Dear Editor:

Thank you very much for providing the opportunity for us to revise our paper.

Thank you very much for your contributions to this paper. And we are all extremely grateful for having a chance to make further improvements. The major and minor suggestions of reviewer2# are very helpful for us. Reading and considering all comments of reviewer2# carefully, we have made some revisions on our paper.

Finally, we write the point-by-point response to answer the reviewer2#'s questions for better communication. If there are still any problems on the method, diction, phrasing, grammar, and spelling, please do not hesitate to tell us and we'll try our best to improve them.

Thank you again for your comments to improve our paper. Wish your journal better and better.

Yours,

Mei Hong

2018-03-18

带格式的：左侧： 3.17 厘米，右侧： 3.17 厘米，指定行和字符网格

Responses to reviewer#2:

All the authors are extremely grateful to you for providing your excellent comments and valuable advices for this paper. Your six major suggestions are very helpful for us. Based on your suggestions, we have made some revisions on our paper. We have streamlined the discussion and explained Why p value was in the range 5 to 15 based on your specific comments.

Thank you again for your valuable comments to improve our submission. If there are still any problems on the method, diction, phrasing, grammar, and spelling, please do not hesitate to tell us and we'll try our best to improve them.

In the following, kind comments you suggested before are in black text with corresponding actions taken by us following in blue.

Major comments:

1. Line633-663: I think there is no need to spend space here to introduce the definition of overfitting and you just have to give a reference. The discussion whether the model is overfitting or not is redundant and the discussion should focus on the good forecast results of new examples. This part of the discussion can be properly streamlined.

Responses：Good suggestions. In the previous paper, the discussion whether the model is overfitting or not is redundant and now the discussion have focused on the

good forecast results of new examples. We have deleted some redundant statements to make this part of the discussion can be concise.

The specific revision can be seen from line632 to line647 in page30-31.

We sincerely hope for your satisfaction with our revision. Thank you again for your kind suggestion.

2. Line371: Why p value was in the range 5 to 15? Is this the experience of the predecessors? Or is it the result of the author's own experiment?

Responses：Good suggestions. In the reference (Cao, 1993), if the system forgets slowly, parameters and will be small and the value should be high. And he made a lot of experiments to prove that the p value was in the range 5 to 15 to this system. So the conclusion of p value was in the range 5 to 15 is based on the experience of the predecessors (Cao, 1993). Now we added the explanation of why p value was in the range 5 to 15 for readers' better understanding.

The specific revision can be seen from line370 in page18.

We sincerely hope for your satisfaction with our revision. Thank you again for your kind suggestion.

3. Line597-615：The purpose of this section is to show that a certain impact on the pattern of the 2nd EOF will not make our forecast unstable. But this section here occupied the space too much and I think there is no need to make a list of table5 alone. The author just says the difference among forecast results of both TC and

MAPE of five different sample data are less. Because the main purpose of this paper is to prove that the prediction accuracy of SST and ENSO of the model. Therefore, it is not necessary for table5 to list separately. It is recommended that this part should be simplified.

Responses： Good suggestions. Based on your suggestion, we have deleted the table5 and make the discussion concise. This part had be simplified.

The specific revision can be seen from line596-609 in page29.

We sincerely hope for your satisfaction with our revision. Thank you again for your kind suggestion.

4. Line243-249: The author introduced the standardization of the data before modelling and it is too wordy here. The author just list the standardized formula here. So the section should be suggested to be simplified.

Responses： Good suggestions. Now we have just listed the standardized formula and deleted the redundant statements. So now the section has been simplified.

The specific revision can be seen from line240-246 in page11-12.

We sincerely hope for your satisfaction with our revision. Thank you again for your kind suggestion.

5. Line269 and 298: The abbreviation appears for the first time, and there is no need to repeat the Pearson correlation coefficient (CC).

Responses：Good suggestions. Now we have revised the Pearson correlation coefficient (CC) as CC and the mean absolute percentage error (MAPE) as MAPE in line294 on page14.

We sincerely hope for your satisfaction with our revision. Thank you again for your kind suggestion.

6. Dynamic model recommendations are consistent, the topic is dynamical-st, followed by several dynamic text in a number of tense inconsistency, it is recommended to be consistent.

Responses：Good suggestions. Now we have revised all the “dynamic” as the “dynamical” for the consistency.

The specific revision can be seen in the whole paper.

We sincerely hope for your satisfaction with our revision. Thank you again for your kind suggestion.

Minor comments:

1. Line649: “the forecast results of the Cross-validated” should be revised as” the forecast results of the cross-validated”.

Responses：Good suggestions. Now we have revised “the forecast results of the Cross-validated” as “ the forecast results of the cross-validated” in line631 in page30.

We sincerely hope for your satisfaction with our revision. Thank you again for your kind suggestion.

2. Line 30, “dynamical reconstruction” is more appropriate

Responses： Good suggestions. Now we have revised as “dynamical reconstruction” in line30 on page2.

We sincerely hope for your satisfaction with our revision. Thank you again for your kind suggestion.

3. Line 35, ”pearson” should be ‘’Pearson”

Responses：Good suggestions. Now we have revised “pearson” as “Pearson” in line35 on page2.

We sincerely hope for your satisfaction with our revision. Thank you again for your kind suggestion.

4. Line 36, “approximately” should be ‘’approximate” or “about”

Responses：Good suggestions. Now we have revised “approximately” as “approximate” in line36 on page2.

We sincerely hope for your satisfaction with our revision. Thank you again for your kind suggestion.

5. Line 38,”but” should be “but also”

Responses：Good suggestions. Now we have revised “but” as “but also” in

line38 on page2.

We sincerely hope for your satisfaction with our revision. Thank you again for your kind suggestion.

6. Line 52,"influences" should be "influence"

Responses： Good suggestions. Now we have revised "influences" as "influence" in line51 on page3.

We sincerely hope for your satisfaction with our revision. Thank you again for your kind suggestion.

7. Line 57,"gradually improved" should be "gradual improvement"

Responses：Good suggestions. Now we have revised "gradually improved" as "gradual improvement" in line56 on page3.

We sincerely hope for your satisfaction with our revision. Thank you again for your kind suggestion.

8. Line 67,"large a amount of" should be " a large amount of "

Responses：Good suggestions. Now we have revised "large a amount of" as "a large amount of" in line66 on page3.

We sincerely hope for your satisfaction with our revision. Thank you again for your kind suggestion.

9. Line 75,"advanced" should be " been advanced "

Responses：Good suggestions. Now we have revised“advanced” as “been advanced” in line74 on page4.

We sincerely hope for your satisfaction with our revision. Thank you again for your kind suggestion.

10. Line 91,”This is because” should be “It is because that”

Responses：Good suggestions. Now we have revised“This is because” as “It is because that” in line90 on page4.

We sincerely hope for your satisfaction with our revision. Thank you again for your kind suggestion.

The following is the a marked-up manuscript version:

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Forecasting experiments of a dynamical-statistical model of the sea surface temperature anomaly field based on the improved self-memorization principle

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Abstract: With the objective of tackling the problem of inaccurate long-term El Niño Southern Oscillation (ENSO) forecasts, this paper develops a new dynamical-statistical forecast model of sea surface temperature anomaly (SSTA) field. To avoid single initial prediction values, a self-memorization principle is introduced to improve the ~~dynamic~~dynamical reconstruction model, thus making the model more appropriate for describing such chaotic systems as ENSO events. The improved dynamical-statistical model of the SSTA field is used to predict SSTA in the equatorial eastern Pacific and during El Niño and La Niña events. The long-term step-by-step forecast results and cross-validated retroactive hindcast results of time series T_1 and T_2 are found to be satisfactory, with a ~~pearson~~ Pearson correlation coefficient of approximate~~ly~~ 0.80 and a mean absolute percentage error (MAPE) of less than 15%. The corresponding forecast SSTA field is accurate in that not only is the forecast shape similar to the actual field, but also the contour lines are essentially the same. This model can also be used to forecast the ENSO index. The temporal correlation coefficient is 0.8062, and the MAPE value of 19.55% is small. The difference between forecast results in spring and those in autumn is not high, indicating that the improved model can overcome the spring predictability barrier to some extent. Compared with six mature models published previously, the present model has an advantage in prediction precision and length, and is a novel exploration of the ENSO forecast method.

Keywords: Dynamical-statistical forecast model; self-memorization principle; sea surface temperature field; long-term forecast of ENSO

1. Introduction

The El Niño Southern Oscillation (ENSO), the well-known coupled atmosphere –ocean phenomenon, was firstly proposed by Bjerknes (1969). The ENSO phenomenon can influence~~s~~ regional and global climates, so the prediction of ENSO has received considerable public interest (Rasmusson and Carpenter, 1982; Glantz et al., 1991).

Over the past two to three decades, one might reasonably expect the ability to predict warm and cold episodes of ENSO at short and intermediate lead times to have gradual improvement~~gradually improved~~ (Barnston et al., 2012). Many countries have been focusing on ENSO forecasts since the 1990s, and the ENSO forecast has become one of the important research topics in the International Climate Change and Predictability Research plan. The U.S. International Research Institute for Climate and Society, the U.S. Climate Prediction Centre, Japan Meteorological Agency, and European Centre for Medium-Range Weather Forecasting have developed different coupled atmosphere–ocean models to forecast ENSO (Saha et al., 2006; Molteni et al., 2007, Zheng et al., 2016) .

The forecast models can generally be divided into two types (Palmer et al., 2004, Zheng et al., 2017). The first type is typified by a ~~dynamic~~dynamical model, which mathematically expresses physical laws that govern how the ocean and the atmosphere interact. The second type is typified by a statistical model, which requires a large amount of ~~large a amount of~~ historical data and analyses the data to do forecasting (Chen et al., 1995; Moore et al., 2006).

Over the past three decades, ENSO predictions have made remarkable progress, reaching a stage where reasonable statistical and numerical forecasts (Jin et al., 2008)can be made 6–12 months in advance (Wang et al., 2009a). . However, there are three problems remaining to be resolved (Zhang et al., 2003a): (1) The current ENSO predictions are mainly limited to the short term, such as annual and seasonal predictions; (2) Although the representation of ENSO in coupled models has been advanced~~advanced~~ considerably during the last decade, several aspects of the simulated climatology and ENSO are not well reproduced by the current generation of coupled models. The systematic errors in SST are often very large in the equatorial Pacific, and model representations of ENSO variability are often weak and/or incorrectly located (Neelinet al. 1992; Mechoso et al. 1995; Delecluse et al. 1998; Davey et al. 2002). (3) Coupled models of ENSO predictions initialized from observed initial states tend to adjust towards their own climatological mean and variability, leading to forecast errors. The errors associated with such adjustments tend to be more pronounced during boreal spring, which is often called the ‘‘spring predictability barrier’’ (Webster et al., 1999). More efficient models are therefore desired (Belkin and Niyogi, 2003; Weinberger and Saul, 2006). Therefore, the idea of combining dynamical and statistical methods to improve weather and climate prediction has been developed in many studies (Huang et al., 1993;Yu et al., 2014a; Yu et al.,2014b). By introducing genetic algorithms (GAs), Zhang et al. (2006) inverted and reconstructed a new dynamical-statistical forecast model of the tropical Pacific sea surface temperature (SST) field using historic statistical data (Zhang et al.,

2008). However, there is one flaw in the forecast model: the time-delayed SST field. It is because that~~This is because~~ ENSO is a complicated system with many influencing factors. To overcome information insufficiency in the forecast model, Hong et al. (2014) selected the tropical Pacific SST, SSW and SLP fields as three modelling factors and utilized the GA to optimize model parameters.

However, the above dynamical prediction equations which were ,proposed by Hong et al.(2014), greatly depend on a single initial value, creating long-term forecasts over 8 months that diverged significantly. These unsatisfactory results indicate that this model needs to be improved. Cao (1993) first proposed the self-memorization principle, which transforms the dynamical equations with the self-memorization equations, wherein the observation data can determine the memory coefficients. This method has been widely used in forecast problems in environmental, hydrological and meteorological fields (Feng et al., 2001; Gu, 1998; Chen et al., 2009). The method can avoid the question of initial conditions for the differential equations, so it can be introduced here to improve the proposed dynamical forecast model.

Therefore, an improved dynamical-statistical forecast model of the SST field and its impact factors with a self-memorization function was developed. The improved model can absorb the information from past observations.

This paper is organized as follows: Research data and forecast factors are introduced in section 2. In Section 3 the reconstruction of the dynamical model of SSTA field is described. To improve the reconstruction model, the self-memorization

principle is introduced in Section 4. Model forecast experiments are described in Section 5, and conclusions are given in Section 6.

2. Research data and forecast factors

2.1 Data

The monthly average SST data were obtained from the UK Met Office Hadley Centre for the region (30°S-30°N；120°E-90°W). The gridded 1° × 1° Met Office Hadley Sea Ice and SST dataset (HadISST1; Rayner et al. 2003) includes both in situ and available satellite data. The sea areas provide important information on ocean-atmosphere coupling in the East and West Pacific Ocean and the El Niño /La Niña events. The reanalysis data, zonal winds and sea level pressures were obtained from the National Center for Environmental Forecast of America and the National Center for Atmospheric Research (Kalnay et al., 1996). The sea surface height (SSH) field was obtained from Simple Ocean Data Assimilation (SODA) data (James and Benjamin, 2008). Outgoing longwave radiation (OLR) was obtained from the National Oceanic and Atmospheric Administration (NOAA) satellites, at a resolution of 0.5° × 0.5°(Liebmann and Smith, 1996).The Southern Oscillation Index (SOI) data were obtained from the Climate Prediction Center (CPC). The time series of all data were from Jan. 1951 to Dec. 2010, 720 months in total.

2.2 EOF deconstruction

The sea surface temperature anomaly (SSTA) field can be calculated from the SST field and can be deconstructed into time (coefficients)-space (structure) using the empirical orthogonal function (EOF) method. Detailed information on the EOF

method can be seen in the related references (Dommenget & Latif, 2002). We have used covariance matrix，because the covariance matrix was selected to diagnose the primary patterns of co-variability in the basin-wide SSTs, rather than the patterns of normalized covariance (or correlation matrix).

