

1 **Using kinetic energy measurements from altimetry to detect shifts in the**
2 **positions of fronts in the Southern Ocean**

3 Don P. Chambers¹

4 ¹ College of Marine Science, University of South Florida, St. Petersburg, FL

5 Correspondence to: D. Chambers (donc@usf.edu)

6

7 **Abstract.** A novel analysis is performed utilizing cross-track kinetic energy (CKE) computed

8 from [along-track](#) sea surface height anomalies. The mid-point of enhanced kinetic energy
9 averaged over three-year periods from 1993 to [2016](#) is determined across the Southern Ocean

10 and examined to detect shifts in frontal positions, based on previous observations that kinetic

11 energy [is high around fronts in the Antarctic Circumpolar Current system due to jet instabilities](#). It

12 is demonstrated that although the CKE does not represent the full eddy kinetic energy (computed

13 from crossovers), the shape of the enhanced regions along groundtracks is the same, and CKE

14 has a much finer spatial sampling of 6.9 km. Results indicate no significant shift in the front

15 positions across the Southern Ocean, on average, although there are some localized, large

16 movements. This is consistent with other studies utilizing sea surface temperature gradients, the

17 latitude of mean transport, [and probability of jet occurrence](#), but [is](#) inconsistent with studies

18 utilizing the movement of contours of dynamic topography.

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28 **1. INTRODUCTION**

29 There is as much we don't know about the circulation of the Southern Ocean as we do.
30 Although the current system is routinely called the Antarctic Circumpolar Current (ACC), it
31 consists of several fronts with distinct water properties to the north and south of the fronts
32 (Nowlin and Clifford, 1982; Orsi et al., 1995; Belkin and Gordon, 1996). The most significant of
33 these fronts, responsible for the majority of the ACC volume transport (e.g., Cunningham et al.,
34 2003), are the Subantarctic Front (SAF) and the Polar Front (PF). However, even this is not a
35 realistic picture of the circulation in the Southern Ocean, since at any specific time, there can be
36 from three to ~~ten~~ narrow jets around the fronts that are highly variable in strength and location,
37 masking the specific frontal boundary (Sokolov and Rintoul, 2007, 2009a, 2009b; Saltee et al.,
38 2008; Thompson et al., 2010; Thompson and Richards, 2011; Langlais et al., 2011; Graham et
39 al., 2012; Chapman, 2014; Gille, 2014; Kim and Orsi, 2014; Shao et al., 2015; Chapman, 2017a).
40 Although positions of fronts have been estimated throughout the Southern Ocean, primarily
41 using gradients of subsurface density measured from hydrographic sections (Orsi et al., 1995),
42 contours of dynamic topography (Sokolov and Rintoul 2007, 2009a, 2009b; Langlais et al.,
43 2011), or a combination Kim and Orsi (2014), in many places there are no strong currents that
44 can be measured near the front position (Chapman, 2014; 2017a).

45 Because of the highly variable nature of jets and the lack of clear observational detection of
46 fronts in some areas, the literature has become muddled over the difference between a front and a
47 jet, primarily because the "front" is rarely observed at any specific time due to the high-
48 variability of jets (Thompson et al., 2010; Thompson and Richards, 2011; Chapman 2014;
49 2017a). However, even in the presence of highly variable jets, methods have been developed to
50 determine mean fronts positions in a probabilistic sense. Thompson et al. (2010) demonstrated

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58 | [one could define fronts in the Southern Ocean by computing probability density functions of](#)
59 | [potential vorticity in an eddy-resolving general ocean circulation model. Chapman \(2014, 2017a\)](#)
60 | [later showed this could also be done using localized gradients in dynamic topography \(i.e., high](#)
61 | [geostrophic velocity\) using satellite altimeter observations, but again, only as statistical](#)
62 | [probability. This is because these areas of enhanced gradients and velocity are more reflective of](#)
63 | [jets, which strengthen and die, appear and disappear, bifurcate and join back together. Because of](#)
64 | [this, they can only be detected on average 10-15% of the time. However, Chapman \(2014,](#)
65 | [2017a\) has demonstrated that, at least in a mean sense, fronts defined by mean dynamic](#)
66 | [topography contours \(commonly known as the “contour method”\) do lie within the probability](#)
67 | [distribution inferred from “gradient” methods.](#)

68 | An open question is how the [fronts and jets](#) that comprise the ACC will respond in a
69 | warming climate. Analysis of climate models [\(which cannot simulate jets in the Southern Ocean\)](#)
70 | suggests that as the atmosphere warms, the winds that drive the fronts [and jets](#) of the ACC will
71 | migrate south (e.g., Fyfe and Saenko, 2006; Swart and Fyfe, 2012). It should be noted, however,
72 | that the mean position of the southern hemisphere westerlies in the models lies significantly
73 | equatorward of the true position [\(e.g., Figure 2 in Fyfe and Saenko, 2006\)](#). Thus, it is not entirely
74 | clear whether the model is predicting a true shift in the wind position, or whether the model has
75 | not yet reached equilibrium with winds in the proper location.

76 | Still, based on these model results, researchers have been testing [the](#) hypothesis that as winds
77 | in the Southern Ocean shift south, the frontal positions and jets will also migrate south. So far,
78 | the results are mixed. [Using the contour method and tracking how the dynamic topography](#)
79 | [contours associated with a front position shift in time, Sokolov and Rintoul \(2009b\) found that](#)
80 | [the SAF and PF had both moved south by approximately 60 km over 15 years between 1993 and](#)

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Deleted: proposed a method based on finding the contour of a mean dynamic topography associated with the steepest meridional gradient of dynamic topography (i.e., zonal geostrophic current) and associate this with a front or jet. They could then track the latitude of that contour over time to deduce if the front had moved. When averaged over all longitudes, their analysis indicated

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2008, Kim and Orsi (2014) recently updated this analysis and found that while the average frontal position across the Southern Ocean indicates a strong southward shift, this is due primarily to substantial shifts only in the Indian Ocean sector. They found no significant shifts throughout the Pacific or Atlantic Ocean sectors using the contour method.

The primary assumption of these analyses is that if a contour of dynamic topography shifts south, it is uniquely caused by a front moving south. This is not necessarily true. Gille (2014) recently demonstrated that all contours in the Southern Ocean have shifted south on average, and that this follows from the observed rise in sea level – as the sea surface height rises, the contours will appear to shift south. While this breaks down at the far south and north of the ACC where dynamic topography gradients are small, these areas are far away from the PF and SAF and so have not been considered in previous analyses. Gille (2014) used a different measure to determine the position of the ACC fronts, based on the latitude of the mean surface transport of the ACC measured by altimetry, which is in essence a mean location of all the jets in the Southern Ocean. She found no significant shift on average, but considerable interannual variability, especially regionally.

