

Dear colleagues, we appreciate the effort of the editor and reviewers. The reviewers comments were particularly useful for improving the text and clarify some missing information. You will find attached a detailed point-by-point answer to all the comments and questions. We are looking forward to your opinion on the possible publication in Ocean Science. Although most comments gave rise to corrections, the few on which we did not agree with the reviewers have led to a more detailed rewriting of the corresponding section of the paper, as detailed in the attached rebuttal.

A detail response to the reviewers are described below. The comments from the reviewer are reproduced in bold, and our answer is in normal font.

### **In reply to reviewer 1:**

**Overview** This paper describes the design of a drifting buoy, to measure directional waves using a low-cost accelerometer to obtain 'heave' spectra and the Global Navigation Satellite Systems (GNSS) signal to obtain the directional components of the wave spectra and the ambient current. The paper describes the design of the SKIB system in some detail, then analyses results from an experiment where several buoys are deployed in the Chenal du Four, with strong tidal currents and current gradients, adjacent to a moored Datawell Directional Waverider buoy. The SKIB buoy performance is validated against a SWIFT buoy and stereo-video as well as the Waverider. Then there is a discussion about the high-frequency interaction of waves and currents. **General Remarks** There is a lot of interesting information in this paper but there is a need for clarification of its aims. Is it about presenting a new instrument or an application in the Chenal du Four (this seems to be an afterthought), a lot more of the content is about the buoy and other wave measurement systems. The summary and conclusion are very cursory and there are a lot of errors and typos (mainly annotated on the m/s). The paper does not appear to be ideally-suited to publication in Ocean Science, although it falls within the topics described, there are not many papers published on waves and instrumentation. It might be better submitted to Ocean Engineering or to Continental Shelf Research as a follow-up to the Pearman et al. (2014) paper. In order to be accepted it needs major revision. **Detailed Corrections**

**1.**In the Introduction, please make clear what the motivation and aims of the study are. It is not clear whether the main aim is to design and test the instrument or gather data on wave-current interaction. The stated intention is 'to capture the response of surface gravity waves to horizontal current gradients, in order to better interpret airborne and satellite imagery of waves and current features'. After listing previous instrument developments, please clarify why it is necessary to develop another buoy. What is the novelty in the work presented in this paper?

We have clarified that the objective of measuring shorter wave components and wave-current interactions require a relatively small buoy which was not available. We have now written on page 3, line 4:

*In this context, existing wave buoys are generally too large to properly respond to short gravity waves. We have thus developed a low cost drifting buoy, the "surface kinematics buoy" (SKIB), specially developed for wave-current interaction studies*

**2.** Section 2 presents standard directional analysis of wave spectra from combined vertical plus horizontal motion, using FFT and co- and quad-spectra. There is some confusion about the nomenclature at the bottom of page 3 (lines 23 onwards).

**What are termed the ‘moments of the directional distribution’ are usually referred to as the angular harmonics, which can be derived only for the first 4 terms (Longuet-Higgins et al., 1963). This section needs correction.**

**A good reference is the COST 714 book (2005) which shows the various ways of deriving a directional distribution and the limitations due to observation systems. It is usual to separate the 2D frequency-direction spectrum into two parts multiplied together: a frequency distribution and a directional distribution (frequency-dependent) based on some simple pattern such as  $\cos^2\theta$ . However none of this is new.**

We beg to disagree. Because buoys do not measure the directional spectrum but only “moments”, we prefer to only work with measured parameters, or parameters that are derived by simple manipulations of the moments, e.g. the mean direction and spread. This is most useful for validation (e.g. O’Reilly et al. 1996). We have thus added,

*The spectra and co-spectra of these time series can provide the first five Fourier coefficients of the angular distribution, also known as angular moments,  $a_0(f_p)$ ,  $a_1(f_p)$ ,  $b_1(f_p)$ ,  $a_2(f_p)$  and  $b_2(f_p)$ ...*

**Check also lines 13-18 on p 10. 3. In section 3.2 there are a lot of acronyms for the electronic components which should be defined or identified as trade names.**

We have simplified the buoy electronics description by removing unnecessary description of standard electronics equipment (e.g. Zigbee), and giving the full name of parts that were only referred to by their acronyms. For example,

*Micro Secure Digital High Capacity (SDHC) memory card*

**4. In section 3.2 can the authors clarify the cost of the basic SKIB-STM system.**

We have added the following in section 3.2,

*Standard prices for all the parts in the year 2015 was about 1100 euros for all electronics, half of which is for the Iridium and GPS equipment, and another 1100 euros for the hull and mounts inside of the hull. That expensive choice of the hull was, in our case, justified by a possible re-use for other oceanographic applications.*

**Is this system accurate enough - later it is clear that SKIB-SBG is better**

There is of course always a trade-off between cost and accuracy. The accuracy limit is mostly due to the relative high noise floor of the STM accelerometer chosen. Indeed the SBG sensor is necessary for measuring small amplitude long waves, but in the case of the short waves that we focus on, the STM is good enough. This was clarified in the text and we add more information about it in the conclusions.

**(NB please standardise how this is referred to – SKIB IMU is also used).**

We verified and standardised the use of SKIB-STM and SKIB-SBG.

**5. In section 3.3 the upper limit of the useful frequency range is 0.8Hz, this is not really extending the frequency range to high frequency as claimed but rather similar, especially since the frequency range for directional parameters is limited to 0.5Hz.**

As clarified in section 3.3 and in the conclusion, this statement on the limitations is only for the directions due to our choice of GPS antenna and processing. The heave spectrum is still valid up to 1 Hz. This may seem like a modest increase from the 0.6 Hz of Datawell Waveriders, but this is still a factor 2.8 in wavelengths.

**6. Section 4 describes the results from a short deployment in October 2015. Figs 4 and 5 refer to September 2016 and should appear in section 3. 7.**

The figure had been misplaced. This is now corrected.

**Section 5 ‘Summary and conclusions’ is far too short and superficial.**

We have now expanded section 5, in particular adding some comments on the costs and the performance of the two SKIB models, as well as a reference to the recent paper by Sutherland and Dumont (2018), who used a SKIB-SBG.

**8. Standardise the way of referring to the Datawell Directional Waverider – it is variously referred to as Datawell, Waverider etc.**

This has been corrected to “Datawell”, which implicitly refers to the Mark III Directional Waverider model from Datawell.

**9. In Figure 7 the colours would be more usefully applied to identify different buoys – this would require changing Fig 6 also.**

We have kept the colors to better identify that it does not matter which buoy measures what, but rather, in which region is the buoy, so that we can reduce the variability of the random wave measurement by averaging the different buoys together. This averaging allows us to use shorter time records and thus observe strong gradients that would otherwise be lost if we computed average spectra over 30 minutes .



## In reply to reviewer 2

2) The manuscript describes a novel low-cost surface kinematic buoy, the SKIB system, composed of a GPS and an accelerometer. The intention is to capture waves, currents and their interactions. The paper is structured as a method paper (introduction, parameters, setup including in situ and field validation, an exemplary field application, and conclusions) and well written. I see a couple of minor issues, that can be improved, however in general I consider it publishable after inclusion of the following aspects.

Minor issues and suggestions:

**Title:** I would not try to use upper cases for the abbreviated SKIB, but to stick to lower cases (also throughout the text). It confuses the reader and it is easy to guess why SKIP was chosen as a systems name. Additionally I am not sure, if double plural is correct for the last two words or if it should read “. . .for wave-current interaction studies”

We modified the name for lower cases "surface kinematic buoy" and corrected the plural as suggested.

**Abstract:** Well written and structured. Contains all essential information. I suggest to quantify the outcomes in lines 8 and 9.

We have added the following sentence to the abstract,

*The use of low-cost accelerometers and a spherical ribbed and skirted hull design provides acceptable heave spectra  $E(f)$  from 0.09 to 1 Hz with an acceleration noise level  $(2\pi f)^4 E(f)$  close to  $0.023 \text{ m}^2\text{s}^{-3}$ .*

**L21: What do you mean by “short instrumented spar buoy” Measurable parameters and processing:**

A spar buoy is commonly used to describe the shape of the buoy. A spar buoy is a tall and thin buoy that floats upright in the water and is characterized by a small water plane area.

([https://en.wikipedia.org/wiki/Spar\\_buoy](https://en.wikipedia.org/wiki/Spar_buoy) )

**L11: Why a linear interpolation and not any other function?**

Linear interpolation is the most simple method. We do not expect significant differences with other methods.

**Buoy design and validation: Page 4, L18: Who is T. T. Janssen and why mentioning here?**

We have removed this confusing sentence. For your information, T. T. Janssen is not the CEO of Spooondrift (<https://spooondrift.co/> ) and has been working on wave buoy design for many years (e.g. Herbers et al. 2012).

**Page 4, L19: Provide paper reference instead of internet link.**

We are not aware of papers describing this buoy. We have thus preferred to remove this sentence.

**Page 5, L1ff.: The description of the mechanical design is rather short and not suited to follow, if someone wants to repeat your experiment. Please provide more information on the mechanical design (drawing in the appendix?) and also specify, what alternatives had been tested respectively, why this design is the best.**

The following sentences has been added

*With all these constraints in mind we found that a nearly spherical shape with ribs and an additional skirt provided a good water-following behavior, whereas spherical shapes performed more poorly. Three-dimensional printing was tested without much success due to the porosity of the printed material.*

**Page 5, L4: figure 1.b and 2.a,b. Subsection heading: SKIB electronics (be consistent using upper/lower cases in headings)**

We have corrected all to lower case.

