



High-resolution diapycnal mixing map of the Alboran Sea thermocline from seismic reflection images

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Abstract. The Alboran Sea is a dynamically active region where the salty and warm Mediterranean water first encounters the incoming milder and cooler Atlantic water. The interaction between these two water masses originates a set of sub-mesoscale structures and a complex sequence of processes that entail mixing close to the thermocline. Here we present a high-resolution map of the diapycnal diffusivity around the thermocline depth obtained using acoustic data recorded with a high-resolution multichannel seismic system. The map reveals a patchy thermocline, with areas of strong diapycnal mixing juxtaposed with others of weaker mixing. The patch size is of a few kms in the horizontal scale and of 10-15 m in the vertical one. The comparison of the obtained maps with the original acoustic images shows that vigorous mixing tends to occur in areas of internal wave instability, whereas mixing levels in more stable areas is lower. These results are also compared with others obtained using conventional probes. The values obtained using the two methods agree within uncertainty bounds, and they are also consistent with reference theoretical values. Overall, our results demonstrate that high-resolution seismic systems allow to remotely quantify mixing at the thermocline depth with a lateral resolution of $O(10^1$ m).

KEYWORDS: Thermocline mixing, Seismic Oceanography, Diapycnal diffusivity map.

1. INTRODUCTION

30 Diapycnal diffusivity (k_p) around the thermocline plays a major role to control the strength and pattern of the ocean circulation, because it determines heat and salt heterogeneity at different spatial scales. This process usually occurs in a vertically stratified regime, affecting adjacent layers with the same density but different temperature and salinity (Stewart, 2008). In terms of processes, mixing in the ocean can be separated in two categories. One is related to internal wave (IW) breaking, which produces turbulent motion and changes the density stratification; while the second concerns the development of high frequency dynamic instabilities that are formed due to shear (Gregg, 1987; Laurent and Garrett, 2002). As the spatial scale decreases, mixing leads to an unbalanced pressure field that can result in a collapse and dispersion of mixing waters through isopycnals (Thorpe, 2005). The value of k_p depends on the buoyancy frequency (N) and the dissipation rate (ε) as indicated by the so-called Osborn (1980) relationship:

$$k_p = \Gamma \varepsilon / N^2 \quad (1)$$

45 This value, where $\Gamma = 0.2$ is the empirically defined mixing efficiency (Osborn and Cox, 1972), corresponds to the mixing between isopycnal layers in the thermocline. The global mean k_p value



is of the order of $10^{-4} m^2 s^{-1}$ (Munk and Wunsch, 1998), which corresponds to the value required to keep overturning in the thermocline. It has been shown that if $k_\rho < 10^{-5} m^2 s^{-1}$ there is not enough energy to generate mixing (Gregg, 1989).

50 If the flow is conservative, ε must be independent of the spatial scale, but it might present small variations due to the fact that it involves work against buoyancy, so that mechanical energy is transformed to heat through turbulent motions. In the presence of strong shear, ε tends to increase (Thorpe, 2005), reaching a maximum value close to the Kolmogorov scale (Gargett and Holloway, 1984). Good knowledge of its behavior provides important clues on available energy and its
55 transfer between spatial scales.

The loss rate of kinetic energy in the turbulent motion is commonly expressed as:

$$\varepsilon = \left(\frac{\nu}{2}\right) \langle S_{ij} S_{ij} \rangle \quad (2)$$

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$$S_{ij} = \left(\frac{\partial u_i}{\partial x_j} + \frac{\partial u_j}{\partial x_i}\right) \quad (3)$$

Where $\nu = 1.064 \times 10^{-6} m^2 s^{-1}$ is the kinematic viscosity and the tensor S_{ij} is a function of the velocity components in the three orthogonal directions (Thorpe, 2005). Conventional in-situ techniques
65 that are commonly used to directly measure k_ρ have the problem that they are intrusive, in the sense that the measuring itself modifies the mixing levels at the small scales. In addition, although measures are accurate in the vertical dimension, sampling in the horizontal direction is much poorer, particularly in the $\sim 10^3$ - $10^1 m$ range (Klymak and Moum, 2007 a, b). Since this is the range of scales at which the transition between isotropic internal wave and anisotropic turbulence motion
70 (i.e. mixing) occurs, the observational evidence of mixing patterns and the understanding of the underlying physical mechanisms are rather limited so far. Overall direct measures and observations are too few to create a global mixing map with the required resolution to feed the models with appropriate dissipation ranges (Smyth et al., 2011). This makes it in turn difficult to integrate mixing into large-scale ocean dynamics models. Its effects are simulated instead through the
75 incorporation of eddy diffusivity coefficients, which are tuned *ad hoc* to match the large-scale distribution of ocean observables. While this approach allows to properly reproduce regional spatial-temporal patterns, it severely hampers the long-term predictive capability of ocean dynamics and, in turn, that of climate models. Improving our knowledge on the short-term and small scale mixing mechanisms and integrating them into large-scale models remain thus as an
80 outstanding challenge.

To overcome this issue, remote sensing techniques have recently started to be used (e.g. Gibson et al., 2007). One of these alternative techniques is the multichannel seismic (MCS) system, an
85 acoustic method providing quasi-synoptic images of the thermohaline boundaries in the ocean interior to full ocean depth, with a lateral resolution of up to $\sim 10^1 m$ (Holbrook and Fer, 2005). Several recent works have demonstrated that it is actually possible to map k_ρ using measures of the horizontal wavenumber (k_x) spectra of the vertical displacements of thermohaline boundaries imaged with MCS systems (Sheen et al., 2009; Holbrook et al., 2013; Fortin et al., 2016). However, these studies use conventional, relatively low resolution MCS acquisition systems with source
90 energy concentrating below $\sim 50 Hz$. In addition, these systems are not well-suited to image the



shallowest ocean layers (i.e. $< 200\text{ m}$), but deeper water levels ($\geq 400\text{ m}$ depth). At these depth levels, the changes in the internal structure are usually less marked than those around the thermocline. In a recent work, Sallares et al. (2016) showed that high resolution MCS (HR-MCS) systems, which use a small energy and higher-frequency source, allow imaging the thermohaline structure as shallow as $\sim 30\text{ m}$ with a lateral resolution of $\sim 15\text{ m}$ and $\sim 2\text{ m}$ in the vertical direction. This resolution is three- to four-fold better than that of conventional MCS systems used at deeper ocean levels. Therefore, it has the potential to image sub-mesoscale structures and processes that affect the thermocline at scales of kilometers to tens of meters, therefore contributing to cover the existing observational gap. Despite its potential, HR-MCS systems have never been used to date to quantify diapycnal mixing at the thermocline depth.