Another factor other than sea level rise can cause the dynamic topography contour to shift south -- if the magnitude and width of the jet has changed. This is demonstrated in Figure 1, where we show the mean dynamic topography from two jet scenarios: 1) where the peak of two Gaussian shaped jets have shifted south, and 2) where the peak has not shifted, but the magnitude has decreased, the width has broadened, and the shape has become slightly skewed. Although the resulting topography profiles are not identical, they are similar, and both suggest a southward movement of dynamic topography contours.

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169 Researchers using other methods also find little or no southern migration of the fronts or jets
170 in the Southern Ocean as a whole. Graham et al. (2012) used a high-resolution model to show
171 that the Polar Front and Subantarctic Front are constrained by bathymetry, even in increasing and
172 shifting winds. Shao et al. (2015) utilized the skewness of sea level anomalies to identify front
173 positions, and found no southward motion, but did find changes in the east Pacific correlated
174 with the Southern Annual Mode. Chapman (2017a), using positions of fronts determined from
175 the probability of jet locations, also found no significant southward movement, but high
176 interannual variability. Finally, Freeman and Lovenduski (2016a) used weekly estimates of the
177 Polar Front position determined from satellite sea surface temperature (SST) gradients to show
178 no significant southward shift between 2002 and 2014 on average, except in the Indian Ocean.
179 They also found a statistically significant northward shift of the PF in part of the south Pacific.

180 Thus, recent studies all agree that the Subantarctic Front and Polar Front have not shifted
181 south, even though there is evidence the winds have shifted south in the austral summer months
182 (Swart and Fyfe, 2012). It should be noted that when averaged over the full calendar year,
183 however, there has been no significant shift in the wind position (Swart and Fyfe, 2012).

184 In this paper, we develop a new method to study variability in the position of the fronts in the
185 Southern Ocean, based on tracking the location of envelopes of kinetic energy measured by
186 satellite altimetry. It is known from modeling studies that the front positions are associated with
187 increased kinetic energy, due to instabilities in the jets and interactions with bathymetry
188 (Thompson et al., 2010; Thompson and Richards, 2011). After demonstrating that kinetic energy
189 computed from along-track satellite altimetry forms relatively wide envelopes of enhanced
190 energy that occur within the probability range of jets and fronts (e.g., Chapman, 2017a), we track
191 the positions of these envelopes from 1993 until 2016 to quantify if the envelopes have shifted

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207 south by a statistically significant amount. This is based on the assumption that if the front and
208 jets around the front have shifted south, then the envelope of high kinetic energy should also
209 move by a comparable amount. Since the kinetic energy calculation is based on estimating
210 gradients of sea level anomalies, this approach is similar to other gradient methods for detecting
211 fronts or jets (e.g., Chapman, 2014; 2017a; Gille, 2014; Freeman and Lovenduski, 2016a). It
212 differs from these approaches, however, in that instead of determining individual gradients and
213 tracking these over time, it looks for regions of high gradients (i.e., high energy) surround by
214 regions of low gradient (i.e., low energy). This allows us to detect envelopes for every time-
215 period considered, instead of only a fraction of the time, allowing for better tracking of the
216 change over time.

217 Section 2 will describe the data and methods used, while section 3 will present results,
218 including evaluation of the method for detecting mean positions of fronts and for tracking their
219 change over time. Section 4 will discuss the results in the context of previous studies and
220 evaluate the usefulness of the method.

221 2. DATA AND METHODS

222 We utilize geostrophic surface current anomalies computed from the 24-year record of 1-Hz
223 sea surface height (SSH) data along the TOPEX/Poseidon (T/P) groundtrack in the Southern
224 Ocean (Figure 2). The altimetry data used are from four separate altimeter missions:
225 TOPEX/Poseidon (January 1993 – January 2002), Jason-1 (February 2002 – July 2008), Jason-2
226 (August 2008 – August 2016), and Jason-3 (August 2016 – December 2016). Because the
227 official TOPEX/Poseidon (T/P) geophysical data records (GDRs) have not been updated since
228 the late 1990s, we utilize the corrected data products from the Integrated Multi-Mission Ocean
229 Altimeter Data for Climate Research provided by Beckley et al. (2010) at the NASA PO.DAAC

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244 [site \(https://podaac.jpl.nasa.gov/Integrated_Multi-Mission_Ocean_AltimeterData\)](https://podaac.jpl.nasa.gov/Integrated_Multi-Mission_Ocean_AltimeterData). Jason-1 data
245 [are from the GDR-C version and were downloaded from the NASA PO.DAAC site in June 2010.](#)
246 [Jason-2 are from the GDR-D version and were downloaded from NOAA NODC](#)
247 [\(ftp://ftp.nodc.noaa.gov/pub/data.nodc/jason2\)](ftp://ftp.nodc.noaa.gov/pub/data.nodc/jason2) between August 2012 and June 2016. Jason-3 are
248 [also from the GDR-D version and were downloaded from NOAA NODC](#)
249 [\(ftp://ftp.nodc.noaa.gov/pub/data.nodc/jason3\)](ftp://ftp.nodc.noaa.gov/pub/data.nodc/jason3) on August 7 and 8, 2017.

250 [We utilize the 1-Hz along-track SSH data from the four altimeters and compute sea level](#)
251 [anomalies by interpolating the DTU10 mean sea surface model \(Andersen and Knudsen, 2009;](#)
252 [http://www.space.dtu.dk/english/Research/Scientific_data_and_models/downloaddata\)](http://www.space.dtu.dk/english/Research/Scientific_data_and_models/downloaddata) to the
253 [SSH location using bilinear interpolation. The DTU10 mean sea surface model is based on SSH](#)
254 [from multiple altimeters averaged over 17 years in a rigorous and consistent manner \(Andersen](#)
255 [and Knudsen, 2009\). T/P, Jason-1, and Jason-2 data were all included. All recommended](#)
256 [geophysical and surface corrections \(e.g., water vapor, ionosphere, sea state bias, ocean tides,](#)
257 [inverted barometer, etc\) have been applied, to correct for biases introduced by atmospheric](#)
258 [signal refraction and sea state effects \(e.g., Chelton et al., 2001\).](#)

259 [We utilize this record rather than the gridded products based on mapping SSH from multiple](#)
260 [altimeters \(e.g., Ducet et al., 2000; Pujol et al., 2016\), because the along-track data have a finer](#)
261 [resolution in space \(6.9 km along the groundtrack\) and we recently demonstrated that the](#)
262 [mapped altimetry data underestimated eddy kinetic energy \(EKE\) throughout the Southern](#)
263 [Ocean compared to using along-track data by as much as 60-70% \(Hogg et al., 2015\). While the](#)
264 [along-track sea level anomalies are filtered to reduce noise and thus may attenuate some signal,](#)
265 [the filtering used \(described later in this section\), is less than that used for the mapped data,](#)
266 [which uses observations from as long as 20 days and 200 km away to influence the mapped](#)

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270 value. By filtering only alongtrack data, the time differences are small (a few minutes at most),
 271 and the spatial influence is less than 100 km. Tests with unfiltered data accounting for estimated
 272 random noise in the sea level anomaly data suggests attenuation of kinetic energy is minimal
 273 with this approach and, more importantly, that the shape of the kinetic energy envelope does not
 274 significantly change.

