1	A study on some basic features of inertial oscillations
2	and near-inertial internal waves
3	Shengli Chen, Daoyi Chen, Jiuxing Xing
4	Shenzhen Key Laboratory for Coastal Ocean Dynamic and Environment, Graduate School at
5	Shenzhen, Tsinghua University, Shenzhen 518055, China.
6	Correspondence to: Jiuxing Xing (jxx2012@sz.tsinghua.edu.cn)
7	
8	
9	
10	
11	
12	
13	
14	
15	
16	
17	
18	
19	
20	
21	
22	

## 23 Abstract

24 Some basic features of inertial oscillations and near-inertial internal waves are investigated by simulating 25 a two-dimensional (x-z) rectangular basin (300 km  $\times$  60 m) driven by a wind pulse. For the homogeneous 26 case, near-inertial motions are pure inertial oscillations. The inertial oscillation shows typical opposite 27 currents between surface and lower layers, which is formed by the feedback between barotropic waves 28 and inertial currents. For the stratified case, near-inertial internal waves are generated at land boundaries 29 and propagate offshore with increasing frequencies, which induce tilting of velocity contours in the 30 thermocline. The inertial oscillation is uniform across the whole basin, except near the coastal boundaries 31 (~20 km) where it quickly declines to zero. This boundary effect is related to great enhancement of 32 nonlinear terms, especially the vertical nonlinear term ( $w\partial \mathbf{u}/\partial z$ ). With inclusion of near-inertial 33 internal waves, the total near-inertial energy has a slight change, with occurrence of a small peak at  $\sim$ 50 34 km, which is similar to previous researches. We conclude that, for this distribution of near-inertial energy, 35 the boundary effect for inertial oscillations is primary, and the near-inertial internal wave plays a 36 secondary role. Homogeneous cases with various water depths (50 m, 40 m, 30 m, 20 m) are also 37 simulated. It is found near-inertial energy monotonously declines with decreasing water depth, because 38 more energy of initial wind-driven currents is transferred to seiches formed by barotropic waves. For the 39 case of 20 m, the seiches energy even slightly overpasses the near-inertial energy. We suppose this is an 40 important reason why near-inertial motions are weak and hardly observed in coastal regions.

41

42 **Keywords:** inertial oscillations, near-inertial internal waves, near-inertial energy

- 43
- 44
- 45
- 46

47

## 49 1. Introduction

50 Near-inertial motion has been observed and reported in many seas (e.g. Alford et al., 2016; Webster, 51 1968). It is mainly generated by changing winds at the sea surface (Pollard and Millard, 1970; Chen et 52 al., 2015b). The passage of a cyclone or a front can induce very strong near-inertial motions(D'Asaro, 53 1985), which can last for 1-2 weeks and reach a maximum velocity magnitude of 0.5-1.0 m/s (Chen et 54 al., 2015a; Zheng et al., 2006; Sun et al., 2011). In deep seas, the near-inertial internal wave propagates 55 downwards to transfer energy to depth (Leaman and Sanford, 1975; Fu, 1981; Gill, 1984; Alford et al., 56 2012). The strong vertical shear of near-inertial currents may play an important role in inducing mixing 57 across the thermocline (Price, 1981; Burchard and Rippeth, 2009).

In shelf seas, near-inertial motions exhibit a two-layer structure, with an opposite phase between currents in the surface and lower layers (Malone, 1968; Millot and Crepon, 1981; MacKinnon and Gregg, 2005). By solving a two-layer analytic model using the Laplace transform, Pettigrew (1981) found this 'baroclinic' structure can be formed by inertial oscillations without inclusion of near-inertial internal waves. Due to similar vertical structure and frequencies, inertial oscillations and near-inertial internal waves are hardly separable, and could easily be mistakenly recognized as each other.

64 In shelf seas, the near-inertial energy increases gradually offshore, and reaches a maximum near the shelf 65 break, found both in observations (Chen et al., 1996) and model simulations (Xing et al., 2004; Nicholls 66 et al., 2012). Chen and Xie (1997) reproduced this cross-shelf variation both in linear and nonlinear 67 simulations, and attribute it to large values of the cross-shelf gradient of surface elevation and the vertical 68 gradient of Reynolds stress near the shelf break. By using the analytic model of Pettigrew (1981), 69 Shearman (2005) argued that the cross-shelf variation is controlled by baroclinic waves which emanate 70 from the coast to introduce nullifying effects on the near-inertial energy near shore. Kundu et al. (1983) 71 found a coastal inhibition of near-inertial energy within the Rossby radius from the coast, which is 72 attributed to the downward and offshore leakage of near-inertial energy near the coast. As many factors 73 seems to have effects, the mechanism controlling the cross-shelf variation of near-inertial energy seems 74 complicated.

