

We are appreciated for comments from two referees and the editor, which help us to improve this manuscript much. All the comments from referees and the editor and our responses (*italic*) are listed one by one below. And the manuscript with tracked changes is attached afterwards.

Anonymous Referee #1

Aim of study is to investigate the absence of hypothesised even numbered modes of osculation within standing wave systems - called Seiches. Using MITGCM for an idealized basin 600km long (60m water depth) this is studied. The motivation, hypothesis and conclusion appears to be unclear, and needs to be stated; Further, the writing style also needs to be improved and much more detail and confidence in reported results are needed in my opinion. For example, a conclusion is needed in which the authors should state why study this phenomena (Why is this important?)? What was found? What this means for the scientific community (and stake holders)?

RE: This study aims to explore properties of near-inertial motions. We included the absence of even mode seiches because the seiches process occurs together with near-inertial motions. Actually they are very different topics. After a careful consideration, we decide to remove this section about the seiches and focus on discussing the near-inertial motion. Instead we add a new section (Section 5) to study the dependence of near-inertial motions on the water depth. The abstract, introduction and conclusion have been modified to make things much clearer. Please see the mark-up version of the manuscript.

Below are some further suggested changes to the text, but this is not a full list. Suggested improvements to text: Abstract - add more detail to explain why this study is about, why important, what was one and what this means.

RE: Accepted and revised.

L25 - what kind of basin? an idealised rectangular? cer-tainly appears large enough for Coriolis (inertial oscillations) How was it studied? (i.e. a model).

RE: Added.

L26 - what is "vertical stratification" I think you mean "stratified"

RE: Revised.

L27 what are "even modes" explain further please to aid reader L53 (and throughout document)- please add space between references - for example here, "2016;Webster" should be "2016; Webster" L55 "motions(D'.." please add space and check throughout document

RE: These have been revised all through the manuscript.

L90 - 91. Nice clear aim, but why is this important? What is your hypothesis? Please be clear.

RE: *Added.*

L100 - So you use the MITGCM model. Please add much more detail about this model both here and in the introduction. Why use this model? How do you know the model is correct? What are the discretised equations? How is wind stress parameterized into the model? Are the boundary conditions non-slip? What density of water is assumed? Furthermore, how can you be confident of the model results? I am sure this is a classical problem and could be compared to other models and theory for example (i.e. I could be mean here and ask if you used a different model would you get the same result?). Lastly, what stratification is used in the second case? what temperature, at what depth is thermocline?

RE: *All these details have been added in the Section 2.*

Anonymous Referee #2

The authors set out to describe inertial oscillations in a lake (or a cross section of an embayment – I'm not quite sure which). We are never told why they do this, or what the overall aim/hypothesis is, or what new knowledge we are going to get. The writing is sketchy and needs to be improved. However, at the end of the day, I don't think there is much new in this study, and I will outline why below.

RE: *This study aims to explore properties of near-inertial motions. We included the absence of even mode seiches because the seiches process occurs together with near-inertial motions. Actually they are very different topics. After a careful consideration, we decide to remove this section about the seiches and focus on discussing the near-inertial motion. Instead we add a new section (Section 5) to study the dependence of near-inertial motions on the water depth. For detail, the purpose of this study is:*

1. *Discuss the cross-shelf distribution of near-inertial energy. As mentioned in the Introduction (Lines 66-76), observations show the near-inertial energy is maximum near the shelf break, from which it declines onshore and offshore. There has been a couple of research on discussing it, but no common interpretation is reached. Nicholls et al. (2012) simulated the near-inertial motion in the Caspian Sea, and found that the decrease of near-inertial energy depends on the distance from the coast, rather than correlated with the water depth. By solving the*

analytical model with a constant water depth, Pettigrew (1981) argued the near-inertial wave is responsible for the decline of near-inertial energy near the coast. Therefore, we set up a simulation with a constant water depth to explore their ideas. The water depth is shallow (60 m) as in the shelf seas. The basin is chosen to be very wide (300 km) to guarantee that the near-inertial waves generated at one end do not reach the other end during simulated duration. In our simulation, a gradual offshore increase of near-inertial energy is present in the case with only inertial oscillations. A small peak of near-inertial energy can be seen at ~50 km offshore in the case including the near-inertial waves. We conclude that the boundary effect on inertial oscillations play a dominant role, and the effect of near-inertial wave is secondary. This result is quite different from previous research.