Here we use the above-mentioned method of extracting $k_p(x, z)$ maps from MCS images (Sheen et al., 2009; Holbrook et al., 2013), but applied for the first time to HR-MCS data acquired in the Alboran Sea (Westernmost Mediterranean). The result is a high-resolution mixing map of the ocean at the thermocline depth ($30\text{-}150\text{ m}$) along a 35 km -long transect (Fig. 1a). This method can be used in other regions where the water column is sufficiently stratified to record the acoustic impedance variations (density \times sound speed contrasts between neighboring layers).

The rest of the manuscript is structured as follows: in section 2 we present the hydrographic context, and the observations; then we describe the acquisition system and the method applied to estimate k_p from the seismic data. The results are described in section 3, whereas the discussion about the imaged structures and their likely causes is presented in section 4. Finally section 5 summarizes the main conclusions.

2. DATA AND METHODOLOGY

The Alboran Sea is characterized by the continuous exchange between Mediterranean Water (MW) and Atlantic Water (AW) through the Strait of Gibraltar. This exchange concentrates near the surface (between $\sim 30\text{ m}$ and 200 m); where the shallow, moderately saline and cold incoming AW ($< 50\text{ m}$) interacts with the deeper, warmer, saltier and stable outgoing MW, producing another water mass referred to as Modified Atlantic Water (MAW). In this framework, internal waves, strong horizontal shear instability, and prominent thermohaline stratification are generated. These particular features reflect the complex dynamic setting of the area, with kinetic energy being transferred between isopycnals from large to small scales, leading eventually to overturning, isotropic turbulence and irreversible mixing.

The data set used in this work, which includes collocated seismic and oceanographic measurements, was collected in the framework of the IMPULS-2006 experiment. Here, we concentrate our analysis on one of the seismic profiles (IMPULS-3), which was acquired on board the Spanish R/V Hesperides using a HR-MCS system. The acquisition started on May 16th at 23:43 and finished on May 17th at 04:00. In total, some 4 hours to record a 38 km -long profile. The acquisition system consisted of a 4.75 liters source with a peak frequency at 150-190 Hz. The corresponding size of the Fresnel zone, a proxy of the horizontal resolution (e.g. Sheriff and Geldart, 1995), is $\sim 15\text{ m}$. The streamer was 300 m -long and had 48 channels, with a group spacing



135 of 6.25 m. The shot interval was 15 m, giving a Common Mid-Point (CMP) gathers (Yilmaz and Doherty, 1987) fold of 6. The location of the different data is displayed in Fig. 1a.

This profile was first processed and used to estimate the k_x energy spectra of the vertical displacements of the seismic reflectors (Sallares et al., 2016). A total of 68 reflectors with lengths
 140 1.5-21 km and a signal-to-noise ratio higher than 8 within the frequency range of 40–240 Hz were identified and used for the analysis. Vertical profiles of temperature and pressure were recorded simultaneously with the seismic acquisition using 4 XBT's; whereas the salinity and buoyancy profiles were obtained from an XCTD, dropped three days after the seismic acquisition. Water current profiles have also been used in the study, but they are not coincident with the seismic acquisition (see location in Fig. 1a). They were obtained during the SAGAS experiment on board
 145 the Spanish R/V Sarmiento de Gamboa using an ADCP ocean surveyor 75, in the same season as the seismic experiment but 4 years later.

The HR-MCS profile shown in Fig. 2 reveals a number of laterally coherent seismic reflectors that
 150 are assumed to follow isopycnals (Biescas et al., 2014). The analysis of the obtained k_x spectra allowed identifying three sub-ranges that control dynamics around the thermocline depth at increasingly small spatial scales. Thus at scales larger than the horizontal buoyancy wavelength ($L_N \approx 90$ m), motions are dominated by the internal wave field; then the spectra rolls off reflecting the presence of shear instabilities of probably the Kelvin-Helmholtz (KH) type, which appear to
 155 collapse at a scale of ~ 30 m, giving rise to turbulence at even smaller scales. A detailed description of these ranges and their scales is presented in Sallares et al. (2016). In the present work, we use the energy levels obtained from the k_x spectral analysis of the reflectors to estimate the variations of ε and k_ρ along the whole profile.

160 Since our dataset does not include direct measurements of turbulence, we use the XCTD and ADCP data to estimate a vertical profile of k_ρ based on Gregg's (1989) model; hereafter referred to as Gregg89. The Gregg89 model assumes that energy dissipation in the thermocline is made through IW energy transfer by wave-wave interaction. This model links shear current at different depths as:

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$$\varepsilon = 7 \times 10^{-10} N^2 / N_0^2 < S_{10}^4 / S_{GM}^4 > \quad (4)$$

$$S_{10}^4 = 4.22 [(\Delta U / \Delta z)^2 + (\Delta V / \Delta z)^2]^2 \quad (5)$$

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$$S_{GM}^4 = 2 [(3\pi/2) j_x E_{GM} b N_0^2 k^c (N/N_0)^2]^2 \quad (6)$$

Where $N_0 = 5.2 \times 10^{-3} s^{-1}$ is the reference buoyancy frequency, S_{10} is the shear variance calculated from the meridional (V) and zonal (U) velocity variations according to the depth (Z), and S_{GM} is the variance for the Garrett-Munk model (Gregg, 1989), where j_x is a mode number, E_{GM} is the
 175 Garrett-Munk energy density, b is a scale factor, and k is the horizontal wavenumber.