We used the smooths function with MATLAB to smooth the SSTA field before the EOF deconstruction, which is five points two times moving, mainly filtering out some noise points and outliers. Then an EOF analysis of smoothed anomalies was performed, and the first two SSTA EOFs are shown in Figs. 1a and 1c. The principal component (PC) time series corresponding to the first and second EOFs are shown in Figs. 1b and 1d. The first EOF pattern, which accounted for 61.33% of the total SSTA variance, represented the mature ENSO phase (El Niño or La Niña), and the corresponding PC time series was highly correlated (with a correlation coefficient of 0.85) with the cold tongue index (SST anomaly averaged over 4 °S–4 °N, 180°–90 ° W) over the whole period. The second EOF, accounting for 14.52% of the total SSTA variance, indicated the ENSO signal beginning to enhance. Compared with the first mode, these were slightly attenuated in terms of the scope and intensity. The above analysis is similar to the EOF analysis of the SSTA field in the previous studies (Johnson et al., 2000;Timmermann et al., 2001). This indicates that the front two variance contribution modes can describe the main characteristics of the SSTA field and El Niño/La Niña. Therefore, we can choose the T_1, T_2 time series EOF decomposition modes as the modelling objects.

2.3 Selection of other prediction model factors

158 Considering the complexity of computation, the amount of variables in the
159 equations of our model can't be too large, usually 3 or 4 for the best. This has been
160 explained in our previous studies (Zhang et al., 2006; Zhang et al., 2008). If there are
161 more than 4 variables in the modeling equation, it will cause the amount of
162 parameters such as $a_1, a_2, ...a_n, b_1, b_2, ...b_n, ...$ too large. The huge computation makes it
163 difficult to be precisely modeled. Thus, the total number of parameters in the model of
164 five variables was 102, which may cause an overfitting problem. Hence, when we
165 selected the model of five or six variables which entailed large amounts of
166 computation that made precision difficult, and too many parameters might cause an
167 overfitting phenomenon. If we choose only two or even fewer variables, the forecast
168 performance is poor too. Too few variables cause too small reconstructed parameters,
169 resulting in amounts of important information missing out in the model. Thus, four
170 variables are best for dynamically and accurately modeling. Because we have chosen
171 two time series in section2.2 as the modeling objects, now we should select the other
172 two ENSO intensity impact factors.

173 The ENSO intensity impact factor is an important issue in ENSO prediction.
174 Previous studies have been completed in this area, which found that teleconnection
175 patterns, temperature, precipitation, wind and SSH may affect ENSO strength. For
176 example, Trenberth et al. (1998) noted that PNA, SOI and OLR in the Pacific
177 Intertropical Convergence Zone (ITCZ) are all closely related to ENSO.
178 Webster(1999) pointed out after the 1970, Indian Ocean dipole (IOD) is not only
179 affected by ENSO, but also affected the strength of ENSO (Ashok et al., 2001). Yoon

and Yeh (2010) reported that the Pacific Decadal Oscillation (PDO) disrupts the linkage between El Ni˜no and the following Northeast Asian summer monsoon (NEASM) through inducing the Eurasian pattern in the mid-high latitudes. The vast majority of studies (Tomita and Yasunari, 1996; Zhou and Wu, 2010; Kim et al., 2017) have concentrated on the impacts of ENSO on the East Asian winter monsoon(EAWM). During the EAWM season, ENSO generally reaches its mature phase and has the most prominent impact on the climate. Wang et al. (1999a) and Wang et al. (1999b) suggested that the zonal wind factors in the eastern and western equatorial Pacific play a critical role in the phase of transition of the ENSO cycle, which could excite eastward propagating Kelvin waves and affect the SSTA in the equatorial Pacific. Zhao et al. (2012) analyzed the characteristics of the tropical Pacific SSH field and its impact on ENSO events.

Based on the above analysis, we have selected nine factors, which may be closely related with the ENSO index (Niño3.4).

(1)The zonal wind in the eastern equatorial Pacific factor (u1) was calculated as the grid-point average of zonal wind in the area [5 °S ~ 5 °N, 150 °W ~ 90 °W].

(2) The zonal wind in the western equatorial Pacific factor (u2) was calculated as the grid-point average of zonal wind in the area [0 °~ 10 °N; 135 °E ~ 180 °E].

(3) The PNA teleconnection factor was obtained from the CPC.

(4) the dipole mode index factor (DMI) was obtained from SSTA for June-July-August (JJA) based on Saji(1999) method.

(5) The SOI factor was obtained from the CPC.

(6) The PDOI factor was obtained from department of Atmospheric Sciences in the university of Washington. The web is http://tao.atmos.washinton.edu/pdo/RDO.latest.

(7) The EAWM index (EAWMI) factor was proposed by Yang et al. (2002), which is defined by the meridional 850-hPa winds averaged over the region (20 °~40 °N, 100 °~140 °E).

(8) The OLR in the ITCZ factor was calculated as the grid-point average of OLR in the area [10 °N～20 °N，120 °E～150 °E].

(9) The SSH factor was calculated as the grid-point average of the SSH data in the area [10 °S ~ 10 °N; 120 °E ~ 60 °W].

A correlation analysis of the above factors was carried out and the results are shown in Table 1.

Table 1 shows that SOI and EAWMI have the stronger correlation with the front two time series T_1, T_2 than the other 7 factors. The results are also consistent with previous research (Clarke and Van Gorder, 2003; Drosdowsky, 2006; Zhang et al., 1996; Wang et al., 2008; Yang and Lu, 2014). Therefore, the first time series T_1, the second time series T_2, SOI and EAWMI will be selected as prediction model factors.

3. Reconstruction of dynamical model based on GA

Takens' delay embedding theorem (Takens, 1981) provides the conditions under which a smooth attractor can be constructed from observations made with a generic function. Later results replaced the smooth attractor with a set of arbitrary box-counting dimensions and the class of generic functions with other classes of

functions. Takens had shown that if we measured any single variable with sufficient accuracy for a long period of time, it would be possible to construct the underlying dynamical structure of the entire system from the behavior of that single variable using delay coordinates and the embedding procedure. It was therefore possible to construct a dynamical model of system evolution from the observed time series. Introducing this idea here, four time series of the T_1, T_2, SOI and EAWMI factors were chosen to construct the dynamical model.

The basic idea of statistical-dynamical model construction is discussed in Appendix A and was introduced in our previous work (Zhang et al., 2006; Hong et al., 2014).

A simplified second-order nonlinear dynamical model can be used to depict the basic characteristics of atmosphere and ocean interactions (Fraedrich, 1987). Suppose that the following nonlinear second-order ordinary differential equations are taken as the dynamical model of reconstruction. In the equations, x_1, x_2, x_3, x_4 were used to represent the time coefficient series of T_1, T_2, SOI and EAWMI.

$$
\begin{aligned}
\frac{dx_1}{dt} &= a_1x_1 + a_2x_2 + a_3x_3 + a_4x_4 + a_5x_1^2 + a_6x_2^2 + a_7x_3^2 + a_8x_4^2 + a_9x_1x_2 + a_{10}x_1x_3 + a_{11}x_1x_4 + a_{12}x_2x_3 + a_{13}x_2x_4 + a_{14}x_3x_4 \\
\frac{dx_2}{dt} &= b_1x_1 + b_2x_2 + b_3x_3 + b_4x_4 + b_5x_1^2 + b_6x_2^2 + b_7x_3^2 + b_8x_4^2 + b_9x_1x_2 + b_{10}x_1x_3 + b_{11}x_1x_4 + b_{12}x_2x_3 + b_{13}x_2x_4 + b_{14}x_3x_4 \\
\frac{dx_3}{dt} &= c_1x_1 + c_2x_2 + c_3x_3 + c_4x_4 + c_5x_1^2 + c_6x_2^2 + c_7x_3^2 + c_8x_4^2 + c_9x_1x_2 + c_{10}x_1x_3 + c_{11}x_1x_4 + c_{12}x_2x_3 + c_{13}x_2x_4 + c_{14}x_3x_4 \\
\frac{dx_4}{dt} &= d_1x_1 + d_2x_2 + d_3x_3 + d_4x_4 + d_5x_1^2 + d_6x_2^2 + d_7x_3^2 + d_8x_4^2 + d_9x_1x_2 + d_{10}x_1x_3 + d_{11}x_1x_4 + d_{12}x_2x_3 + d_{13}x_2x_4 + d_{14}x_3x_4
\end{aligned}
\tag{1}
$$

Based on the parameter optimization search method of GA in Appendix A, the

time coefficient series of T_1, T_2, SOI and EAWMI from January 1951 to April 2008 are chosen as the expected data to optimize and retrieve model parameters. In order to eliminate the dimensionless relationship between variables, data standardization $x_{nor} = \frac{x - x_{\min}}{x_{\max} - x_{\min}}$ is to transform data from different orders of magnitude to the same order of magnitude~~, thus making the data comparable. So we used $x_{nor} = \frac{x - x_{\min}}{x_{\max} - x_{\min}}$ to normalize the raw value of each of the four predictors, then we used the normalized value to model and forecast~~. Finally, we made forecast results revert back to the raw data magnitude by $x = x_{nor}(x_{\max} - x_{\min}) + x_{\min}$.

In order to quantitatively compare the relative contribution of each item of our model to the evolution of the system, we calculated the relative variance contribution. The formula is as follows: $R_i = \frac{1}{n}\sum_{j=1}^{n}[\frac{T_i^2}{\sum_{i=1}^{14} T_i^2}], i = 1,2,...,14$, Where n is the length of the data, $T_i = a_1x_1, a_2x_2, ..., a_{14}x_3x_4$ is the item in the equation. According to our previous research (Hong et al., 2007), the variance contribution of the real item reflecting the performance of the model has a large proportion, while the variance contribution of the false term is almost zero, so we delete the weak items of $R_i < 0.01$.

After deleting the weak items, the nonlinear dynamical model of the first time series T_1, the second time series T_2, SOI and EAWMI can be reconstructed as follows:

$$\frac{dx_1}{dt} = F_1 = -0.3328x_1 + 1.2574x_2 - 0.3511x_3 - 0.0289x_1^2 + 3.1280x_3^2 + 0.0125x_1x_2 + 2.7805x_1x_3 - 1.5408x_2x_4$$

$$\frac{dx_2}{dt} = F_2 = 1.0307x_1 - 3.1428x_2 + 0.3095x_4 + 4.2301x_1^2 - 1.2066x_2^2 + 2.5024x_4^2 - 0.2891x_1x_3 + 0.7815x_1x_4 - 0.4266x_3x_4$$

$$\frac{dx_3}{dt} = F_3 = -2.3155x_1 + 3.2166x_3 + 1.5284x_4 - 1.4527x_2^2 - 0.0034x_3^2 - 4.1206x_4^2 - 0.0025x_1x_4 + 0.0277x_2x_3 + 1.2860x_2x_4$$

$$\frac{dx_4}{dt} = F_4 = 0.4478x_2 - 0.0268x_4 + 0.8995x_1^2 - 2.3890x_3^2 + 0.2037x_4^2 + 1.3035x_1x_2 + 2.0458x_1x_4 - 2.0015x_2x_4$$

(2)

The model required testing. Because the training period was from January 1951 to April 2008, we chose T_1, T_2, SOI and EAWMI of May 2008, which were not used as initial forecast data in the modeling. Next, the Runge–Kutta method was used to do the numerical integration of the above equations, and every step of the integration was regarded as 1 month's worth of forecasting results. As a result, forecast results of four time series over a period of 20 months were obtained. Here, the focus was on the forecast results of T_1 and T_2, as shown in Fig.2.

The pearson correlation coefficient (CC) (Wang et al. 2009b) and the mean absolute percentage error (MAPE)(Hu et al. 2001) are employed as objective functions to calibrate the model. The CC evaluates the linear relationship between the observed and predicting values and MAPE measures the difference between the observed and predicting values.

From Fig. 2, forecast performance of T_1 and T_2 within 5 months was better. Using T_1 as an example, the CC between model predictions and corresponding observations over the first five months forecasts was 0.8966 and MAPE was 8.32%. However, after 5 months, MAPE increased rapidly, and was 31.29% at 10 months. The model forecast then significantly diverged from observations, and the forecast became inaccurate. After 10 months, the forecast results became increasingly worse,

which indicated that the forecast of the model after 5 months was unacceptable. The forecast results of T_2 were similar to those of T_1.

The model's skill should be further assessed by cross-validated retroactive hindcasts of the time series. As in the above example, omitting a portion of the time series (12 months, Jan. 1951 to Dec. 1951) from observations, we trained the model based on the data from Jan. 1951 to Dec. 2010, and then predicted the omitted segments (12 months, Jan. 1951 to Dec. 1951). Then in the next prediction experiment, the omitted segment is Jan.1952 to Dec. 1952 and the training samples are Jan. 1951 to Dec.1951 and Jan.1953 to Dec.2010. So the forecast time series is Jan.1952 to Dec. 1952.We then repeated this procedure by moving the omitted segment along the entirety of the available time series. Each experiment has used the different training sample and ~~have~~ established the different model equation (but the method is the same). The similar process of the cross-validated retroactive hindcasts has also been used in the previous literatures (Hu et al., 2017).

Finally, we obtained cross-validated retroactive hindcast results of T_1 and T_2, as shown in Fig. 3. So the forecast results of 60 cross experiment (each experiment is the prediction of the 12 month as Fig.2) according to the time sequence can merger into a new time series (from Jan.1951-Dec.2010), and then ~~the pearson correlation coefficient (~~CC~~)~~ and ~~the mean absolute percentage error (~~MAPE~~)~~ can be calculated by the new prediction time series and the time series of the actual value. Figure 3 is combined results of the 60 forecast experiments.

As Fig. 2, the forecast performance of T_1 and T_2 in Fig. 3 was not satisfactory.