2. *Clarify the difference between inertial oscillations and near-inertial waves. When I was still a PhD student several years ago, I was confused with these two stuff. Many research just mentioned them as near-inertial motions. Through comparison of these simple simulations with and without vertical stratification, I am right now very clear with their differences. In shelf seas, currents associated with inertial oscillations have opposite phases between the upper and lower layers. This property is very similar to the mode-1 structure of internal wave. Thus many research mistakenly related it to near-inertial internal waves. In our simulations, we can see this vertical structure is mainly induced by inertial oscillations (the case without stratification). The inclusion of near-inertial internal waves only produces a slight tilting of thermocline. We are sure such a comparison is valuable and easy to understand, especially for new researchers who are interested in the near-inertial motion, though this comparison is very simple.*
3. *Explore more detail about the two-layer structure of inertial oscillations. Yes, this feature is due to the condition of zero crossing flow toward the land boundary. Some study briefly mentioned the role of barotropic waves. But it is not clear how the barotropic wave evolves to induce this structure. We checked out many references, but none has clarified this issue in detail. For such a fundamental property of inertial oscillation in shelf seas, it deserve a further study and a detailed interpretation. In our study, we give details on this process, many of which have not be shown in previous study. A new point is about the importance of the feedback between the barotropic wave and inertial currents.*

More response to specific comments :

1. 2m vertical seems quite coarse for the study.

RE: *Simulations are reset and run with 1 m in vertical.*

2. How long are the simulations?

RE: *200 hours. Added.*

3. Why the chosen magnitude of the wind?

RE: *The speed of 20 m/s is a normal value during passage of storm or clone, and is able to generate significant inertial oscillations and near-inertial internal waves.*

4. It must also be noted that the barotropic Rossby radius is almost 500 km for the current set-up, so there will be interactions within the basin which must be quantified.

RE: *The width of the basin has been modified to be 300 km.*

5. L223-224: show the computation and use SI units.

RE: *The computation is just a quite simple estimation method for internal waves for a two-layer stratification. Km/h is more useful in our description.*

6. Appendix: this is textbook stuff and can be omitted. Instead a reference can be added.

RE: *Deleted.*

From the topic editor

The paper is interesting comparison between theoretical work and a non-linear numerical model (MIT model) on inertial currents and waves. The revised version is clear presentation of the model results and gives some insight into to the differences between the model and published theory.

However, the reviewers have commented on the fact that the model is only 2 dimensional with lateral boundaries. It is therefore only applicable to a lake or an embayment on the shelf. It would be interesting to look at an extension to where one boundary was open to replicate the response to a transverse continental shelf.

The revised version can be published with minor revisions. I have attached a version which has corrections to the English.

RE: *We are very glad that you think it is an interesting comparison between theory and simulation, which is our motivation. It is definitely a good direction to run some new cases with open boundaries.*