Alternatively, the model proposed by Batchelor (1959); hereafter referred as Batchelor59, estimates k_ρ as a function of the energy transfer from large to small scales in the turbulent regime. This model assumes that the energy exchange from mechanical to caloric due to N and ε can be
 180 approximated as:



$$\varphi_{\zeta}^T = \left(\frac{4\pi\Gamma}{N^2}\right) C_T \varepsilon_T^{2/3} (2\pi k)^{-5/3} \quad (7)$$

Where φ_{ζ} is the energy spectrum of the isopycnals vertical displacement; and C_T is a
185 proportionality constant (Sreenivasan, 1996). We apply this model to estimate the mixing rates
over the seismic profiles. These two models are then used to compare and analyze the mixing
behavior in the water column.

In summary, both models Gregg89 and Batchelor59, are used to estimate the mixing rates from
190 two independent data sets: XCTD-ADCP and seismic data, respectively. Results obtained using
both models are then compared to gain confidence in the proposed methodology. We then analyze
and discuss the high resolution 2D map resulting from the seismic data in terms of mixing.

3. RESULTS

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To identify the dissipation signature in the seismic profile, we first calculate the energy level in
the turbulent subrange from our data by averaging the value obtained for all reflectors within a
1200 m-wide and 15 m-high window. We then apply Batchelor59 model, Eq. (7), to estimate ε
using the obtained energy level within the window, with $\Gamma=0.2$, $C_T=0.3$ and N according to depth.
200 Finally, we apply Eq. (1) using the $\varepsilon(x, z)$ values obtained above to estimate $k_{\rho}(x, z)$. These steps
are repeated within a sliding window that moves 30 m in the horizontal direction and 3 m in the
vertical one at each step along the seismic profile. As a result we obtain a smoothly varying k_{ρ} map
that covers the whole profile (Fig. 3). The resolution of the obtained map is therefore of ~ 30 m in
the horizontal and ~ 3 m in the vertical, safe enough given the theoretical limit of the size of the
205 Fresnel zone (~ 15 m) in the lateral direction, and of the Rayleigh criterion of $\lambda/4$ (~ 2 m) in the
vertical one. The goal is being able to identify processes occurring in the transition between the
internal wave and the turbulence sub-regimes, such as the intensity and scales of variability of the
mixing patches, the location and size of the hotspots and their potential relationship with
oceanographic features such as IWs or shear instabilities.

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3.1. Probe-based $k_{\rho}(z)$ profile

To have a reference value to compare with the MCS-based k_{ρ} maps, we have first calculated a $k_{\rho}(z)$
profile for shallow waters (< 200 m) using the XCTD and ADCP data and applying Gregg89 model
215 (Eqs. 4-6). To do this we have used ADCP measures averaged within 10 m-depth bins. By doing
this, we obtain an average value for the shear variance of $S_{10}^4 = 0.28$ s^{-1} , whereas the reference
value of the shear variance obtained from the Garrett-Munk model (Gregg, 1989) is $S_{GM}^4 = 0.013$
 s^{-1} . This gives an average dissipation rate $\langle \varepsilon \rangle \approx 1.3 \times 10^{-8}$ Wkg^{-1} , and an average diapycnal
diffusivity $\langle k_{\rho} \rangle \approx 10^{-3.0}$ m^2s^{-1} for the targeted depth range (Fig. 4a). The $k_{\rho}(z)$ profile obtained from
220 the XCTD and ADCP is also shown in Fig. 4a, together with the global averages for overturning
($\langle k_{\rho} \rangle \approx 10^{-4}$ m^2s^{-1}) as well as the average pelagic diffusivity in the ocean ($\langle k_{\rho} \rangle \approx 10^{-5}$ m^2s^{-1}).

We obtain minimum values of the mixing rate at 50-55 m, 68-73 m, and 100-125 m. The absolute
minimum of $k_{\rho} = 10^{-5.2}$ m^2s^{-1} is obtained at ~ 115 m. Deeper than this, the mixing variability is



225 smaller. The Turner angle and buoyancy frequency (Fig. 4b) indicate that the region is mostly stable with a slight tendency to double-diffusion ($Tu \sim 45^\circ$).

It is worth noting that, at this specific location, the vertical $\varepsilon(z)$ and $k_\rho(z)$ values are one order of magnitude higher than the global average ones. The higher values probably reflect the effect of overturning in the thermocline. While probe-based measurements are well-suited to investigate mixing variability the vertical dimension, they do not provide information on the variability in the horizontal dimension with a comparable level of detail. As explained above, to do this we have used estimations of ε and k_ρ based on the HR-MCS data, but applying Batchelor59 model (Eq. 7) in this case.

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3.2. High-resolution multichannel seismics-based $k_\rho(x, z)$ map

The $k_\rho(x, z)$ map displayed in Fig. 3 has average values of $\langle \varepsilon \rangle \approx 6.5 \times 10^{-9} \text{ Wkg}^{-1}$ and $\langle k_\rho \rangle \approx 10^{-2.7} \text{ m}^2 \text{ s}^{-1}$. These values are comparable, within uncertainty bounds, to those obtained from the XCTD and ADCP data but, at the same time, they are over an order of magnitude higher than the global ocean reference value of $k_\rho \approx 10^{-4.0} \text{ m}^2 \text{ s}^{-1}$ (Fig. 4a).

