We are very appreciated for comments from two referees, which help us to improve this manuscript much. Our responses are italic. And the manuscript with tracked changes is attached behind.

Anonymous Referee #1

Aim of study is to investigate the absence of hypothesised even numbered modes of osculation within standing wave systems - called Seiches. Using MITGCM for an idealized basin 600km long (60m water depth) this is studied. The motivation, hypothesis and conclusion appears to be unclear, and needs to be stated; Further, the writing style also needs to be improved and much more detail and confidence in reported results are needed in my opinion. For example, a conclusion is needed in which the authors should state why study this phenomena (Why is this important?)? What was found? What this means for the scientific community (and stake holders)?

RE: This study aims to explore properties of near-inertial motions. We included the absence of even mode seiches because the seiches process occurs together with near-inertial motions. Actually they are very different topics. After a careful consideration, we decide to remove this section about the seiches and focus on discussing the near-inertial motion. Instead we add a new section (Section 5) to study the dependence of near-inertial motions on the water depth. The abstract, introduction and conclusion have been modified to make things much clearer. Please see the mark-up version of the manuscript.

Below are some further suggested changes to the text, but this is not a full list. Suggested improvements to text: Abstract - add more detail to explain why this study is about, why important, what was one and what this means. RE: Accepted and revised.

L25 - what kind of basin? an idealised rectangular? cer-tainly appears large enough for Coriolis (inertial oscillations) How was it studied? (i.e. a model). RE: *Added*.

L26 - what is "vertical stratification" I think you mean "stratified" RE: *Revised*.

L27 what are "even modes" explain further please to aid reader L53 (and throughout document)- please add space between references - for example here, "2016;Webster" should be "2016; Webster" L55 "motions(D'.." please add space and check throughout document

RE: These have been revised all through the manuscript.

L90 - 91. Nice clear aim, but why is this important? What is your hypothesis? Please be clear. RE: *Added*.

L100 - So you use the MITGCM model. Please add much more detail about this model both here and in the introduction. Why use this model? How do you know the model is correct? What are the discretised equations? How is wind stress parameterized into the model? Are the boundary conditions non-slip? What density of water is assumed? Furthermore, how can you be confident of the model results? I am sure this is a classical problem and could be compared to other models and theory for example (i.e. I could be mean here and ask if you used a different model would you get the same result?). Lastly, what stratification is used in the second case? what temperature, at what depth is thermocline?

RE: All these details have been added in the Section 2.

Anonymous Referee #2

The authors set out to describe inertial oscillations in a lake (or a cross section of an embayment - I'm not quite sure which). We are never told why they do this, or what the overall aim/hypothesis is, or what new knowledge we are going to get. The writing is sketchy and needs to be improved. However, at the end of the day, I don't think there is much new in this study, and I will outline why below.

RE: This study aims to explore properties of near-inertial motions. We included the absence of even mode seiches because the seiches process occurs together with near-inertial motions. Actually they are very different topics. After a careful consideration, we decide to remove this section about the seiches and focus on discussing the near-inertial motion. Instead we add a new section (Section 5) to study the dependence of near-inertial motions on the water depth. For detail, the purpose of this study is:

1. Discuss the cross-shelf distribution of near-inertial energy. As mentioned in the Introduction (Lines 66-76), observations show the near-inertial energy is maximum near the shelf break, from which it declines onshore and offshore. There has been a couple of research on discussing it, but no common interpretation is reached. Nicholls et al. (2012) simulated the near-inertial motion in the Caspian Sea, and found that the decrease of near-inertial energy depends on the distance from the coast, rather than correlated with the water depth. By solving the analytical model with a constant water depth, Pettigrew (1981) argued the

near-inertial wave is responsible for the decline of near-inertial energy near the coast. Therefore, we set up a simulation with a constant water depth to explore their ideas. The water depth is shallow (60 m) as in the shelf seas. The basin is chosen to be very wide (60 km) to guarantee that the near-inertial waves generated at one end do not which the other end during simulated duration. In our simulation, a gradual offshore increase of near-inertial energy is present in the case with only inertial oscillations. A small peak of near-inertial energy can be seen at ~50 km offshore in the case including the near-inertial waves. We conclude that the boundary effect on inertial oscillations play a dominant role, and the effect of near-inertial wave is secondary. This result is quite different from previous research.