**Page 5, L13: 2.5 VDC Page 5, L15: prograded (you used American English throughout the text)**

We have corrected to American English throughout the text.

**Page 5, L16: the Xbee module was not described/mentioned before**

Xbee is indeed a particular brand of modems that uses the Zigbee protocol (based on [IEEE 802.15.4](#)) . We have removed this mention of Xbee to make the text less confused.

**Page 5, L17: the 802.15.4 specification seems not necessary here**

Indeed, this was removed for clarity.

**Page 5, L20: . . .are mounted. . . Page 5, L21: . . . vacuum-sealed (see figure 1). Page 5, L23: In those buoys the IMU SBG Ellipse were used, set to an. . . Page 5, L28: The laboratory tests. . .**

We have followed these modifications in the text.

**Figure 1: Explain STM and SBG in caption. Explain SKIP meaning in caption. A figure with caption should be understandable in its own. “Micro-controller board. . .”**

The caption modified in order to explain all the main electronic components as suggested.

**Figure 2: BBWAVES is mentioned here for the first time and not explained in the text.**

“BBWAVES” was replaced by “oceanographic campaigns”, as “BBWAVES” was the name for the experiment “Broad Band Waves experiment”.

**Page 8, L7: Who can something follow 3 methods? Why not restrict to one citation?**

We have kept only the last reference, which is indeed based on the two previous works.

**Table 1: . . .height. . . (not hight). Check text, this happened 3 times in the manuscript.**  
This typo has been corrected.

**Page 10, L9ff: You state that parameters overlap within confidence intervals. True for Hs but really close. Please comment.**

The differences are commented in the following lines,

*The Largest differences are between the SKIB STM and SWIFT buoys and are associated with the filtering of low frequency content in the SWIFT processing chain (fig.3.b), and unfiltered low frequency noise in the SKIB STM. However,*

**Page 20, L11: The largest difference. . . Page 20, L11: associated (doubled) Page 11, L9: . .with RSME. . . (in figure 4, you use RSME not RSMD) Page 11, L19: measured (doubled)\**  
**Figure 4: Please explain NRSME. Wave evolution in current gradients: Figure 6: Here you name the region: “Four channel” while in the text you name it “Chenal du Four”. Be consistent. Page 14, L1: Figure 8 is mentioned in the text before figure 7.**  
All the text correction proposed were accepted and included in the text.

**Figure 7: Axis fonts used differ from other figures.**

Same fonts were not available because the figures were made using different softwares.

**Figure 8: ..The color of the lines follow. . . ??**

Text correction accepted.

**Summary and conclusions:**

**Page 17, L2: Can you quantify “low-cost”?**

**Either here or before in the text. You talked about the sensor cost but never mentioned the whole system.**

The cost of electronics and hull is now given in section 3.2

*Standard prices for all the parts in the year 2015 was about 1100 euros for all electronics, half of which is for the Iridium and GPS equipment, and another 1100 euros for the hull and mounts inside of the hull. That expensive choice of the hull was, in our case, justified by a possible re-use for other oceanographic applications.*

**General comment: This section is rather short and could be improved by a deeper reflection on the implications and applications of the SKIB, its next steps and further improvements.**

We have now expanded section 5, in particular adding some comments on the costs and the performance of the two SKIB models, as well as a reference to the recent paper by Sutherland and Dumont (2018), who used a SKIB-SBG.

**References: Not consistent in using abbreviated or full journal names, e.g. for J. Phys. Oceanogr.**

Journal abbreviation removed.

**Author's changes in manuscript.**

A detailed version of the modifications in the manuscript are add in a separate PDF version of the manuscript where modification from the previous version are highlighted in the text.

# A Surface Kinematics Buoy (SKIB) for wave-current interaction studies

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**Abstract.** Global Navigation Satellite Systems (GNSS) and modern motion-sensor packages allow the measurement of ocean surface waves with low-cost drifters. Drifting along or across current gradients provides unique measurements of wave-current interactions. In this study, we investigate the response of several combinations of GNSS receiver, motion-sensor package and hull design in order to define a prototype “surface kinematic buoy” (SKIB) that is particularly optimized for measuring wave-current interactions, including relatively short wave components (~~relative frequency around 1 Hz~~) that are important for air-sea interactions and remote sensing applications. The comparison with existing Datawell Directional Waverider and SWIFT buoys, as well as stereo-video imagery demonstrates the ~~accuracy~~ performance of SKIB. The use of low-cost accelerometers and a spherical ribbed and skirted hull design ~~provide~~ provides acceptable heave spectra ~~while velocity~~  $E(f)$  from 0.09 to 1 Hz with an acceleration noise level  $(2\pi f)^4 E(f)$  close to  $0.023 \text{ m}^2\text{s}^{-3}$ . Velocity estimates from GNSS receivers yield a mean direction and directional spread. Using a low-power acquisition board allows autonomous deployments over several months with data transmitted by satellite. The capability to measure current-induced wave variations is illustrated with data acquired in a macro-tidal coastal environment.

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## 1 Introduction

Many devices have been developed to measure ocean waves, from in situ moored or drifting sensors, to remote sensing systems using optical or radar devices (COST Action 714 Working Group 3, 2005). Each measurement system has a specific range of applications defined by the required space and time resolution and coverage, water depth ~~and~~ current speed. ~~These~~ They have been very useful in studying upper ocean processes or monitoring sea states for various applications.

Among all these, surface buoys such as the Datawell ~~directional~~ Directional Waverider have been reference instruments for the estimation of the sea surface elevation frequency spectra from measurements of buoy acceleration. The combined horizontal

and vertical accelerations give the first five moments of the directional spectrum that can be used to estimate the directional wave spectrum (e.g. Benoit et al., 1997). In conditions with strong currents, e.g. more than 1 m/s, it is usually impossible to measure waves with a moored surface buoy, due to the tension on the mooring line. This problem is avoided with drifting buoys, but the nature of the measurement is different. Drifting buoys will not measure long time series at the same location, but they can provide a unique along-section measurement of waves following the current (Pearman et al., 2014).

Several such drifting buoys have been developed recently for different applications (Herbers et al., 2012; Thomson, 2012; Reverdin et al., 2013). With our focus on relatively short gravity waves, with wavelength between 1 and 30 m, there is a trade-off between the size of the device and its response to the waves. In practice, the buoy cannot be too small so that it is easily found and recovered, nor too large so that it follows the motion of these short gravity waves. Besides waves, the time-evolution of the buoy position can also be used to estimate surface currents in cases where the wind force on the buoy is negligible.

Herbers et al. (2012) proposed a compact and low-cost 45-cm diameter GPS-Tracked drifting buoy. This buoy uses a GPS receiver for absolute position tracking. Compared with Datawell these authors find that the horizontal wave orbital displacements are accurately resolved, although, the vertical sea surface displacements were not well resolved by standard GPS measurements, requiring to attach an external high precision antenna to the drifter.

Thomson (2012) developed the Surface Wave Instrument Float with Tracking (SWIFT), a multi-sensor drifter buoy. This short instrumented spar buoy has a 0.3 m diameter and 2.15-m height, and has been designed to measure wind, waves, whitecap properties and underwater turbulence and current profiles. Wave measurements are derived from the phase-resolving GPS, that contain the wave orbital motions relative to the earth reference frame. The relatively large size of the buoy is needed for the other measurements, and it results in a very weak response for wave frequencies above 0.4 Hz. Obviously, the SWIFT buoy design has other benefits, such as the use of an acoustic Doppler current profiler that allows to investigate the effect of the vertical current shear on the waves (Zippel and Thomson, 2017).

Reverdin et al. (2013) developed a surface wave rider (called “Surpact”) to measure sea state and atmospheric sea level pressure as well as temperature and salinity at a small fixed depth from the surface. Surpacts use a floating annular ring (28 cm diameter) with a rotating axis across it to which the instrumented tag is attached and uses the vertical acceleration to obtain the power spectrum between 0.2 Hz and 2.2 Hz.

~~Within limitations, the changing position of drifting buoys can also be used to estimate near surface currents, with buoy trajectories representing the result of the integral of wind and current forcing over the entire buoy.~~

~~Our intention is to capture~~ Our goal of measuring the response of surface gravity waves to horizontal current gradients, in order to better interpret airborne and satellite imagery of waves and current features (e.g. Kudryavtsev, 2005; Rascle et al., 2014, 2017). Further, away from the coasts, it is now understood that surface currents are the main cause of the variability of wave properties at small spatial scales (Ardhuin et al., 2017; Quilfen et al., 2018) and more measurements are required to better understand the processes at play, and improve on the parameterizations of numerical wave models (e.g. Ardhuin et al., 2009; van der Westhuysen et al., 2012).

~~The~~ In this context, existing wave buoys are generally too large to properly respond to short gravity waves. We have thus developed a low cost drifting buoy, the "surface kinematics buoy" (SKIB), specially developed for wave-current interaction

[studies. Its design, tests and validations are presented here.](#) This paper is organized as follows. Section 2 presents the relations between parameters recorded by the various devices used in our study and the wave spectrum. Section 3 explains the design of SKIB and validation in the laboratory and in situ. Section 4 describes an example application to measurements of waves and currents, and conclusions follow in section 5.

## 2 Measurable parameters and processing

For random wind waves, the variance of the sea surface elevation field can be described using variance density spectrum  $E(f_r, \theta)$ , or the action density spectrum  $N(k, \theta)$ , where  $N(k, \theta) = E(f_r, \theta)/\sigma$ ,  $f_r = 2\pi/\sigma$  is the intrinsic (relative) wave frequency,  $\theta$  is the wave direction.