75 In this paper, simple two-dimensional simulations are used to investigate some basic features of near76 inertial motions. Cases with and without vertical stratification are simulated to examine properties and

differences of inertial oscillations and near-inertial internal waves. The horizontal distribution of nearinertial energy is discussed in detail. Also cases with various water depths are simulated to investigate
the dependence of near-inertial motions on the water depth.

80 2. Model Settings

81 The simulated region is a two-dimensional shallow rectangular basin (300 km  $\times$  60 m). Numerical 82 simulations are done by the MIT general circulation model (MITgcm) (Marshall et al., 1997), which 83 discretizes the primitive equations and can be designed to model a wide range of phenomena. There are 84 1500 grids in the horizontal ( $\Delta x = 200$  m) and 60 grids in vertical ( $\Delta z = 1$  m). The water depth is 85 uniform, with east and west sides being land boundaries. The vertical and horizontal eddy viscosities are 86 assumed constants as  $5 \times 10^{-4}$  m<sup>2</sup>/s and 10 m<sup>2</sup>/s, respectively. The Coriolis parameter is  $5 \times 10^{-5}$  s<sup>-1</sup> (at a 87 latitude of 20.11 N). The bottom boundary is no-slip. The model is forced by a spatially uniform wind 88 which is kept westward and increases from 0 to 0.73 N/m<sup>2</sup> (corresponding to a wind speed of 20 m/s) for 89 the first three hours and then suddenly stops. The model runs for 200 hours in total, with a time step of 90 4 seconds. The first case is homogeneous, while the second one has a stratification of two-layer structure 91 initially. For the stratified case, the temperature is 20 °C in the upper layer (-30 m<z<0), and 15 °C in the 92 lower layer (-60 m<z<-30 m). The salinity is constant, so the density is determined by the temperature. 93 Except stratification all settings of these two cases are the same.

#### 94 **3.** Inertial oscillation

95 The first case is without the presence of vertical stratification. Thus near-inertial internal wave is absent,

and the near-inertial motion is pure inertial oscillations.

## 97 3.1 Vertical structures

98 The model simulated velocities (Fig. 1) vary near the inertial period (34.9 hours). Spectra of velocities 99 (not shown) indicate maximum peaks located exactly at the inertial period. The spectra of u also have a 100 smaller peak at the frequency of the first mode seiche. As this simulation is two-dimensional, i.e., the 101 gradient along *y*-axis is zero, the seiche has little energy in v which shows clearly regular variation at the 102 inertial frequency.

In the vertical direction, currents display a two-layer structure, with their phase being opposite betweensurface and lower layers. They are maximum at the surface, and have a weaker maximum in the lower

105 layer ( $\sim 40$  m), with a minimum at the depth of  $\sim 20$  m. The velocity gradually diminishes to zero at the 106 bottom due to the bottom friction. This is the typical vertical structure of shelf-sea inertial oscillations, 107 which have been frequently observed (Shearman, 2005; MacKinnon and Gregg, 2005). In practice, this 108 vertical distribution can be modified due to presence of other processes, such as the surface maximum 109 being pushed down to the subsurface (e.g. Chen et al., 2013). Note that without stratification in this 110 simulation the near-inertial internal wave is absent. However, this two-layer structure of inertial 111 oscillations looks 'baroclinic', which makes it easy to be mistakenly attributed to the near-inertial internal 112 wave (Pettigrew, 1981).

It is interesting that currents of non-baroclinic inertial oscillations reverse between the surface and lower layers. This is usually attributed to the presence of the coast, which requires the normal-to-coast transport to be zero, thus currents in upper and lower layers compensate each other (Millot and Crepon, 1981; Chen et al., 1996). However, it remains unclear how this vertical structure is established.

117 As the westward wind blows for first three hours, the initial inertial current is also westward and only 118 exists in the very surface layer (Fig. 2). In the lower layer there is no movement initially. Thus a westward 119 transport is produced, which generates a rise (in the west) and fall (in the east) of elevation near coastal 120 boundaries. The elevation slope behaves in a form of barotropic wave which propagates offshore at a 121 great speed (87 km/h). The current driven by the barotropic wave is eastward, and uniform vertically. 122 Therefore, with arrival of the barotropic wave the westward current in the surface is reduced, and the 123 movement in the lower layer commences (Fig. 2). After passage of the first two barotropic waves 124 (originated from both sides), currents in the lower layer have reached a relatively great value, while 125 currents in the surface layer have been largely decreased (Fig. 3a). Accordingly, the depth-integrated 126 transport diminishes a lot. This is like a feedback between inertial currents and barotropic waves. If only 127 the depth-integrated transport of currents exist, barotropic waves will be generated, which reduce the 128 surface currents but increase the lower layer currents, thus reduces the current transport. It will end up 129 with inertial currents in the surface and lower layers having opposite directions and comparable 130 amplitudes. As seen from Fig. 1b, the typical vertical structure of inertial currents is established within 131 the first inertial period.