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Figure 5 displays the $k_\rho(x, z)$ map superimposed with the HR-MCS data. It is interesting to note that the range of horizontal variability is similar to that observed in the vertical dimension, although there is no clear visual correspondence between the k_ρ anomalies and the most obvious of the imaged oceanographic features such as IWs. The range of variability is of over three orders of magnitude, locally reaching an extreme value of $k_\rho \approx 10^{-1.5} \text{ m}^2 \text{ s}^{-1}$ at a depth of $\sim 55 \text{ m}$ and at 16 km along the line; and a minimum value of $k_\rho \approx 10^{-4.5} \text{ m}^2 \text{ s}^{-1}$ at $\sim 95 \text{ m}$ depth and 20 km along the line, which is close to the global oceanic average. Numerous patches with k_ρ values exceeding $10^{-2} \text{ m}^2 \text{ s}^{-1}$ with a characteristic size of $1\text{-}2 \text{ kms}$ in the horizontal dimension and $\sim 10 \text{ m}$ in the vertical are found throughout the whole section (i.e., yellowish anomalies in Figs. 3 and 5). Not only the average depth value, but also the vertical size of the anomalies, as well as the range of k_ρ variation, are in agreement with the probe-based values (Fig. 4). The contribution of the high k_ρ patches to the local average is outstanding, raising it from a background average value of $\sim 10^{-4} \text{ m}^2 \text{ s}^{-1}$ to $\sim 10^{-2.5} \text{ m}^2 \text{ s}^{-1}$.

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To try to understand the existing relationships between mixing variability and water dynamics, we have chosen two horizons that spatially coincide with anomalously high (H1) and low (H2) mixing patches, and we have individually analyzed the structures observed in the different sub-regimes.

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3.3 Analysis of a high dissipation area (H1)

H1 is located at $\sim 50 \text{ m}$ depth and has a length of $\sim 5.5 \text{ km}$ ($31.5\text{-}37 \text{ km}$ along profile). It was selected because it is laterally coherent for several kms and, it also coincides with one of the high mixing hotspots (Fig. 5). Its corresponding k_x spectrum is displayed in Fig. 6a.

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To calculate k_ρ over the whole horizon (Fig. 7a) we used the spectral energy obtained within a 1 km -wide window moving laterally 30 m at each step along the whole profile. The estimated average value for the whole H1 is $k_\rho \approx 10^{-2.6} \text{ m}^2 \text{ s}^{-1}$. To analyze the features that contribute to the energy



270 spectrum in the different scales, and to compare them in turn with the k_ρ values obtained along the
entire reflector length, the horizon has been filtered at wavelength bands attributed to subranges
dominated by internal waves (3000-100 m, IW subrange) and shear instabilities (100-33 m,
transitional subrange) (Sallares et al., 2016). As a reference, the local horizontal buoyancy
wavelength, estimated from the XCTD data is $l_N \approx 90$ m. The different spectral subranges can be
275 seen in Fig. 6a, where one of the main features is the steep slope spectra at the intermediate scale
(instabilities) that is associated with the loss of energy in the wave field due to dissipation (e.g.
Samodurov et al., 1995). The variation of the slope spectra at intermediate scale involves a direct
relation with the evolutionary stage of the vortex sheet linked to shear instabilities (Waite, 2011).

280 A striking feature is the notable, sudden decrease in the amplitude of the features observed in the
transitional subrange at ~ 34.7 km along the profile (red dashed line in Fig. 7). Interestingly, a
change in the k_ρ value is also observed at this point. Left of it (31.5-34.7 km along profile), the
average k_ρ value is $10^{-2.5} \text{ m}^2 \text{ s}^{-1}$, while right of this point (34.7-37 km), it is $10^{-3.0} \text{ m}^2 \text{ s}^{-1}$. Although
both values are higher than the average global value for meridional overturning circulation, the
285 highest local average values are obtained in the region where the clearest, largest amplitude
features, possibly representing KH billows (Sallares et al., 2016), are imaged. Conversely, there is
no clear correlation between internal wave amplitude and k_ρ variations.

3.4 Analysis of a low dissipation area (H2)

290 H2 is located at ~ 95 m depth and has a length of ~ 4.0 km (18-22 km along profile). It was selected
because its location coincides with a relatively weak mixing area, according to the k_ρ map (Fig. 5).
The corresponding k_x spectrum is shown in Fig. 6b. As in the previous case, we have first
calculated k_ρ using the spectral energy values within 1 km-wide window, moving laterally 30 m at
295 each step, along the whole reflector length. The average value for the whole horizon is $k_\rho \approx 10^{-4.1}$
 $\text{m}^2 \text{ s}^{-1}$, so considerably lower than in H1 but close to the global average value. We have
subsequently filtered H2 at the IW (3000-100 m) and transitional (100-33 m) sub-ranges and
compared it with the obtained k_ρ values (Fig. 8). In this case, we have identified three different
segments as a function of their average k_ρ value. The first and third segments (18-19.6 km and
300 20.4-22 km, respectively) display average k_ρ values that coincide, within error bounds, with those
of the global ocean average. In particular, we obtain $k_\rho \approx 10^{-4.0} \text{ m}^2 \text{ s}^{-1}$, for the first segment, and k_ρ
 $\approx 10^{-3.8} \text{ m}^2 \text{ s}^{-1}$, for the third one. The second or breaking segment, instead, displays a value of k_ρ
 $\approx 10^{-4.8} \text{ m}^2 \text{ s}^{-1}$, which is well below the global ocean average.

305 4. DISCUSSION

The spatial variability observed along isopycnals based on the spectral analysis of the seismic data
allows identifying a number of local features at different evolutionary stages. These features are
the manifestation of relevant oceanographic processes, such as breaking IWs, hydrodynamic
310 instabilities, and turbulence. Those can be identified by the disruption of the finestructure in the
seismic image and the high variability or disappearance of some seismic reflectors.

The quick variations observed in the k_ρ vertical profile (Fig. 2), together with the slight tendency
to double-diffusion identified in the Turner angle, suggest that the system is prone to be affected



315 by advection processes (e.g. Kunze and Sanford, 1996). Mixing appears to concentrate within the
MAW, where the shear values are the highest in the study area, and not deeper than > 110 m,
where there is no remarkable shear and the system is weakly stratified. The shear to strain ratio
calculated applying the Gregg89 model ($S_{10}^4/S_{GM}^4 = 21$), indicates that the energy in the IW field
is higher than that of the GM model, which usually has a value of 3. We can therefore make the
320 assumption that the energy is distributed in the whole inertial range where the water structures are
stable (e.g. Munk, 1981). Similar results were obtained by Holbrook et al, (2013), who registered
a shear to strain ratio of 17. The IWs can therefore be considered as an energy distributor from
anisotropic to isotropic motions. The k_ρ value obtained from XCTD and ADCP using Gregg89
model is $k_\rho \approx 10^{-3.0} m^2 s^{-1}$, whereas we obtain $k_\rho \approx 10^{-2.7} m^2 s^{-1}$ using MCS data and the Batchelor59
325 model. These similar values obtained based on different models and using independent techniques
are well above the global average, suggesting that the energy transfer to small scales is highly
efficient in the studied area.