For linear waves, the wavenumber  $k$  is related to the intrinsic wave frequency, the frequency measured by a drifting buoy following the current,

$$\sigma^2 = gk \tanh(kD). \quad (1)$$

where  $D$  is the water depth, and  $g$  the acceleration of the gravitational force.

In the presence of a horizontal current vector  $\mathbf{U}$  that is vertically uniform, the intrinsic frequency differs from the absolute frequency  $f_a = \omega/(2\pi)$  observed in a reference frame attached to the solid Earth,

$$\omega = \sigma + \mathbf{k} \cdot \mathbf{U}. \quad (2)$$

A near-surface shear would lead to an effective current that varies with the wavenumber (Stewart and Joy, 1974).

When drifting with the surface current vector  $(u, v)$ , a surface buoy can measure the three components of the acceleration vector  $(a_x, a_y, a_z)$ , the GPS horizontal Doppler velocities  $(u, v)$  and positions  $(x, y, z)$ . In practice the accelerations and horizontal velocities have relatively low noise and can be used to measure waves. In our SKIB acquisition system, the GPS data is sampled at 1 Hz while the accelerometer is sampled at 25 Hz and they are independent systems.

The spectra and co-spectra of these time series can provide the ~~moments of the directional distribution of the spectrum  $E(f_r, \theta)$ , that are the first terms in a Fourier expansion of the directional distribution,  $E(f_r)$~~  first five Fourier coefficients of the ~~angular distribution, also known as angular moments,  $a_0(f_r)$ ,  $a_1(f_r)$ ,  $b_1(f_r)$ ,  $a_2(f_r)$  and  $b_2(f_r)$~~  (Longuet-Higgins et al., 1963; Kuik et al., 1998). ~~From that it is possible to obtain the directional distribution of the spectrum  $E(f_r, \theta)$~~  (Longuet-Higgins et al., 1963).

From the first moments it is customary to define a mean direction  $\theta_1(f_r)$  and directional spread  $\sigma_1(f_r)$ ,

$$\theta_1(f_r) = \tan^{-1}(b_1/a_1), \quad (3)$$

$$\sigma_1(f_r) = \sqrt{2 \left( 1 - \sqrt{a_1^2 + b_1^2} \right)}. \quad (4)$$



When only velocity measurement are available, one can only access  $E(f_r)$ ,  $a_2(f_r)$ ,  $b_2(f_r)$ , which give the two following parameters,

$$\theta_2(f_r) = \frac{1}{2} \tan^{-1} (b_2/a_2), \quad (5)$$

$$\sigma_2(f_r) = \sqrt{0.5 \left( 1 - \sqrt{a_2^2 + b_2^2} \right)}. \quad (6)$$

For completeness, here are how the spectra of and co-spectra  $C_{xy}$  of two quantities  $x$  and  $y$ , with  $x$  or  $y$  replaced by  $h$  for heave, and  $u$  or  $v$  for the horizontal velocity components, are linked to the ~~directional~~angular moments,

$$\begin{pmatrix} a_1(f_r) \\ b_1(f_r) \\ a_2(f_r) \\ b_2(f_r) \end{pmatrix} = \int_0^{2\pi} \begin{pmatrix} \cos \theta \\ \sin \theta \\ \cos 2\theta \\ \sin 2\theta \end{pmatrix} E(f_r, \theta) d\theta / \int_0^{2\pi} E(f_r, \theta) d\theta = \begin{pmatrix} C_{uh} / \sqrt{C_{hh}(C_{uu} + C_{vv})} \\ C_{vh} / \sqrt{C_{hh}(C_{uu} + C_{vv})} \\ (C_{uu} - C_{vv}) / (C_{uu} + C_{vv}) \\ 2C_{uv} / (C_{uu} + C_{vv}) \end{pmatrix}. \quad (7)$$

We estimated the auto- and cross-spectra following Welch (1967), using Fourier transforms over time series of 5000 samples, with a 50% overlap, and using a Hann window. The resulting spectra have a frequency resolution of 0.005 Hz and 24 degrees of freedom (12 independent windows and 11 overlapped windows).

Because the GPS and accelerometer have different sampling frequencies, the buoy displacements are linearly interpolated on the accelerometer sampling time steps. This is only required for the co-spectrum of the horizontal displacements  $C_{uv}(f)$ , and quadrature-spectra of horizontal and vertical displacements  $C_{uh}(f)$ ,  $C_{vh}(f)$ .

Here we will focus on frequencies between 0.06 to 0.80 Hz for our investigation of current gradients. We will also discuss the full frequency range for a validation of the buoy behavior.

### 3 Buoy design and validation

#### 3.1 Hull shape and constraints of deployment at sea

~~We performed a first experiment in September 2014 using buoys provided by T. T. Janssen. These were early prototypes that evolved into the Spotter buoy (<https://spoondrift.co/>). They functioned very well, using GPS-derived orbital velocities giving estimates of  $E(f_r)$ ,  $\theta_2(f_r)$  and  $\sigma_2(f_r)$  up to a frequency of 0.5 Hz. These buoys had a spherical plexiglass hull and were deployed with a lead weight attached to their bottom with a rope to provide some stability. This weight introduces a mass-spring resonance at a frequency of 0.8 Hz, making the measurement of wave properties in the frequency range 0.5 to 1 Hz difficult. A similar resonance exists for the short spar SWIFT buoys, due to their shape.~~

The hull shape is clearly important when resolving short wave components. The main drivers are the stability of the buoy, we typically want to have the top of the buoy stay above ~~its bottom~~the water, in particular for GPS acquisitions and radio transmission, we also wish to avoid rotation of the buoy relative to the water around it, and finally the buoy has to be big enough to be visible for recovery and small enough to be easily handled and to follow the motion of short waves. One final driver is the overall cost of the ~~hull~~buoy. Because they also measure whitecaps with a camera and turbulence in the water, the

SWIFT buoys use a spar shape that is 1.8 m tall. Such a shape is not ideal for short wave measurements because it is resonant for heave excitation at a frequency around 0.8 Hz.

With all these constraints in mind we found that a nearly spherical shape with ribs and an additional skirt provided a good water-following behavior, whereas spherical shapes performed more poorly. Three-dimensional printing was tested without much success due to the porosity of the printed material. For the small number of buoys that we needed we finally settled on glass spheres, for which we had other oceanographic uses ~~, encased in a plastic ribbed cage for buoyancy in deep water moorings.~~ The standard ribbed cage for these spheres (figures 1) was augmented by a 3 cm wide skirt, as shown in figures 1 and 2.a, b. and 2, providing a nice water-following capability.

### 3.2 SKIB Electronics

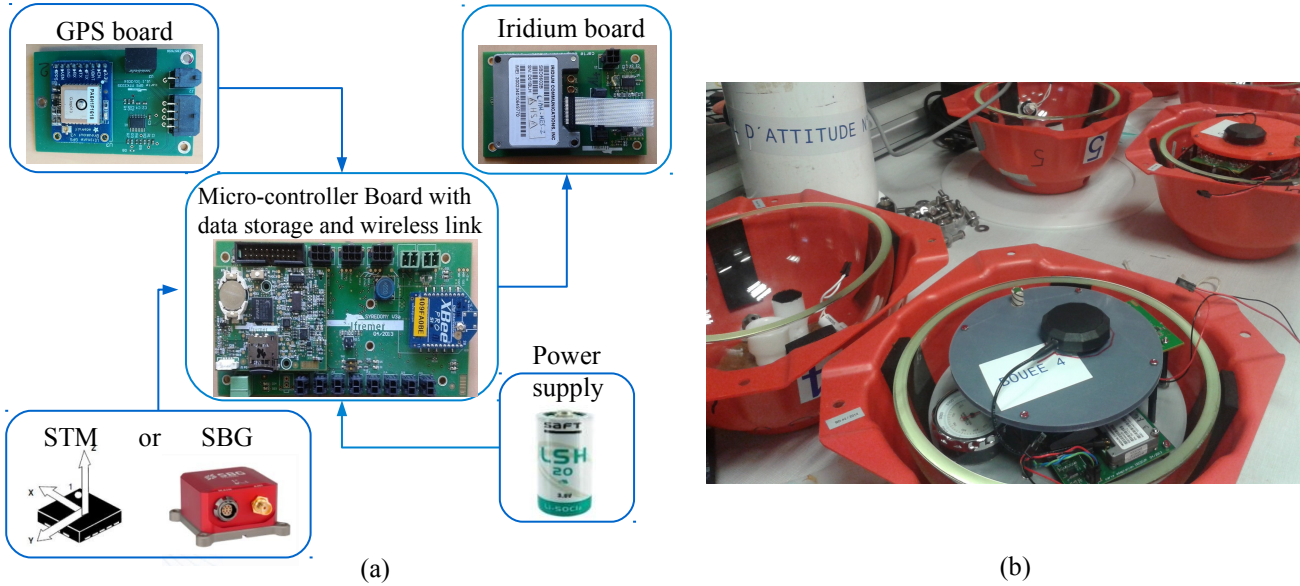
The accelerometer and the GPS system are directly integrated in a general-purpose oceanographic "Advanced Low Energy Electronic System" (ALEES) board developed by Ifremer/RDT especially for ~~applications which autonomous applications~~ that need very low power consumption. This generic board uses a 32 bits micro-controller ~~32bits EFM32 cortex M3,~~ working at 48MHz, 1Mb flash memory and 128Kb RAM. The data is stored in a ~~SDHC micro~~ standard Micro Secure Digital High Capacity (SDHC) memory card. The GPS and the accelerometer acquisitions are not synchronized and the acquisition rates are ~~1Hz and 25Hz~~ 1 Hz and 25 Hz respectively.