#### 132 **3.2** Horizontal distributions of inertial energy

133 The inertial velocities are almost entirely the same across the basin (Fig. 4), except near the boundary. 134 This indicates that inertial oscillations have a coherence scale of almost the basin width. This is because 135 in our simulation the wind force is spatially uniform, and the bottom is flat. The inertial velocities in the 136 lower layer have slightly more variation across the basin than those in the surface layer, because inertial 137 velocities in the lower layer is correlated to propagation of barotropic waves as discussed in 3.1, while the surface inertial currents are driven by spatially uniform wind. In shelf sea regions, the wind forcing 138 139 is usually coherent as the synoptic scale is much larger, however, the topography that is mostly not flat 140 could generate barotropic waves at various places, and thus significantly decrease coherence of inertial 141 currents in the lower layer.

The spectra of velocities in the inertial band are almost uniform except near the boundaries (Fig. 5), consistent with the velocities. Near the boundaries, the inertial energy declines gradually to zero from  $x=\sim20$  km to the coast wall. The east side has slightly greater inertial energy and a bit wider boundary layer compared to the west side.

146 We calculate the nonlinear and inertial terms in the momentum equation and find that nonlinear terms 147 are of relatively high values initially within 2 km away from the land boundary (Fig 6bc), where the 148 inertial term is smaller (Fig 6a). For the time-averaged values (Fig 6d), the vertical nonlinear term is two 149 times more than the horizontal nonlinear term. The inertial term drops sharply near the boundary, and 150 rises gradually with the distance away from the boundary. At x>15km, it keeps an almost constant value 151 which is much greater than nonlinear terms. Thus it is concluded that the significant decrease of inertial 152 oscillations near the boundary is due to influence of nonlinear terms, especially the vertical nonlinear 153 term.

## 154 4. Near-inertial internal waves

In addition to inertial oscillations, near-inertial internal waves are usually generated along when the vertical stratification is present. However, due to their close frequencies inertial oscillations and nearinertial internal waves are difficult to be separated. Thus we run a second simulation with the presence of stratification to investigate differences that near-inertial internal waves introduce.

159 4.1 Temperature distributions

160 Fig. 7 shows the evolution of temperature profiles with time. One can see an internal wave packet is

161 generated at the west coast, and then propagates offshore. The wave phase speed is around 1 km/h, 162 consistent with the theoretical value computed using the stratification. Before arrival of internal waves, 163 the temperature at mid-depth diffuses gradually due to vertical diffusion in the model. For a fixed position 164 at x=20 km (Fig. 8), the temperature varies with the inertial period (34.9 hours) and the amplitude of 165 fluctuation declines gradually with time. At x=60 km and x=100 km, the strength of internal waves is 166 much reduced. And wave periods are shorter initially, followed by a gradually increase to the inertial 167 period. At x=140 km, the internal wave becomes as weak as the background disturbance.

168 A spectral analysis of the temperature at mid-depth (z=-30 m) is shown in Fig. 9a. The strongest peak is 169 at near the inertial frequency (0.69 cpd), but only confined to the region close to the boundary (x<40 km). 170 In the region 20 km < x < 70 km, the energy is also large at higher frequencies of 0.8-1.7 cpd. This generally 171 agrees with properties of Poincaré waves. During a Rossby adjustment, the waves with higher 172 frequencies propagate offshore at greater group speeds, thus for places further offshore the waves have 173 higher frequencies (Millot and Crepon, 1981). While the wave with a frequency closest to the inertial 174 frequency moves at the slowest group velocity, and it takes a relatively long time to propagate far offshore, 175 thus it is mostly confined to near the boundary. By solving an idealized two-layer model equation, the 176 response of Rossby adjustment can be expressed in form of Bessel functions (Millot and Crepon, 1981; 177 Gill, 1982; Pettigrew, 1981), as in Fig. 9cd showing the spectra of mid-depth elevation. The difference 178 from our case is obvious. The frequency of theoretical near-inertial waves increase gradually with the 179 distance from the coast, while in our case this property is absent. And the theoretical inertial energy has 180 a e-folding scale of almost the Rossby radius (54 km), while in our case the e-folding scale is much 181 smaller (~15 km).

## 182 4.2 Velocity distributions

With presence of near-inertial internal waves, the contours of velocities near the thermocline tilt slightly (Fig. 10d), and indicates an upward propagation of phase, thus a downward energy flux. This can also be seen in vertical spirals of velocities (Figs. 10e and 10f). With only inertial oscillations, current vectors mostly point toward two opposite directions. Once the near-inertial wave is included, the current vectors gradually rotate clockwise with depth.

188 The spatial distribution of the near-inertial energy is also slightly changed compared to the case with only

inertial oscillations (Fig. 11 and Fig. 5). It is also greatly reduced to zero in the boundary layer (0-20 km)
like the case without stratification. But at ~50 km away from the boundary the inertial energy reaches a
peak. Further away (>100 km) it becomes a constant. This spatial distribution of inertial energy is similar
to that observed in shelf seas, with maximum near the shelf break (Chen et al., 1996; Shearman, 2005).
In our case, the boundary layer effect which induces a sharp decrease to zero makes a major contribution,
and near-inertial internal waves which bring a small peak further offshore make a secondary influence.