275 One can only compute EKE from alongtrack data at crossover points, where the ascending
 276 and descending groundtracks cross (Figure 2). Knowing the groundtrack angle with the north
 277 meridian (θ) one can compute the zonal ($d\eta/dy$) and meridional gradients ($d\eta/dx$) of SSHA
 278 directly from the gradients of SSHA for the ascending pass ($d\eta/dr_{asc}$) and descending pass
 279 ($d\eta/dr_{des}$) using simple geometry (Parke et al., 1987)

$$\frac{d\eta}{dy} = \frac{\left[\frac{d\eta}{dr_{asc}} - \frac{d\eta}{dr_{des}} \right]}{2 \sin \theta}, \quad \frac{d\eta}{dx} = \frac{\left[\frac{d\eta}{dr_{asc}} + \frac{d\eta}{dr_{des}} \right]}{2 \cos \theta} \quad (1)$$

281 noting that this formulation assumes the gradients represent the derivative of the northern SSHA
 282 relative to the southern SSHA (for both the ascending and descending passes). Once this is
 283 computed, the velocities can be computed directly from the zonal and meridional gradients:

$$u = -\frac{g}{f} \frac{d\eta}{dy}, \quad v = \frac{g}{f} \frac{d\eta}{dx} \quad (2)$$

285 where g is the acceleration due to gravity, and f is the Coriolis parameter

286 This formulation assumes that the velocity field has not changed significantly between the
 287 times the two passes fly over the crossover point. At high latitudes, the majority of crossovers (\geq
 288 78%) have a time separation of less than 3 days. At 40° , the average propagation speed of an
 289 eddy is about 3 cm s^{-1} [Chelton et al., 2007], meaning the eddy would have only been displaced

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303 by 8 km at most over this period. At higher latitudes, this is even less. Considering the diameter
 304 of eddies at these latitudes are of order 100 km [Chelton et al., 2007], the movement is not large
 305 enough to cause a significant change in velocity at the point. The primary problem with
 306 velocities computed from crossovers is the smaller number compared to using gridded data, or
 307 the time-varying, anomalous geostrophic current normal to the groundtrack (u_T). This can be
 308 computed directly from the derivative of the SSH anomaly (η) along the ground-track distance
 309 (dr) from

$$u_T = -\frac{g}{f} \frac{d\eta}{dr} \quad (3)$$

311 This cross-track current is a projection of both the zonal (u) and meridional (v) components of
 312 the full anomalous velocity field. However, neither u nor v can be determined unambiguously
 313 from u_T . Here, we merely examine the variability of u_T without making any assumptions
 314 concerning how it may be related to the full velocity, or u and v .

315 Because derivatives of SSHA (Equations 1 and 3) have to be computed numerically (here,
 316 center-differences are used) and η contains significant noise at the 1 Hz sampling-rate of the
 317 altimeters, we optimally interpolate η along-track using a model of the covariance of the signal
 318 and error. We used the method of Wunsch (2006, Chapter 3) and a covariance function modeled
 319 as a Gaussian with a roll-off of 98 km and random noise of 2 cm, which was determined from the
 320 autocovariance of all TOPEX/Poseidon, Jason-1, and Jason-2 SSHA data from 1993-2015
 321 between 40°S and 65°S.

322 Once $u_T(t)$ was computed at each 1-sec bin along the groundtracks in Figure 2 for each 10-
 323 day repeat cycle, the cross-track kinetic energy (CKE) was computed as $CKE(x,t) = 0.5 u_T(x,t)^2$,

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338 where x here is used to denote a generic 1-sec bin along the ground track. We also computed the
339 full EKE at the more limited crossover points as $EKE(x,t) = 0.5(u(x,t)^2 + v(x,t)^2)$.

340 The CKE values were averaged over the entire 24-year record and examined for each
341 groundtrack segment (both ascending and descending) to judge where CKE was exceptionally
342 high (Figure 3). We also computed CKE using the raw values of η with no optimal interpolation
343 and compared to that computed with optimal interpolation. The locations of high CKE were the
344 same, although values were significantly higher with the unsmoothed data. The quiescent regions
345 of the ocean also showed considerably more noise, making it more difficult to determine
346 boundaries of elevated CKE. For this reason, the values determined from the optimally
347 interpolated data were used.

348 Several criteria were utilized to quantify where the high CKE values were considered to be
349 associated with fronts. First, we constrained the southern boundary to be 5° south of the Orsi et
350 al. (1995) values of the PF and the northern boundary to be 5° north of the SAF. Secondly, we
351 used a lower-limit for CKE of $200 \text{ cm}^2 \text{ s}^{-2}$ for detection and tested that the width of the envelope
352 of high CKE above the lower-limit was at least 100 km. The requirement that the envelope be
353 greater than 100 km was done to reduce the impact of eddies in an otherwise quiescent region,
354 since the diameter of eddies in the Southern Ocean is about 100 km. The CKE lower-limit was
355 determined via iteration with different limits. For each case, the average center of the CKE
356 envelope averaged over 24-years (based on the mean of the first and last points to exceed the
357 lower-limit) was computed and compared visually to the Orsi et al. (1995) front positions. 200
358 $\text{cm}^2 \text{ s}^{-2}$ was selected because there were a significant amount of CKE envelope centers clustered
359 around the Orsi et al. (1995) fronts and the envelopes were found for every 10-day repeat cycle.
360 Using a higher limit resulted in fewer detections, especially when smaller time-averages were

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368 used. Using a lower limit, we could find more potential front positions based on CKE, but many
369 were far from the front positions estimated by Orsi et al (1995).

370 An example of a detected high CKE envelope is shown in Figure 3, based on the average of
371 CKE between 1993 and 2015 computed from T/P-Jason satellite pass 207 in the south Indian
372 Ocean. This pass starts at 64.3°S near the prime meridian and extends to 41.2°S and 41°E
373 longitude. There is clearly a wide envelope of enhanced CKE greater than $200 \text{ cm}^2 \text{ s}^{-2}$ between
374 55°S and 47°S.