1. Line 33, 'increasing' replaced by 'higher'.

RE: *Accepted and revised.*

2. Line 42, delete 'formed'.

RE: *Accepted and revised.*

3. Line 80, offshore is not the coast. I do not understand this highlighted phrase.
RE: *It means the inertial energy is leaked downward to the lower layer and offshore, thus the inertial energy near the coast is reduced. This sentence has been slightly changed to make it clearer.*
4. Line 81, 'seems complicated' replaced by 'is not clear'.
RE: *Accepted and revised.*
5. Line 85, 'of' replaced by 'between'.
RE: *Accepted and revised.*
6. Line 126, you should either mention the corresponding density difference between the top and bottom layer, or give the thermal expansion coefficient, because this controls the long baroclinic wave speed.
RE: *We clarify this by adding a sentence: The salinity is constant, and the density is linearly determined by the temperature, with an expansion coefficient of $2 \times 10^{-4} \text{ }^{\circ}\text{C}^{-1}$.*
7. Line 127, this seems contradict the previous sentence.
RE: *Deleted as suggested.*
8. Line 179, period of the first mode seiche?
RE: *It is 6.9 hours which is added.*
9. Line 204, 'great' replaced by 'large'.
RE: *Accepted and revised.*
10. Line 219, 'correlated' replaced by 'related'.
RE: *Accepted and revised.*
11. Line 254, use hours as well to be consistent with line 248.
RE: *As circle per day is a more common and intuitive unit, we think it better to keep using cpd.*
12. Line 264, It would be worth giving the values for the barotropic and baroclinic Rossby radii in the method section.
RE: *Yes, we give these values in the method section (end of the Section 2).*
13. Line 295, 'overpasses' replaced by 'exceeded', and 'sum' replaced by 'total'.
RE: *Accepted and revised.*
14. Line 302, 'suppressing' replaced by 'suppression'.
RE: *Accepted and revised.*

15. Line 335, 'low' replaced by 'lower'.

RE: *Accepted and revised.*

16. Line 341, this is a comparison of theory with a numerical model, and therefore you need explain why the features are more realistic. Where are the observations to test the theory or model against? The model is more complex than the theory.

For example the effect of the non-linear terms and this is perhaps.

RE: *Yes, it is mainly due to nonlinearity of the model which brings the difference. We add a sentence to clarify this. Actually, I do not find any references which use observation to test this theoretical feature about the varying frequencies of the Rossby adjustment. It is a good idea to try it.*

17. Line 364, 'makes' replaced by 'has'.

RE: *Accepted and revised.*

There are many places missing 'a' or 'the' as the editor pointed out. We have accepted and revised them all. Thanks a lot for such a careful review.

A study on some basic features of ~~seiches~~, inertial oscillations and near-inertial internal waves

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Abstract

Some basic features of ~~seiches~~, inertial oscillations and near-inertial internal waves are investigated by simulating a two-dimensional (x-z) ~~rectangular shallow~~-basin (~~300 km × 60 m~~) ~~initialized driven~~ by a wind pulse. ~~Two cases with and without the vertical stratification are conducted.~~ For the homogeneous case, ~~near-inertial motions are pure inertial oscillations~~ ~~seiches and inertial oscillations dominate.~~ ~~We find even modes of seiches disappear, which is attributed to a superposition of two seiches generated at east and west coastal boundaries. They have anti-symmetric elevations and a phase lag of $n\pi$, thus their even modes cancel each other.~~ The inertial oscillation shows typical opposite currents between surface and lower layers, which is formed by the feedback between barotropic waves and inertial currents. For the stratified case, near-inertial internal waves ~~are generated~~ are generated at land boundaries and propagate offshore with ~~increasing higher~~ frequencies, which induce tilting of velocity contours in the thermocline.

The inertial oscillation is uniform across the whole basin, except near the coastal boundaries (~20 km) where it quickly declines to zero. This boundary effect is related to great enhancement of nonlinear terms, especially the vertical nonlinear term ($w\partial\mathbf{u}/\partial z$). With the inclusion of near-inertial internal waves, the total near-inertial energy has a slight change, with occurrence of a small peak at ~50 km, which is similar to previous researches. We conclude that, for this distribution of near-inertial energy, the boundary effect for inertial oscillations is primary, and the near-inertial internal wave plays a secondary role.

Homogeneous cases with various water depths (50 m, 40 m, 30 m, 20 m) are also simulated. It is found near-inertial energy monotonously declines with decreasing water depth, because more energy of the initial wind-driven currents is transferred to seiches by barotropic waves. For the case of 20 m, the seiches energy even slightly exceeds the near-inertial energy. We suppose this is an important reason why near-inertial motions are weak and hardly observed in coastal regions.