- 2. Clarify the difference between inertial oscillations and near-inertial waves. When I was still a PhD student several years ago, I was confused with these two stuff. Many research just mentioned them as near-inertial motions. Through comparison of these simple simulations with and without vertical stratification, I am right now very clear with their differences. In shelf seas, currents associated with inertial oscillations have opposite phases between the upper and lower layers. This property is very similar to the mode-1 structure of internal wave. Thus many research mistakenly related it to near-inertial internal waves. In our simulations, we can see this vertical structure is mainly induced by inertial oscillations (the case without stratification). The inclusion of near-inertial internal waves only produces a slight tilting of thermocline. We are sure such a comparison is valuable and easy to understand, especially for new researchers who are interested in the near-inertial motion, though this comparison is very simple.
- 3. Explore more detail about the two-layer structure of inertial oscillations. Yes, this feature is due to the condition of zero crossing flow toward the land boundary. Some study briefly mentioned the role of barotropic waves. But it is not clear how the barotropic wave evolves to induce this structure. We checked out many references, but none has clarified this issue in detail. For such a fundamental property of inertial oscillation in shelf seas, it deserve a further study and a detailed interpretation. In our study, we give details on this process, many of which have not be shown in previous study. A new point is about the importance of the feedback between the barotropic wave and inertial currents.

More response to specific comments :

2m vertical seems quite coarse for the study.
 RE: *Simulations are reset and run with 1 m in vertical.*

2. How long are the simulations? RE: 200 hours. Added.

3. Why the chosen magnitude of the wind?RE: *The speed of 20 m/s is a normal value during passage of storm or clone, and is*

able to generate significant inertial oscillations and near-inertial internal waves.

- 4. It must also be noted that the barotropic Rossby radius is almost 500 km for the current set-up, so there will be interactions within the basin which must be quantified.
- RE: The width of the basin has been modified to be 300 km.
- 5. L223-224: show the computation and use SI units.

RE: The computation is just a quite simple estimation method for internal waves for a two-layer stratification. *Km/h* is more useful in our description.

6. Appendix: this is textbook stuff and can be omitted. Instead a reference can be added.

RE: Deleted.

1	A study on some basic features of seiches, inertial
2	oscillations and near-inertial internal waves
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5	Shenzhen, Tsinghua University, Shenzhen 518055, China.
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23 Abstract

24	Some basic features of seiches, inertial oscillations and near-inertial internal waves are investigated by
25	simulating a two-dimensional (x-z) rectangular shallow-basin (300 km \times 60 m) initialized driven by a
26	wind pulse. Two cases with and without the vertical stratification are conducted. For the homogeneous
27	case, near-inertial motions are pure inertial oscillations seiches and inertial oscillations dominate. We find
28	even modes of seiches disappear, which is attributed to a superposition of two seiches generated at east
29	and west coastal boundaries. They have anti-symmetric elevations and a phase lag of $n\pi$, thus their even
30	modes cancel each other. The inertial oscillation shows typical opposite currents between surface and
31	lower layers, which is formed by the feedback between barotropic waves and inertial currents. For the
32	stratified case, near-inertial internal waves are generated are generated at land boundaries and propagate
33	offshore with increasing frequencies, which induce tilting of velocity contours in the thermocline.
34	The inertial oscillation is uniform across the whole basin, except near the coastal boundaries (~20 km)
35	where it quickly declines to zero. This boundary effect is related to great enhancement of nonlinear terms,
36	especially the vertical nonlinear term ($w\partial \mathbf{u} / \partial z$). With inclusion of near-inertial internal waves, the
37	total near-inertial energy has a slight change, with occurrence of a small peak at ~50 km, which is similar
38	to previous researches. We conclude that, for this distribution of near-inertial energy, the boundary effect
39	for inertial oscillations is primary, and the near-inertial internal wave plays a secondary role.
40	Homogeneous cases with various water depths (50 m, 40 m, 30 m, 20 m) are also simulated. It is found

41 near-inertial energy monotonously declines with decreasing water depth, because more energy of initial

42 wind-driven currents is transferred to seiches formed by barotropic waves. For the case of 20 m, the

43 seiches energy even slightly overpasses the near-inertial energy. We suppose this is an important reason

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- 44 why near-inertial motions are weak and hardly observed in coastal regions.
- 45