375 The mean CKE profile pictured in Figure 3 has multiple local maxima, most likely associated
376 with variability of the narrow jets that surround the front. As shown by Chapman (2017a), these
377 jets (evidenced in higher gradients of SSHA) do not occur around a front 100% of the time. At
378 most, they occur about 30% of the time, and more often less than 15% of the time. Figure 4
379 shows the behavior of CKE along this pass for different 3-year periods. Note that the number of
380 clearly defined maxima ranges from a low of 4 for the 2014-2016 average to 9 in 1993-1995.
381 While other studies have estimated positions of these maxima in SSHA gradients on daily
382 intervals (e.g., Chapman, 2017a), one does not obtain a consistent number of maxima each time,
383 making the determination of shifts difficult. Moreover, note that although there are two general
384 peaks in CKE in the long-term mean profile, the minimum between them is still higher than 200
385 $\text{cm}^2 \text{ s}^{-2}$. A minimum is also not well defined in several of the shorter averaging periods (for
386 example, 2008-2010).

387 Thus, instead of attempting to track all the maxima of CKE individually – analogous to
388 tracking steepest gradients, as in Thompson et al. (2010), Graham et al. (2012), or Chapman
389 (2017a) – we track an estimate of the center of the envelope of enhanced CKE, as it exists in all
390 averaging periods. The assumption we make in doing this is that the localized maxima are

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Deleted: The value of $200 \text{ cm}^2 \text{ s}^{-2}$ was chosen over a lower value because it was found that the regions selected with the $200 \text{ cm}^2 \text{ s}^{-2}$ were consistent from one 10-day period to another. Using lower minimum values resulted in areas of high CKE activity being detected in some cycles, but not others. An example is the small rise in mean CKE at 41°S in Figure 3. Although the mean CKE is about $150 \text{ cm}^2 \text{ s}^{-2}$, suggestive of a jet, this all but disappears for some periods of time. This behavior of jets has been observed in models (e.g., Thompson and Richards, 2011). Thus, the minimum CKE was selected to be as conservative as possible.
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420 associated with variable jets, but the position of the envelope of high CKE is related to the front.

421 There are many different ways to compute a “center” of the envelope, ranging from the
422 average of the two end points, to a centroid calculation, to computing the point where the integral
423 of CKE over distance is balanced on both sides, which we call the “half-power point.” We have
424 selected the latter to use, as it defines a “center” closer to the peak of CKE in the envelope. This
425 is advantageous when the CKE curve is slightly skewed, with less magnitude on one side and
426 more on the other. Assuming that the variability (and hence CKE) would be highest near the
427 front (i.e., what is assumed in studies using the gradient method), finding a center of the
428 envelope that is biased toward peak CKE is a reasonable approach.

429 The half-power point (x_{mid}) is computed so that

430
$$\int_{x_{south}}^{x_{mid}} CKE(x) dx = \frac{1}{2} \int_{x_{south}}^{x_{north}} CKE(x) dx \quad (4)$$

431 where x_{south} and x_{north} are computed by first finding the maximum of CKE in the envelope above
432 $200 \text{ cm}^2 \text{ s}^{-2}$, then finding the first value to the north just below 25% of that peak along with the
433 similar value to the south (shown in Figure 3). Values other than 25% of the peak were tested.
434 Using value greater than this, up to 50%, resulted in no significant difference in the half-power
435 point. Using values smaller resulted in some boundaries not being defined. Thus, 25% of peak
436 CKE was considered reasonable. If multiple regions of enhanced CKE were found along the
437 same track, this process was carried out for each of them. This was done for all the 24-year mean
438 CKE profiles to establish the mean locations of the fronts between 1993 and 2016.

439 A similar procedure was done for CKE averaged over discrete 3-year intervals, starting in
440 January 1993 and ending in December 2016. A 3-year average was used to reduce the influence

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Deleted: Most of the other profiles examined had similar features. We initially tried tracking each of the maxima, but that quickly became complicated because sometimes the four or local maxima would become five, or even just one. This is likely due to the instability of the jets around the front. In order to ensure consistency and assuming the mean of the region of high CKE followed the front position, the half-power point, or centroid, of the CKE bump was computed. This is similar in principle to the computation made by Gille (2014) of the latitude of the mean ACC transport, except here we are focused on mean of the CKE around a particular front, not over all the fronts of the ACC. ... [4]

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472 of individual eddies on determining the envelope, and to reduce interannual variations in the
 473 front position, which have been observed in other studies at some locations (e.g., Kim and Orsi,
 474 2014; Shao et al., 2015). In particular, Kim and Orsi (2014) and Shao et al. (2015) found
 475 significant correlation with the Southern Annular Mode, which has a quasi-biennial oscillation
 476 (Hibbert et al., 2010). By averaging over three years, we found 8 distinct, statistically
 477 uncorrelated samples of CKE for each groundtrack from which to deduce shifts in the half-power
 478 point.

479 3. RESULTS AND ANALYSIS

480 The first thing tested was how well CKE represented the full EKE. If CKE does not have the
 481 same general shape as EKE, then using it as a proxy for EKE to determine high energy envelopes
 482 is not valid. After finding satellite passes with high CKE as discussed in Section 2, EKE was
 483 computed along the same pass, using the crossover method (Equations 1 and 2).

484 Although CKE is lower than EKE along all groundtracks (see Figure 5 for examples), the
 485 pattern of KE rise then fall is virtually identical. CKE, however, has the benefit of higher and
 486 more regular sampling. Thus, we conclude CKE is a reasonable proxy for locating front positions
 487 even though it may not be useful for quantifying the full energy of the anomalous currents.

488 Four general types of enhanced CKE were found (Figures 4 and 5). In most regions, the
 489 envelope in CKE is more or less symmetrical (52% of cases). Only a few profiles have two
 490 distinct regions of enhanced CKE that were identified, with a clearly defined minimum below
 491 $200 \text{ cm}^2 \text{ s}^{-2}$ between them in all time periods (3% of cases). 20% of the passes have multiple
 492 peaks that vary in time but have no consistent minimum between the peaks (i.e., Figure 4), while
 493 25% have a skewed envelope (Figure 5), with a long rise in CKE followed by a sharp drop-off.

494 In all cases, though, the shape of the CKE envelope closely follows that of EKE, although the

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538 amplitude was attenuated, by anywhere from 25-50%. Having closer samples of CKE, however,
539 allows for a better computation of the half-power point and possible shifts.

540 Figure 6 shows the locations of the half-power points determined from the mean CKE
541 profiles, along with estimate of the front position based on different methods: density gradients
542 from historical hydrographic sections (Orsi et al., 1995), dynamic topography contours (Kim and
543 Orsi, 2014), and the gradient of sea surface temperature (Freeman and Lovenduski, 2016a).
544 There are two estimates of the SAF and SACCF, and three of the PF. One of the PF estimates
545 (from Freeman and Lovenduski, 2016a) includes the standard deviation of the daily estimates.