303 The model forecast significantly diverged from observations, and the forecast became
304 inaccurate. The CC of T_1 and T_2 between model predictions and corresponding
305 observations were 0.3411 and 0.4176, respectively. Additionally, the MAPE of T_1 and
306 T_2 were 65.42% and 57.56%, respectively. This indicates that the forecast of the model
307 in the long -term was inaccurate and unacceptable.
308 The forecast result may be inaccurate when the integral forecasting time is long.
309 There will be a significant divergence which will cause an ineffective forecast. To
310 improve the forecast accuracy, the forecast not only depends on the integral equation
311 but also on a single initial value. Choosing the different initial value will cause
312 different forecast accuracy. For example, in a total of 60 cross-validated retroactive
313 hindcasts examples, the minimum MAPE was 37.65%, while the maximum MAPE
314 was 89.88%. Aforecast, depending on a single initial value, will cause instability of
315 the forecast results. These two problems are addressed by introducing the
316 self-memorization principle in the next section.
317

318 ## 4. Introduction of self-memorization dynamics to improve the
319 ## reconstructed model

320 In the above discussion, it was shown that the accuracy of the forecast results of
321 equation (2) were unsatisfactory. To improve long-term forecasting results, the
322 principle of self-memorization can be introduced into the mature model (Gu, 1998;
323 Chen et al., 2009). The principle of self-memorization dynamics (Cao, 1993; Feng et
324 al., 2001) can be seen in Appendix B.
325 Based on Eq. (B10) in Appendix B, the improved model can be expressed as

follows:

$$\begin{cases} x_{1t} = \sum_{i=-p-1}^{-1} \alpha_{1i} y_{1i} + \sum_{i=-p}^{0} \theta_{1i} F_1(x_{1i}, x_{2i}, x_{3i}, x_{4i}) \\ x_{2t} = \sum_{i=-p-1}^{-1} \alpha_{2i} y_{2i} + \sum_{i=-p}^{0} \theta_{2i} F_2(x_{1i}, x_{2i}, x_{3i}, x_{4i}) \\ x_{3t} = \sum_{i=-p-1}^{-1} \alpha_{3i} y_{3i} + \sum_{i=-p}^{0} \theta_{3i} F_3(x_{1i}, x_{2i}, x_{3i}, x_{4i}) \\ x_{4t} = \sum_{i=-p-1}^{-1} \alpha_{4i} y_{4i} + \sum_{i=-p}^{0} \theta_{4i} F_4(x_{1i}, x_{2i}, x_{3i}, x_{4i}) \end{cases} \quad (3)$$

where y_i is replaced by the mean of two values at adjoining times; i.e., $y_i \equiv \frac{1}{2}(x_{i+1} + x_i)$; F is the ~~dynamic~~dynamical core of the self-memorization equation, which can be obtained from Eq. (2); and α and θ are the memory coefficients, the formula for which can be found in Appendix B.

If the values of α and θ can be obtained, Eq. (3) can be used to obtain the results of final prediction. The memory coefficients α and θ in Eq. (3) were calibrated using the least-squares method with the same data (January 1951 to April 2008) as those used in Section 3. Eq. (3) can be deconstructed as follows (M is the length of the time series):

$$X = \begin{bmatrix} x_{11} \\ x_{12} \\ \cdot \\ \cdot \\ \cdot \\ x_{1M} \end{bmatrix}, \alpha = \begin{bmatrix} \alpha_{-p-1} \\ \alpha_{-p} \\ \cdot \\ \cdot \\ \cdot \\ \alpha_{-1} \end{bmatrix}, Y = \begin{bmatrix} y_{-p-1,1} & y_{-p,1} & \cdots & y_{-1,1} \\ y_{-p-1,2} & y_{-p,2} & \cdots & y_{-1,2} \\ \cdot & \cdot & & \cdot \\ \cdot & \cdot & & \cdot \\ \cdot & \cdot & & \cdot \\ y_{-p-1,M} & y_{-p,M} & \cdots & y_{-1,M} \end{bmatrix}, \Theta = \begin{bmatrix} \theta_{-p} \\ \theta_{-p+1} \\ \cdot \\ \cdot \\ \cdot \\ \theta_0 \end{bmatrix},$$

$$F = \begin{bmatrix} F_{-p,1} & F_{-p+1,1} & \cdots & F_{0,1} \\ F_{-p,2} & F_{-p+1,2} & \cdots & F_{0,2} \\ \cdot & \cdot & & \cdot \\ \cdot & \cdot & & \cdot \\ \cdot & \cdot & & \cdot \\ F_{-p,M} & F_{-p+1,M} & \cdots & F_{0,M} \end{bmatrix}$$

The matrix equation is:

$$X = Y\alpha + F\theta \qquad (4)$$

where $Z = [Y \vdots F]$, $W = \begin{bmatrix} \alpha \\ \vdots \\ \Theta \end{bmatrix}$.

Eq. (4) can be written as:

$$X = ZW \qquad (5)$$

The memory coefficients vector W can be calibrated using the least squares method:

$$W = (Z^T Z)^{-1} Z^T X \qquad (6)$$

The memory coefficients a, θ can be obtained from Eq. (6). We then made a prediction using the self- memorization equation (3), which used the p values before t_0.

The coefficients in F and W were used with the same training data from January 1951to Apr.il 2008. In the forecast examples, we trained both the coefficients in F and W at the same time, but in the paper we describe them separately to facilitate the reader for better understanding.

5. Model prediction experiments

5.1 Forecast of time series T_1 and T_2

The training sample for the model was from January1951 to April 2008. Here, from Eq. (3), the forecast results using T_1, T_2, SOI and EAWMI factors can be calculated, called as step-by-step forecast.

When the retrospective order p is confirmed, step-by-step forecasts can be

carried out. For example, when the T_1,T_2, SOI and EAWMI values of May 2008 were forecast, y_i was obtained from the previous p +1 time of T_1,T_2, the SOI and the EAWMI data, and $F_i(x_{1i}, x_{2i}, x_{3i}, x_{4i})$ was obtained from the previous p times of T_1,T_2, the SOI and the EAWMI data. All four equations were integrated simultaneously. Taking these in Eq. (3), we can get the T_1,T_2, SOI and EAWMI values of May 2008, which these can be taken as the initial values for the next prediction step. Then, the T_1,T_2, SOI and EAWMI values from June 2008 and so on, can be generated.

5.1.1 Determination of p

Based on the self-memorization principle, the self-memorization of the system determines the retrospective order p (Cao, 1993). If the system forgets slowly, parameters a and θ will be small and the p value should be high. The SSTA field forecasts were on a monthly scale, the change of which was slow in contrast to large-scale atmospheric motion. So parameters a and θ were small, and generally, the p value was in the range 5 to 15(Cao, 1993).

The retrospective order p was obtained by a trial calculation method. We selected the p values in the range 4 to 16 to construct the model. The CC and MAPE of long-term fitting test (from February 1951 to December 2010) are shown in Table 2, which can be used as the standard to determine the retrospective order p.

Table 2 indicates that when $p = 6$, the MAPE values of long-term fitting test were the smallest and the CCs were the largest. Also, when p from 5 to 9, The CCs were all more than 0.58 and the forecast results were all good, which is consistent with our interpretation of the physical mechanisms in section 6.2 below. SOI and

381 EMWMI were 5-12 months lead relationships with SST (Xu et al., 1993; Chen et al,
382 2010; Wang et al., 2003). Using a cumulative period of SOI, EMWMI 5-8 months
383 ahead as initial values can help improve the final forecast results. Our results in table
384 2 are consistent with the actual physical ENSO process. Therefore, we selected the
385 retrospective order as p=6.

386 Then, the prediction experiments can be carried out, based on improved
387 self-memorization Eq. (3).

388 The improved self-memorization equation of T_1,T_2, SOI and EAWMI can then be
389 established. After the differential equation was discretely dealt with, the memory
390 coefficients were solved by the least-squares method given in section 4 (Training
391 period is January 1951 to April 2008). Finally, the improved prediction equation of
392 T_1,T_2, SOI and EAWMI, based on the self-memorization principle, can be expressed
393 as:

394
$$\begin{cases} x_{1t}=\sum_{i=-7}^{-1}\alpha_{1i}y_{1i}+\sum_{i=-6}^{0}\theta_{1i}F_1(x_{1i},x_{2i},x_{3i},x_{4i}) \\ x_{2t}=\sum_{i=-7}^{-1}\alpha_{2i}y_{2i}+\sum_{i=-6}^{0}\theta_{2i}F_2(x_{1i},x_{2i},x_{3i},x_{4i}) \\ x_{3t}=\sum_{i=-7}^{-1}\alpha_{3i}y_{3i}+\sum_{i=-6}^{0}\theta_{3i}F_3(x_{1i},x_{2i},x_{3i},x_{4i}) \\ x_{4t}=\sum_{i=-7}^{-1}\alpha_{4i}y_{4i}+\sum_{i=-6}^{0}\theta_{4i}F_4(x_{1i},x_{2i},x_{3i},x_{4i}) \end{cases} \quad (7)$$

395 where

396
$$\alpha=[\alpha_{ij}]=\begin{bmatrix} 0.0315 & -2.113 & 0.0284 & 2.1468 & 0.0688 & -0.7014 & 1.3248 \\ 0.4088 & -1.887 & -1.0233 & 1.5485 & 0.9028 & 1.0255 & -0.6443 \\ -0.9088 & -0.2557 & 0.9671 & -0.0054 & 1.0568 & 2.9764 & -0.5234 \\ 0.2088 & -1.0567 & 0.4891 & -0.5066 & -0.4890 & 1.4555 & 1.0966 \end{bmatrix}$$

$(i=0,1,...,4;\ j=-7,-6,...,-1)$

397 $$\theta=[\theta_{ij}]=\begin{bmatrix} 0.0485 & 0.0425 & -1.7688 & 0.8543 & 2.8901 & -0.1788 & -0.9066 \\ 0.07642 & 0.0941 & -1.2466 & -0.2288 & 0.1097 & 2.3221 & -1.4228 \\ -0.5288 & 1.2368 & -0.5568 & -0.0155 & 0.2886 & -0.1560 & 1.2775 \\ 1.5335 & -0.2887 & -0.5336 & -0.6072 & -0.5611 & 1.0225 & -1.0625 \end{bmatrix}$$

$(i=0,1,...,4;\ j=-6,-5,...,0)$

398 The step-by-step forecast was performed. The retrospective order $p=6$ means
399 that earlier seven observation data ($p+1=7$) should be used during the forecasting
400 process. The forecast results per month were saved for the next period predictions.

401 5.1.2 Long-term step-by-step forecasts of T_1 and T_2

402 To test the actual forecast performance of the above improved model, long-term
403 step-by-step forecasts of T_1 and T_2 from May 2008 to December 2010 for 20 months
404 were carried out, as shown in Fig. 4. The forecast results of T_1 and T_2 were good.
405 Within 8 months, the CCs of T_1 and T_2 were 0.9163 and 0.9187. MAPEs of T_1 and
406 T_2 were small, only 5.86% and 6.78%. The forecast time series from 8 months to 14
407 months gradually diverged, but the trend was acceptable. The CCs of T_1 and T_2
408 reached 0.8375 and 0.8251, and MAPEs of T_1 and T_2 were 8.32% and 9.11%. After
409 14 months, forecast began to diverge and the error started to increase, but the CCs of
410 T_1 and T_2 remained about 0.6899 and 0.6782, and MAPEs reached 18.31% and
411 19.44%, which can be acceptable.

412 **5.2 Cross-validated retroactive hindcasts of time series T_1 and T_2**

413 As in section 3, the model's skill should be further assessed by cross-validated
414 retroactive hindcasts of the time series. Because our step-by-step forecasts need the
415 earlier seven observation data ($p+1=7$), we can obtain cross-validated retroactive
416 hindcast results of T_1 and T_2 from August 1951 to December 2010, as shown in Fig.

5.

From Fig. 5, the forecast performance of T_1 and T_2 was good. The CCs of T_1 and T_2 were 0.7124 and 0.7036, respectively. The MAPEs of T_1 and T_2 were small, only 19.57% and 19.79%, respectively. The peaks and valleys of T_1 and T_2 were also forecasted accurately. The forecast results indicated that the cross-validated retroactive hindcast results of T_1 and T_2 were close to the observed values. Compared to Fig. 3, the improved model had better forecast abilities than the original model.

Many researchers (Zhang et al., 2003b; Smith, 2004) have used Oceanic Niño Index (ONI) which is used by the U.S. NOAA Climate Prediction Center to determine the El Niño and La Niña years. It defined that the ONIs of five consecutive months in winter were all more than 0.5 (less than -0.5) is the ElNiño (La Niña) year. Based on the above criterion, we can divide the total 60 years (1951-2010) into three categories. It includes the 18 examples of ElNiño year (such as 1958, 1964, 1966, etc.), 22 examples of LaNiña year (such as 1951, 1955, 1956, etc.) and the remaining 20 experiments of the neutral year. Since the details in Fig.5 is not clear, we list the forecast results of 60 experiments (including 18 El Niño examples, 22 La Niña examples and 20 Neutral examples) in table 3.

From table 3, the average of CC of both T_1 and T_2 of 60 experiments within 6 months was more than 0.84 and MAPE was less than 8%. The average of CC within 12 months was more than 0.74 and MAPE was less than 12%. According to the literature (Barranel et al., 1999), when MAPE was less than 15%, which means the error was not great and the forecast results were good. Obviously, the forecast results

of ElNiño / LaNiña experiments were a little worse than those of neutral examples, which means the forecast ability of our model for the abnormal situation was a little worse than those for the normal situation. But even for ElNiño / LaNiña experiments, the average of CC was still more than 0.7 and MAPE was less than 15%, which means the error was not too large and was still within an acceptable range.

5.3Forecast of the SSTA field

When we obtained the forecast results of the time coefficient series T_1 and T_2, we submitted them into the following equation to reconstruct the forecast SSTA field:

$$\hat{x}_t = \sum_{n=1}^{2} E_n \bullet T_{nt}, t = 1,2,...,12 \qquad (8)$$

where E_n, T_{nt} are the EOF space fields and forecast time coefficients, respectively, and $\hat{x}_{tj}$ is the forecast SSTA field reconstructed by EOF.