The integrated accelerometer is a STMicroelectronics model LIS3DH (this is the SKIB STM buoy version), already incorporated in the ALEES board for other uses, namely the detection of strong motions for under-water sensors. This low-cost (less than 2 USD) component was chosen for its very low power use, between 2 and 6  $\mu A$  at 2.5 V.

A specific board was designed to control the GPS acquisition and send the buoy position via the IRIDIUM board. We typically ~~programmed~~ programed the buoy to send position messages every 10 min, in order to be able to find the instruments at sea in highly variable currents. ~~The ALEES board and Xbee module are plugged in a SYREDOMY board for an underwater wireless pop-up system.~~ The ALEES and GPS boards can be controlled by a ~~802.15.4. Zigbee wireless link with an application layer.~~ Zigbee wireless link. This wireless link also allow the user to setup the buoy and to recover the data without opening the glass spheres, allowing to powering on and off the system.

All the system, including the electronic boards, battery pack and antennas (~~Xbee~~ Zigbee, GPS, Iridium) ~~is~~ are mounted inside a 10-inch diameter glass sphere, which is vacuum-sealed ~~. See figure 1. (see fig.1).~~ Standard prices for all the parts in the year 2015 was about 1100 euros for all electronics, half of which is for the Iridium and GPS equipment, and another 1100 euros for the hull and mounts inside of the hull. That expensive choice of the hull was, in our case, justified by a possible re-use for other oceanographic applications.

For a detailed validation we have also integrated a more accurate sensor in two of the SKIB buoys (this is the SKIB SBG buoy version). In those buoys ~~were used the IMUSBG Ellipse N, set with an Inertial Measurement Unit (IMU) SBG Ellipse~~ were used, set to an acquisition rate of 50 Hz. However, this sensor significantly increases the ~~equipments~~ equipment cost and consumption, with a unit price typically above 4000 USD.



**Figure 1.** Surface kinematic buoy (SKIB) a) main electronics components: Micro-controller board (EFM32 cortex M3), with data storage and wireless link; GPS board; Iridium board; STM accelerometer or SBG IMU Elipse N. b) SKIBs with top cover removed, showing the 10-inch diameter glass spheres used to seal all the electronic components.

### 3.3 Laboratory tests and in situ validation

Buoy testing started with verification of expected acceleration accuracy in a wave tank, followed by a comparison with in situ measurements with a reference wave buoy.

The ~~Laboratory~~ laboratory tests were very useful for testing various hull shapes, from spheres to short cylinders. These led to the addition of the plastic skirt that effectively removes rotations around the horizontal axes, with a limited impact on the water-following capacity for short wave components. This final design has a heave transfer function close to 1 up to 0.8 Hz, decreasing to 0.6 at 1 Hz, as established in wave basin tests (Thomas, 2015). This extends to high frequency the useful range of buoys such as Datawell ~~waveriders or SWIFs~~ Waveriders or SWIFs. For in situ validation, the SKIB buoy was deployed drifting within 200 m of a ~~directional~~ Mark III Datawell ~~directional~~ Directional Waverider of 70 cm diameter, moored in a region of weak currents with a mean water depth of 60 m, at 48.2857°N, and 4.9684°W. This Waverider buoy is part of the permanent CEREMA wave buoy network, with the World Meteorological Organization number 62069 (Ardhuin et al., 2012). This buoy provides measurements of the first five moments for frequencies 0.025 to 0.580 Hz, based on accelerometer data.

Contrary to Herbers et al. (2012) who strapped their new acquisition system on a Waverider buoy, we wanted to validate the full system, including the hull response. As a result the different sensors do not measure the same waves (with the same phases) but should be measuring the same sea state, i.e. the same spectrum, moments, and derived parameters.

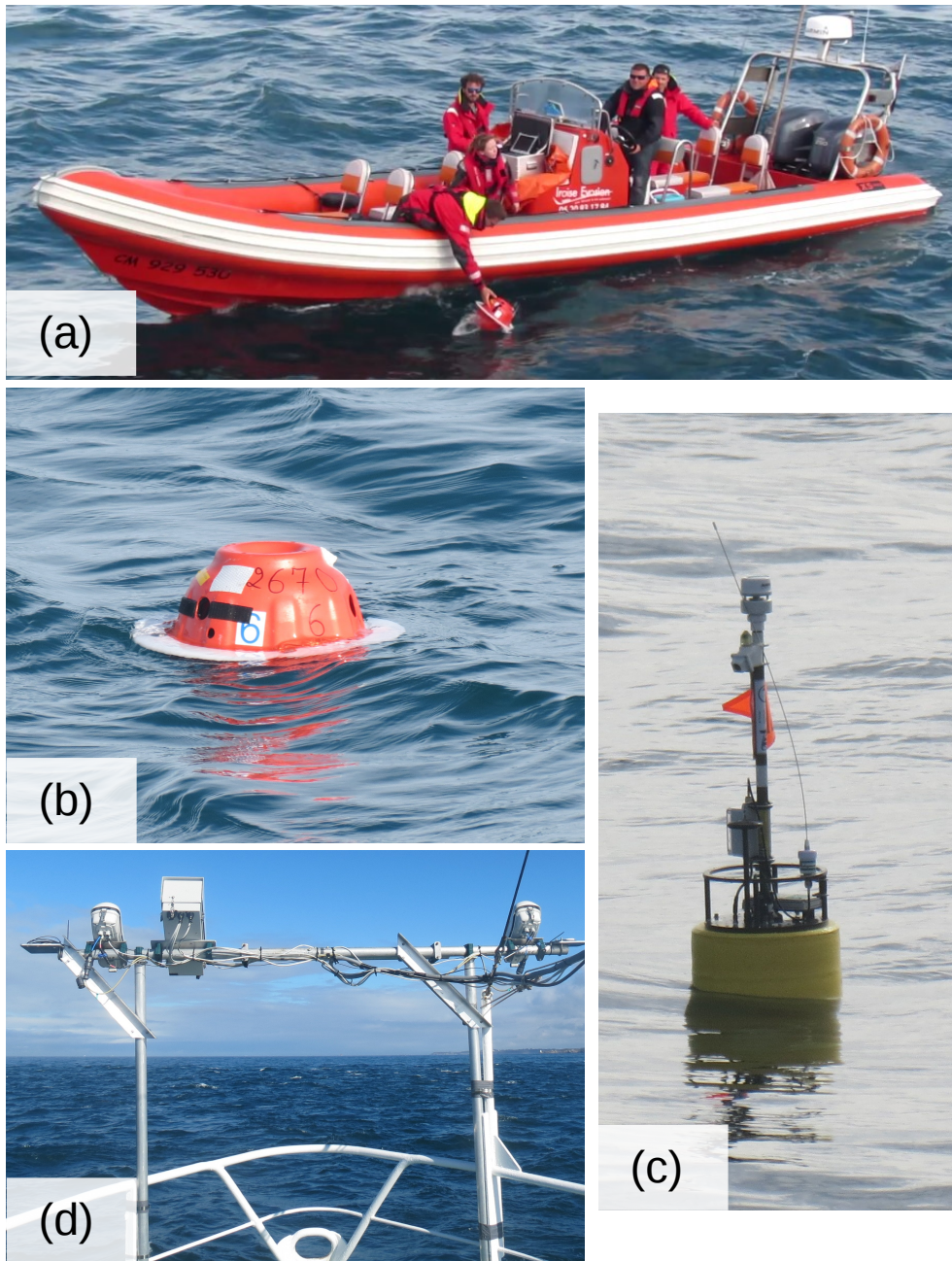
The test presented here was performed on 21 September 2016, from 10:44 to 11:56 UTC, following a similar test in 2015 with only a SKIB and a with a different GPS receiver but the same hull, and a Datawell [Waverider](#). The results were very similar. In the 2016 experiment, we also deployed a SWIFT buoy (Thomson, 2012) and a ship-mounted stereo video wave system (Benetazzo et al., 2016). Pictures of all these systems are shown in figure 2, as used during the experiment.

The SWIFT model used is shown in the water in figure 2.c. It uses a GPS receiver integrated with an IMU (Microstrain 3DM-GX3-35), a Doppler velocity profiler (Nortek AquadoppHR), an autonomous meteorological station ultrasonic anemometer (AirMar PB200), a digital video recorder system, and real time tracked radio frequency transmitter. The wave spectra for each 10-min burst are calculated as the ensemble average of the fast Fourier transform of 16 subwindows with 50% overlap, which results in 32 degrees of freedom and a frequency bandwidth  $df = 0.0117$  Hz in the range  $0.05 < f < 0.5$ . The IMU data gives information ~~of~~ [about](#) the tilt and horizontal rotation, as well as accelerations, of the SWIFT as it follows wave motions. Note that the hull shape of the SWIFT follows displacements and velocities at the sea surface, but not surface slopes. Hence, only velocities and accelerations are used in wave processing. Post-processing of the merged GPS and IMU data applies as classic RC filter to exclude signals at frequencies lower than  $f < 0.04$  Hz.