46 Keywords: inertial oscillations, near-inertial internal waves, near-inertial energy

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55	1. Introduction
56	If a water particle is subject to no force except the Coriolis force, it will move at the local inertial
57	frequency (namely inertial motions). In reality, its frequency is usually slightly biased by other processes
58	(Kunze, 1985). Near-inertial motion has been observed and reported in many seas (e.g. Alford et al.,
59	2016; Webster, 1968). It is mainly generated by changing winds at the sea surface (Pollard and Millard,
60	1970; Chen et al., 2015b). The passage of a cyclone or a front can induce very strong near-inertial
61	motions(D'Asaro, 1985), which can last for 1-2 weeks and reach a maximum velocity magnitude of 0.5-
62	1.0 m/s (Chen et al., 2015a; Zheng et al., 2006; Sun et al., 2011). In deep seas, the near-inertial internal
63	wave propagates downwards to transfer energy to depth (Leaman and Sanford, 1975; Fu, 1981; Gill,
64	1984; Alford et al., 2012). The strong vertical shear of near-inertial currents may play an important role
65	in inducing mixing across the thermocline (Price, 1981; Burchard and Rippeth, 2009).
66	In shelf seas, near-inertial motions exhibit a two-layer structure, with an opposite phase between currents
67	in the surface and lower layers (Malone, 1968; Millot and Crepon, 1981; MacKinnon and Gregg, 2005).
68	By solving a two-layer analytic model using the Laplace transform, Pettigrew (1981) found this
69	'baroclinic' structure can be formed by inertial oscillations without inclusion of near-inertial internal
70	waves. DTherefore, due to similar vertical structure and frequencies, inertial oscillations and near-inertial
71	internal waves are hardly separable, and could easily be mistakenly recognized as each other.
72	In shelf seas, the near-inertial energy increases gradually offshore, and reaches a maximum near the shelf
73	break, found both in observations (Chen et al., 1996) and model simulations (Xing et al., 2004; Nicholls
74	et al., 2012). Chen and Xie (1997) reproduced this cross-shelf variation both in linear and nonlinear

simulations, and attribute it to large values of the cross-shelf gradient of surface elevation and the vertical

76 gradient of Reynolds stress near the shelf break. By using the analytic model of Pettigrew (1981),

77	Shearman (2005) argued that the cross-shelf variation is controlled by baroclinic waves which emanate
78	from the coast to introduce nullifying effects on the near-inertial energy near shore. Kundu et al. (1983)
79	found a coastal inhibition of near-inertial energy within the Rossby radius from the coast, which is
80	attributed to the downward and offshore leakage of near-inertial energy near the coast. As many factors
81	seems to have effects, the mechanism controlling the cross-shelf variation of near-inertial energy seems
82	complicated
83	In this paper, simple two-dimensional simulations are used to investigate some basic features of near-
84	inertial motions. Cases with and without vertical stratification are simulated to examine properties and
85	differences of inertial oscillations and near-inertial internal waves. The horizontal distribution of near-
86	inertial energy is discussed in detail. Also cases with various water depths are simulated to investigate
87	the dependence of near-inertial motions on the water depth.
88	

Buring the occurrence of near inertial motions, the wind force can also easily generate a seiche in close or semi-close basins (de Jong, 2003). A seiche is a standing wave formed in an enclosed or partially enclosed body of water, which has been widely observed in lakes, harbors, bays and seas (Miles, 1974;Metzner et al., 2000;Drago, 2009;Breaker et al., 2010). It has a period ranging from several minutes to several hours. In some regions its amplitude can reach several meters (e.g.Wang et al., 1987), which can induce flooding and cause damage to fishery and coastal facilities. In a closed rectangular basin of length L and depth H, the seiche period is given by the Merian's formula:

96
$$T = \frac{2L}{n\sqrt{gH}}$$
 (1)

97 where n=1, 2, 3, ... is the mode number. Csanady (1973, using the Laplace transform) found that even
98 modes of seiches were absent. However, the absence of even mode seiches has not been reported in
99 observation or model simulations, probably due to irregular topography in reality which makes it difficult
100 to compute the exact period of each mode. And it is not known why even modes disappear from the
101 perspective of physics which we want to explore.