We found no direct correlation between the presence of IWs and k_ρ . Thus, IW-induced mixing is
330 clearly not efficient enough to keep the overturning (Figs. 7 and 8). No clear correlation between
IW amplitude and k_ρ variation is found along H1 and H2 reflectors. This lack of correlation agrees
with Klymak and Moum (2007 a) assumption, suggesting a weak dependence of mixing rates on
IW energy. The mixing rates are more reliably measured in smaller scale regimes, in this case the
transitional regime to turbulence. In our case, a number of “mixing patches” have been identified
335 at specific locations in the k_ρ map (Fig. 3), which appear to spatially coincide with areas of IW
instability. These mixing hotspots likely represent a significant source of regional diapycnal
mixing at the boundary layer between the MAW and the MW (30 – 200 m), which is subject to
vertical stratification and shear values of $3.2 \times 10^{-3} s^{-1}$. The mixing and energy transfer between
these two water masses constitutes the main energy source of the region. The smooth and relatively
340 deep seafloor along the profile (> 800 m in average; Fig. 9b), allows discarding mixing hotspots
to be a consequence of water-seafloor interaction. Given that the MAW-MW boundary layer is
subject to shear (Fig. 9a), we hypothesize that the direct cause of mixing hotspots is the
development of IW shear instabilities. This could explain both the peak values of k_ρ and the high
variability along the profile.

345 The k_ρ values along H1 are over the global average for overturning along most of the reflector
($\langle k_\rho \rangle \approx 10^{-2.5} m^2 s^{-1}$), with lower values only at specific points (Fig. 7a). These points are located to
the right of 34.7 km, where k_ρ sharply decreases. The spatial correspondence between high
diffusivity values and the presence of KH billows at the transitional subrange is consistent with
350 the hypothesis that a causal relationship exists between the two. This is conceptually equivalent to
the mechanism proposed by Gregg (1987), where mixing at the transitional subrange occurs
principally at vortex sheets through wave-instability. We could therefore hypothesize that the
presence of a vortex sheet left of 34.7 km along profile produces the high mixing values; whereas
to the right, there is no vortex sheet and the ocean is more stable. Similar results suggesting a
355 patchy ocean interior, although at larger scales and deeper levels, were also presented by Sheen et
al. (2009) and Fortin et al. (2016). Our work confirms these previous results and suggests that the
variation is probably due to the high mixing induced by the shear instabilities; which enhances in
turn energy transfer to smaller scales.



360 5. CONCLUSIONS

We have used acoustic images obtained with a high-resolution MCS system to produce 2D diapycnal mixing maps at the thermocline depth. Our results confirm a high level of diapycnal variability and the presence of marked mixing patches in the water column. The $k_{\rho}(x, z)$ map
365 obtained by applying the Batchelor59 model to the seismic data, has an average $\langle k_{\rho} \rangle \approx 10^{-2.7} m^2 s^{-1}$, comparable in both magnitude and range of vertical variability with the value of $\langle k_{\rho} \rangle \approx 10^{-3.0} m^2 s^{-1}$ obtained applying the Gregg89 model to XCTD and ADCP data. The obtained values are high enough to account for overturning at thermocline depths. The mixing hotspots have a characteristic size of 10-15 m in the vertical dimension, and 1-2 km in the horizontal one. They are
370 located at different depths within the thermohaline layer, although they appear to concentrate in highly sheared regions. Both the mixing values and the vertical scale of the features imaged with the two independent methods and approaches are consistent within uncertainty bounds; confirming that HR-MCS is a useful technique to study processes and structures occurring at the sub-mesoscale, which are difficult to be studied otherwise.

375 The relationship between mixing variability and ocean dynamics at different spatial scales is investigated by analyzing the spectral amplitudes along two seismic horizons in the internal waves and transitional subranges. On the one hand, we found no clear correlation between the location of the mixing patches and the presence and amplitude of IWs, confirming that IWs do not appear
380 to produce overturning. Conversely, a correspondence exists between the location of shear instabilities and mixing hotspots, suggesting a causal relationship between both features. Areas displaying the most vigorous instabilities coincide with the highest estimated diapycnal mixing values, which are well above the average global value for meridional overturning. This observation suggests that the energy transfer from anisotropic to isotropic scales is highly efficient at
385 thermocline depths within the studied area.

Overall, our study shows that the HR-MCS technique can be used to study sub-mesoscale structures and processes at the thermocline level, provided that the stratification is strong enough to produce acoustic reflectivity that can be recorded by the system. The high-resolution 2D maps
390 produced from the seismic reflectivity could help improving the estimates of the parameters to be incorporated in numerical models of ocean dynamics.

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400 David M. Holland from the Center for Global Sea Level Change (CSLC) – NYUAD, Abu Dhabi UAE.

APPENDIX A



405 Table A1. Parameters used in text

Variable	Value	Description
f	0.00008613 s ⁻¹	Coriolis f. at 36°
N	5 cph = 0.00138 s ⁻¹	Buoyancy frequency (ocean average)
V	0.207 m s ⁻¹	RMS amplitude of velocity fluctuations
ν	0.000001064 m ² s ⁻¹	Kinematic Viscosity
C_T	0.4	Proportionality constant
Γ	0.2	Empirical value of mixing efficiency (Osborn and Cox, 1972).