After reconstruction of the space mode (treated as constant) and time coefficient series (model prediction), the forecast of the SSTA fields was obtained, based on the forecast results of T_1 and T_2 in Section 5.2. For economy of space, we cannot draw all of the forecasted SSTA fields, so we selected a strong El Niño event (December 1997), a strong La Niña event (December 1999) and a neutral event (November 2002) as examples.

Fig. 6 shows the forecast SSTA field during a strong El Niño event. From the actual SSTA field in December 1997 (Fig. 6a), an obvious warm tongue structure occurred in the area of [10°S～5°N，90°W～150°W] in the Eastern Equatorial Pacific, and a warm anomalous distribution arose in the west Pacific, which indicated a weak El Niño event. The forecasted SSTA field of December 1997 is shown in Fig. 6b. Although the range of warm tongue was a litter bigger than the actual situation, the

forecast shape was similar to the actual field and also the contour lines were similar. The average MAPE between the forecast field and the actual field is 8.56%, which was controlled within 10%. The forecast results of the improved model event were quite good for the El Niño event.

Fig.7 shows the forecasted SSTA field of a strong La Niña event. From the actual SSTA field in December 1999 (Fig. 7a), an obvious cold pool occurred in the area of [10°S～10°N，120°W～180°W] in the Equatorial Pacific, which covered the Niño3.4 area. This SSTA field presented a strong strength La Niña event. The forecast SSTA field from December 1999 is shown as Fig. 7b. Although the strength of the cold pool was weaker than the actual situation, the forecast shape was similar to that of the actual field. The average MAPE between the forecast field and the actual field was 9.69%. The errors were larger than that of the El Niño event, but they can be controlled within 10%, which is acceptable.

Fig. 8 shows the forecasted SSTA field of a neutral event. From the actual SSTA field in November 2002 (Fig. 8a), a warm pool occurred in the area of [10°S～10°N，120°W～180°W] in the Equatorial Pacific, which covered the Niño3.4 area. However, the warm pool was small and weak, which represented a neutral event. The forecasted SSTA field from November 2002 is shown in Fig. 8b. Comparing Figures 6, 7 and 8, we can see that the forecasted SSTA field of a neutral event was a little worse than that of the El Niño and La Niña events. The forecasted shape of the SSTA field basically described the actual situation, but the warm pool in the Niño3.4 area was stronger and bigger than that of the actual situation, which indicated a borderline El

Niño event. The average MAPE between the forecasted field and the actual field was 14.50%, which was big but can be accepted.

We obtained the average values of MAPE of 18 El Niño events, 22 La Niña events and 20 neutral events, which were 9.52%, 9.88% and 14.67%, respectively, representing a good SSTA field forecasting ability of our model.

5.4 Forecast of ENSO index

The ENSO index can be represented as the sea surface temperature anomaly (SSTA) in the Niño-3.4 region (5 °N-5 °S, 120 °-170 °W) and the ENSO index forecast was the 3-month forecast (Barnston et al. 2012). So we also can pick up the ENSO index from the above forecasted SSTA field. The forecast results of the ENSO index within 20 months can also be obtained. The definition of lead time can be seen in the reference (Barnston et al. 2012). Therefore, similar to the forecast experiment in section 5.1, a succession of running 3-month mean SST anomalies with respect to the climatological means for the respective prediction periods, averaged over the Niño 3.4 region, can be obtained, as demonstrated in Fig. 9.

The evaluation criteria of the ENSO index is the temporal correlation (TC), its definition and specific calculation steps can be seen in these literatures (Kathrin et al.,2016; Nicosia et al. 2013); The TC is often used to measure the prediction effect of the ENSO index. For example, Barnston et al.in 2012 also used the TC to compare the forecast skill of 21 real-time seasonal ENSO models.

The forecast results within lead times of 18 months are shown in Fig. 9, which demonstrate that the forecast results of the ENSO index are good. Within lead time of

12 months, the TC was 0.8985 and the MAPE value was small, only 8.91%. In addition, the borderline La Niña event in 2008–2009 was predicted well. After lead times of 12 months, forecasts began to diverge and the errors started to increase. Although the TC remained approximately 0.61, MAPE reached 18.58%. Therefore, a moderate strength El Niño event that occurred in 2009/10 was not predicted.

We should give more examples to test the ENSO prediction ability of our model. As in section 5.3, we can divide 60 examples as three types, which are examples of ElNiño year, LaNiña year and neutral year. Finally, we can obtain the forecast results of different types of examples in different lead times, as shown in table 4.

From table 4, the average TC of 60 experiments was 0.712 and the average MAPE was 7.62% within 12 months for all seasons of lead time, which indicates that the overall ENSO forecast ability of our model was good. The forecast results of the El Niño examples were significantly worse than those of La Niña examples, while the forecast results of La Niña examples were significantly worse than those of neutral examples, which show the model forecast ability of the abnormal state was worse than the normal state of the ENSO index. Even for the forecast results of El Niño examples, the average TC was still above 0.6 and the average MAPE can be controlled below 10%, which means the forecast results were still in the acceptable range. Our model not only accurately predicted the stronger El Niño and La Niña phases but also the neutral states.

The ENSO forecast often had a spring predictability barrier (Webster, 1999), which was most prominent during decades of relatively poor predictability

(Balmaseda et al., 1995).To test our model, the skill should be computed over the entire time series and separately for seasonal subsets of the time series. From the table4, we can see that although the forecast results of the present model in the spring were worse than in the autumn, the margin was not high, which means the model can overcome the "spring predictability barrier," to some extent.

5.5 Compared with six mature models

Barnston et al. (2012) compared many ENSO forecast models. Based on his research, we selected four high quality dynamical models, including ECMWF, JMA, the National Aeronautics and Space Administration Global Modelling and Assimilation Office (NASAGMAO) and the National Centre for Environmental Prediction Climate Forecast System (NCEP CFS; Version1). Two high quality statistical models also be selected, including the University of California, Los Angeles Theoretical Climate Dynamics (UCLA-TCD) multilevel regression model and the NOAA/NCEP/CPC constructed Analogue (CA) model. The detail of the above models can be seen in these references (Reynolds al., 2002; Luo et al., 2005; Barnston et al., 2012).

We then compared the forecast ability of the above six models with that of our model. All of the experiments of our model and six other models were conducted under the same conditions using the same historical data for modelling and the same initial values to forecast. In the CPC website, there are detailed explanations of six models' training samples and the initial values. So we do not need to install all these models on their own machines and run them for forecasting. We just made training

551 samples and initial values of our model were the same with those of selected six
552 models. At an 8-month lead time, the TC of our model for all seasons combined was
553 0.613 (Fig. 10). In brief, the forecast ability of the ECMWF model was slightly better
554 than that of our model but the ability of the other 5 models was worse than that of our
555 model. While, in regard to the forecast length, the TC within 12 months of our model
556 is greater than 0.6, which was superior to the ECMWF model. In addition, the forecast
557 results of the UCLA-TCD model and the CPC CA model reduced quickly after
558 5-month lead times, so the forecast ability of our model was more stable than them.
559 The root mean square error (RMSE) was also examined to assess the
560 performance of discrimination and calibration. Barnston et al. (2012) believed that all
561 seasonal RMSE values contributed equally to a seasonally combined RMSE. So we
562 drew figure 11 to show seasonally combined RMSE.
563 From Fig. 10 and Fig. 11, we can see the highest correlation tend to have
564 lower RMSE. So the RMSE of our model was slightly higher than that of ECMWF
565 model, but it was much lower than those of the other 5 models. Figure 11 and Figure
566 12 is the average TC and RMSE of the 240 experiments of compared with six mature
567 models, covers a variety of different types of ENSO and different lead time. So those
568 samples should be really representative.

569 # 6. Conclusions and discussion

570 ## 6.1 Conclusions

571 A new forecasting model of the SSTA field was proposed based on a
572 ~~dynamic~~dynamical system reconstruction idea and the principle of

573 self-memorization. The approach of the present paper consisted of the following
574 steps:
575 (1) The SST field can be time (coefficients)-space (structure) deconstructed
576 using the EOF method. Take T_1, T_2, SOI and EAWMI and consider them as
577 trajectories of a set of four coupled quadratic differential equations based on the
578 ~~dynamic~~dynamical system reconstruction idea. The parameters of this
579 ~~dynamic~~dynamical model were estimated using a GA.
580 (2) The forecast results of the ~~dynamic~~dynamical model can be improved by
581 the self-memorization principle. The memory coefficients in the improved
582 self-memorization model were obtained using the GA method.
583 (3) The long-term step-by-step forecast results and cross-validated
584 retroactive hindcast results of time series T_1 and T_2 are all found to be good, with the
585 CC of approximately 0.80 and the MAPE of less than 15%.
586 (4) The improved model was used to forecast the SSTA field. The
587 forecasted SSTA fields of three types of events are accurate. Not only is the forecast
588 shape similar to the actual field but also the contour lines are similar.
589 (5) The improved model was also used to forecast the ENSO index. The
590 average TC of 60 examples within 12 months is 0.712, and the MAPE value is small,
591 only 7.62%, which proves that the improved model has better forecasting results of
592 the ENSO index. Although the forecast results of the model in the summer were
593 worse than in the winter, the margin was not high, which means that the model can
594 overcome the spring predictability barrier to some extent. Finally, compared with the

six mature models, the new dynamical-statistical forecasting model has a scientific significance and practical value for the SST in the eastern equatorial Pacific and El Niño/La Niña event predictions.

6.2 Discussion

L'Heureux et al.(2013) reported that using different data sets and time periods, the 2nd EOF is not stable, being entirely due to the strong trend. So we need to do more experiments to prove that we choose the second mode of EOF to be appropriate, and whether different time periods will make us forecast unstable or not. Our original data is the monthly average SST data from January 1951 to Dec. 2010, which are 60 years. We will increase the length of the data for 20 years (Jan.1931 –Dec.2010), for 10 years (Jan.1941- Dec.2010) and decrease the length of the data for 10 years (Jan.1961- Dec.2010), for 20 years (Jan.1971- Dec.2010). And then we use the same method to reconstruct a model and forecast the ENSO index as section5.4.The results show ~~The prediction results are shown in the table5.~~

~~From the table, we can see that~~ in the 60 experiments, ~~the prediction results of the data period increased by 20 years are the best, and the prediction results of the data period decreased by 20 years is the worst. This is because the more data we use, the more information it contain. But from the table we can also see~~ the difference among forecast results of both TC and MAPE of five different sample data are less, and no abnormal change suddenly worse or better appear. All these indicate that using different data sets and time periods, even though may have a certain impact on the pattern of the 2nd EOF, but the impact on our forecast is not great and it will not

make our forecast unstable.

Actually, how many variables and which variables are used in our model become a key issue to be resolved. We are a complex four factor differential equations coupling model. We are a complex coupled model of four factor differential equations, so we are more concerned with the correlation between each other. The correlation must be considered as an important criterion to select the factors, but in order to further verify the correctness of the selection criterion, we have carried out the prediction experiments (the 60 cross-validated retroactive hindcasts experiments of the ENSO index for all seasons combined at lead times of 8 months) of different variables.

We can see that for all the forecast results of the models of different variables, the prediction results of T_1,T_2,SOI is the best among those of the three factors and the prediction result of $T_1,T_2,\mathrm{SOI,EAWMI}$ is the best among those of the four factors. But the prediction result of $T_1,T_2,\mathrm{SOI,EAWMI}$ is best among all, which proves that our selection factors are correct. In our previous study (Hong et al., 2015), the model of the Western Pacific subtropical high was established by using the correlations as a criterion to select factors and their forecast results are also good. Now we use the correlations as a criterion to select factors is also in line with our previous research.

~~The definition of overfitting: The learned hypothesis may fit the training set very well, but fail to predict to new examples (fail to fit additional data or predict future observations reliably).~~

~~The potential for overfitting depends not only on the number of parameters and~~

~~data but also the conformability of the model structure with the data shape, and the magnitude of model error compared to the expected level of noise or error in the data(Burnham and Anderson, 2002). So there are many reasons causing the overfitting phenomenon. But this does not mean having many parameters relative to the number of observations inevitably causes the overfitting problem (Golbraikh et al., 2003). There is no evidence that more parameters will be certain to result in overfitting.~~ Based on the definition of overfitting and the previous studies(Golbraikh et al., 2003; Everitt and Skrondal,2010), there is no evidence that more parameters will be certain to result in overfitting. ~~we~~ We can judge whether a model is overfitting or not by the accuracy of prediction results of independent samples (Golbraikh and Tropsha, 2002; Qin and Li, 2006).

In the sample training, our model does not purposely pursue the high degree of the training samples fitting and improve the effectiveness of the independent generalization. In fact in our paper the forecast results of the ~~Cross~~cross-validated retroactive hindcasts (section 5.2) and the independent samples validation (table3 and table4) are both good. Especially, the independent samples validation of the ENSO index as the table4, we have carried out the 240 independent sample validation prediction of four seasons of different ENSO events and the coverage of independent samples test is very wide. Moreover, compared with 6 mature prediction models, the forecast results of our model are also good, which prove the overfitting problem does not exist in our model. ~~According to the previous literature (Islam and Sivakumar, 2002; Sivakumar et al.,2001), we can see that prediction principle and structure of the~~

~~phase space reconstruction (PSR) of dynamical system is not the same with the traditional neural network and in the small sample situation the forecasting results of PSR model are better than those of the traditional neural network (Sivakumar et al. ,2002), which can be verified in the independent sample test (table3 and table4).~~ So according to the definition of overfitting, we can say the over fitting phenomenon does not exist in our model.

Compared with the original model, why the improved model has good forecast results and can overcome the spring predictability barrier to some extent are as follow: Recently, many studies have pointed out that spring is the most unstable season of the air - sea interaction and the error is likely to develop or grow in the spring, resulting in the spring predictability barrier (Zhang et al, 2012; Philander et al., 1992). When the original model uses the indexes in summer as the initial values to predict, the SOI factor representing the air-sea interaction is most unstable in the spring and the EMWMI factor does not have much influence on ENSO in summer, so the forecast results using the indexes in summer as the initial values are certainly much worse than those using the indexes in the winter as the initial values. That is why our original model does not overcome the spring predictability barrier.