102 In this paper, we try to use simple simulations to investigate some basic properties of the inertial

103 oscillation and the near-inertial internal wave and differences between them. Generation of two-layer

104	structure of inertial oscillations and horizontal distribution of near inertial energy are investigated in
105	details. The model is simple two-dimensional (x=600 km, z=60 m) and forced by a wind pulse with land
106	boundaries at both two sides. The missing of even mode seiches is also found and interpreted. Two cases
107	with and without vertical stratification are explored. Model settings are introduced in Section 2. In the
108	homogeneous case (Section 3), properties of seiches and inertial oscillations are investigated. In the
109	stratified case (Section 4), we study the difference near inertial internal waves introduce. Summary and
110	discussion are presented in the final section (Section 5).

111 2. Model Settings

112	The simulated region is a two-dimensional shallow rectangular basin (300 km \times 60 m). Numerical
113	simulations are done by the MIT general circulation model (MITgcm) (Marshall et al., 1997), which
114	discretizes the primitive equations and can be designed to model a wide range of phenomena There are
115	1500 grids in the horizontal ($\Delta x = 200$ m) and 60 grids in vertical ($\Delta z = 1$ m). The model is two
116	dimensional (i.e., the gradient along y is zero), with 3000 grids in the horizontal (x; $\Delta x = 200$ m) and
117	$\frac{30 \text{ grids in the vertical } (z; \Delta z = 2 \text{ m})}{2 \text{ m}}$. The water depth is uniform $\frac{(60 \text{ m})}{2}$, with east and west sides
118	boundaries being elosed (land)land boundaries. The vertical and horizontal eddy viscosities are assumed
119	constants as 5×10^{-4} m ² /s and 10 m ² /s, respectively. The Coriolis parameter is 5×10^{-5} s ⁻¹ (at a latitude of
120	N). The bottom boundary is no-slip. The model is forced by a spatially uniform wind which is
121	kept westward and increases from 0 to 0.73 N/m^2 (corresponding to a wind speed of 20 m/s) for the first
122	three hours and then suddenly stops. The model runs for 200 hours in total, with a time step of 4 seconds.
123	The first case has no vertical stratification is homogeneous, while the second one has a stratification of
124	two-layer structure initially. For the stratified case, <u>#the temperature is 20°C in the upper layer (-30</u>
125	m <z<0), (-60="" 15°c="" and="" constant,="" density="" in="" is="" is<="" layer="" lower="" m).="" m<z<-30="" salinity="" so="" th="" the=""></z<0),>
126	determined by the temperature.
127	Except stratification all settings of these two cases are the same,
128	3. Inertial oscillation Results without vertical stratification
129	3.— <u>The first case is without the presence of vertical stratification. Thus near-inertial internal wave is</u>

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130 <u>absent, and the near-inertial motion is pure inertial oscillations</u>

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带格式的: 字体: (默认) Times New Roman, 10 磅, 加 粗 131 For the first case without vertical stratification, seiches and inertial oscillations are two dominant 132 processes. 133 3.1 Seiches 134 Due to the westward flow driven by the wind, the water level goes up at the west coast and down at the 135 east coast initially (Fig 1). A wave front propagates from each end at the speed of the barotropic wave 136 $(\sqrt{gH} = 24 \text{ m/s or } 87 \text{ km/h})$. As the wind stress and the water depth are uniform across the basin, the 137 elevation at the west is antisymmetric to that at the east (i.e. with the same amplitude but opposite phase). 138 The spectra of elevations is shown in Fig 2. At the inertial frequency, the elevation energy is slightly 139 increased. The most energetic peak is at the first mode of seiches, which is slightly biased by the earth 140 rotation effect. With the rotation, the wave frequency for each mode of seiche is given by (see the 141 Appendix):

142
$$-\frac{\omega_n^2 - f^2 + \frac{n^2 \pi^2 g H}{L^2}}{-(2)}$$
 (2)

where *f* is the inertial frequency, *n* the mode number, *g* the gravity acceleration, *H* the water depth, and *L* the basin width. As in most cases the horizontal scale of a closed basin is relatively small (<200 km),
the second term on the right hand side of Eq. (2) is much greater than the inertial frequency term, thus
the rotation effect is usually negligible. Here due to a large basin width (600 km), the rotation effect is
obvious.-

148 The energy of the first mode is minimal at the middle of the basin (i.e., x=300 km) and maximal at two 149 boundaries. The second mode energy is almost negligible. The third mode, which has three nodes, is 150 much more energetic than the second mode. The fourth mode vanishes, while the fifth mode can be seen 151 with five nodes although it has relative low energy. In a word, the even modes are absent. In the real 152 world, due to irregular topography, there is uncertainty in computing the exact period of each mode, and 153 the research on higher modes is limited. Csanady (1973, using the Laplace transform) found the even 154 modes of seiches absent. Here we propose an alternative way combining physics and mathematics to interpret this phenomenon. 155

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156 As derived from the appendix, the elevation of a seiche in a closed basin can be given by

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smaller peak at the frequency of the first mode seicher this simulation is two-dimensional, i.e., the
gradient along *y*-axis is zero, the seiche has little energy in v which shows clearly regular variation at the
inertial frequency.