APENDIX B

Buoyancy Reynolds number

410

Gargett et al, (1988) use an index to know if the system is isotropic or not, and hence if the allowing know if the buoyancy flux is substantial to generate turbulence and therefore a high mixing level (Thorpe, 2005). The index depends on kinematic viscosity and is called Buoyancy Reynolds number:

415

$$R_B = \varepsilon / \nu N^2 \quad (\text{B1})$$

420

The mean kinematic viscosity in the ocean is $\nu = 1 \times 10^{-6} \text{ m}^2 \text{ s}^{-1}$. Some properties of the inertial subrange are consistent with isotropy for values of $R_B < O(10^2)$. To consider anisotropy and avoid serious underestimates of mixing, Smyth and Moum (2000) propose that values > 200 are related with confidence to high mixing levels due to free viscous effects. For our submesoscale regime $R_B = 3200$, a value that reasserts the coherence of the mixing levels calculated. The MCS data present a high confidence level.

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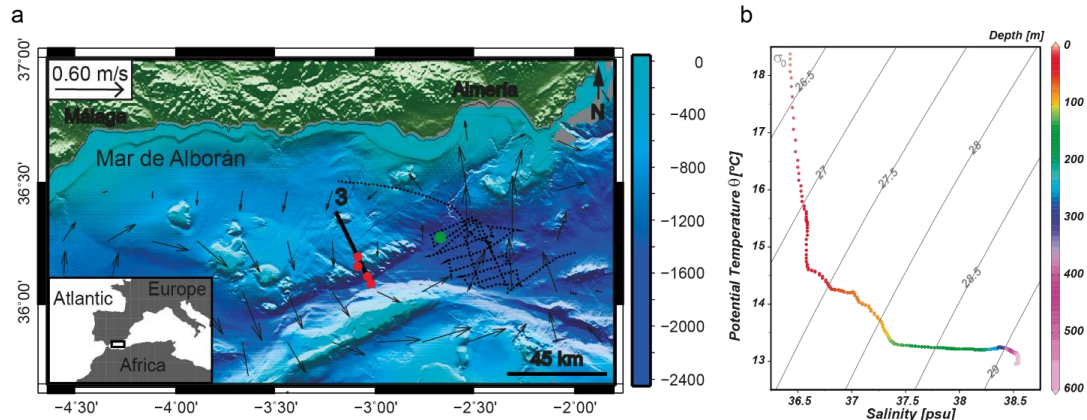


Figure 1. (a) Bathymetric map of the Alboran Sea and location of the data used in the study. HR-MCS profile acquired during the IMPULS-2006 experiment (black line labelled 3), eXpendable Bathy-Thermograph (XBTs) profilers (red circles), eXpendable Conductivity Temperature Depth (XCTD) probe (green circle). Acoustic Doppler Current Profiler (ADCP) lines (black dotted line). Geostrophic velocity for May 17th, 2006 (gray arrows). (b) Temperature-Salinity diagram from XCTD probe. σ_0 is the potential density in kg/m^3 . Color scale indicates depth.

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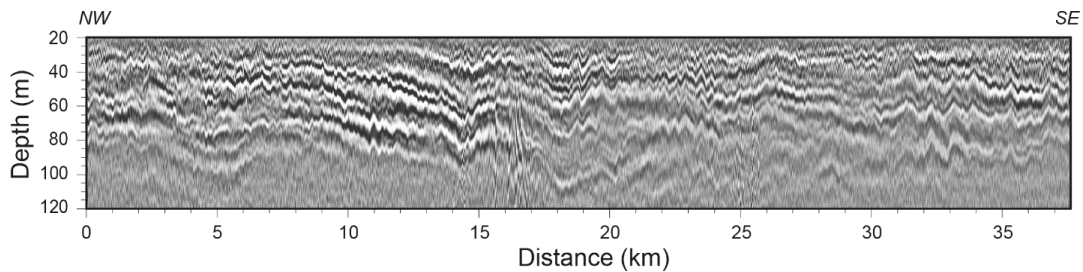
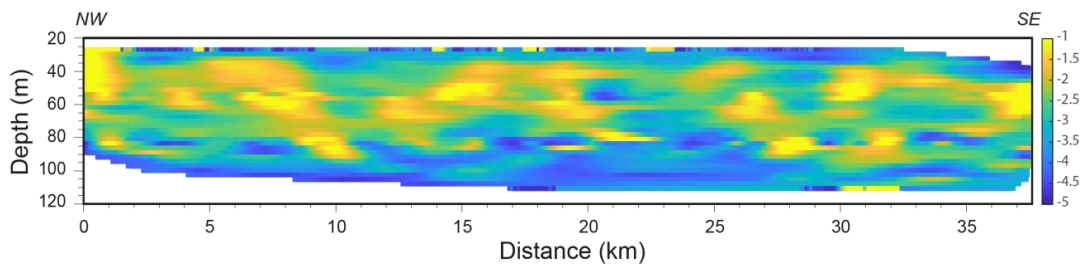


Figure 2. Depth-converted high-resolution multichannel seismic profile (See Fig. 1a for location).



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Figure 3. $k_\rho(x, z)$ map obtained along the seismic profile indicated in Fig.1, following the procedure explained in the text.

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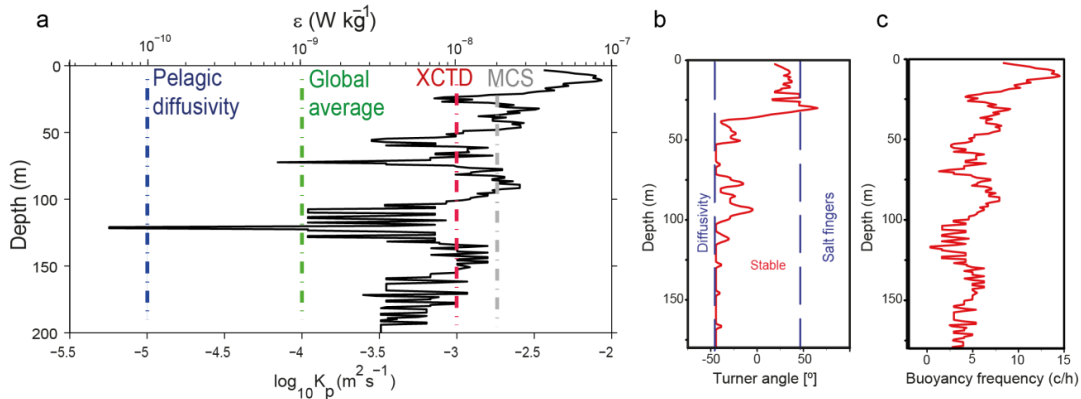