195

# 5. Dependence on the water depth

In coastal regions, near-inertial motions are rarely reported. It is speculated that the strong dissipation and bottoms friction in coastal region suppress the development of near-inertial motions. However, Chen (2014) found the water depth is also a sensitive factor, with significant reduction for the case with smaller water depth. Here we will run cases with different water depths and clarify why the near-inertial energy changes with water depth. Homogeneous cases with water depths of 50 m, 40 m, 30 m, 20 m are simulated. The vertical interval for all cases is 1 m. All the other parameters including viscosities are the same as the homogeneous case of 60 m.

203 For each case, the currents are band-pass filtered to obtain near-inertial currents. Then near-inertial 204 kinetic energy can be calculated. As seen in Fig. 12, the near-inertial energy gradually declines with 205 decreasing water depth. In this dynamics system, the other dominant process are the seiches induced by 206 barotropic waves. As the elevation induced by seiches is anti-symmetric in such a basin, the potential 207 energy is little. The kinetic energy of siehces can also be calculated by the band-pass filtered currents. 208 We find the energy of seiches, by contrast, increases gradually with decreasing water depth. For the case 209 of 60m, the near-inertial energy is much greater than the seiches energy. But for the case of 20 m, the 210 energy of seiches has overpasses the near-inertial energy slightly. The sum energy of these two processes 211 almost keeps constant with varying water depth. For a shallower water depth, the reduction of near-212 inertial energy equals the increase of seiches energy. The initial current is wind-driven and only 213 distributes in the surface layer. The unbalanced across-shelf flow generates elevation near the land 214 boundary which propagates offshore as barotropic waves and form seiches. Part of the energy goes to 215 form inertial oscillations. For a shallower water depth, the elevation is enlarged, and more energy is 216 transferred to form seiches, thus with weakened near-inertial motions. Therefore, in coastal regions with 217 water depth less than 30m, the near-inertial motion is weak, due to the suppressing of barotropic waves.

218 As seen in Section 3.1, inertial oscillations behave in a two-layer structure, with currents in the upper 219 layer in opposite phase with those of lower layer. In terms of kinetic energy, for the case of 60 m (Fig. 220 13), the near-inertial motion is maximized in the very surface, minimized near the depth of 20 m, and 221 then gradually increases with depth to form a much smaller peak at 40 m. Near the bottom, the near-222 inertial energy gradually reduces to zero due to bottom friction. When we set the bottom boundary 223 condition from nonslip to slip, such a boundary structure vanishes, and near-inertial energy become 224 constant in the lower layer. For other cases of 20 m and 40 m, their vertical profile are almost the same 225 as the 60m case. The minimum positions are all located at 1/3 of the water depth. This implies the vertical 226 distribution of near-inertial energy is independent of water depth. Note that in our cases, the vertical 227 viscosity is set as a constant value. In practice, the viscosity in thermocline is usually significantly 228 reduced, thus the minimum position of near-inertial energy is located just below the mixed layer.

229 6. Summary and discussion

230 Idealized simple two-dimensional (x-z) simulations are conducted to examine the response of a shallow 231 closed basin to a wind pulse. The first case is homogeneous, in which properties the near-inertial motion 232 is pure inertial oscillations. It has a two-layer structure, with currents in the surface and lower layers 233 being opposite in phase, which has been reported frequently in shelf seas. We find that the inertial current 234 is confined in the surface layer initially. The induced depth-integrated transport generates barotropic 235 waves near boundaries which propagates quickly offshore. The flow driven by the barotropic wave is 236 independent of depth and opposite to the surface flow. Thus the surface flow is reduced but the flow in 237 the lower layer is increased, as a result the transport diminishes. This feedback between barotropic waves 238 and currents continues and ends up with the depth-integrated transport vanishes, i.e., inertial currents in 239 upper and low layers having opposite phases and comparable amplitudes. In our simulation, within just 240 one inertial period the typical structure of inertial currents has been established. By solving a two-layer 241 analytic model using the Laplace transform, Pettigrew (1981) also found the vertical structure of opposite 242 currents associated with inertial oscillations. He argued that the arrival of a barotropic wave for a fixed 243 location cancels half of the inertial oscillation in the surface layer, and initiates an equal and opposite 244 oscillation in the lower layer. Our simulations further demonstrate the role of barotropic waves in forming 245 this feature, and shows some more realistic details during this process.