182 In the vertical direction, currents display a two-layer structure, with their phase being opposite between 183 surface and lower layers. They are maximum at the surface, and have a weaker maximum in the lower 184 layer (~40 m), with a minimum at the depth of ~20 m. -The velocity gradually diminishes to zero at the bottom due to the bottom friction. This is the typical vertical structure of shelf-sea inertial oscillations, 185 186 which have been frequently observed (Shearman, 2005; MacKinnon and Gregg, 2005). In practice, this 187 vertical distribution can be modified due to presence of other processes, such as the surface maximum 188 being pushed down to the subsurface (e.g. Chen et al., 2013). Note that without stratification in this 189 simulation the near-inertial internal wave is absent. However, this two-layer structure of inertial 190 oscillations looks 'baroclinic', which makes it easy to be mistakenly attributed to the near-inertial internal 191 wave (Pettigrew, 1981).

It is interesting that currents of non-baroclinic inertial oscillations reverse between the surface and lower
layers. This is usually attributed to the presence of the coast, which requires the normal-to-coast transport
to be zero, thus currents in upper and lower layers compensate each other (Millot and Crepon, 1981;
Chen et al., 1996). <u>However, it remains unclear how this vertical structure is established. Here we try to</u>
give more detail on how this process works.-

197 As the westward wind blows for first three hours, the initial inertial current is also westward and only 198 exists in the very surface layer (Fig. 24). In the lower layer there is no movement initially. Thus a 199 westward transport is produced, which generates a rise (in the west) and fall (in the east) of elevation 200 near coastal boundaries. The elevation slope behaves in a form of barotropic wave which propagates 201 offshore at a great speed (87 km/h). The current driven by the barotropic wave is eastward, and uniform 202 vertically. Therefore, with arrival of the barotropic wave the westward current in the surface is reduced, 203 and the movement in the lower layer commences (Fig. 24). After passage of the first two barotropic 204 waves (originated from both sides), currents in the lower layer have reached a relatively great value, 205 while currents in the surface layer have been largely decreased (Fig. 35a). Accordingly, the depth-206 integrated transport diminishes a lot. This is like a feedback between inertial currents and barotropic 207 waves. If only the depth-integrated transport of currents exist, barotropic waves will be generated, which 8

reduce the surface currents but increase the lower layer currents, thus reduces the current transport. It will end up with inertial currents in the surface and lower layers having opposite directions and comparable amplitudes. As seen from Fig. 13b, the typical vertical structure of inertial currents is established within the first inertial period. At a place further offshore, such as at x=200 km, the barotropic wave takes about two more hours to arrive compared with x=70 km, thus the maximum value of inertial currents in lower layer is lagged behind that in surface layer (Fig. 5b).

214 3.2.2 Horizontal distributions of inertial energy

215 The inertial velocities are almost entirely the same across the basin (Fig. 46), except near the boundary. 216 This indicates that inertial oscillations have a coherence scale of almost the basin width. This is because 217 in our simulation the wind force is spatially uniform, and the bottom is flat. The inertial velocities in the 218 lower layer have slightly more variation across the basin than those in the surface layer, because inertial 219 velocities in the lower layer is correlated to propagation of barotropic waves as discussed in 3.2.1, while 220 the surface inertial currents are driven by spatially uniform wind. In shelf sea regions, the wind forcing 221 is usually coherent as the synoptic scale is much larger, however, the topography that is mostly not flat 222 could generate barotropic waves at various places, and thus significantly decrease coherence of inertial 223 currents in the lower layer.

The spectra of velocities in the inertial band are almost uniform except near the boundaries (Fig. 75), consistent with the velocities. Near the boundaries, the inertial energy declines gradually to zero from $x=\sim20$ km to the coast wall. The east side has slightly greater inertial energy and albit wider boundary layer compared to the west side.