Figure 4. (a) Depth profile of $\epsilon(z)$ and $k_p(z)$ obtained from XCTD and ADCP data and applying Gregg89 model. The blue dotted line is the pelagic diffusivity in the ocean ($k_p \approx 10^{-5} \text{ m}^2 \text{ s}^{-1}$), the
 555 green dotted line is the global average for overturning ($k_p \approx 10^{-4} \text{ m}^2 \text{ s}^{-1}$), the red dotted line is the average vertical profile from XCTD and ADCP data ($k_p \approx 10^{-3.0} \text{ m}^2 \text{ s}^{-1}$) and the gray dotted line is the average vertical profile from MCS data ($k_p \approx 10^{-2.7} \text{ m}^2 \text{ s}^{-1}$). (b) Turner angle showing ranges, the blue dotted lines shows where the water column is unstable to diffusivity ($Tu < -45^\circ$), stability ($-45^\circ < Tu < 45^\circ$) and prone to salt fingering ($Tu > 45^\circ$), and (c) buoyancy profile calculated with the XCTD data.
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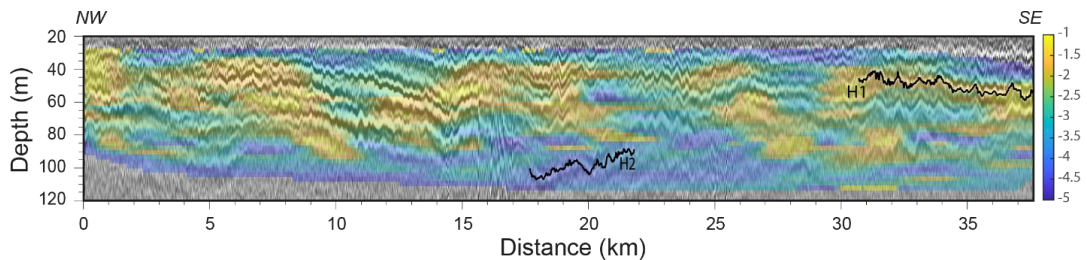
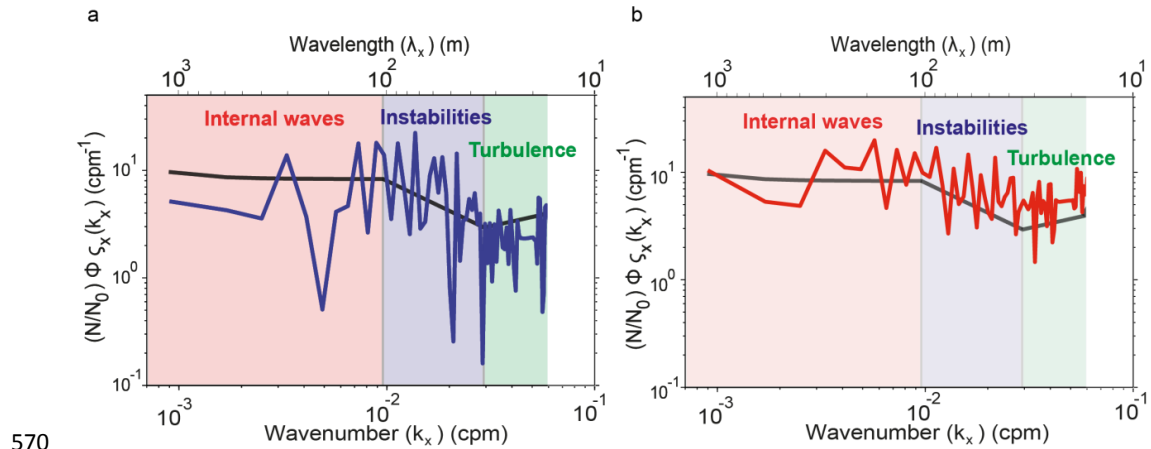
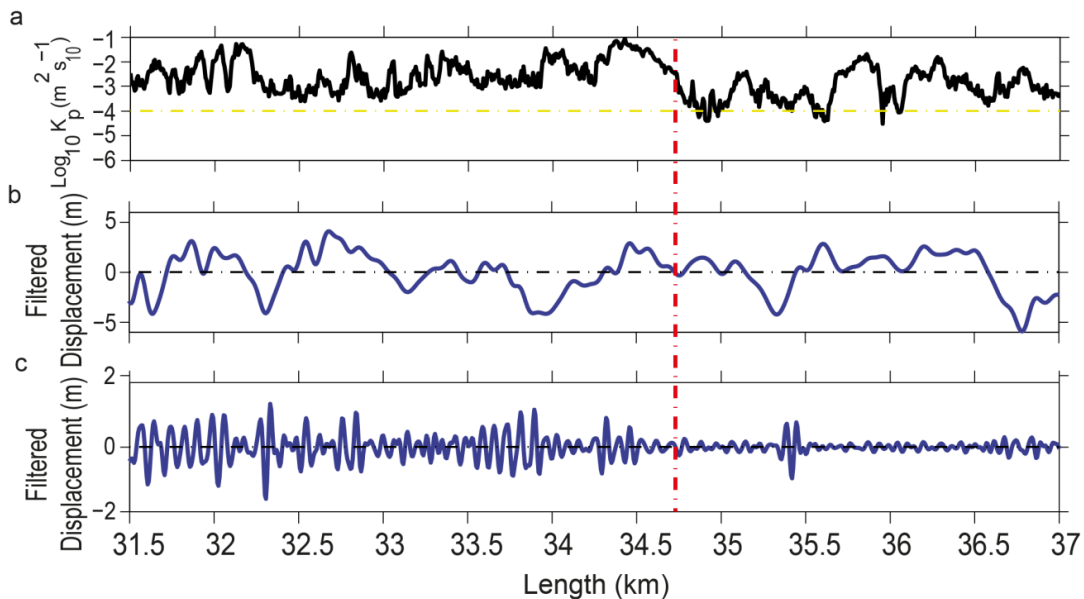


Figure 5. High-resolution $k_p(x, z)$ map overlapped with the HR-MCS image. Solid lines labelled H1 and H2, display acoustic reflectors located within relatively high- and low-dissipation areas.