546 It is important to note the large differences in estimates for the same front, which indicates
547 how uncertain these calculations are. For instance, in the Indian Ocean at 50°E, Freeman and
548 Lovenduski (2016a) find the PF at the same location that Orsi et al. (1995) found the SAF, while
549 Kim and Orsi (2014) find it significantly farther south. The SAF determination using the contour
550 method (Kim and Orsi, 2014) is substantially farther north than the one determined from
551 hydrographic data (Orsi et al., 1995) at most longitudes.

552 Many estimates from the half-power points of enhanced CKE occur between the same front
553 estimated by different methods, indicating they are at least within the uncertainty bounds of
554 frontal detection by other methods. Other values are at locations either north or south of the other
555 front estimates by as much as 3°, but it should be noted that the standard deviation of the PF
556 estimated by Freeman and Lovenduski (2016a,b) averages 2-3°, indicating these positions
557 estimated from CKE are well within the level of expected frontal variability.

558 Probably a better method for determining frontal position is to examine the probability of jets
559 occurring (Chapman, 2017a) (Figure 7). The CKE-defined mean front positions lie within the
560 probability envelopes, giving more confidence that the CKE measure is providing a comparable

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565 [measure of frontal position in many areas. The only location where CKE-defined fronts don't](#)
566 [agree well with the probability field from Chapman \(2017a\) is just west of the dateline, where](#)
567 [two points lie between levels of high jet \(and hence front\) probability.](#)

568 [Still, the good comparison is reassuring that the method developed in Section 2 is](#)
569 [successfully detecting regions of high energy related to jets around fronts. Since the movement](#)
570 [of jet positions has been used to estimate movement of the fronts \(e.g., Chapman, 2017a\), a](#)
571 [comparable calculation with positions of high CKE seems reasonable.](#)

572 [To quantify movement of the envelope of enhanced CKE, a linear trend is fit to the 8](#)
573 [estimations of the half-power point from 1993-2016 for each location shown in Figures 5 and 6.](#)
574 [Analysis of the residuals about the trend indicated they were random \(lag-1 autocorrelation < 0.1](#)
575 [for all cases\), so standard error was computed by scaling the formal error from the covariance](#)
576 [matrix determined in ordinary least squares by the standard deviation of the residuals. This was](#)
577 [also scaled up to account for the degrees of freedom lost by estimating the trend by \$\sqrt{n/n_{EDOF}}\$,](#)
578 [where \$n = 8\$, and \$n_{EDOF} = 6\$. Finally, the 90% confidence interval was computed by scaling by](#)
579 [1.94 for 6 effective degrees of freedom assuming a normal t-distribution of the residuals.](#)

580 [The results indicate considerable regional variability in the change of the half-power point](#)
581 [over 24 years, with large uncertainty bars \(Figure 8\). This is due to the substantial temporal](#)
582 [variability in the positions, which can be seen in Figure 4, where the leading edge of the CKE](#)
583 [envelope varies by over 1 degree of latitude \(over 100 km\) between 1993-1995 and 2011-2012.](#)
584 [To better see significant changes outside the uncertainty \(90% confidence\) interval, one can](#)
585 [compute the signal to noise ratio \(SNR = trend/uncertainty\). Examining this \(Figure 9\), one can](#)
586 [see there are some regions where the half-power point has moved southward by a significant](#)
587 [distance over the last 24 years \(13.6% of points\), but there are also points where it has moved](#)

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Deleted: Although a potential front position is not found along every groundtrack, they are typically found in areas where currents are strong and close to perpendicular with the ascending or descending groundtracks. It is also clear that there are more sites found along the SAF than the PF. A few are found between the two fronts, but this is likely due to either errors in the older front database of Orsi et al. (1995), changes since the hydrographic data used in that study were collected, or jets between the fronts. One location is found substantially south of the Polar Front, and is likely related to the weaker Southern ACC front. ... [9]

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618 north (9.6%). For the majority of points (76.8%), there is no statistically significant change,
619 meaning no movement of the front is as likely as either a southward or northward shift due to the
620 high variability in 3-year positions.

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622 4. DISCUSSION AND CONCLUSIONS

623 The results from the analysis of the positions of enhanced kinetic energy suggest no overall
624 shift in the frontal positions across the Southern Ocean, but some large, localized movements.

625 The region indicative of some southward shift between 90°E and 170°E is in approximately the
626 same area where Kim and Orsi (2014) and Freeman and Lovenduski (2016a) also reported large
627 shifts, between 1992 to 2011 and 2002 and 2014, respectively. However, Freeman and

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628 Lovenduski only examined the Polar front, and Kim and Orsi (2014) only found large shifts in
629 the PF and the southern ACC front. They found shifts of order 50-100 km in the SAF where the
630 points in this study cluster, which is considerably smaller than the individual shifts we find

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631 between 90°E and 170°E along the SAF. However, the overall average over the region between
632 90°E and 170°E (-29 km per decade, or -66.7 km in 23 years), is consistent with what Kim and
633 Orsi (2014) found.

634 Kim and Orsi (2014) and Freeman and Lovenduski (2016a) also found slight northward
635 shifts in the front positions in the southeast Pacific, between 200°E-270°E. We also find some
636 locations in this region with a significant northward shift in the SAF. Kim and Orsi (2014) found
637 the shift of the SAF was about 30-40 km between 1992 and 2011. Our results suggest larger
638 shifts in some areas; averaged over the area, our results are 46 km per decade to the north, or 106

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649 km from 1993-2015, which is consistent with the average over the region computed by [Freeman](#)
650 [and Lovenduski \(2016a\)](#) from sea surface temperature data, but for the Polar Front.

651 [Kim and Orsi \(2014\)](#) suggest that the shift of the fronts in the Indian Ocean were not directly
652 related to shifts in winds, but instead were caused by an expansion of the Indian subtropical gyre.
653 They linked the shift in the southeastern Pacific to wind changes related to mainly the Southern
654 Annular Mode in that region (Kim and Orsi, 2014).

655 Overall, this study supports the recent studies by Kim and Orsi (2014), Gille (2014), [Freeman](#)
656 [and Lovenduski \(2016a\)](#), [and Chapman \(2017a\)](#). All find that, while the frontal positions of the
657 ACC are highly variable in time, there is no statistically significant shift in the fronts to the south
658 on average. This study utilized a novel technique to reach this conclusion, which adds to the
659 robustness of evidence that there has not been a shift in the frontal positions. Thus, while the
660 fronts may eventually shift south in a warming climate, there is no strong evidence that it is
661 happening at the moment.

662 Other studies have shown significant positive trends in the Southern Ocean that have been
663 connected to the warming climate. These include changes in the ocean heat content in the upper
664 ocean between the 1930s-1950s and 1990s (e.g., Böning et al., 2008; Gille, 2008), increases in
665 the heat content of deep water between the 1990s and 2005 (e.g., Purkey and Johnson, 2010),
666 and increases in eddy kinetic energy in the Indian and Pacific Oceans since 1993 (Hogg et al.,
667 2015). Observational evidence of shifts in the winds, however, indicates that while there may be
668 a slight southward shift in winds during the southern hemisphere summer, the overall yearly
669 average shift is not significant (Swart and Fyfe, 2012). Thus, the growing consensus that fronts
670 have not shifted to the south, on average, is consistent with observations of no significant shift in
671 the yearly averaged winds.