228 We calculate the nonlinear and inertial terms in the momentum equation and find that nonlinear terms 229 are of relatively high values initially within 2 km away from the land boundary (Fig 8be6bc), where the 230 inertial term is smaller (Fig 8a6a). For the time-averaged values (Fig 8d6d), the vertical nonlinear term is two times more than the horizontal nonlinear term. The inertial term drops sharply near the boundary, 231 232 and rises gradually with the distance away from the boundary. At x>15km, it keeps an almost constant 233 value which is much greater than nonlinear terms. Thus it is concluded that the significant decrease of 234 inertial oscillations near the boundary is due to influence of nonlinear terms, especially the vertical 235 nonlinear term.

236 4. Near-inertial internal waves

In addition to inertial oscillations, near-inertial internal waves are usually generated along when the vertical stratification is present. However, due to their close frequencies inertial oscillations and nearinertial internal waves are difficult to be separated. Thus we run a second simulation with the presence of stratification to investigate differences that near-inertial internal waves introduce. The temperature is 20° C in the upper layer (-30 m<z<0), and 15^{\circ}C in the lower layer (-60 m<z<-30 m). The salinity is econstant, so the density is determined by the temperature.

243 4.1 Temperature distributions

244 Fig. 9-7 shows the evolution of temperature profiles with time. One can see an internal wave packet is 245 generated at the west coast, and then propagates offshore. The wave phase speed is around 1 km/h, 246 consistent with the theoretical value computed using the stratification. Before arrival of internal waves, 247 the temperature at mid-depth diffuses gradually due to vertical diffusion in the model. For a fixed position 248 at x=20 km (Fig. <u>108</u>), the temperature varies with the inertial period (34.9 hours) and the amplitude of 249 fluctuation declines gradually with time. At x=60 km and x=100 km, the strength of internal waves is 250 much reduced. And wave periods are shorter initially, followed by a gradually increase to the inertial 251 period. At x=140 km, the internal wave becomes as weak as the background disturbance.

252 A spectral analysis of the temperature at mid-depth (z=-30 m) is shown in Fig. 11a9a. The strongest peak is at near the inertial frequency (0.69 cpd). but only confined to the region close to the boundary (x<40 253 km). In the region 20km<x<70km, the by is also large at higher frequencies of 0.8-1.7 cpd. This 254 255 generally agrees with properties of Poincar éwaves. During a Rossby adjustment, the waves with higher 256 frequencies propagate offshore at greater group speeds, thus for places further offshore the waves have 257 higher frequencies (Millot and Crepon, 1981). While the wave with a frequency closest to the inertial 258 frequency moves at the slowest group velocity, and it takes a relatively long time to propagate far offshore, 259 thus it is mostly confined to near the boundary. By solving an idealized two-layer model equation, the 260 response of Rossby adjustment can be expressed in form of Bessel functions (Millot and Crepon, 1981; 261 Gill, 1982; Pettigrew, 1981), as in Fig. 11ed-9cd showing the spectra of mid-depth elevation. The difference from our case is obvious. The frequency of theoretical near-inertial waves increase gradually 262 263 with the distance from the coast, while in our case this property is absent. And the theoretical inertial

264 energy has a e-folding scale of almost the Rossby radius (54 km), while in our case the e-folding scale is

265 much smaller (~15 km).

266 4.2 Velocity distributions

With presence of near-inertial internal waves, the contours of velocities near the thermocline tilt slightly
(Fig. <u>12d10d</u>), and indicates an upward propagation of phase, thus a downward energy flux. This can
also be seen in vertical spirals of velocities (Figs. <u>12e-10e</u> and <u>12f10f</u>). With only inertial oscillations,
current vectors mostly point toward two opposite directions. Once the near-inertial wave is included, the
current vectors gradually rotate clockwise with depth.

The spatial distribution of the near-inertial energy is also slightly changed compared to the case with only 272 273 inertial oscillations (Fig. 13-11 and Fig. 75). It is also greatly reduced to zero in the boundary layer (0-274 20 km) like the case without stratification. But at ~50 km away from the boundary the inertial energy 275 reaches a peak. Further away (>100 km) it becomes a constant. This spatial distribution of inertial energy 276 is similar to that observed in shelf seas, with maximum near the shelf break (Chen et al., 1996; Shearman, 277 2005). In our case, the boundary layer effect which induces a sharp decrease to zero makes a major 278 contribution, and near-inertial internal waves which bring a small peak further offshore make a secondary 279 influence.