570 Figure 6. (a) Horizontal spectrum of the vertical displacement of reflector H1 (blue) (see location
 in Fig. 5). (Black line) Reference line that follows theoretical slopes of Garret-Munk internal wave
 model (Garret and Munk, 1979), Kelvin-Helmholtz instabilities (Waite, 2011), and Batchelor
 575 model for turbulence (Batchelor, 1959). The methodology applied to calculate the spectra is
 described in Sallares et al (2016), (b) same as in (a) for reflector H2 (red) in this case.



580 Figure 7. (a) Diapycnal mixing obtained along H1 (see details of calculation in the text). (b) Signal
 filtered at wavelength ranges of the IW sub-range (3000-100 m), (c) and the transitional subrange
 (100-33 m). The dashed red line identifies the “breaking point” referred to in the text.

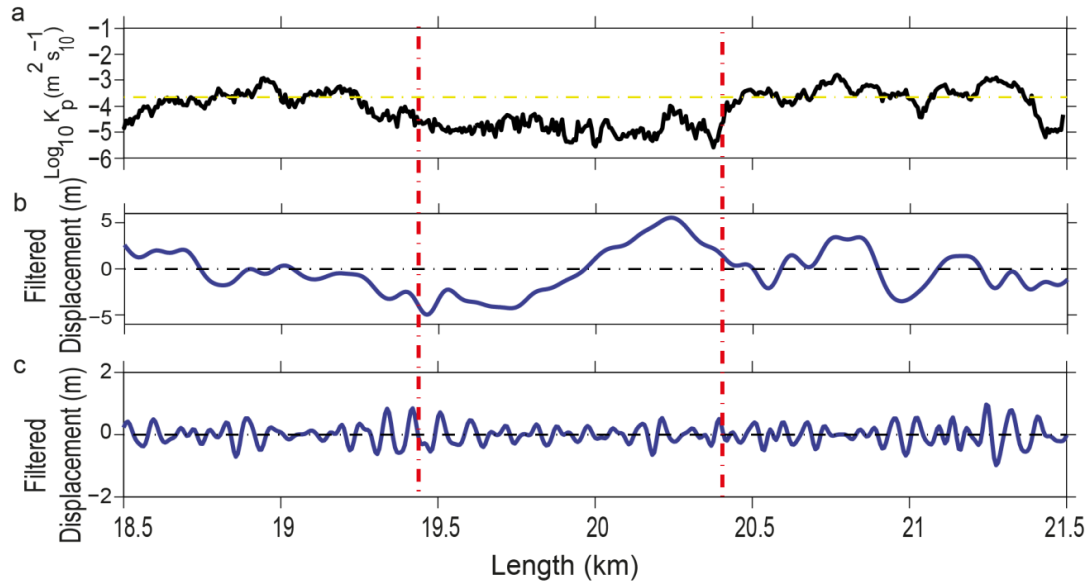


Figure 8. (a) Diapycnal mixing obtained along H2 (see details of calculation in the text). (b) Signal filtered at wavelength ranges of the IW sub-range (3000-100 m), (c) and the transitional subrange (100-33 m). The dashed red lines identifies the “breaking segment” referred to in the text.

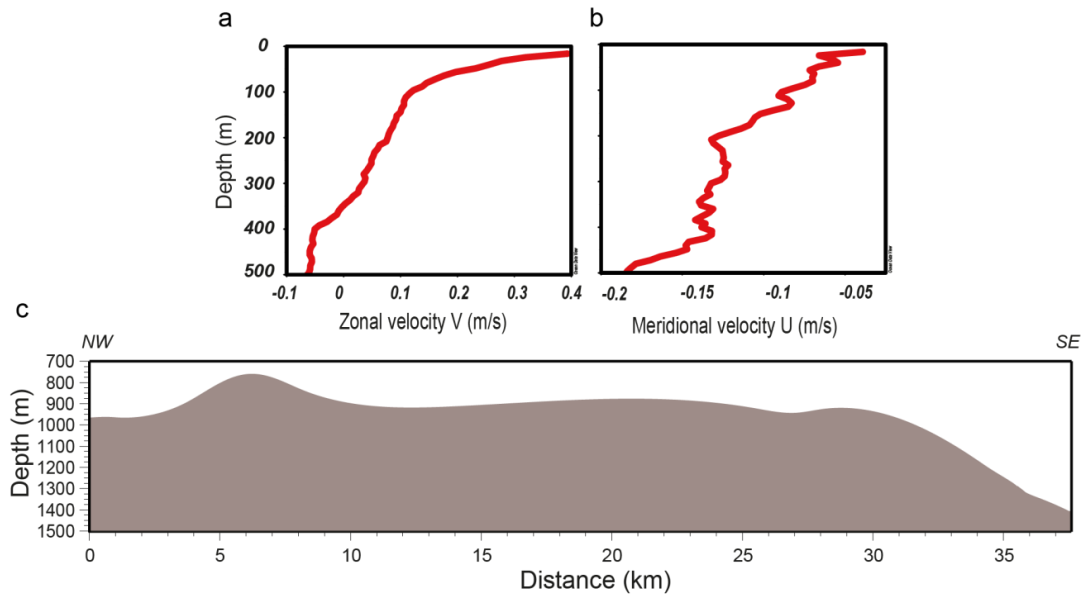


Figure 9. (a) Current velocity profile from ADCP data, SAGAS in May, 2010. (V) The zonal velocity variations, and (b) (U) the meridional velocity variations according to the depth. (c) Bathymetric profile over the seismic profile.