However, the introduction of the self-memorization dynamics principle can help our model overcome the spring predictability barrier to some extent. Although the lead time is still summer (such as JJA), the information of the initial value actually contains the previous p + 1 month (in this case p = 6, which contains the information of the previous seven months, including the information of T_1, T_2 , SOI, EMWMI

683 factor in winter (January, February), spring (March, April, May) and summer (June
684 and July)). From the dynamical analysis, in this situation, the information and
685 interaction relationship of four factors have been a long period (from winter to
686 summer) accumulated, containing much air-sea interaction processes and winter
687 monsoon continued abnormal information, so the forecast results of our improved
688 model will be much better than the original model which simply uses only one initial
689 value. That is why the improved model overcomes the spring predictability barrier to
690 some extent.

691 The forecast results of our model are good, but it still has some problems:

692 (1) The inclusion of these terms and the physical processes do these terms in
693 equation (2) represent are important, especially for the discussion of dynamical
694 characteristics of the dynamical model. But now we are difficult to give a clear
695 meaning. Now the main work of our paper is the prediction experiments of the model.
696 For the reason of time and length, this paper mainly discusses the prediction results of
697 the model. The physical processes do these terms represent and the discussion of the
698 dynamical characteristics of the model will be the focus of our next work. Before this,
699 we have also used the Takens' delay embedding theorem to reconstruct the dynamical
700 model of the Western Pacific subtropical high(WPSH). And Based on the
701 reconstructed dynamical model, dynamical characteristics of WPSH are analyzed and
702 an aberrance mechanism is developed, in which the external forcings resulting in the
703 WPSH anomalies are explored, which have been published (Hong et al., 2016). We
704 also study the bifurcation and catastrophe of the West Pacific subtropical high ridge

index of a nonlinear model (Hong et al., 2017). Based on our previous method and work, our next work is to analyse the physical processes and the dynamical characteristics of the SST field.

(2)The experiments in the present study have proven that the forecasting results of the improved model are good for large-scale systems, such as ENSO events, and the forecasting period has been extended. However, for small-scale systems, such as Hurricanes, whether the forecast results could be improved using the present improved model needs to be further verified.

(3) Our paper focuses primarily on these defined indices with T_1, T_2 to reconstruct a prediction model. Maybe, we can select variables (predictor) based on EOF analysis and our model may be a more physically oriented model. Maybe we can learn from Yim et al. (2013; 2015) to draw correlation maps between these fields and the SSTA field and select the predictors from physical considerations. All these above questions require that a lot of experiments to be carried out.

These items will be our future work.

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APPENDIX A: THE PRINCIPLE OF DYNAMICAL MODEL RECONSTRUCTION

Suppose that the physical law of a nonlinear system going by over time can be expressed as the following difference form:

$$\frac{q_i^{(j+1)\Delta t} - q_i^{(j-1)\Delta t}}{2\Delta t} = f_i(q_1^{j\Delta t}, q_2^{j\Delta t}, ..., q_i^{j\Delta t}, ..., q_N^{j\Delta t}) \quad j = 2,3,.....M-1 \tag{A1}$$

where f_i is the generalized nonlinear function of $q_1, q_2, ..., q_i, ..., q_N$, N is the number of variables, and M is the length of observed data. $f_i(q_1^{j\Delta t}, q_2^{j\Delta t}, ..., q_i^{j\Delta t}, ..., q_N^{j\Delta t})$ can be assumed to contain two parts: G_{jk} representing the expanding items which contain variable q_i, P_{ik} just representing the corresponding parameters which are real numbers ($i = 1, 2, ..N$, $j = 1,2,...M$, $k = 1,2,..., K$).

It can be supposed as follows:

$$f_i(q_1, q_2, ..., q_n) = \sum_{k=1}^{K} G_{jk} P_{ik} \tag{A2}$$

$D = GP$ is the matrix form of Eq.(A2), in which

$$D = \begin{Bmatrix} d_1 \\ d_2 \\ ... \\ d_M \end{Bmatrix} = \begin{Bmatrix} \frac{q_i^{3\Delta t} - q_i^{\Delta t}}{2\Delta t} \\ \frac{q_i^{4\Delta t} - q_i^{2\Delta t}}{2\Delta t} \\ ... \\ \frac{q_i^{M\Delta t} - q_i^{(M-2)\Delta t}}{2\Delta t} \end{Bmatrix}, \quad G = \begin{Bmatrix} G_{11}, G_{12}, ...G_{1K} \\ G_{21}, G_{22}, ...G_{2,K} \\ ... \\ G_{M1}, G_{M2}, ...G_{M,K} \end{Bmatrix}, \quad P = \begin{Bmatrix} P_{i1} \\ P_{i2} \\ ... \\ P_{iK} \end{Bmatrix} \tag{A3}$$

Parameters of the above equation can be determined through inverting the observed data. Vector P which satisfies the above equation can be solved, based on a given vector D. Assuming q is unknown, it is a nonlinear system. However, assuming

746 P is unknown, it is a linear system.

747 With the restriction $S=(D-GP)^T(D-GP)$ as a minimum, GA is introduced as an
748 optimization solution search in the model parameters space.

749 Assuming that the parameters matrix P is the population (solutions), the
750 $S=(D-GP)^T(D-GP)$ is an objective function, $l_i=\frac{1}{S}$ is the value of individual
751 fitness, and $L=\sum_{i=1}^{n} l_i$ is the value of total fitness. The operating steps of GA include:
752 creation and coding of initial population (solutions), fitness calculation, the choice of
753 male parents, crossover and variation, etc. A detailed theoretical explanation can be
754 got from Wang (2001). The step length is 1 month during the calculation. After
755 optimization searches and genetic operations, the target value can be rapidly
756 converged on and each optimal parameter of the dynamical equations can be obtained.

757 Through the above approach, we can obtain parameters of a nonlinear
758 dynamical system, and reconstruct the nonlinear dynamical equations from observed
759 data.

760

761 **APPENDIX B: THE MATHEMATICAL PRINCIPLE OF**
762 **SELF-MEMORIZATION DYNAMICS OF SYSTEMS**

763 The dynamical equations of a system can be expressed as:

764 $$\frac{\partial x_i}{\partial t}=F_i(x,\lambda,t)\ i=1,2,...,J \qquad \text{(B1)}$$

765 where J is an integer, x_i is the ith variable of the system state, and λ is
766 the parameter. Equation (B1) represents the relationship between a source function

767 F and a local change of x . Obviously, x is a scalar function with time t and

768 space r_0 . A set of time $T=[t_{-p}...t_0...t_q]$ can be considered, where t_0 is an initial

769 time. A set of space $R=[r_a...r_i...r_\beta]$ can be considered, where r_i is a spatial point.

770 An inner product in space $L^2:T\times R$ is defined by:

771 $$(f,g)=\int_a^b f(\xi)g(\xi)d\xi,\ f,g\in L^2 \qquad \text{(B2)}$$

772 Accordingly, a norm can be defined as:

773 $$\|f\|=[\int_a^b (f(\xi)^2 d\xi]^{1/2}$$

774 For a completion L^2, it can become a Hilbert space H. A generalized one

775 in H can be regarded as a solution of the multi-time model. By introducing a

776 memorization function $\beta(r,t)$, we can obtain:

777 $$\int_{t_0}^t \beta(\tau)\frac{\partial x}{\partial \tau}d\tau=\int_{t_0}^t \beta(\tau)F(x,\tau)d\tau \qquad \text{(B3)}$$

778 where r in $\beta(r,t)$ can be dropped through fixing on the spatial point r_0. Suppose

779 that function $\beta(r,t)$ and variable x etc. are all continuous, differentiable and

780 integrable, an integration by the left parts of Eq. (B3) can be made as:

781 $$\int_{t_0}^t \beta(\tau)\frac{\partial x}{\partial \tau}d\tau=\beta(t)x(t)-\beta(t_0)x(t_0)-\int_{t_0}^t x(\tau)\beta'(\tau)d\tau \qquad \text{(B4)}$$

782 where $\beta'(t)=\partial\beta(t)/\partial t$. The mean value theorem can be introduced into the third

783 term in Eq. (B4), the following equation can be obtained:

784 $$-\int_{t_0}^t x(\tau)\beta'(\tau)d\tau=-x^m(t_0)[\beta(t)-\beta(t_0)] \qquad \text{(B5)}$$

785 where $x^m(t_0)\equiv x(t_m), t_0<t_m<t$. Substituting Eq. (B4) and Eq. (B5) in Eq. (B3) and

786 carrying out an algebraic operation, the following equation can be obtained:

$$x(t)=\frac{\beta(t_0)}{\beta(t)}x(t_0)+\frac{\beta(t)-\beta(t_0)}{\beta(t)}x^m(t_0)+\frac{1}{\beta(t)}\int_{t_0}^{t}\beta(\tau)F(x,\tau)d\tau \qquad \text{(B6)}$$

Because the x value which is at initial time t_0 and middle time t_m, only on the fixed point r_0 itself, relates to the first term and the second term in Eq. (B6), they are be called as a self-memory term. Also, we can call the third term as an exogenous effect, i.e., which is contributed by other spatial points.

Similarly as Eq. (B4), for multi-time t_i, $i=-p,-p+1\ldots,t_0,t$, it gives

$$\int_{t_{-p}}^{t_{-p+1}}\beta(\tau)\frac{\partial x}{\partial\tau}d\tau+\int_{t_{-p+1}}^{t_{-p+2}}\beta(\tau)\frac{\partial x}{\partial\tau}d\tau+\ldots+\int_{t_0}^{t}\beta(\tau)\frac{\partial x}{\partial\tau}d\tau=\int_{t_{-p}}^{t}\beta(\tau)F(x,\tau)d\tau.$$

After the same term $\beta(t_i)x(t_i), i=-p+1,-p+2,\ldots,0$ was eliminated, we have

$$\beta(t)x(t)-\beta(t_{-p})x(t_{-p})-\sum_{i=-p}^{0}[\beta(t_{i+1})-\beta(t_i)]x^m(t_i)-\int_{t_{-p}}^{t}\beta(\tau)F(x,\tau)d\tau=0 \qquad \text{(B7)}$$

As a matter of convenience, we set $\beta_t\equiv\beta(t),\beta_0\equiv\beta(t_0),x_t\equiv x(t),x_0\equiv x(t_0)$; the following text uses similar notations. Then, Eq. (B7) can be expressed as:

$$\beta_t x_t-\beta_{-p}x_{-p}-\sum_{i=-p}^{0}x_i^m(\beta_{i+1}-\beta_i)-\int_{t_{-p}}^{t}\beta(\tau)F(x,\tau)d\tau=0 \qquad \text{(B8)}$$

Setting $x_{-p}\equiv x_{-p-1}^m,\beta_{-p-1}=0$, the Eq. (B8) can be written as:

$$x_t=\frac{1}{\beta_t}\sum_{i=-p-1}^{0}x_i^m(\beta_{i+1}-\beta_i)+\frac{1}{\beta_t}\int_{t_{-p}}^{t}\beta(\tau)F(x,\tau)d\tau=S_1+S_2 \qquad \text{(B9)}$$

S_1 is called as a self-memory term and S_2 is called as an exogenous effect term.

For the convenience of calculations, the above self-memorization equation can be discretized. The differential by difference and the summation can replace the

integration in Eq. (B9), and the mean of two values which are at adjoining times; i.e., $x_i^m \approx \frac{1}{2}(x_{i+1} + x_i) \equiv y_i$ can simply replace x_i^m.

Taking an equal time interval $\Delta t_i = t_{i+1} - t_i = 1$ and incorporating β_i and β_t, we can obtain a discretized self-memorization equation as follows:

$$x_t = \sum_{i=-p-1}^{-1} \alpha_i y_i + \sum_{i=-p}^{0} \theta_i F(x,i) \qquad \text{(B10)}$$

where F is the ~~dynamic~~dynamical kernel of the self-memorization equation, $\alpha_i = \frac{(\beta_{i+1} - \beta_i)}{\beta_t}$; $\theta_i = \frac{\beta_i}{\beta_t}$.

Based on Eq. (B10), the above technique performed computations and the forecast can be called as a self-memorization principle.

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Fig.11. RMSE in standardized units, as a function of lead time for all seasons combined. Each line highlights one model.