246 The second case is set up with idealized two-layer stratification, thus near-inertial internal waves are

247 generated. For a fixed position, velocity contours show clear obvious tiltings near the thermocline, and 248 velocity vectors display clearly anti-cyclonic spirals with depth. These could be useful clues to examine 249 occurrence of near-inertial internal waves. Near the land boundary the vertical elevation generates 250 fluctuations of thermocline that propagate offshore. The energy of near-inertial internal waves is confined 251 to near the land boundary (x < 40 km). At positions further offshore, the waves have higher frequencies. 252 This is generally consistent with properties of Rossby adjustment process. However, our simulated result 253 also shows evident discrepancies from theoretical values obtained in classic solutions of Rossby 254 adjustment problem.

255 The inertial oscillation has a very large coherent scale of almost the basin scale (600 km). It is uniform 256 in both amplitude and phase across the basin, except near the boundary (~20 km offshore). The energy 257 of inertial oscillations declines gradually to zero from x=20 km to the coast. This boundary effect is 258 attributed to influence of nonlinear terms, especially the vertical term ( $w\partial \mathbf{u} / \partial z$ ), which are greatly 259 enhanced near the boundary, and overweighs the inertial term ( $f\mathbf{u}$ ). When near-inertial internal waves 260 are produced in the stratified case, the distribution of total near-inertial energy is modified slightly near 261 the boundary. A small peak appears at ~ 50 km offshore. This is similar to the cross-shelf distribution of 262 near-inertial energy observed in shelf seas (Chen et al., 1996; Shearman, 2005). This energy distribution 263 has been attributed to different reasons, such as downward and offshore leakage of near-inertial energy 264 near the coast (Kundu et al., 1983), the variation of elevation and Reynolds stress terms associated with 265 the topography (Chen and Xie, 1997) and the influence of the baroclinic wave (Shearman, 2005; Nicholls 266 et al., 2012). In our simulations, this horizontal distribution of near-inertial energy is primarily controlled 267 by the boundary effect on inertial oscillations, and the near-inertial internal wave makes a secondary 268 effect.

Homogeneous cases with various water depths (50 m, 40 m, 30 m, 20 m and 10 m) are also simulated. The inertial energy is reduced with decreasing water depth, while the energy of seiches, by contrast, increases for the shallower case. For the case of 10 m, the seiches energy has slightly overpassed the inertial energy. It is interesting that the reduction of inertial energy just equals the increase of seiches energy, which implies more energy of initial wind-driven currents is transferred to the seiches for the shallower cases, and thus less energy goes to the inertial process. This is probably an important reason why near-inertial motions is weak and rarely reported in shallow coastal regions.

#### 276 Acknowledgements

277 We are very appreciated for comments from John Huthnance. This study is supported by the National

278 Basic Research Program of China (2014CB745002, 2015CB954004), the Shenzhen government

279 (201510150880, SZHY2014-B01-001), and the Natural Science Foundation of China (41576008,

41276006, U1405233, and 40976013). Shengli Chen is sponsored by the China Postdoctoral Science

- 281 Foundation (2016M591159).
- 282
- 283
- 284

#### 285 References

- 286 Alford, M. H., Cronin, M. F., and Klymak, J. M.: Annual Cycle and Depth Penetration of Wind-Generated
- Near-Inertial Internal Waves at Ocean Station Papa in the Northeast Pacific, Journal of Physical
   Oceanography, 42, 889-909, 10.1175/jpo-d-11-092.1, 2012.
- 289 Alford, M. H., MacKinnon, J. A., Simmons, H. L., and Nash, J. D.: Near-Inertial Internal Gravity Waves in
- the Ocean, Ann Rev Mar Sci, 8, 95-123, 10.1146/annurev-marine-010814-015746, 2016.
- 291 Burchard, H., and Rippeth, T. P.: Generation of Bulk Shear Spikes in Shallow Stratified Tidal Seas,

292 Journal of Physical Oceanography, 39, 969-985, 10.1175/2008jpo4074.1, 2009.

- 293 Chen, C., and Xie, L.: A numerical study of wind-induced, near-inertial oscillations over the Texas-
- Louisiana shelf, Journal of Geophysical Research: Oceans, 102, 15583-15593, 10.1029/97jc00228,
  1997.
- Chen, C. S., Reid, R. O., and Nowlin, W. D.: Near-inertial oscillations over the Texas Louisiana shelf, J
   Geophys Res-Oceans, 101, 3509-3524, 10.1029/95jc03395, 1996.
- Chen, C. S.: Study on Several Features of the Near-inertial Motion, PhD, Xiamen University, 107 pp.,
  2014.
- 300 Chen, G., Xue, H., Wang, D., and Xie, Q.: Observed near-inertial kinetic energy in the northwestern
- 301 South China Sea, J Geophys Res-Oceans, 118, 4965-4977, 10.1002/jgrc.20371, 2013.
- 302 Chen, S., Hu, J., and Polton, J. A.: Features of near-inertial motions observed on the northern South
- 303 China Sea shelf during the passage of two typhoons, Acta Oceanologica Sinica, 34, 38-43,

304 10.1007/s13131-015-0594-y, 2015a.

