts has determined the three-year verification period used in our study. A longer verification  
414 period could evidently have reduced the sampling uncertainty in the analyses and thereby sharpened the  
415 conclusions. On the other hand, the three-year verification is not short compared to the study by Bunney  
416 and Saulter (2015) or the CMEMS verification report by Tuomi et al.(2017)

417 **7.2.2 Choice of observational base**

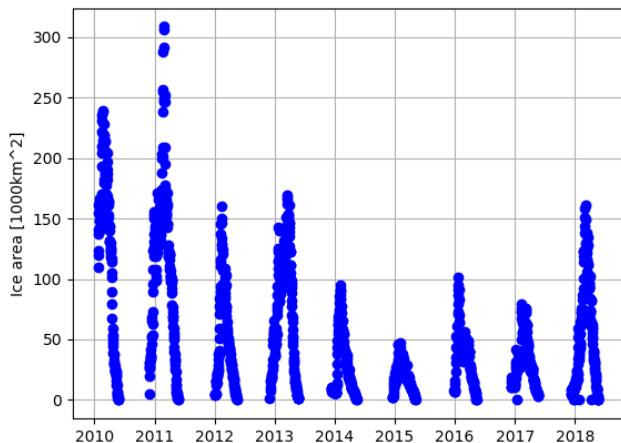
418 The present verification is based on observations at near-hourly resolution from a number of sites in the  
419 Baltic Sea. Therefore, in the majority of the Baltic Sea, verification is not possible, which limits the firmness  
420 of our conclusions.

421 SWH derived from satellite-borne altimeters (Kudryavtseva and Soomere, 2016) offers an alternative,  
422 which could be pursued in a future study. These data have a fair spatial coverage but at the cost of a  
423 temporal resolution of one day or less. This means that maximum wave heights connected to severe storms  
424 may easily be missed. Nevertheless, these data has proven useful for verification in the Baltic Sea by (Tuomi  
425 et al., 2011)

426 **7.3 Effect of sea ice coverage**

427 The main effect of sea ice on formation of waves is to limit the fetch. Furthermore, when a developed wave  
428 field approaches an ice-covered area, the wind and the waves decouple, so that the waves act more like  
429 swell, propagating through ice-covered areas while losing energy by breaking up the ice cover. The WAM  
430 model does not account for such interactions, and sea ice, when dense enough, acts as a solid shield that  
431 effectively removes all local wave energy in the model. It is implicitly assumed that dense ice will also be  
432 thick enough for this to be approximately correct. In the Baltic Sea, that may not always be the case, and  
433 therefore sea ice occurrence may represent a systematic error source in the present study. Another effect  
434 of sea ice in the Baltic is that the wave observing systems are withdrawn when ice is expected. This may  
435 cause a systematic bias in the verification analysis if strong winds during winter are left out.

436 Based on Copernicus sea ice charts produced by the Finnish Meteorological Institute the ice conditions for  
437 the Baltic have been evaluated. The Finnish ice charts are produced on a grid of approximately  $1 \text{ km}^2$  with a  
438 temporal resolution of approximately one day in the ice season. Data is available from 2010 onwards. The  
439 average ice conditions for February for all years and the three years in focus can be found in Figure S12. All  
440 three years 2015-2017, and in particular 2015, have a smaller ice cover relative to the period 2010-2018.



441

442 **Figure 13 Integrated sea ice area of the Baltic Sea based on Finnish ice charts**

443 Another way to illustrate this is considering the Baltic Sea integrated sea ice area, depicted in Figure 13,  
 444 which shows that the years 2015-2017 have the lowest sea ice area over the whole period 2010-2018.  
 445 Therefore, we may anticipate that systematic errors arise from the occurrence of sea ice are relatively  
 446 small.

447 **8 Conclusion**

448 For most sites, we find that the HIGH forecast class does not perform better than the LOW forecast class in  
 449 forecasting SWH. These sites are all positioned well away from coasts in deep water and are thus freely  
 450 exposed from all directions. This suggests that the resolution of the bathymetry and the spectral resolution  
 451 are adequate. For these offshore sites, introducing ensembles increases the performance of the forecasts,  
 452 whether as in the LOWENSMEAN deterministic forecasts and the LOWENS probabilistic forecasts. A similar  
 453 conclusion generally holds for the binary forecast of exceeding a threshold.

454 For one site, Vahemedal just outside Tallin, the HIGH forecast class performs better than the other classes.  
 455 The bathymetry near Vahemedal is complex and relatively shallow, thus the bathymetry affects the wave  
 456 field and an improved description will therefore improve the modelled wave field. Further verification with  
 457 near-coast stations may reveal whether this conclusion is general for coastal areas.

458 For high wave heights, there are significant systematic biases for most sites shared among all three forecast  
 459 configurations. These are most probably to be ascribed to model deficiencies and act to mask any  
 460 differences in performance between the different forecast classes. Also the RMSE becomes large for large  
 461 observed SWH. This is expected since small timing errors in the predicted wave time series will have larger  
 462 impacts on the model-observation match-up when the SWH is large. The present study therefore suggests  
 463 that for offshore conditions, there are no indications that a further increase of the resolution of the WAM  
 464 model will result in enhanced forecast performance. In addition, the results show that introducing  
 465 ensembles increases the performances. This is both true for deterministic forecast in the form of ensemble  
 466 mean and for probabilistic forecast. For nearshore conditions conclusions are based on only one site, but  
 467 results from this indicates that increasing the resolution gives better forecasts, while introducing ensembles

468 does not. This can be due to both enhanced spatial resolution, allowing a better representation of shadow  
469 and shallow water effects, and/or spectral resolution.

470 The results of the present study thus underpins that a wave model setup with an equidistant grid cannot  
471 deliver optimal wave forecasts for both coastal and offshore conditions. This is particularly true for the  
472 Baltic Sea, where very small spatial scales are found in the archipelago near the coasts of Sweden and  
473 Finland (Björkqvist et al., 2017b). Besides implementing a 0.1 naut. miles model, these authors improved  
474 forecasts by introducing semi-empirical modifications to the wave model. Cavalieri et al. (2018) also write  
475 about this and discuss other approaches. These include one-way nesting, used in the present study (see  
476 Section 2), multi-cell grids (Bunney and Sauter, 2015), and triangular unstructured grids (e.g. Zijlema,  
477 2010). These techniques may be worth testing for the Baltic Sea.

478 Finally, we note the under-spread in the ensemble forecasts demonstrated in Section 6.4. This points to a  
479 potential for improving the combined weather-wave system.

480

481

482 *Data availability.* Model data is available from the authors upon request, whereas wave observations can  
483 be found on the CMEMS server.

484 *Competing interests.* The authors declare that they have no conflict of interest.

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490

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