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686 | The only evidence supporting a hypothesis that ACC fronts have shifted southward since the
687 | 1990s comes from mapping the location of contours of constant dynamic topography over time
688 | (e.g., Sokolov and Rintoul, 2009b; Kim and Orsi, 2014). As Gille (2014) argued and as we have
689 | demonstrated based on a simple thought experiment (Figure 1), there are other equally plausible
690 | explanations for the apparent southern shift of the contours. Considering that four different
691 | techniques – location of mean transport (Gille, 2014), maximum SST gradients (Freeman and
692 | Lovenduski, 2016a), probability of jet positions (Chapman, 2017a), and the location of enhanced
693 | kinetic energy (this study) – all agree that the fronts have not moved significantly on average,
694 | one has to conclude that the method of using dynamic topography contours to detect changes in
695 | front position is too sensitive to sea level rise be useful for determining shifts in frontal positions,
696 | although it may prove useful for determining the mean position as Chapman (2017a) has argued.
697 |

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707

708 **Acknowledgements**

709 [The author would like to thank Christopher Chapman and an anonymous reviewer for their](#)
 710 [extensive comments on an earlier draft of this paper. Their many suggestions helped the author](#)
 711 [improve the paper substantially.](#) This research was carried out under grant number
 712 NNX13AG98G from NASA and [a grant](#) from NOAA for the NASA/NOAA Ocean Surface
 713 Topography Science Team.

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814 **Figure Captions**

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816 **Figure 1.** a) Mean dynamic topography in the Southern Ocean along a north-south meridian for three
817 scenarios, and b) the corresponding geostrophic velocity, with positive values indicating eastward flow.
818 The scenarios are: an initial state (dashed black line), a shift of the two fronts south by 60 km with no
819 change in magnitude or shape of the currents (red line), and no shift of the mean of the current, but a
820 change in the magnitude and shape (blue line).

821
822 **Figure 2.** Positions of the T/P, Jason-1, Jason-2 and Jason-3 groundtracks used for this study (black
823 lines), and the approximate locations of the Subantarctic Front (red line) and the Polar Front (blue
824 line) as estimated by Orsi et al. (1995). The orange track shows the location of the pass used in analysis
825 shown in Figures 3 and 4. ▾

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827 **Figure 3.** An example profile of mean CKE (1993-2015) along a ground track in the southern Indian
828 Ocean (shown in orange in Figure 2), demonstrating the location of the half-power point and the locations
829 of the southern and northern boundaries of the enhanced CKE envelope. See text for details of the
830 computations. ▾

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832 **Figure 4.** Three-year averages of CKE estimated along pass shown in Figure 2 (solid lines) along with
833 the long-term mean from 1993-2016 (dotted line). ▾

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835 **Figure 5.** Examples of the three types of CKE profiles found (black lines), along with the value of the full
836 EKE computed at crossover points. ▾

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838 **Figure 6.** Mean positions of fronts estimated from CKE (orange dots) along with estimates from other
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840 of dynamic topography, and Freeman and Lovenduski (2016a) based on gradients of sea surface
841 temperature. The Orsi et al. (1995) fronts were downloaded from
842 https://gcmd.nasa.gov/records/AADC_southern_ocean_fronts.html. The Freeman and Lovenduski fronts
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846 **Figure 7.** Mean positions of fronts estimated from CKE (black dots) along with the percent occurrence of
847 a jet between 1993 and 2014 computed by Chapman (2017a). Data were downloaded from
848 <http://dx.doi.org/10.5061/dryad.q9k8r> (Chapman, 2017b). The percent occurrence of the jet was
849 computed by calculating the number of times a jet occurred in the daily files, dividing by the total number
850 of days between January 1993 and December 2014, and multiplying by 100. ▾

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852 **Figure 8.** Estimated trend in the half-power point of CKE for each location shown in Figures 6 and 7, as a
853 function of latitude. Error bars represent the 90% confidence interval. ▾

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855 **Figure 9.** SNR (trend/error in Figure 8). Values larger than 1 indicate a statistically significant northern
856 shift. Values smaller than -1 indicate a statistically significant southern shift. Values between ± 1 indicate
857 no statistically significant shift. ▾

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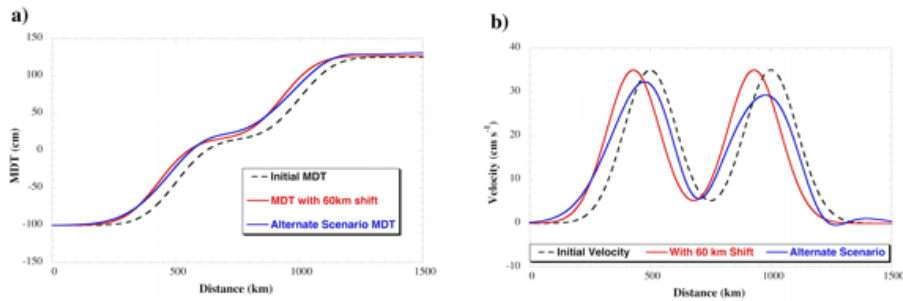
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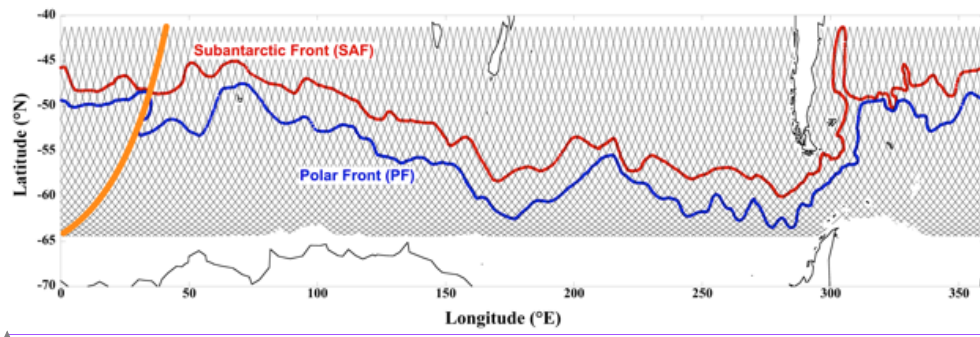
Don Chambers 10/10/2017 4:38 PM
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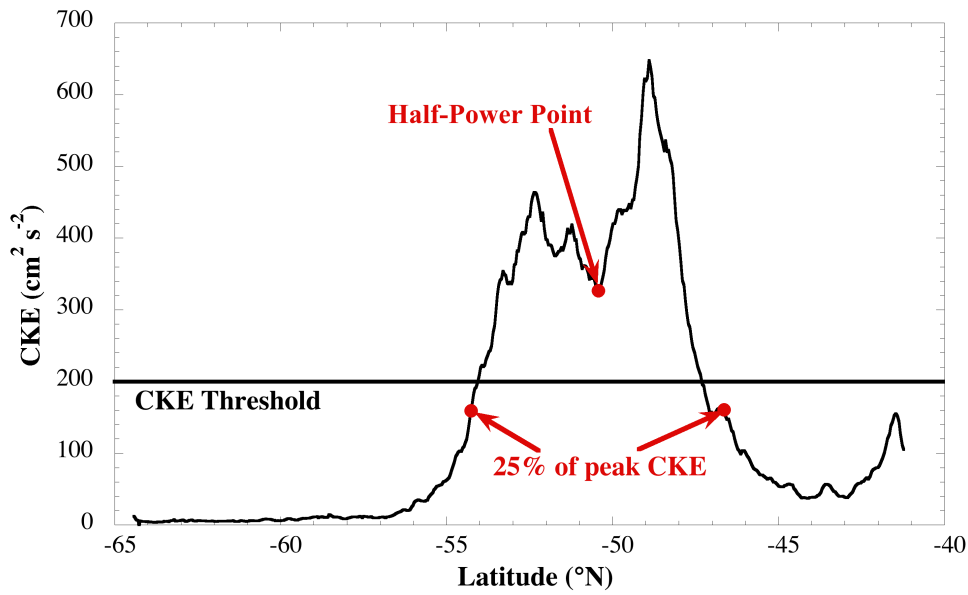