- 305 Chen, S., Polton, J. A., Hu, J., and Xing, J.: Local inertial oscillations in the surface ocean generated by
- time-varying winds, Ocean Dynamics, 65, 1633-1641, 10.1007/s10236-015-0899-6, 2015b.
- 307 D'Asaro, E. A.: The energy flux from the wind to near-inertial motions in the surface mixed layer,
  308 Journal of Physical Oceanography, 15, 1043-1059, 1985.
- 309 Fu, L. L.: Observations and models of inertial waves in the deep ocean, Reviews of Geophysics, 19,
- 310 141-170, 10.1029/RG019i001p00141, 1981.
- Gill, A. E.: Atmosphere-ocean dynamics, Academic Press, 662 pp., 1982.
- 312 Gill, A. E.: On the behavior of internal waves in the wakes of storms, Journal of Physical Oceanography,

- 313 14, 1129-1151, 10.1175/1520-0485(1984)014<1129:otboiw>2.0.co;2, 1984.
- 314 Kundu, P. K., Chao, S. Y., and McCreary, J. P.: Transient coastal currents and inertio-gravity waves, Deep-
- 315 Sea Research Part a-Oceanographic Research Papers, 30, 1059-1082, 10.1016/0198-0149(83)90061-4,
- 316 1983.
- Leaman, K. D., and Sanford, T. B.: Vertical energy propagation of inertial waves: a vector spectral
- analysis of velocity profiles, Journal of Geophysical Research, 80, 1975-1978, 1975.
- 319 MacKinnon, J. A., and Gregg, M. C.: Near-inertial waves on the New England shelf: The role of evolving
- 320 stratification, turbulent dissipation, and bottom drag, Journal of Physical Oceanography, 35, 2408-
- 321 2424, 10.1175/jpo2822.1, 2005.
- 322 Malone, F. D.: An analysis of current measurements in Lake Michigan, Journal of Geophysical
- 323 Research, 73, 7065-&, 10.1029/JB073i022p07065, 1968.
- 324 Marshall, J., Adcroft, A., Hill, C., Perelman, L., and Heisey, C.: A finite-volume, incompressible Navier
- 325 Stokes model for studies of the ocean on parallel computers, Journal of Geophysical Research: Oceans,
- 326 102, 5753-5766, 10.1029/96jc02775, 1997.
- 327 Millot, C., and Crepon, M.: Inertial oscillations on the continental-shelf of the Gulf of Lions -
- 328 observations and theory, Journal of Physical Oceanography, 11, 639-657, 10.1175/1520-
- 329 0485(1981)011<0639:iootcs>2.0.co;2, 1981.
- 330 Nicholls, J. F., Toumi, R., and Budgell, W. P.: Inertial currents in the Caspian Sea, Geophysical Research
- 331 Letters, 39, 10.1029/2012gl052989, 2012.
- Pettigrew, N. R.: The dynamics and kinematics of the coastal boundary layer off Long Island, 1981.
- Pollard, R. T., and Millard, R. C.: Comparison between ovserved and simulated wind-generated inertial
  oscillations, Deep Sea Research, 813-821, 1970.
- Price, J. F.: Upper ocean response to a hurricane, Journal of Physical Oceanography, 11, 153-175,
- 336 10.1175/1520-0485(1981)011<0153:uortah>2.0.co;2, 1981.
- Shearman, R. K.: Observations of near-inertial current variability on the New England shelf, Journal of
  Geophysical Research, 110, 10.1029/2004jc002341, 2005.
- 339 Sun, Z., Hu, J., Zheng, Q., and Li, C.: Strong near-inertial oscillations in geostrophic shear in the
- 340 northern South China Sea, Journal of Oceanography, 67, 377-384, 10.1007/s10872-011-0038-z, 2011.
- Webster, F.: Observation of inertial period motions in the deep sea, Reviews of Geophysics, 6, 473-490, 1968.
- 343 Xing, J. X., Davies, A. M., and Fraunie, P.: Model studies of near-inertial motion on the continental
- 344 shelf off northeast Spain: A three-dimensional two-dimensional one-dimensional model comparison
- 345 study, J Geophys Res-Oceans, 109, 10.1029/2003jc001822, 2004.
- 346 Zheng, Q., Lai, R. J., and Huang, N. E.: Observation of ocean current response to 1998 Hurricane
- 347 Georges in the Gulf of Mexico, Acta Oceanol. Sin., 25, 1-14, 2006.