The stereo video system is the same as used by Leckler et al. (2015), based on a pair of synchronized video cameras ( $2048 \times 2456$  pixels) BM-500GE JAI, mounted with wide angle lenses. ~~However, here~~ [Here](#) the system was installed at the bow of R/V Thalia, a 24.5 m ship of the French coastal oceanographic fleet ([fig.2.d](#)). The cameras are located approximately 7 m above the sea level([fig.2.d](#)), and an Ellipse-D Inertial Measurement Unit is fixed on the bar joining the cameras to correct for ship motion with  $0.2^\circ$  accuracy on all rotation angles. The video processing follows ~~the methods of Benetazzo (2006), Leckler (2013) and Benetazzo et al. (2016).~~ ~~However, instead of use~~ [Benetazzo et al. \(2016\)](#) . ~~The only difference in the present case is that the mean surface plane correction, like in these earlier papers, here which was used for deployment from fixed platforms, is replaced by an optimization of the~~ the rotation matrix ~~is optimized by the quaternions of IMU data and translation obtained by the IMU and GPS data, given by of SBG motion package mounted with the cameras.~~ The resulting surface elevation  $\zeta(x, y, t)$  ~~maps~~ [maps](#)  $\zeta(x, y, t)$  acquired over 30 minute records at 12 Hz are gridded in a 10 by 10 m square surface with 0.1 m resolution. This square is moving with the mean velocity  $U_m$ , relative to the solid Earth, as given by the GPS data. The 3D spectrum  $E(k_x, k_y, f)$  ~~were obtain~~ [was obtained](#) after applying a Hann window in all three dimensions to the elevation maps over time intervals of 85.33 seconds (1024 frames), with 50% overlapping as well. As result, the energy over frequency and wavenumber are in a reference frame moving at the speed  $U_m$ , and the measured radian frequency of the waves  $\sigma_m$  must be corrected by the mean ship velocity ( $U_m$ ) over each time window. So the absolute frequency in an Earth reference frame is  $\omega = \sigma_m - \mathbf{k} \cdot \mathbf{U}_m$ . This procedure is particularly prone to errors for wave components longer than 20 m, that are not resolved in the field of view. These longer components can be treated separately using a slope array estimation of the directional spectrum (e.g. Leckler et al., 2015), but we focus here on the short waves. The stereo heave frequency spectrum  $E(f)$  is obtained by integration over wavenumbers and it is expressed in terms of the absolute frequency  $f_a$ , with  $\omega = 2\pi f_a = \sigma - \mathbf{k} \cdot \mathbf{U}$   [\$\omega = 2\pi f\_a = \sigma + \mathbf{k} \cdot \mathbf{U}\$](#) , where  $\mathbf{U}$  is ~~an unknown current field~~ [a current field that can be estimated using the drifting buoys](#).

A comparison of the different sensors at the same sea state conditions is shown at figure 3. For this comparison the records from each sensor have been synchronized over 10 minute intervals, and averaged over the 30 minutes of the Waverider records





**Figure 2.** Sensors using during ~~BBWAVES-campaign~~-oceanographic campaigns for in situ validation. a) SKIB deployment; b) SKIB buoy; c) SWIFT buoy; d) Stereo video system

and ~~a~~an integration interval from 0.06 to 0.58 Hz. Figure 3.a shows the buoys drift trajectories for the 1 hour of the acquisition, with one color symbol every 10 minute and the track of R/V Thalia. The stereo-video record is 20 minutes, starting at the same time as SKIB and SWIFT acquisitions. The Waverider data correspond to two acquisition of 28 ~~minute~~minutes each, ending at 10:30 and 11:00 UTC.

A closer look at the heave spectra (fig.3.b) shows a good correspondence ~~by-between Datawell~~between Datawell Waverider and SKIB buoys at the peak of the spectrum. The main source of error in the SWIFT data, around the peak of the spectrum, was associated ~~to~~with a high-pass filter applied to the IMU acceleration before each time integration. This part of the SWIFT processing, to obtain  $E(f)$ , were optimized by Thomson et al. (2016) to reduce the low frequency noise and to have best agreement with a Datawell ~~waverider~~Waverider at Ocean Station Papa. This was obtained from the double time-integration of the IMU acceleration, with a high-pass filter at each integration, to reconstruct a wave-resolved time series of sea surface elevations. This generally improves the estimation of the spectrum for  $f > 0.1$  Hz, but it reduces the level of lower frequencies (as it is also observed on fig.3.b).

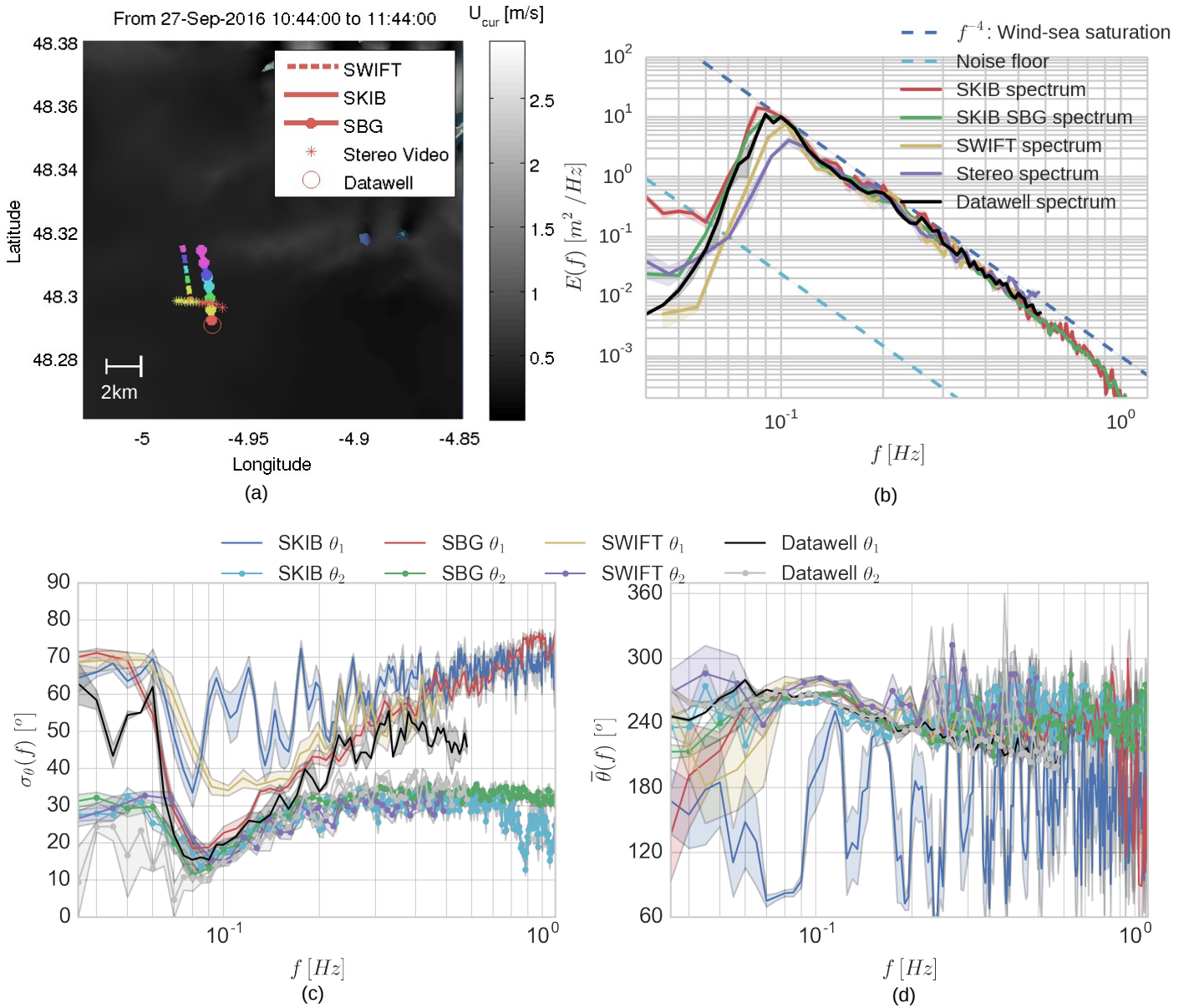
For the SKIBs we have not filtered the acceleration data and the  $E(f)$  was directly obtained ~~form the twice in the time domain~~integration from the double time-integration of the accelerometer data. Other differences are found for the main direction (fig.3.d), that is better retrieved with the SBG IMU. The main benefit of the SBG IMU is the reduction of the noise floor at low frequencies compared to an estimation of the motion from GPS alone. This is most important for swells of long periods and low heights, but not critical for our investigation of wind-seas interacting with currents.

Figure 3.c and 3.d present the estimates of  $\sigma_\theta$  and  $\bar{\theta}$  based on the first and second-order angular moments. We see a significant difference in the wave spread and mean direction estimates, especially in the first-order estimation ( $\sigma_{\theta_1}$  and  $\bar{\theta}_1$ ). This occurs because the accelerometer is not internally synchronized with the GPS and because they have different characteristics errors. The second-order moment depends only ~~of~~on the horizontal displacements while the first-order moments depends of both horizontal and vertical displacements. So, the second-order moments are more accurate, because there is no cross products between different sensors. Although there are differences, the results suggest that the usage of the combination of GPS drifter displacement and vertical acceleration produces a good estimation of the spectrum directionality. These results are particularly important, as the drifter was not equipped with a compass and only used a low-cost GPS receiver. Because the GPS acquisition were limited to 1 Hz in the SKIB with STM accelerometer, the directional analysis are limited to 0.5 Hz (and 0.8 Hz for SBG which uses only accelerometer data).