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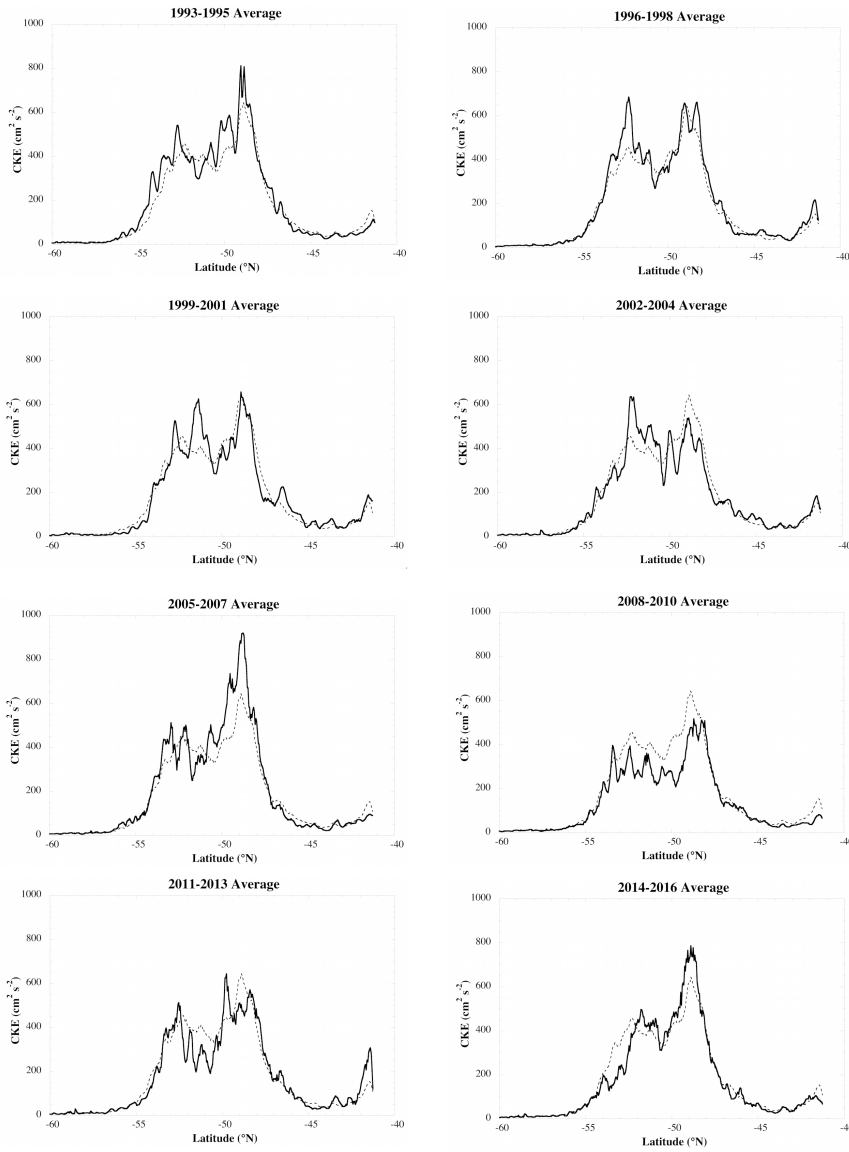
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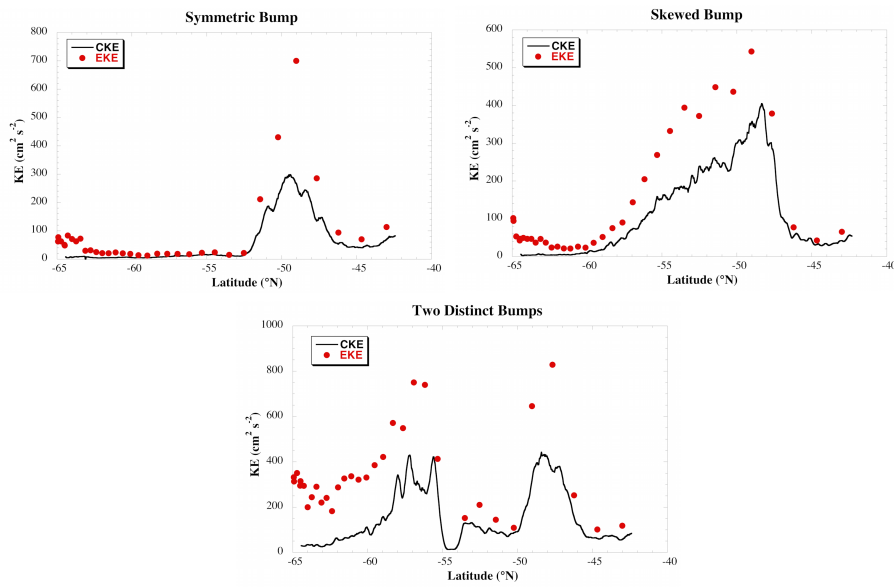
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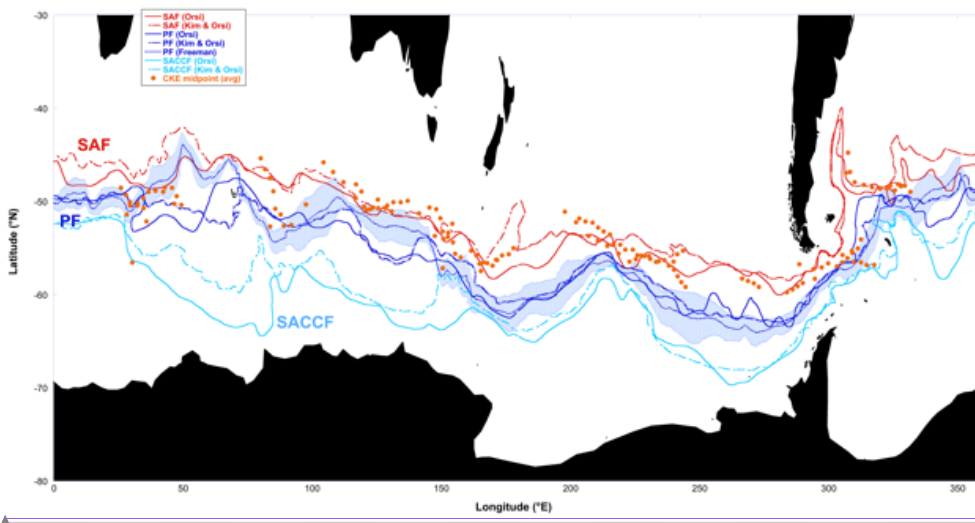