Keywords: inertial oscillations, near-inertial internal waves, near-inertial energy

1. Introduction

~~If a water particle is subject to no force except the Coriolis force, it will move at the local inertial frequency (namely inertial motions). In reality, its frequency is usually slightly biased by other processes (Kunze, 1985).~~ Near-inertial motion has been observed and reported in many seas (e.g. Alford et al., 2016; Webster, 1968). It is mainly generated by changing winds at the sea surface (Pollard and Millard, 1970; Chen et al., 2015b). The passage of a cyclone or a front can induce very strong near-inertial motions (D'Asaro, 1985), which can last for 1-2 weeks and reach a maximum velocity magnitude of 0.5-1.0 m/s (Chen et al., 2015a; Zheng et al., 2006; Sun et al., 2011). In deep seas, the near-inertial internal wave propagates downwards to transfer energy to depth (Leaman and Sanford, 1975; Fu, 1981; Gill, 1984; Alford et al., 2012). The strong vertical shear of near-inertial currents may play an important role in inducing mixing across the thermocline (Price, 1981; Burchard and Rippeth, 2009; [Chen et al., 2016](#)).

In shelf seas, near-inertial motions exhibit a two-layer structure, with an opposite phase between currents in the surface and lower layers (Malone, 1968; Millot and Crepon, 1981; MacKinnon and Gregg, 2005). By solving a two-layer analytic model using the Laplace transform, Pettigrew (1981) found this 'baroclinic' structure can be formed by inertial oscillations without inclusion of near-inertial internal waves. ~~DTherefore,~~ due to similar vertical structure and frequencies, inertial oscillations and near-inertial internal waves are hardly separable, and could easily be mistakenly recognized as each other.

In shelf seas, the near-inertial energy increases gradually offshore, and reaches a maximum near the shelf break, found both in observations (Chen et al., 1996) and model simulations (Xing et al., 2004; Nicholls et al., 2012). Chen and Xie (1997) reproduced this cross-shelf variation both in linear and nonlinear simulations, and attribute it to large values of the cross-shelf gradient of surface elevation and the vertical gradient of Reynolds stress near the shelf break. By using the analytic model of Pettigrew (1981), Shearman (2005) argued that the cross-shelf variation is controlled by baroclinic waves which emanate from the coast to introduce nullifying effects on the near-inertial energy near shore. Kundu et al. (1983) found a coastal inhibition of near-inertial energy within the Rossby radius from the coast, which is

78 attributed to ~~the downward and offshore leakage~~leaking of near-inertial energy ~~near the coast~~downward
79 ~~and offshore~~. As many factors seems to ~~have effects~~work, the mechanism controlling the cross-shelf
80 variation of near-inertial energy ~~_ is not clear~~seems complicated.

81 In this paper, simple two-dimensional simulations are used to investigate some basic features of near-
82 inertial motions. Cases with and without vertical stratification are simulated to examine properties and
83 differences between inertial oscillations and near-inertial internal waves. The horizontal distribution of
84 near-inertial energy is discussed in detail. Also cases with various water depths are simulated to
85 investigate the dependence of near-inertial motions on the water depth.

86
87 ~~During the occurrence of near inertial motions, the wind force can also easily generate a seiche in close~~
88 ~~or semi close basins (de Jong, 2003). A seiche is a standing wave formed in an enclosed or partially~~
89 ~~enclosed body of water, which has been widely observed in lakes, harbors, bays and seas (Miles,~~
90 ~~1974;Metzner et al., 2000;Drago, 2009;Breaker et al., 2010). It has a period ranging from several minutes~~
91 ~~to several hours. In some regions its amplitude can reach several meters (e.g.Wang et al., 1987), which~~
92 ~~can induce flooding and cause damage to fishery and coastal facilities. In a closed rectangular basin of~~
93 ~~length L and depth H, the seiche period is given by the Merian's formula:--~~