A comparison of the different sensors in terms of usual sea state parameters is shown in table 1, with the significant wave height  $H_s$ , mean wave period  $T_{m0,1}$  and peak wave period  $T_p$ . Since the only reliable directions are provided by the GPS data alone, we define the peak wave direction  $D_p$  and the ~~peak wave direction~~mean wave direction ( $\theta_{m,2}$ ) from the second moments as  $\theta_{m,2} = 0.5 \tan^{-1}(B_2/A_2)$  with

$$A_2 = \int E(f) a_2(f) df \quad (8)$$

$$B_2 = \int E(f) b_2(f) df \quad (9)$$



**Figure 3.** Comparison of wave spectra estimates from SKIB, SWIFT, Datawell and Stereo video. (a) Wave sensors path, the colors represent 10-min displacement, starting in read (b)  $E(f)$  Sea surface variance spectral density; (c)  $\sigma_\theta(f)$  Directional spreading from first and second-order directional-angular moments ( $\theta_1$  and  $\theta_2$ ); (d)  $\bar{\theta}(f)$  frequency-dependent mean wave direction from first and second-order directional-angular moments ( $\theta_1$  and  $\theta_2$ ). The shadow in the lines represent the error for a 95% confidence interval.

As reported in table 1, SKIB results generally agree on  $H_s$ ,  $T_{m01}$  and mean directions, with confidence intervals for  $H_s$  overlapping with the reference Waverider buoy.

**Table 1.** Comparison of wave parameters, significant waves ~~hight~~-height ( $H_s$ ), mean absolute wave period ( $T_{m01}$ ) and mean wave direction ( $\theta_{m,2}$ ). The root mean square difference between Waverider and other sensors is given in a second column for each variable. The  $[H_s^-, H_s^+]$  represents the maximum and minimum limits for 95%  $H_s$  confidence interval, considering a chi square distribution (according Young, 1995, eq.5 and 6), for two perfect devices measuring the same random wave field.

Sensor	$H_s$ [m]	$[H_s^-, H_s^+]$	$RMSD$	$T_{m01}$ [s]	$RMSD$	$\theta_{m,2}$ [°]	$RMSD$	$\nu$
Datawell Mark III	2.55	[2.31,2.64]	–	10.49	–	238.1	–	193.4
SKIB STM	2.86	[2.63,2.94]	0.36	10.85	0.91	245.4	8.3	289.9
SKIB SBG	2.55	[2.29,2.65]	0.15	10.52	0.44	231.0	7.3	169.3
SWIFT	2.08	[1.88,2.16]	0.48	9.98	0.89	263.1	25.3	193.4
Stereo video	1.89	[1.73,1.94]	0.63	9.40	0.54	249.6	8.2	253.9

The ~~Largest-largest~~ differences are between the SKIB STM and SWIFT buoys and are ~~associated~~~~associated~~-associated with the filtering of low frequency content in the SWIFT processing chain (fig.3.b), and unfiltered low frequency noise in the SKIB STM. However, for frequencies from 0.1 to 0.5 Hz, the spectra are consistent with the stereo-video and Datawell Waverider data. At higher frequencies, for which we do not have other validation data, the power spectra result follows the same trend and appears realistic up to at least 0.8 Hz, consistent with laboratory tests (Thomas, 2015).

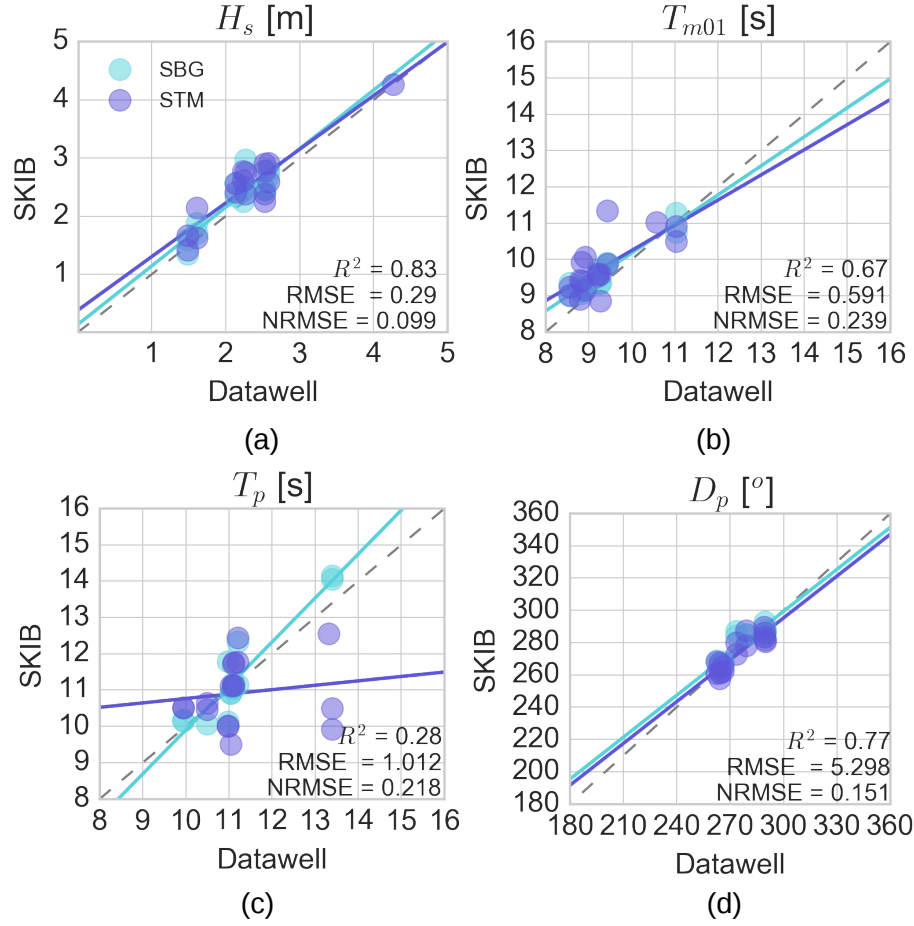
In order to validate the SKIB buoys in different sea state conditions, others deployments were performed next to the buoy 62069, one at August 05, 2015 and ~~other-another~~ four between September 21 and 27 of 2016. For the 2016 experiment, we used two SKIB buoys equipped with SBG IMU and two others with the STM accelerometer. For the 2015 experiment we have only one buoy equipped with the STM accelerometer. Results for integral parameters are presented in figure 4, and a selection of two spectra with different shapes is shown in figure 5.

For most sea states  $H_s$  and  $D_p$  are measured correctly (~~Figfig~~.4.a and d), with ~~RMSD-RMSE~~ around 0.3 m and  $5.3^\circ$  respectively. As expected, the SKIB-SBG agrees best with the Waverider for all the analyzed parameters, and the regression lines for the SBG data (fig.4) are closer to the ideal correlation line (gray dash lines fig.4) than those from the SKIB STM data. In general, the STM accelerometer has more energy at the lower frequencies and this can produce overestimations ~~on-in~~  $H_s$  and  $T_{m01}$  measurements. These errors are confined to frequencies below 0.12 Hz. The main difference between the SKIB and Datawell Waverider was found at the peak wave period ( $T_p$ , ~~Figfig~~.4.c). Higher errors in the identification of the peak frequency are expected a priori as the buoys present different spectral resolutions and different numbers of degrees of freedom (Young, 1995). Again the SKIB-SBG performs better than SKIB-STM.

The ~~buoys-buoy's~~ low frequency noise varies ~~at-according to the~~ each sea state conditions. The ~~error-associated-to-errors~~ associated with the low frequency limit and at the spectrum peak are illustrated in figure 5.

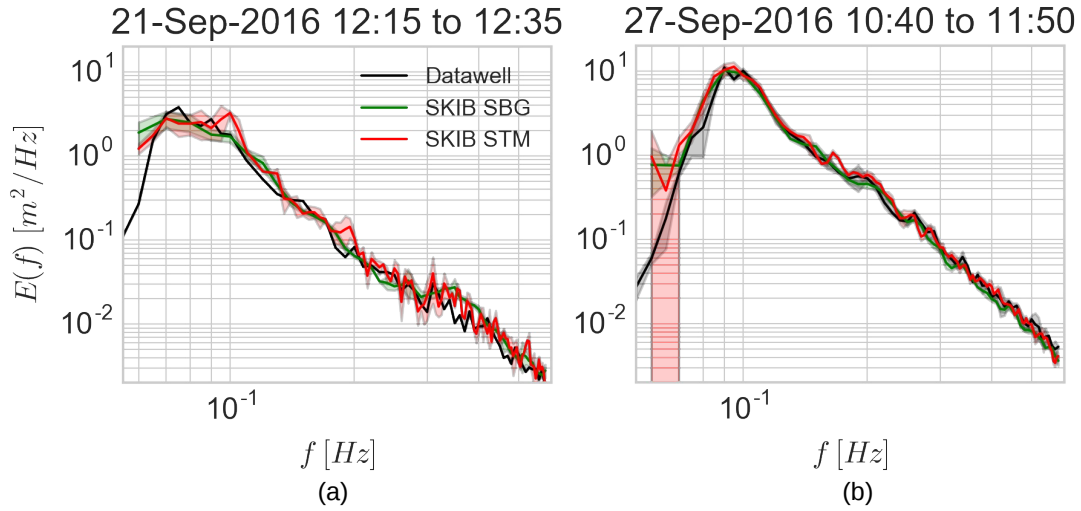
In most sea states analyzed here, the SKIB buoy ~~measured-measured-correctly-correctly~~ measured the sea state condition at frequencies higher than 0.07 Hz. In terms of  $H_s$ , the instrument usually presents a root mean square error within the statistical uncertainty expected for two perfect devices measuring the same random wave field (Young, 1995, eq. 6). However, because of





**Figure 4.** Comparison of the integrated wave parameters estimates from Datawell and SKIB with SBG (IMU sensor) and STM (accelerometer). (a) Significant wave height ( $H_s$ ) (b) Mean waves period ( $T_{m01}$ ) (c) Peak waves period ( $T_p$ ) and (d) Peak direction ( $D_p$ ) for a frequency interval between 0.06 to 0.6 Hz. The regression lines are computed independently for SBG and STM data set. The gray dash line represent the ideal correlation regression line and the statistics coefficient wrote in the figures are computed considered booth data sets, SBG and STM.

a significant low frequency noise in SKIM-STM we reduced the integration interval for this buoy. The low frequency noise was reduced by using the SBG IMU, that presented the best performance among the sensors tested here. In summary, we had a good performance of SKIB for  $f > 0.07$  Hz, that makes it appropriate to use in the investigation of young wind-waves interacting with currents.