280 <u>5. Dependence on the water depth</u>

281 In coastal regions, near-inertial motions are rarely reported. It is speculated that the strong dissipation 282 and bottoms-friction in coastal region suppress the development of near-inertial motions. However, Chen 283 (2014) found the water depth is also a sensitive factor, with significant reduction for the case with smaller 284 water depth. Here we will run cases with different water depths and clarify why the near-inertial energy 285 changes with water depth. Homogeneous cases with water depths of 50 m, 40 m, 30 m, 20 m are 286 simulated. The vertical interval for all cases is 1 m. All the other parameters including viscosities are the 287 same as the homogeneous case of 60 m. 288 For each case, the currents are band-pass filtered to obtain near-inertial currents. Then near-inertial 289 kinetic energy can be calculated. As seen in Fig. 12, the near-inertial energy gradually declines with

- 290 decreasing water depth. In this dynamics system, the other dominant process are the seiches induced by
- 291 barotropic waves. As the elevation induced by seiches is anti-symmetric in such a basin, the potential

292 energy is little. The kinetic energy of siehces can also be calculated by the band-pass filtered currents. 293 We find the energy of seiches, by contrast, increases gradually with decreasing water depth. For the case 294 of 60m, the near-inertial energy is much greater than the seiches energy. But for the case of 20 m, the 295 energy of seiches has overpasses the near-inertial energy slightly. The sum-energy of these two processes 296 almost keeps constant with varying water depth. For a shallower water depth, the reduction of near-297 inertial energy equals the increase of seiches energy. The initial current is wind-driven and only 298 distributes in the surface layer. The unbalanced across-shelf flow generates elevation near the land 299 boundary which propagates offshore as barotropic waves and form seiches. Part of the energy goes to 300 form inertial oscillations. For a shallower water depth, the elevation is enlarged, and more energy is 301 transferred to form seiches, thus with weakened near-inertial motions. Therefore, in coastal regions with 302 water depth less than 30m, the near-inertial motion is weak, due to the suppressing of barotropic waves. 303 As seen in Section 3.1, inertial oscillations behave in a two-layer structure, with currents in the upper 304 layer in opposite phase with those of lower layer. In terms of kinetic energy, for the case of 60 m (Fig. 305 13), the near-inertial motion is maximized in the very surface, minimized near the depth of 20 m, and 306 then gradually increases with depth to form a much smaller peak at 40 m. Near the bottom, the near-307 inertial energy gradually reduces to zero due to bottom friction. When we set the bottom boundary 308 condition from nonslip to slip, such a boundary structure vanishes, and near-inertial energy become 309 constant in the lower layer. For other cases of 20 m and 40 m, their vertical profile are almost the same 310 as the 60m case. The minimum positions are all located at 1/3 of the water depth. This implies the vertical 311 distribution of near-inertial energy is independent of water depth. Note that in our cases, the vertical 312 viscosity is set as a constant value. In practice, the viscosity in thermocline is usually significantly 313 reduced, thus the minimum position of near-inertial energy is located just below the mixed layer.

314 5.

315 6. Summary and discussion

Two sets of i<u>I</u>dealized simple two-dimensional (x-z) simulations are conducted to examine the response of a shallow closed basin_<u>(600 km>60 m)</u>-to a wind pulse. The first case is homogeneous, in which properties <u>the near-inertial motion is pure inertial oscillations</u> seiches and inertial oscillations are investigated. Barotropic waves are generated at two coastal boundaries which then propagate and reflect 320 to form seiches. The seiche has the horizontal structure and frequencies consistent with the theory. 321 Seiches of even number modes are absent, which has been rarely reported. By using the Laplace 322 transform to solve the equations, Csanady (1973) found even mode seiches absent. We interpret it as 323 superposition of two seiches, which are formed by barotropic waves originating from east and west 324 boundaries. They have anti-symmetric elevation and a phase lag of $n\pi$, thus their even mode cancels 325 each other. The mechanism we propose is more physical, and thus a good supplement to explain this 326 phenomenon. Note that for the even modes to be absent the wind forcing and the topography are required 327 to be uniform spatially to keep these two seiches having anti-symmetric elevation.