$$94 \quad T = \frac{2L}{n\sqrt{gH}} \quad (1)$$

95 ~~where n=1, 2, 3, ... is the mode number. Csanady (1973, using the Laplace transform) found that even~~
96 ~~modes of seiches were absent. However, the absence of even mode seiches has not been reported in~~
97 ~~observation or model simulations, probably due to irregular topography in reality which makes it difficult~~
98 ~~to compute the exact period of each mode. And it is not known why even modes disappear from the~~
99 ~~perspective of physics which we want to explore.--~~

100 ~~In this paper, we try to use simple simulations to investigate some basic properties of the inertial~~
101 ~~oscillation and the near inertial internal wave and differences between them. Generation of two layer~~
102 ~~structure of inertial oscillations and horizontal distribution of near inertial energy are investigated in~~
103 ~~details. The model is simple two dimensional (x=600 km, z=60 m) and forced by a wind pulse with land~~
104 ~~boundaries at both two sides. The missing of even mode seiches is also found and interpreted. Two cases~~

with and without vertical stratification are explored. Model settings are introduced in Section 2. In the homogeneous case (Section 3), properties of seiches and inertial oscillations are investigated. In the stratified case (Section 4), we study the difference near inertial internal waves introduce. Summary and discussion are presented in the final section (Section 5).

2. Model Settings

The simulated region is a two-dimensional shallow rectangular basin ($300 \text{ km} \times 60 \text{ m}$). Numerical simulations are done by the MIT general circulation model (MITgcm) (Marshall et al., 1997), which discretizes the primitive equations and can be designed to model a wide range of phenomena. There are 1500 grid points in the horizontal ($\Delta x = 200 \text{ m}$) and 60 grid points in vertical ($\Delta z = 1 \text{ m}$). The model is two dimensional (i.e., the gradient along y is zero), with 3000 grids in the horizontal (x ; $\Delta x = 200 \text{ m}$) and 30 grids in the vertical (z ; $\Delta z = 2 \text{ m}$). The water depth is uniform (60 m), with east and west sides boundaries being closed (land) and boundaries. The vertical and horizontal eddy viscosities are assumed constant as constants as $5 \times 10^{-4} \text{ m}^2/\text{s}$ and $10 \text{ m}^2/\text{s}$, respectively. The Coriolis parameter is $5 \times 10^{-5} \text{ s}^{-1}$ (at a latitude of 20.11° N). The bottom boundary is no-slip. The model is forced by a spatially uniform wind which is kept westward and increases from 0 to 0.73 N/m^2 (corresponding to a wind speed of 20 m/s) for the first three hours and then suddenly stops. The model runs for 200 hours in total, with a time step of 4 seconds. The first case has no vertical stratification is homogeneous, while the second one has a stratification of two-layer structure initially. For the stratified case, the temperature is 20°C in the upper layer ($-30 \text{ m} < z < 0$), and 15°C in the lower layer ($-60 \text{ m} < z < -30 \text{ m}$). The salinity is constant, and the density is linearly determined by the temperature, with an expansion coefficient of $2 \times 10^{-4} \text{ }^\circ \text{C}^{-1}$. The barotropic and baroclinic radii are 485 km and 8 km , respectively.

3.

Except stratification all settings of these two cases are the same.

Inertial oscillation Results without vertical stratification

The first case is without the presence of vertical stratification. Thus the near-inertial internal wave is absent, and the near-inertial motion is a pure inertial oscillation.

For the first case without vertical stratification, seiches and inertial oscillations are two dominant

processes.—

3.1 Seiches

Due to the westward flow driven by the wind, the water level goes up at the west coast and down at the east coast initially (Fig 1). A wave front propagates from each end at the speed of the barotropic wave ($\sqrt{gH} = 24$ m/s or 87 km/h). As the wind stress and the water depth are uniform across the basin, the elevation at the west is antisymmetric to that at the east (i.e. with the same amplitude but opposite phase).