- 349
- 350
- 351
- 352

# 353 Figures

354

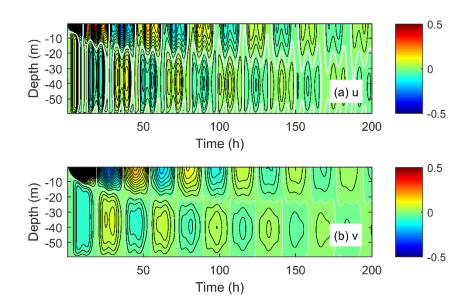
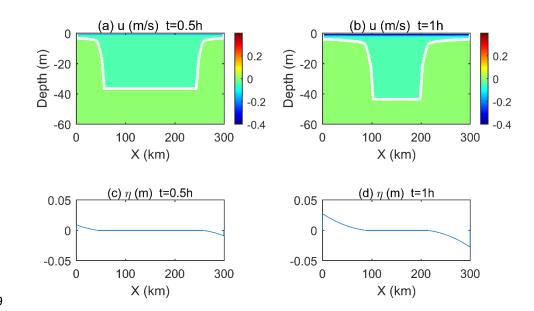




Fig. 1 Velocities (u and v, m/s) at x=70 km. The white lines denote the value of zero. The contour
interval is 0.02 m/s for both panels.

358



359

360 Fig. 2 Snapshots of eastward velocity and elevation ( $\eta$ ) at t=0.5 and 1 hour. The white lines represent

361

the value of zero.

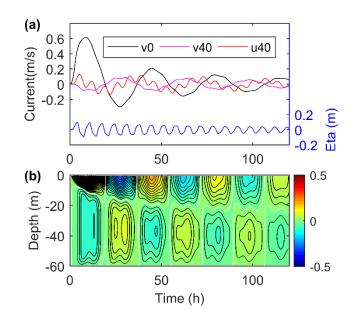
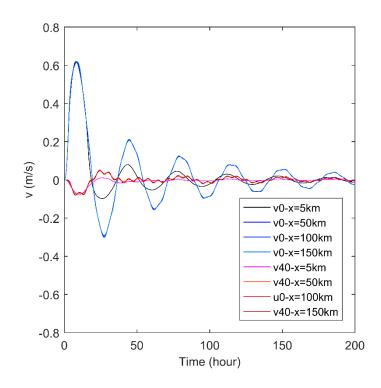


Fig. 3 (a) Time series of velocities and elevation at x=100 km. 'v0' and 'v40' mean the northward
velocity (v) at depths of 0 m and 40 m, and 'u40' is the eastward velocity (u) at 40 m. (b) Contours of v
at x=100 km. The white lines denote the value of zero, and the contour interval is 0.02 m/s.



368 Fig. 4 Time series of the northward velocity (v) at different depths and positions. 'v0' and 'v40' mean v

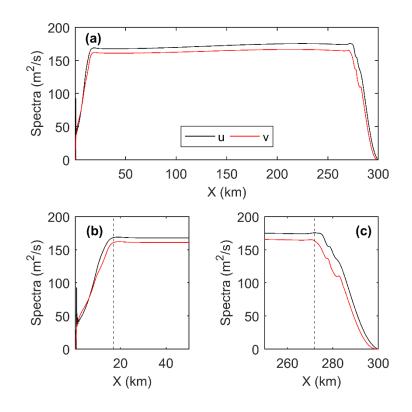
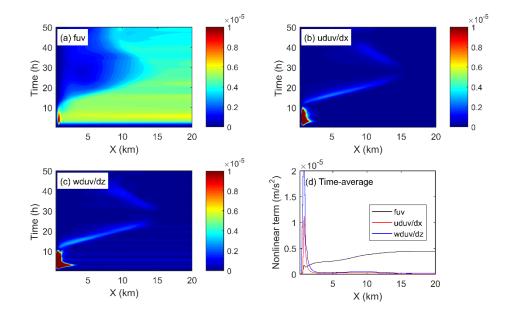


Fig. 5 Spatial variation of power spectra of velocities in near-inertial band for the homogeneous case.

(b) and (c) display detailed values near boundaries.

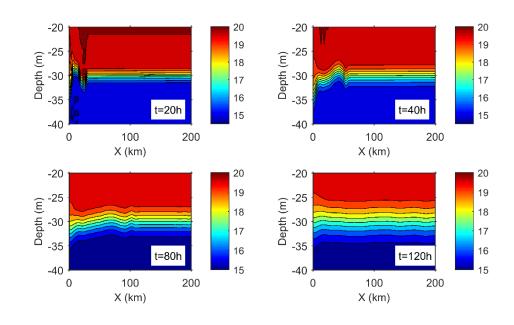


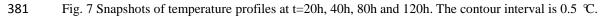


376 Fig 6. Variation of depth-mean inertial and nonlinear terms (m/s<sup>2</sup>). The inertial term (a) is calculated as

|f(u+iv)|, the horizontal nonlinear term (b) is  $|u(\partial u/\partial x+i\partial v/\partial x)|$ , and the vertical nonlinear

378 term (c) is 
$$\left| w \left( \frac{\partial u}{\partial z} + i \frac{\partial v}{\partial z} \right) \right|$$
. (d) Time averaged value for the first 50 hours.