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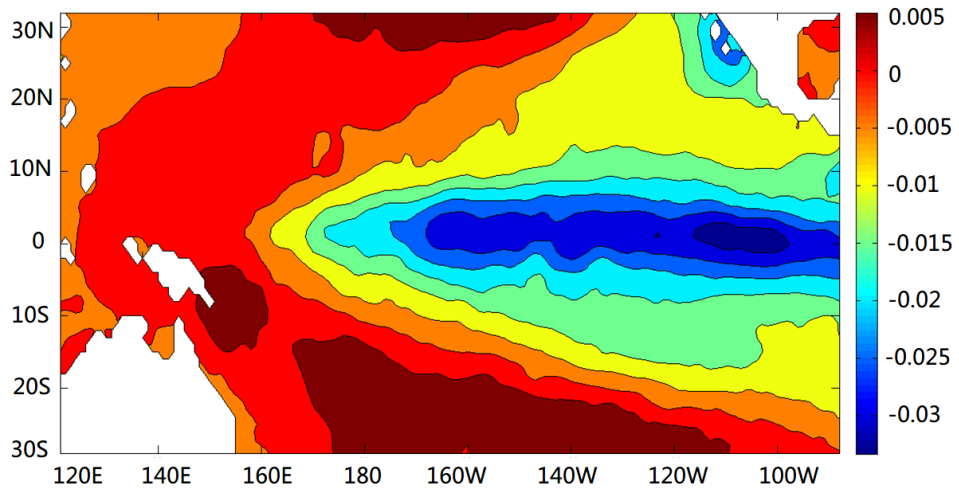
~~**Table5.** The forecast results of the different data periods~~

Figure: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20N
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10S
20S
30S
120E
140E
160E
180
160W
140W
120W
100W
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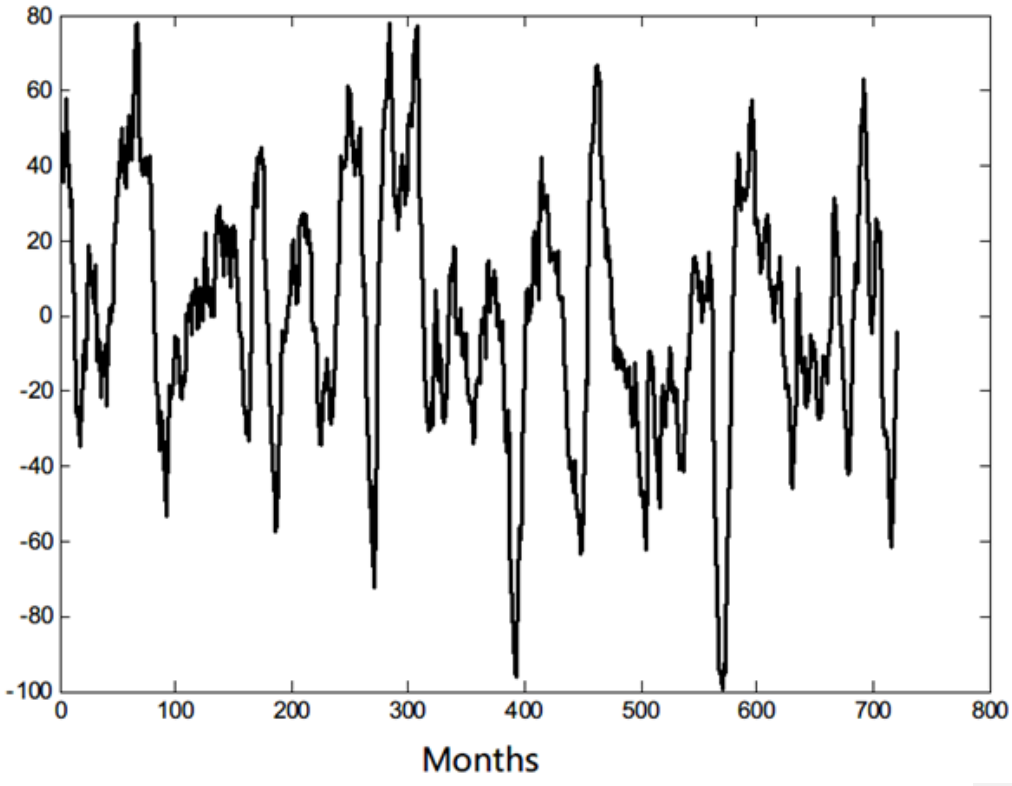
-0.01
-0.015
-0.02
-0.025
-0.03

(a)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60
40
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-20
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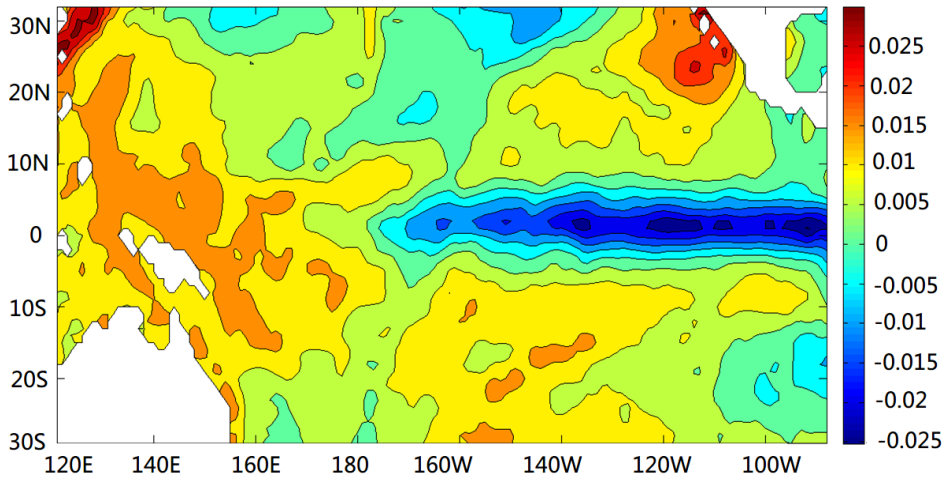
800
Months

(b)



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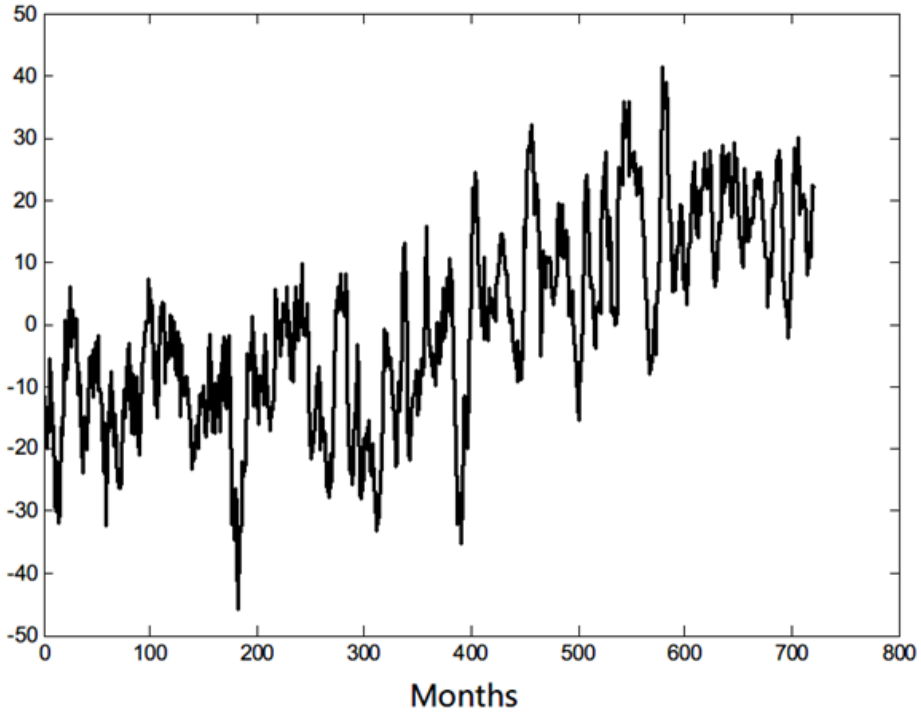

(d)

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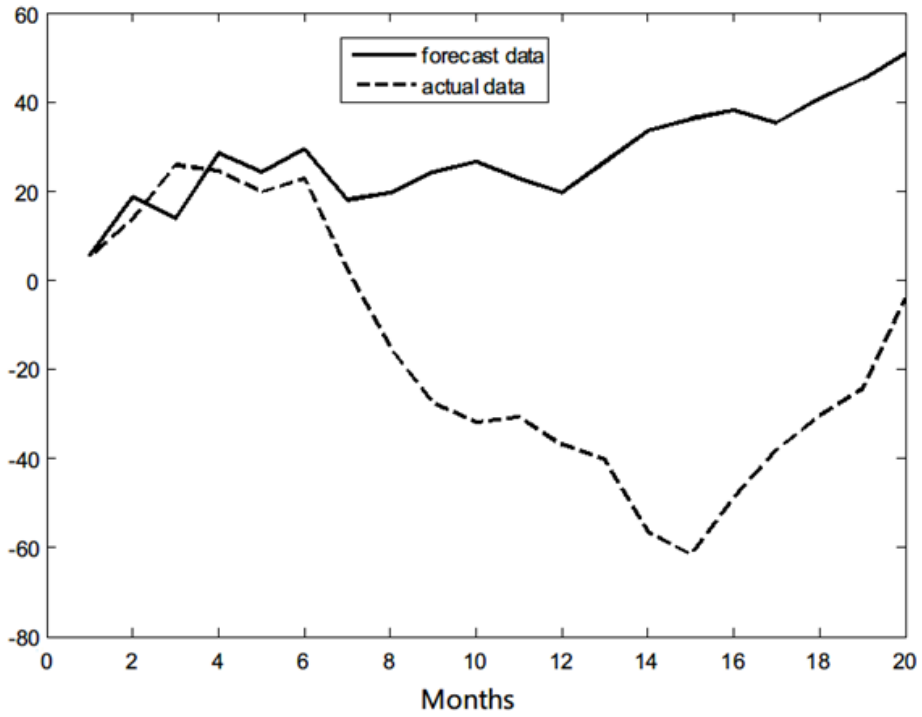
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40
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0
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-60
-80
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2
4
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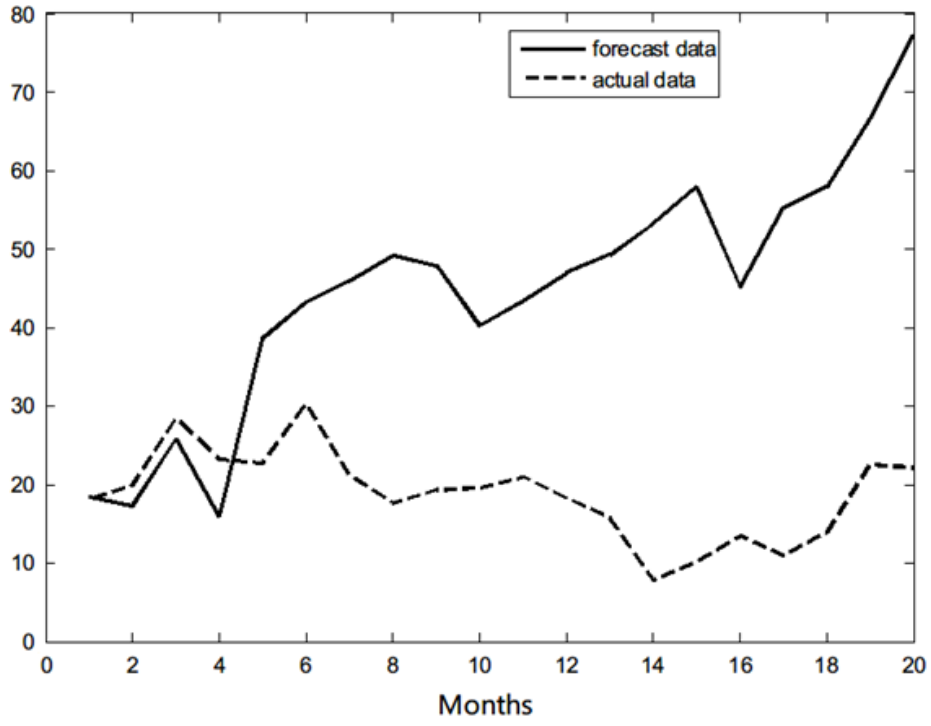
8
10
12
14
16
18
20
Months

(a)


forecast data
actual data
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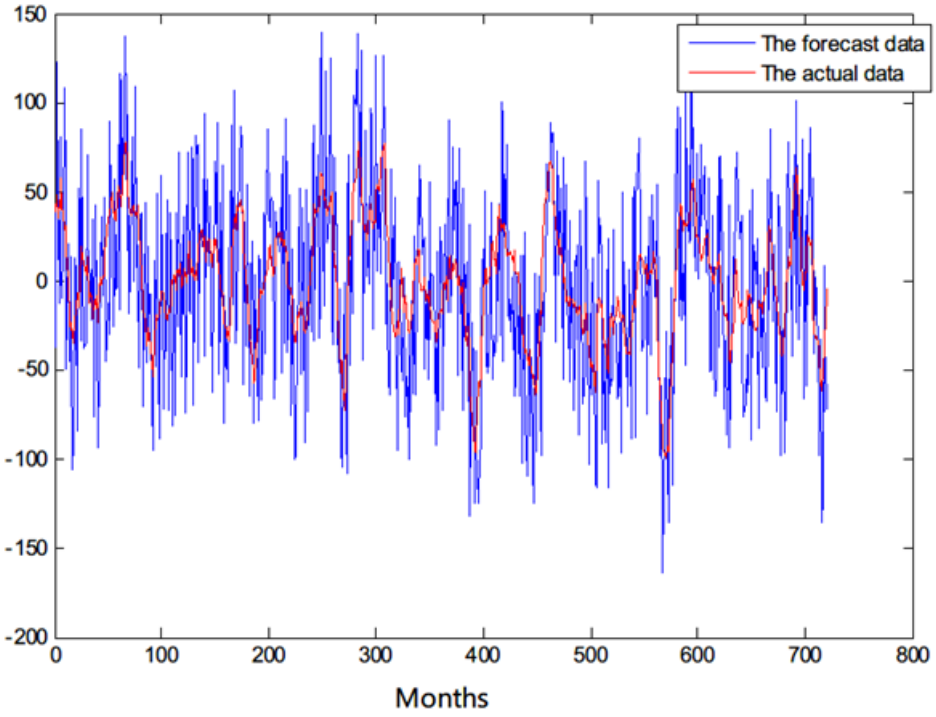
(b)

Fig.2 Forecast results of the first time coefficient series T_1 (a) and the second time coefficient series T_2 (b)of the SSTA field by the original model