328 The inertial oscillation is energetic in the homogeneous case. It has a two-layer structure, with currents 329 in the surface and lower layers being opposite in phase, which has been reported frequently in shelf seas. 330 We find that the inertial current is confined in the surface layer initially. The induced depth-integrated 331 transport generates barotropic waves near boundaries which propagates quickly offshore. The flow 332 driven by the barotropic wave is independent of depth and opposite to the surface flow. Thus the surface 333 flow is reduced but the flow in the lower layer is increased, as a result the transport diminishes. This 334 feedback between barotropic waves and currents continues and ends up with the depth-integrated 335 transport vanishes, i.e., inertial currents in upper and low layers having opposite phases and comparable amplitudes. In our simulation, within just one inertial period me typical structure of inertial currents has 336 337 been established. By solving a two-layer analytic model using the Laplace transform, Pettigrew (1981) 338 also found the vertical structure of opposite currents associated with inertial oscillations. He argued that 339 the arrival of a barotropic wave for a fixed location cancels half of the inertial oscillation in the surface 340 layer, and initiates an equal and opposite oscillation in the lower layer. Our simulations further 341 demonstrate the role of barotropic waves in forming this feature, hows some more realistic details 342 during this process.

The second case is set up with idealized two-layer stratification, thus near-inertial internal waves are generated. For a fixed position, velocity contours show clear obvious tiltings near the thermocline, and velocity vectors display clearly anti-cyclonic spirals with depth. These could be useful clues to examine occurrence of near-inertial internal waves. Near the land boundary the vertical elevation generates fluctuations of thermocline that propagate offshore. The energy of near-inertial internal waves is confined to near the land boundary (x< 40 km). At positions further offshore, the waves have higher frequencies. This is generally consistent with properties of Rossby adjustment process. However, our simulated result
also shows evident discrepancies from theoretical values obtained in classic solutions of Rossby
adjustment problem.

352 The inertial oscillation has a very large coherent scale of almost the basin scale (600 km). It is uniform 353 in both amplitude and phase across the basin, except near the boundary (~20 km offshore). The energy 354 of inertial oscillations declines gradually to zero from x=20 km to the coast. This boundary effect is attributed to influence of nonlinear terms, especially the vertical term ($w\partial \mathbf{u} / \partial z$), which are greatly 355 enhanced near the boundary, and overweighs the inertial term ($f\mathbf{u}$). When near-inertial internal waves 356 357 are produced in the stratified case, the distribution of total near-inertial energy is modified slightly near the boundary. A small peak appears at ~ 50 km offshore. This is similar to the cross-shelf distribution of 358 359 near-inertial energy observed in shelf seas (Chen et al., 1996; Shearman, 2005). This energy distribution 360 has been attributed to different reasons, such as downward and offshore leakage of near-inertial energy 361 near the coast (Kundu et al., 1983), the variation of elevation and Reynolds stress terms associated with 362 the topography (Chen and Xie, 1997) and the influence of the baroclinic wave (Shearman, 2005; Nicholls 363 et al., 2012). In our simulations, this horizontal distribution of near-inertial energy is primarily controlled 364 by the boundary effect on inertial oscillations, and the near-inertial internal wave makes a secondary 365 effect.

Homogeneous cases with various water depths (50 m, 40 m, 30 m, 20 m and 10 m) are also simulated.
The inertial energy is reduced with decreasing water depth, while the energy of seiches, by contrast,
increases for the shallower case. For the case of 10 m, the seiches energy has slightly overpassed the
inertial energy. It is interesting that the reduction of inertial energy just equals the increase of seiches
energy, which implies more energy of initial wind-driven currents is transferred to the seiches for the
shallower cases, and thus less energy goes to the inertial process. This is probably an important reason
why near-inertial motions is, weak and rarely reported in shallow coastal regions.

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$$\eta = c_1 \frac{\cos(\omega_n t) - c_4 \sin(\omega_n t)}{L}$$

$$\nu = C_1 \frac{f}{\omega_n} \sin \frac{n\pi x}{L} \left(C_3 \cos \omega_n t - C_4 \sin \omega_n t \right)$$
(A10c)

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516 Fig. 9 (a) Spectra of the temperature at the mid-depth (z=-30 m). The pink dash line represents the
517 inertial frequency, and the white line is the first mode seiche frequency. (b) Sum of spectra in inertial
518 band with a red line denoting the e-folding value of the peak. (c) Theoretical spectra of mid-depth
519 elevation calculated from the solution in the form of a Bessel function as in Eq. 3.16 of Pettigrew.
520 (1981). (d) Same as (b) but for theoretical spectra.





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597 display detailed values near boundaries.