**Figure 5.** Comparison of Datawell and SKIB with SBG and STM for the sea surface variance spectral density  $E(f)$  for two different field measurements around the Datawell [Waverider](#) buoy "Pierres Noires" (with World Meteorological Organization number 62069). [The statistical parameters are the Pearson's coefficient of determination  \$R^2\$ , the root mean square error \(RMSE\) and the normalized root mean square error \(NRMSE\)](#)

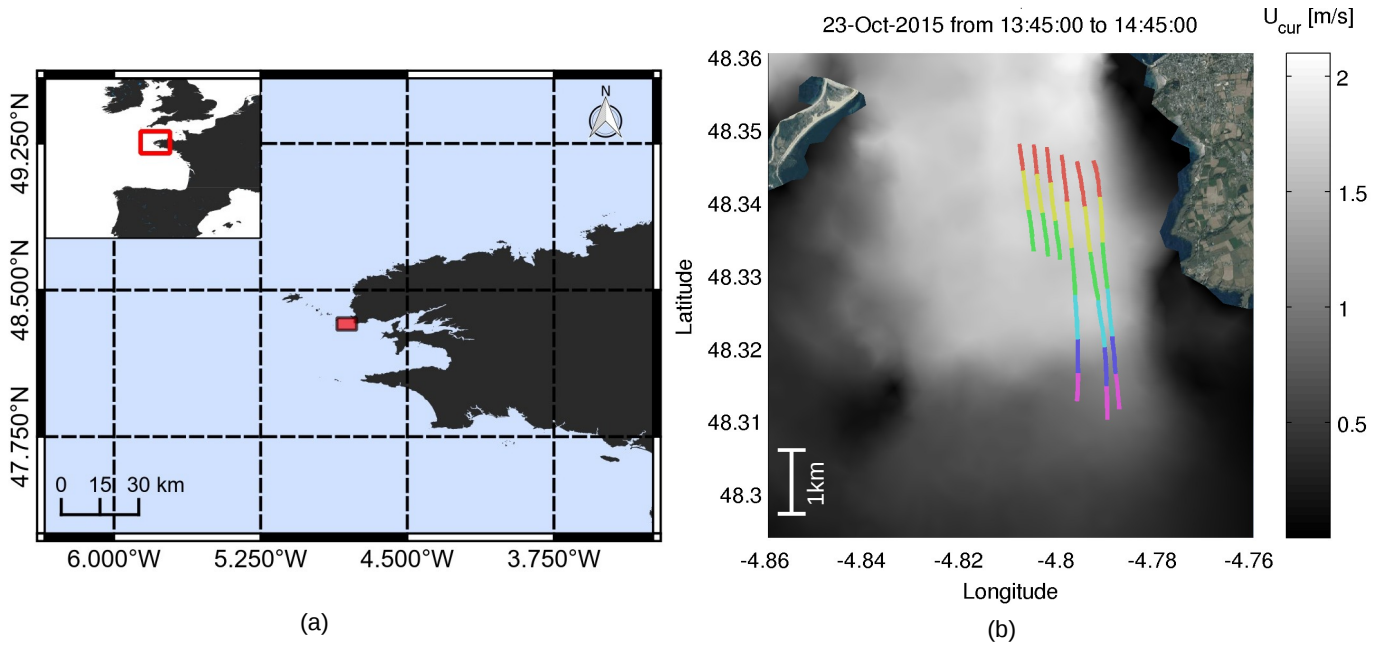
#### 4 Wave evolution in current gradients

Wave properties are largely defined by the wind field and the geometry of the basin in which they develop, but currents can introduce large variations, particularly at small scales (e.g. Phillips, 1984; Masson, 1996; Ardhuin et al., 2017). Current effects are generally strongest for the shortest wave components due to a larger ratio of current speed to phase speed, and can enhance the probability of wave breaking (e.g. Chawla and Kirby, 2002; Zippel and Thomson, 2017).

Here we illustrate the capabilities of SKIB drifters with a deployment through a current gradient that opposes the waves, following the method of Pearman et al. (2014). We deployed buoys in the current upstream of a large gradient area and recorded the evolution of the wave field as the buoys drifted across the current gradient .

The selected area for this study is at the southern end of the Chenal du Four, a passage oriented north-south surrounded by shallow rocks, with Beniguet island to the west, and the mainland to the east (see [Figfig.6](#)). The water depth in this region ranges from 10 to 13 m relative to chart datum, and increases to 25 m at the southern end near latitude  $48.32^\circ$  N. At the time of our measurements, the water depth was the depth relative to chart datum plus 6 m. The tidal flow in this area is stronger in the shallower part of the channel, resulting in a current gradient at the channel mouth that often enhances wave breaking and can lead to hazardous navigation conditions.

On October, 23 from 13:40 to 14:40 UTC of 2015, six drifters buoys were deployed from a small boat (see [Figfig.2a](#)).



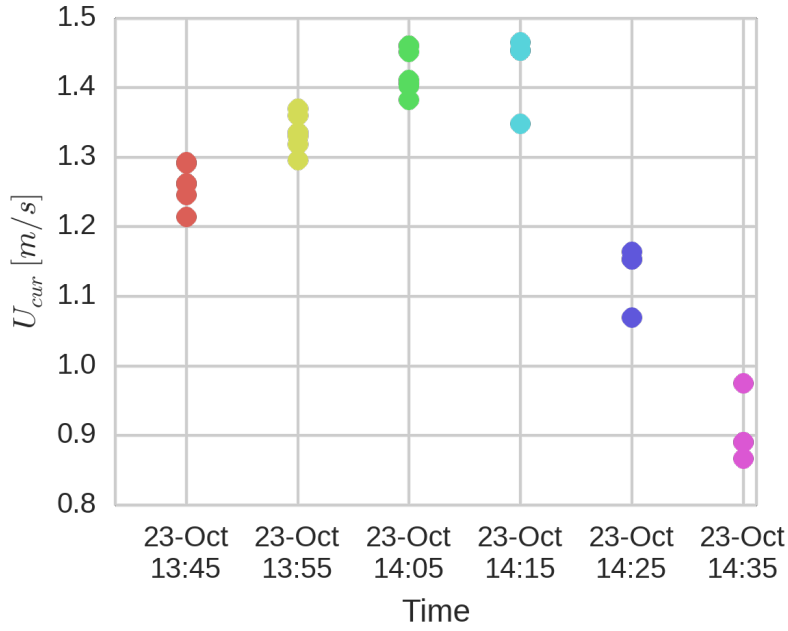
**Figure 6.** Study field location and local experimental conditions a) Chenal du Four ~~channel~~-location b) Local current condition and drifters path. The current field shown here comes from a barotropic model simulation at 250 m resolution (Lazure and Dumas, 2008; Pineau-Guillou, 2013). Colored lines shows the 10-min SKIB displacement over current gradient at 23-October-2015 14:40 UTC.

Winds were approximately 6.2 m/s from the south, blowing against a tidal current of approximately 1.4 m/s (see [Fig.8fig.7](#)). The offshore wave conditions, as recorded by the Waverider buoy, included a 0.9 m swell with a peak period of 13 s coming from the 280°, and a 1.2 m wind-sea. The location of our measurements is well sheltered from the ~~the~~-swell, and swell heights increase as the buoys drift away from Chanel du Four. Figure 7 presents the mean current velocity estimated from the successive GPS positions, for all buoys and each of the 10-minute records over which wave spectra are estimated. After increasing from 1.3 to 1.4 m/s, the current drops to 0.9 m/s over the deeper region. As the waves travel against the current, they first experience the increase in the adverse current from 0.9 to 1.4 m/s.

The corresponding wave spectra are shown in figure 8. There is little variation of the mean direction and directional spread (not shown).

The increase of energy at low frequencies ~~are mostly due by~~ is mostly due to the buoys drifting to more exposed areas in the presence of a swell. The effect of the current on the shape of the wind-waves is analyzed using the non-dimensional saturation spectrum  $B$ , following Phillips (1984). With a velocity increase  $\Delta_{U,1} = 0.6\text{m/s}$  over a 1 km scale we measure an increase of the saturation level at frequencies from 0.35 to 0.5 Hz that does not exceed 50%. The following reduction in wave energy is more pronounced over the 3 km where the current slows down.