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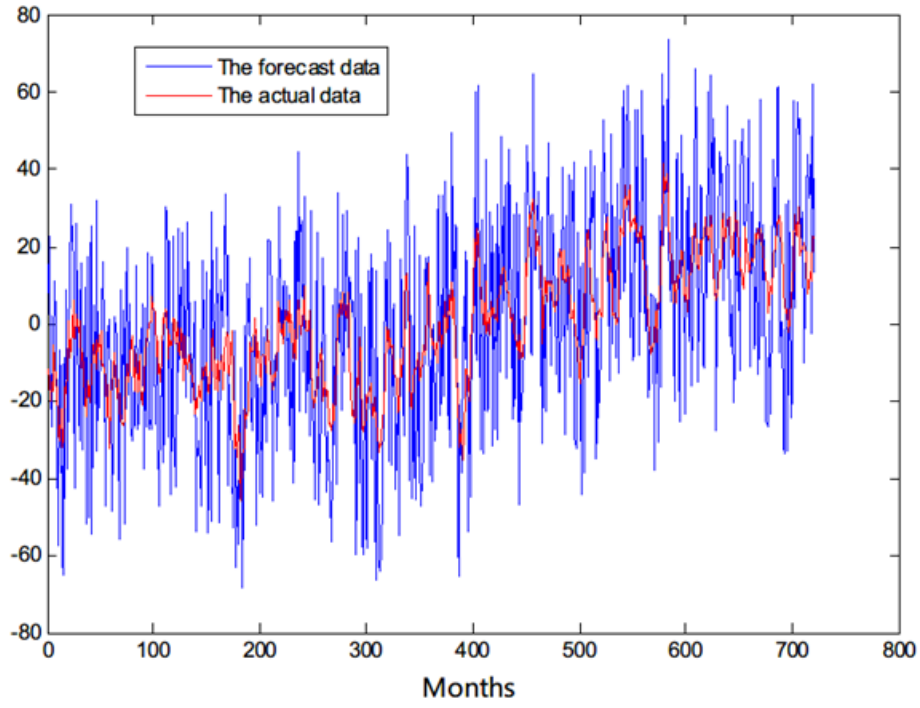
1112 (a)



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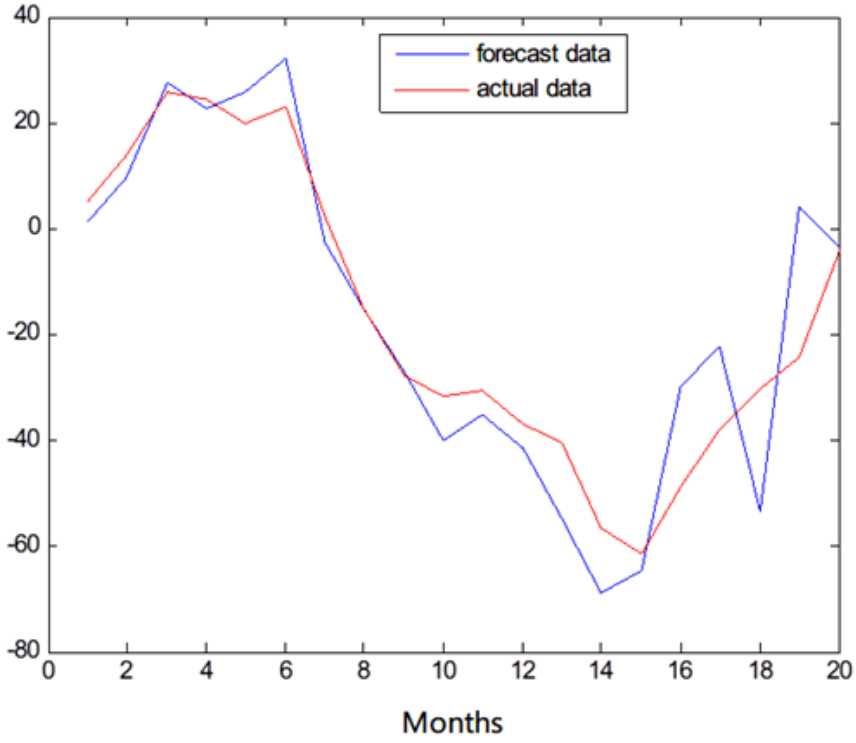
(b)

Fig.3The cross-validated retroactive hindcast results of the first time coefficient series T_1 (a)and the second time coefficient series T_2 (b)of the SSTA field by the original model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actual data
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-20
-40
-60
-80
0
2
4
6
8
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12
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16
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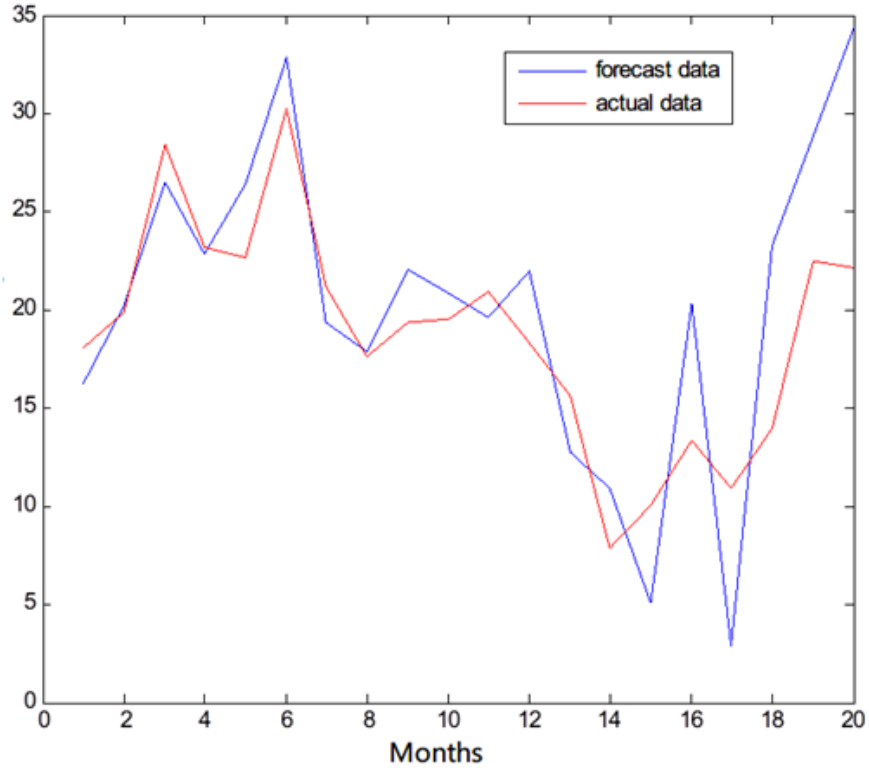
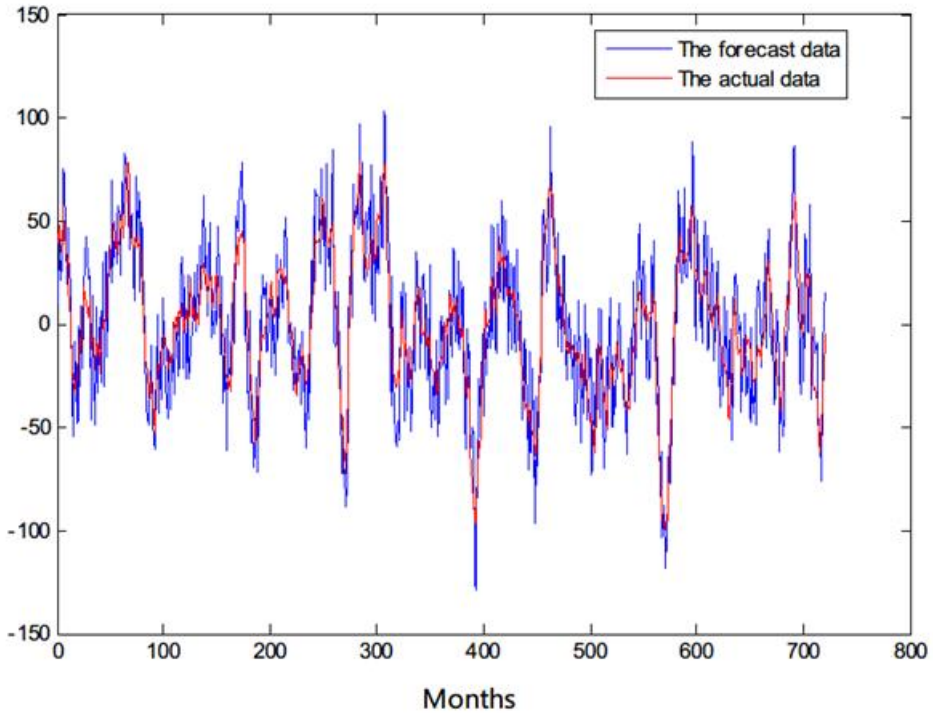
20
Months

(a)



(b)

Fig. 4. Long-term step-by-step forecast results of the first time coefficient series T_1 (a)and the second time coefficient series T_2 (b)of the SSTA field by the improved model


The forecast data
The actual data
150
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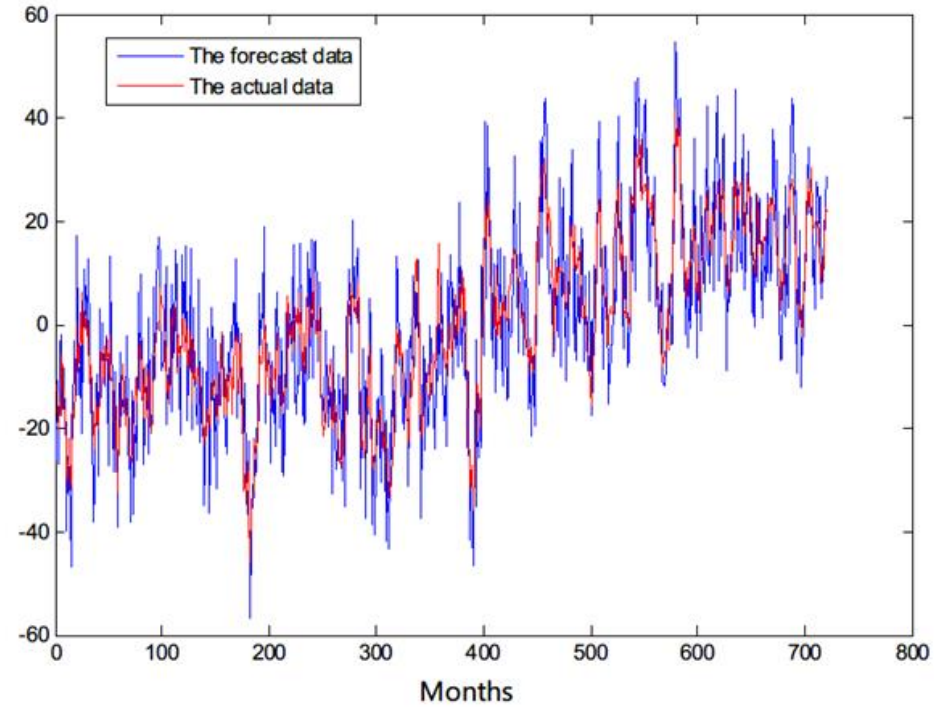
Months

(a)


The forecast data
The actual data
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-20
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400
500
600
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Months

(b)

Fig. 5. The cross-validated retroactive hindcast results of the first time coefficient series T_1 (a)and the second time coefficient series T_2 (b)of the SSTA field by the improved model

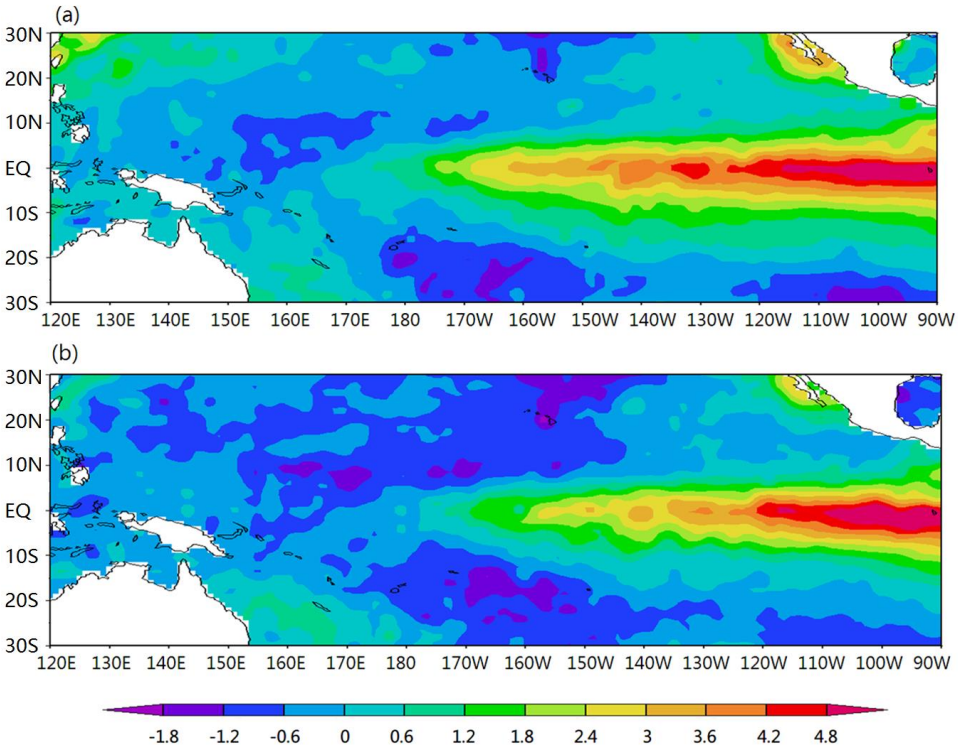

Fig.6. The forecast SSTA field(a) and the actual SSTA field (b)of an El Niño event (Dec.1997)