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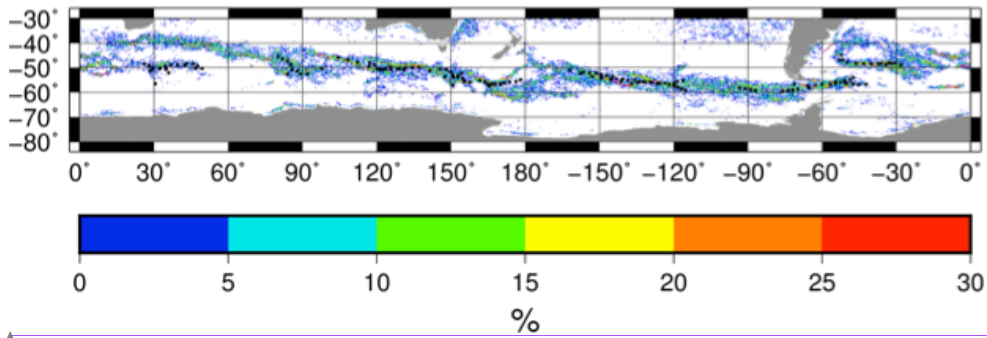
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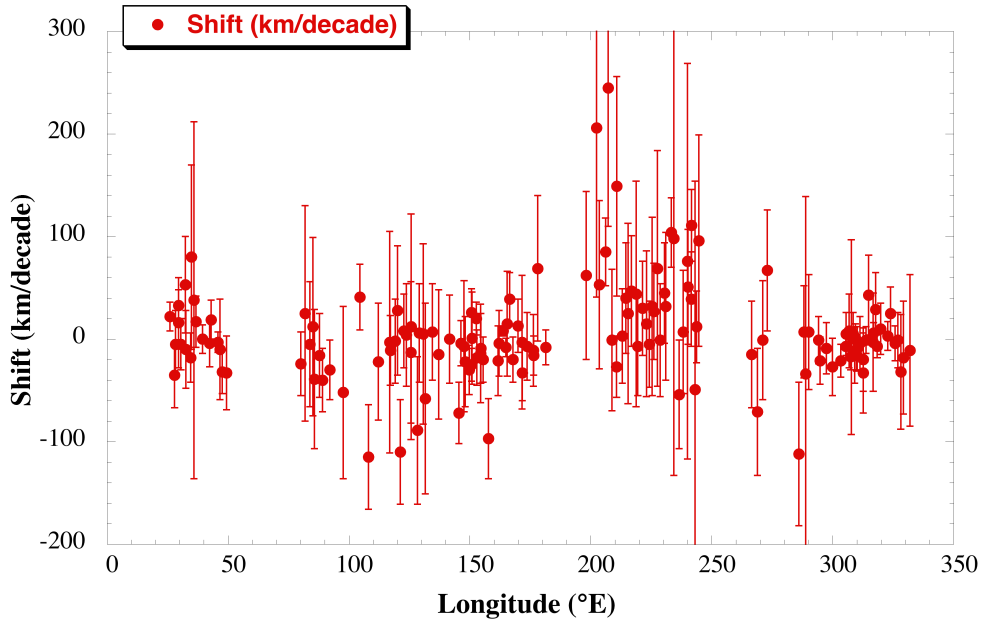
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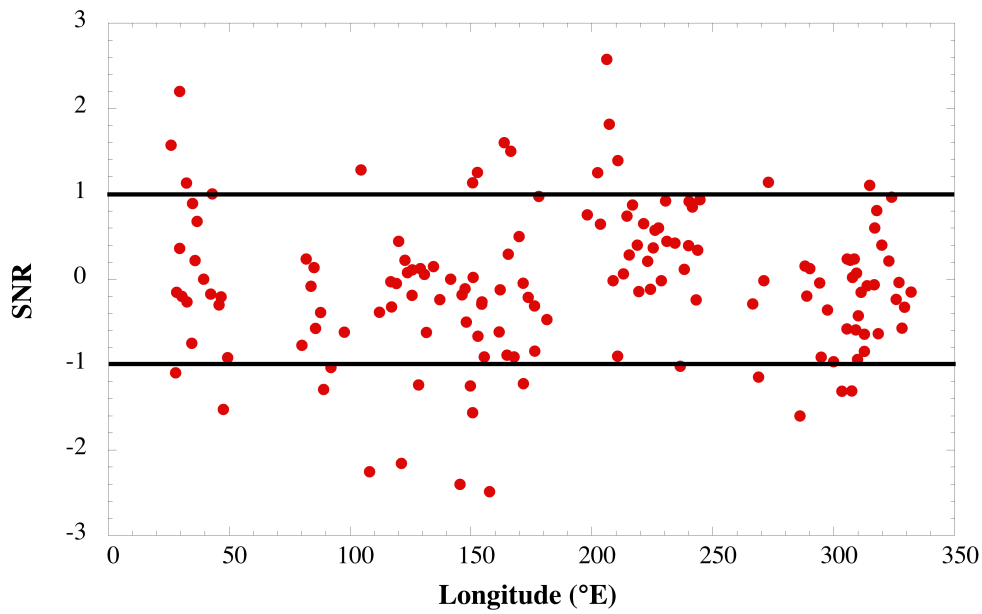
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