The spectra of elevations is shown in Fig 2. At the inertial frequency, the elevation energy is slightly increased. The most energetic peak is at the first mode of seiches, which is slightly biased by the earth rotation effect. With the rotation, the wave frequency for each mode of seiche is given by (see the Appendix):—

$$\omega_n^2 = f^2 + \frac{n^2 \pi^2 gH}{L^2} \quad (2)$$

where f is the inertial frequency, n the mode number, g the gravity acceleration, H the water depth, and L the basin width. As in most cases the horizontal scale of a closed basin is relatively small (<200 km), the second term on the right hand side of Eq. (2) is much greater than the inertial frequency term, thus the rotation effect is usually negligible. Here due to a large basin width (600 km), the rotation effect is obvious.—

The energy of the first mode is minimal at the middle of the basin (i.e., $x=300$ km) and maximal at two boundaries. The second mode energy is almost negligible. The third mode, which has three nodes, is much more energetic than the second mode. The fourth mode vanishes, while the fifth mode can be seen with five nodes although it has relative low energy. In a word, the even modes are absent. In the real world, due to irregular topography, there is uncertainty in computing the exact period of each mode, and the research on higher modes is limited. Csanady (1973, using the Laplace transform) found the even modes of seiches absent. Here we propose an alternative way combining physics and mathematics to interpret this phenomenon.

As derived from the appendix, the elevation of a seiche in a closed basin can be given by

$$\eta_1 = \cos \frac{n\pi x}{L} (A_1 \cos \omega_n t + A_2 \sin \omega_n t) \quad (3)$$

where A_1 and A_2 are arbitrary constants. As we see in Fig 1, a barotropic wave originates from the east and west boundaries. Each barotropic wave can form a seiche. If the wind stress and the water depth are spatially uniform, the elevation induced by the seiche at the west is antisymmetric to that at the east. The wave generated at each end takes some time to reach the other end ($t_0 = L/\sqrt{gH}$), which causes a phase difference of $n\pi$ between seiches driven at two ends (i.e., $\omega_n t_0 = 2\pi/T \times (L/\sqrt{gH}) = n\pi$). If the seiche generated by the barotropic wave originating at the west boundary is denoted by (3), the seiche generated by the wave from the east boundary is expressed as

$$\eta_2 = \cos \frac{n\pi x}{L} [A_1 \cos(\omega_n t + n\pi) + A_2 \sin(\omega_n t + n\pi)] \quad (4)$$

The superposition of these two seiches is

$$\eta_1 + \eta_2 = \cos \frac{n\pi x}{L} [A_1 \cos \omega_n t (1 + \cos n\pi) + A_2 \sin \omega_n t (1 + \cos n\pi)] \quad (5)$$

The odd modes, i.e., $n=1, 3, 5, \dots$, are amplified:

$$\eta_1 + \eta_2 = \cos \frac{n\pi x}{L} (2A_1 \cos \omega_n t + 2A_2 \sin \omega_n t) \quad (n=1, 3, 5, \dots) \quad (6)$$

The even modes, i.e., $n=2, 4, 6, \dots$, cancel each other:

$$\eta_1 + \eta_2 = 0 \quad (n=2, 4, 6, \dots) \quad (7)$$

Therefore, even modes of seiches cancel each other.

Inertial oscillations

3.1 Vertical structures

The model simulated velocities (Fig. 13) vary near the inertial period (34.9 hours). Since the vertical stratification is absent, this near inertial motion is pure inertial oscillations. Spectra of velocities (not shown) indicate maximum peaks located exactly at the inertial period. The spectra of u also have a

smaller peak at the ~~frequency-period~~ of the first mode seiche (6.9 hours). As this simulation is two-dimensional, i.e., the gradient along y-axis is zero, the u/v of seiche has have a value of ω_0/f (equals 5 for the first mode seiche). Thus there is little energy of seiche in v which shows clearly regular variation at the inertial frequency.