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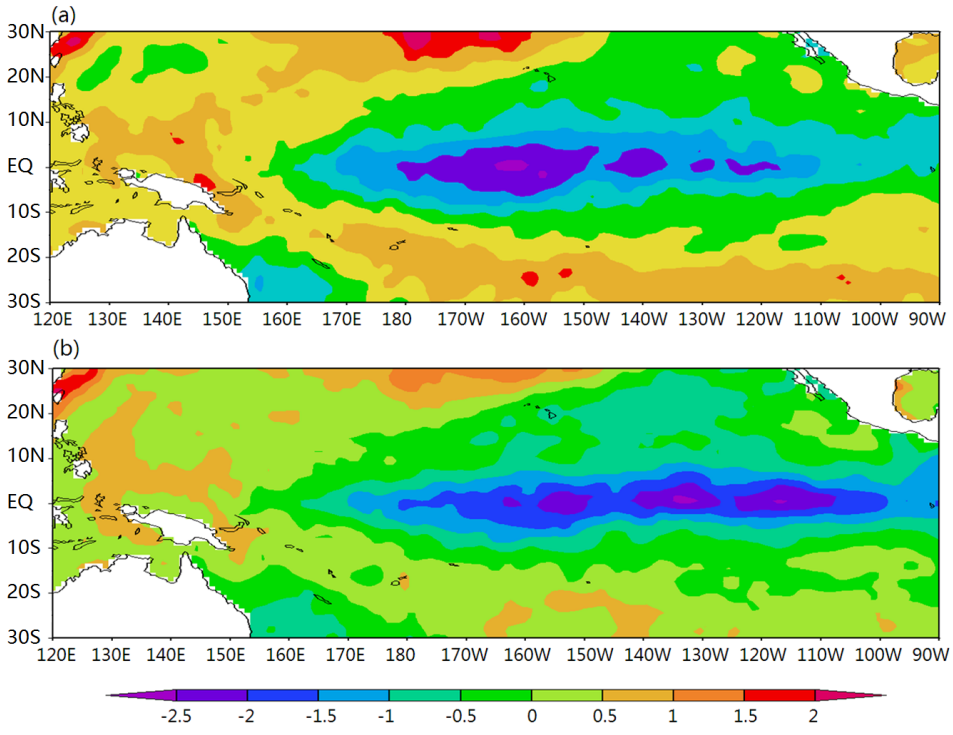

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1160 Fig.7. The forecast SSTA field(a) and the actual SSTA field (b)of a La Niña event (Dec.1999)

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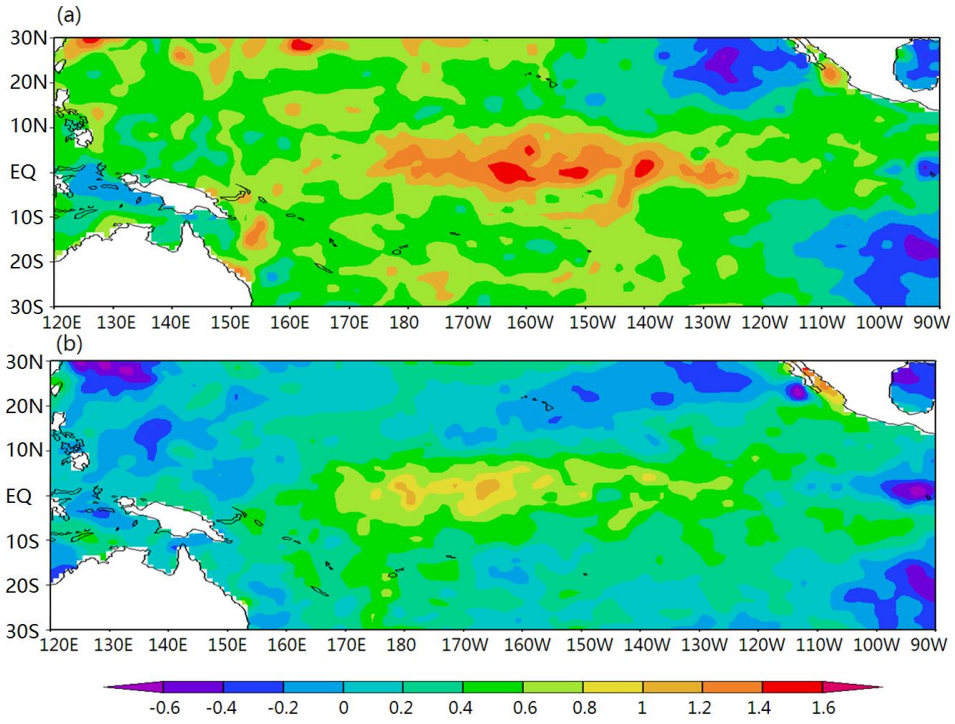

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1171 Fig.8. The forecast SSTA field(a) and the actual SSTA field (b)of neutral event (Nov.2002)

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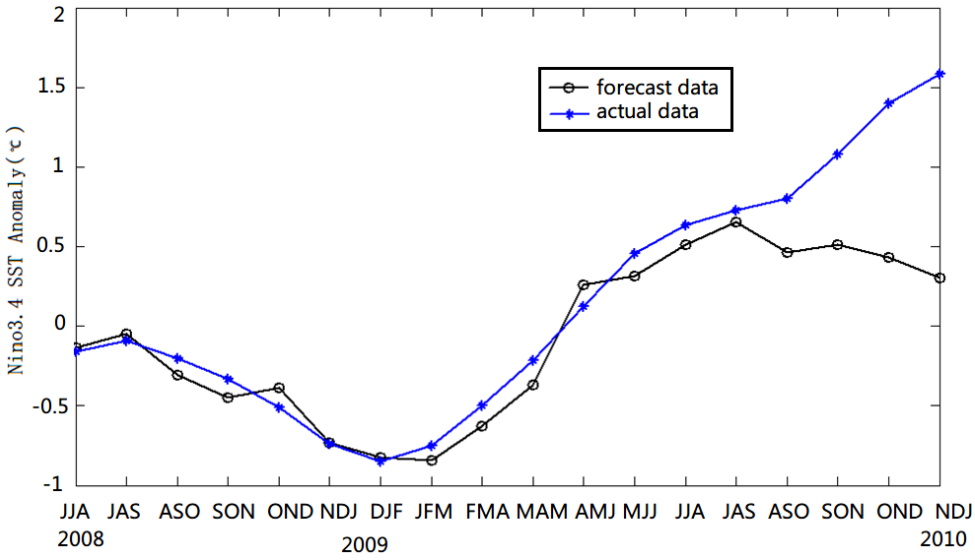
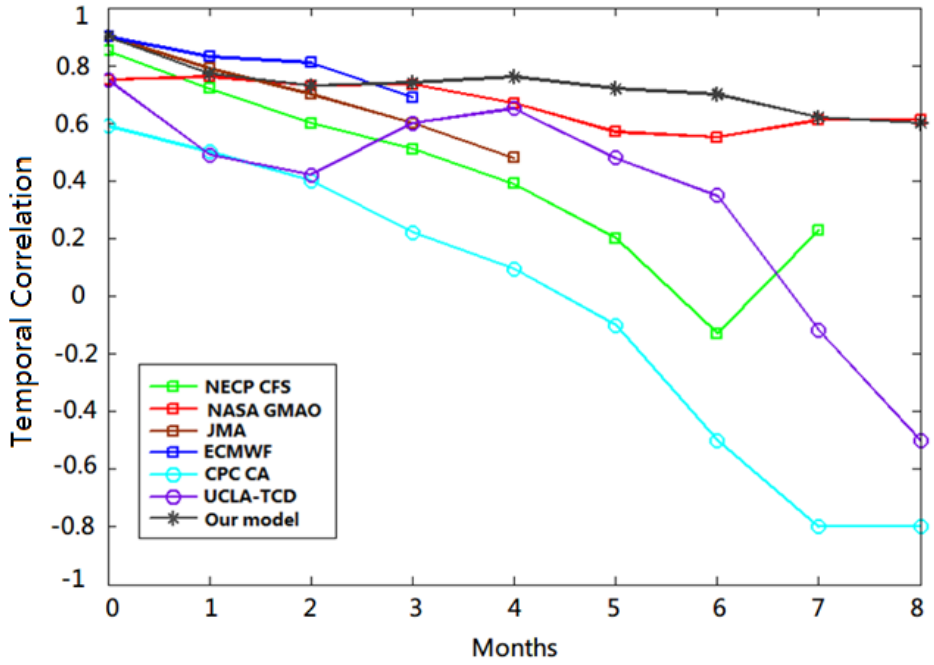


Fig.9. The improved dynamical-statistical model prediction of the ENSO index



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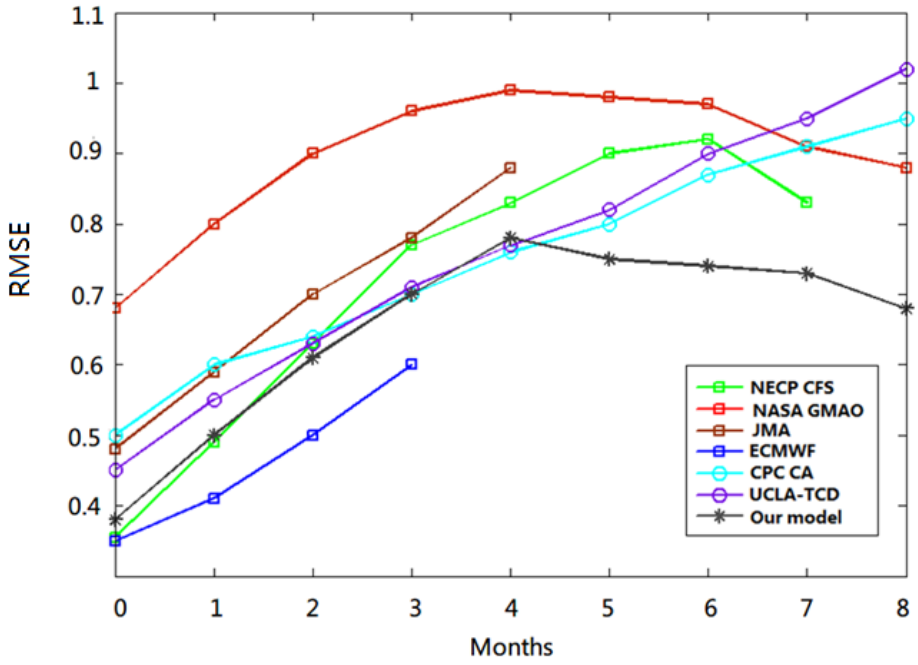

Fig . 11. RMSE in standardized units, as a function of lead time for all seasons combined. Each line highlights one model.

Table:

Table 1. The correlation analysis between the front two time series T_1, T_2 and nine impact factors

factors	u_1	u_2	PNA	DMI	SOI	PDOI	EAWMI	OLR	SSH
T_1	0.3161	0.5684	0.4386	-0.3457	0.7734	0.4081	0.6284	0.3287	0.3363
T_2	0.2118	0.4181	0.2560	-0.2345	0.5232	0.3065	0.4825	0.1816	0.2169

Table 2. The CC and MAPE of long-term fitting test when the retrospective order p is different

p		4	5	6	7	8	9	10
The forecast results of long-term fitting test	CC	0.75	0.73	0.81	0.74	0.70	0.72	0.68
	MAPE	18.42%	19.36%	14.56%	20.39%	25.31%	24.18%	27.33%
p		11	12	13	14	15	16	
The forecast results of long-term fitting test	CC	0.68	0.70	0.65	0.62	0.60	0.62	
	MAPE	28.10%	26.58%	30.91%	33.14%	34.97%	33.56%	

1268 **Table3.** The forecast results of T_1 and T_2 in different examples within 6 and 12 months

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Forecast events	The results within 6-months		The results within 12-months	
	CC	MAPE	CC	MAPE
The average of 18 El Niño examples of T_1	0.824	8.45%	0.719	12.67%
The average of 22 La Niña examples of T_1	0.846	7.68%	0.740	11.28%
The average of 20 Neutral examples of T_1	0.885	6.23%	0.789	9.85%
The average of total 60 examples of T_1	0.850	7.41%	0.748	10.95%
The average of 18 El Niño examples of T_2	0.811	8.79%	0.703	13.28%
The average of 22 La Niña examples of T_2	0.833	7.35%	0.731	11.96%
The average of 20 Neutral examples of T_2	0.896	6.68%	0.795	10.08%
The average of total 60 examples of T_2	0.842	7.64%	0.740	11.71%

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1280 **Table. 4**. The TC and the MAPE between model forecasts and observations within 12 months for
1281 Nov.–Jan., Dec.–Feb., and Jan.–Mar. as lead time of winter, for Feb.–Apr. , Mar.–May and Apr.–June
1282 as lead time of spring, for May-July, June-August and July-Sep. as lead time of summer and for
1283 August-Oct., Sep.-Nov. and Oct.-Dec. as lead time of autumn.

Forecast events	Lead time of all seasons combined		Lead time of summer (MJJ-JJA-JAS)		Lead time of autumn (ASO-SON-OND)		Lead time of winter (NDJ-DJF-JFM)		Lead time of spring (FMA-MAM-AMJ)	
	TC	MAPE	TC	MAPE	TC	MAPE	TC	MAPE	TC	MAPE
The average of 18 El Niño examples	0.604	9.70%	0.569	10.33%	0.632	8.85%	0.677	8.02%	0.538	11.6%
The average of 22 La Niña examples	0.625	8.97%	0.581	9.82%	0.645	8.41%	0.695	7.83%	0.579	9.82%
The average of 20 Neutral examples	0.798	5.96%	0.752	6.86%	0.831	5.31%	0.844	4.60%	0.765	7.07%
The average of total 60 examples	0.712	7.62%	0.633	8.51%	0.786	6.88%	0.776	6.52%	0.653	8.03%

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Table5. The forecast results of the different data periods

Forecast events	The data periods（Jan. 1951-Dec.2010）Lead time of all seasons combined		The data periods（Jan. 1931-Dec.2010）Lead time of all seasons combined		The data periods（Jan. 1941-Dec.2010）Lead time of all seasons combined		The data periods（Jan. 1961-Dec.2010）Lead time of all seasons combined		The data periods（Jan. 1971-Dec.2010）Lead time of all seasons combined	
	TC	MAPE	TC	MAPE	TC	MAPE	TC	MAPE	TC	MAPE
The average of 18 El Niño examples	0.604	9.70%	0.683	9.02%	0.642	9.35%	0.572	10.15%	0.551	10.44%
The average of 22 La Niña examples	0.625	8.97%	0.701	8.33%	0.675	8.55%	0.589	9.42%	0.567	9.82%
The average of 29 Neutral examples	0.798	5.96%	0.845	5.12%	0.821	5.56%	0.746	6.21%	0.721	6.58%
The average of	0.71	7.62%	0.77	7.14%	0.740	7.38%	0.68	7.96%	0.652	8.15%

带格式的：行距：2 倍行距

	~~total 60 examples~~	~~2~~	~~1~~	~~0~~

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带格式的：行距：2 倍行距