Figure 9 shows that the saturation level increases when waves face an accelerating and opposing current. This is similar to the cases studied in Zippel and Thomson (2017), from the Columbia River, in which opposing currents increase the steepness



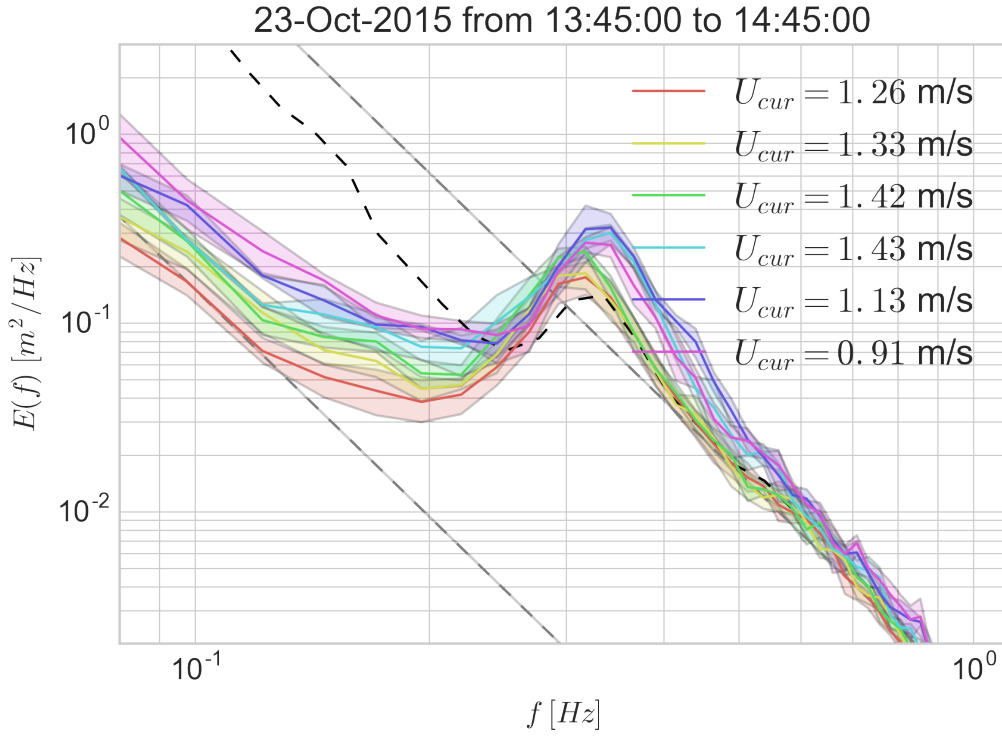
**Figure 7.** Evolution of the current speed during the drift of the buoys. For each time segment, each dot represents a single buoy.

locally (without gradient analysis). In the final portion of the trajectories, the current speed decreases and the saturation relaxes to a lower value.

Given the complex interaction of wave generation by the wind, wave dissipation by breaking and non-linear evolution, there are no simple theoretical results to interpret our observations. Starting from a dynamical balance in the absence of currents, Phillips (1984) provides an analysis of the current effect as a deviation of the wave spectrum from a near-equilibrium state. ~~Assuming~~, assuming that the wind forcing is proportional to  $B$  and a dissipation rate that is proportional to  $B^n$  with  $n \simeq 3$ . For a scale of current variation  $L$ , he finds that the maximum value of  $B$  is

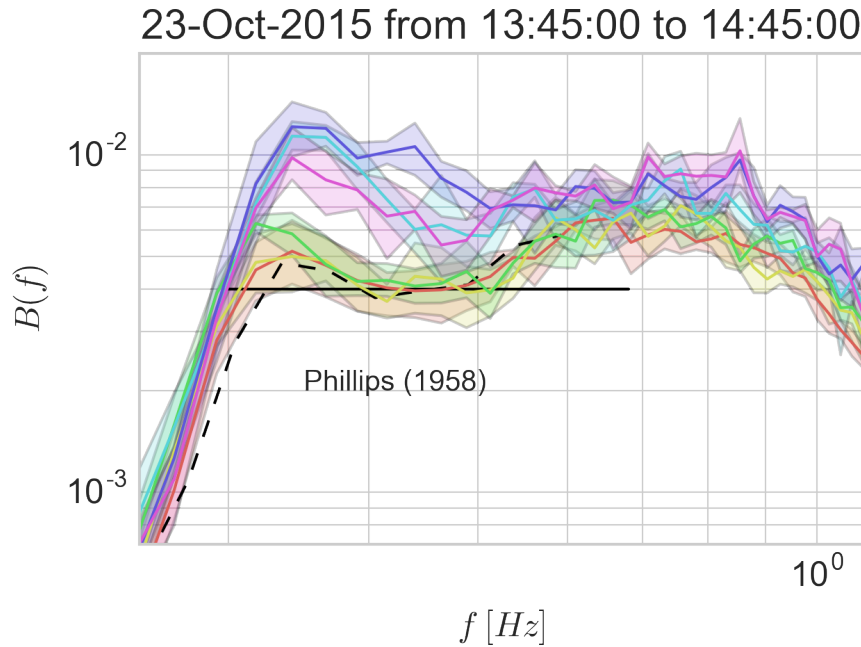
$$B_{\max} = B_0 [1 + 18\Delta_U / (cS)]^{1/(n-1)} \quad (10)$$

where  $B_0$  is the equilibrium level of the saturation outside of the current gradient. In this expression  $c$  is the phase speed and  $S$  is scale of current variation normalized by the wind stress  $L/(2\pi)C_d U_{10}^2/g \simeq 1$ . For a relative frequency  $f_r = 0.4$  Hz,  $S = Lk^2/(2\pi)C_d U_{10}^2/g$ . In our case, taking  $L = 1.5$  km gives  $S = 0.93$  for  $f_r = 0.5$  Hz. With the same parameters,  $\Delta_U = 0.4$  m/s and  $n = 3$  and  $L = 1$  km giving  $S = 1$ , this gives  $B_{\max} = 1.5B_0$  in eq. (10) gives  $B_{\max} = 1.8B_0$ . If  $n$  is reduced to 2,  $B_{\max}/B_0$  is as large as 2.434, and diverges as  $n$  goes to 1. In other words, the dissipation rate must be a very steep function of  $B$  in order to absorb the wind forcing energy that converges into the small region of the current gradient. The limited increase in  $B$  in our data supports  $n > 2$ . With  $n=3$ , eq. (10) gives a reduction in  $B_{\max}/B_0$  from 1.8 at 0.5 Hz to 1.25 at 0.8 Hz, that is consistent with the weaker ratio found for the higher frequencies in figure 9.



**Figure 8.** Variance spectral density evolution on time, 10 min Fourier transform from 23-October-2015 13:40 to 14:40 UTC. The gray dash lines shows the wind-sea saturation  $f^{-4}$  and noise floor at  $E(f)f^4$  limits for the first 10 minutes of acquisition. The ~~colors~~color of the lines follow the buoys displacement as on figure 6. The solid lines shows the spatial mean of the spectral density measured in  $f_r$  during each 10 minutes acquisition. The lines shadow represent 99% confidence interval. The dash dark line is the spectral density measured by Pierre Noires Datawell Waverider buoy at a near offshore location, outside the current region.

For example, a current speed of 1.6 m/s corresponds to blocking conditions for waves with periods shorter than 2 s, that have a group speed slower than 1.6 m/s, and these short waves should be strongly attenuated in a fixed reference frame. However, our measurements are in a reference frame moving with the current, in which the waves, even those with periods shorter than 2 s, are propagating past the drifting buoys. At frequencies above 0.5 Hz, the intrinsic group speed is less than 1.6 m/s and waves must be generated by the local wind and cannot propagate from the south. Our data is consistent with  $n = 3$ , as used in Banner et al. (2000); Ardhuin et al. (2010). For  $f_r = 0.6$  Hz,  $n = 3$  gives  $B_{\max} = 2.26B_0$ .



**Figure 9.** Saturation of the spectral density, time evolution over 10 min Fourier transform from 23-October-2015 13:40 to 14:40 UTC. The colors lines follow the buoys displacement as on figure 8. The solid lines shows the spatial mean of the spectral density measured during each 10 minutes acquisition. The lines shadow represent 99% confidence interval. The dashed black line is the saturation measured at an offshore location by the "Pierre Noires" Datawell buoy.

## 5 Summary and conclusion

The ~~Surface Kinematics Buoy~~ "surface kinematics buoy" (SKIB) is a new ~~low-cost~~ drifter that has been designed for the investigation of wave-current interactions, including relatively short waves from 0.07 Hz and up to 1 Hz in frequency. Here we mostly used the heave data from the accelerometer that was first validated by comparing to reference Datawell ~~waverider~~ Waverider buoy up to 0.6 Hz. ~~The shorter wave components were validated with stereo-video imagery~~ Typical costs for the electronics are around 1100 euros, with an additional 1100 euros for the hull, which could be reduced by using plastics instead of our glass sphere. The combined analysis with the vertical acceleration and buoy velocity from GPS the instrument allowed to measure the directional properties of the waves spectrum without using an internal compass, simplifying the equipment design and reducing the costs. Still, the combination of the GPS velocity and accelerometer posed particular problems, and only the parameters  $\theta_2$  and  $\sigma_2$  obtained from the GPS velocity appear reliable.

For cases in which the steepness of the waves of interest is very small, we have replaced the cheap STM accelerometer by a SBG Ellipse-N inertial navigation unit. This SKIM-SGB model performs better, both for the heave spectrum and for the

directional parameters derived from first moments,  $\theta_1$  and  $\sigma_1$ . This model was used by Sutherland and Dumont (2018) for the investigation of wave propagation in in sea ice.

The capabilities of the new ~~drifter were illustrated~~ drifters were illustrated here by measuring the variation of wave properties across a current gradient that was relatively uniform and along the propagation direction. Such measurements are important for testing existing theories for wave dissipation, such as proposed by Phillips (1984) and now widely used in numerical wave models (e.g. Ardhuin et al., 2010). In particular, the frequency-dependent saturation level is found to respond to current gradients in a way that is consistent with the proposition by Phillips (1984) of a nonlinear dissipation rate. We expect further applications to the investigation of small scale gradients in wave heights and mean square slopes in the presence of current gradients.

*Competing interests.* no competing interests are present

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