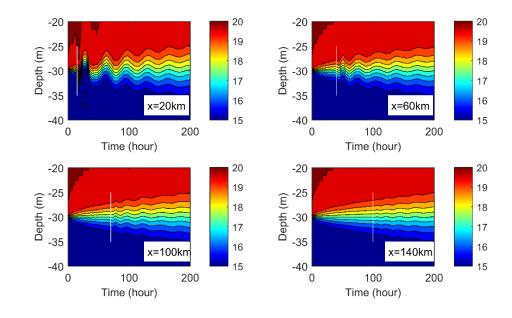




Fig. 8 Time series of temperature at x=20, 60, 100 and 140 km. White lines denote arrival of internal

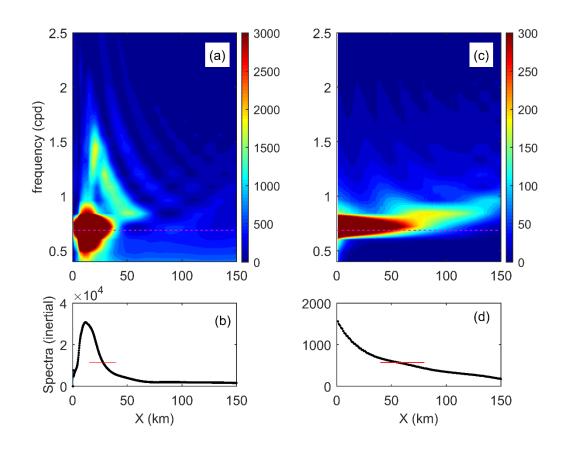


Fig. 9 (a) Spectra of the temperature at the mid-depth (z=-30 m). The pink dash line represents the inertial frequency, and the white line is the first mode seiche frequency. (b) Sum of spectra in inertial band with a red line denoting the e-folding value of the peak. (c) Theoretical spectra of mid-depth elevation calculated from the solution in the form of a Bessel function as in Eq. 3.16 of Pettigrew (1981). (d) Same as (b) but for theoretical spectra.

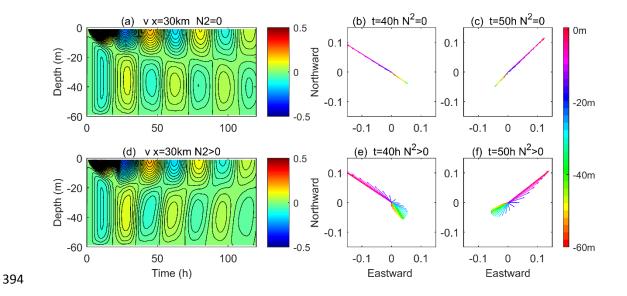
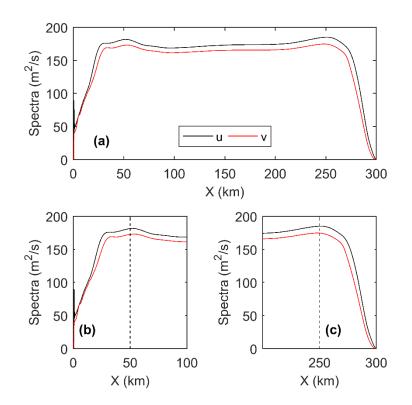
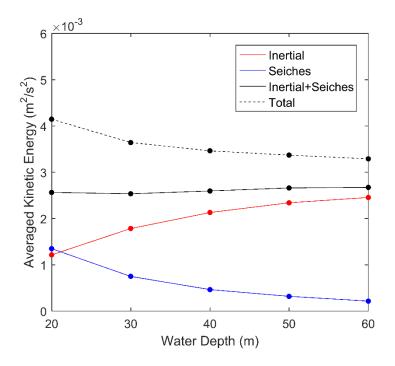


Fig. 10 Distribution of near-inertial currents (v, m/s) and current spirals for the cases without (a, b, c) and with (d, e, f) stratification at x=30 km. The near-inertial currents are obtained by applying a bandpass filter. The contour interval is 0.02 m/s.

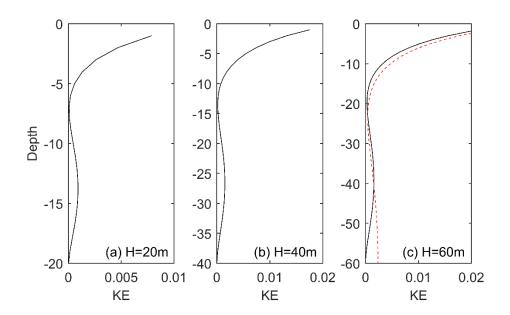


400 Fig. 11 Spatial variation of spectra of velocities in near-inertial band for the stratified case. (b) and (c)
401 display detailed values near boundaries.





404 Fig. 12 The kinetic energy of near-inertial motions and seiches for different water depths. For each
405 case, the currents are ban-pass filtered to get currents for each type of motions which are then averaged
406 over time and integrated over space to obtain a final value.



408

409 Fig. 13 Vertical profile of averaged inertial kinetic energy for the homogeneous cases with water depths

410 of 20 m, 40 m and 60 m. The red dash line in (c) denotes the slip case.