In the vertical direction, currents display a two-layer structure, with their phase being opposite between surface and lower layers. They are maximum at the surface, and have a weaker maximum in the lower layer (~40 m), with a minimum at the depth of ~20 m. —The velocity gradually diminishes to zero at the bottom due to the bottom friction. This is the typical vertical structure of shelf-sea inertial oscillations, which have been frequently observed (Shearman, 2005; MacKinnon and Gregg, 2005). In practice, this vertical distribution can be modified due to presence of other processes, such as the surface maximum being pushed down to the subsurface (e.g. Chen et al., ~~2013~~2015a). Note that without stratification in this simulation the near-inertial internal wave is absent. However, this two-layer structure of inertial oscillations looks ‘baroclinic’, which makes it easy to be mistakenly attributed to the near-inertial internal wave (Pettigrew, 1981).

It is interesting that currents of non-baroclinic inertial oscillations reverse between the surface and lower layers. This is usually ~~attributed due~~ to the presence of the coast, which requires the normal-to-coast transport to be zero, thus currents in upper and lower layers compensate each other (e.g., Millot and Crepon, 1981; Chen et al., 1996). However, it remains unclear how this vertical structure is established step by step. Here we try to give more detail on how this process works.—

As the westward wind blows for the first three hours, the initial inertial current is also westward and only exists in the very surface layer (Fig. 24). In the lower layer there is no movement initially. Thus a westward transport is produced, which generates a rise (in the west) and fall (in the east) of elevation near ~~coastal-land~~ boundaries. The elevation slope behaves in a form of barotropic wave which propagates offshore at a great-large speed (87 km/h). The current driven by the barotropic wave is eastward, and uniform vertically. Therefore, with the arrival of the barotropic wave the westward current in the surface is reduced, and the eastward movement in the lower layer commences (Fig. 24). After the passage of the first two barotropic waves (originated from both sides), currents in the lower layer have reached a relatively great-large value, while currents in the surface layer have ~~been~~ largely decreased (Fig. 35a). Accordingly, the depth-integrated transport diminishes a lot. This is ~~like~~ a feedback between inertial

currents and barotropic waves. If only the depth-integrated transport of currents exist, barotropic waves will be generated, which reduce the surface currents but increase the lower layer currents, and thus reduces the current transport. It will end up with inertial currents in the surface and lower layers having opposite directions and comparable amplitudes. As seen from Fig. 13b, the typical vertical structure of inertial currents is established within the first inertial period. ~~At a place further offshore, such as at $x=200$ km, the barotropic wave takes about two more hours to arrive compared with $x=70$ km, thus the maximum value of inertial currents in lower layer is lagged behind that in surface layer (Fig. 5b).~~

3.2.2 Horizontal distributions of inertial energy

The inertial velocities are almost entirely the same across the basin (Fig. 46), except near the boundary. This indicates that inertial oscillations have a coherence scale of almost the basin width. This is because in our simulation the wind force is spatially uniform, and the bottom is flat. The inertial velocities in the lower layer have slightly more variation across the basin than those in the surface layer, because inertial velocities in the lower layer ~~is correlated to~~ depend on the propagation of barotropic waves as discussed in 3.2.1, while the surface inertial currents are driven by spatially uniform wind. In shelf sea regions, the wind forcing is usually coherent as the synoptic scale is much larger, however, the topography that is mostly not flat could generate barotropic waves at various places, and thus significantly decrease coherence of inertial currents in the lower layer.

The spectra of velocities in the inertial band are almost uniform except near the boundaries (Fig. 75), consistent with the velocities. Near the boundaries, the inertial energy declines gradually to zero from $x \sim 20$ km to ~~the the coast wall~~ land. The east side has slightly greater inertial energy and a slight bit wider boundary layer compared to the west side.

We calculate the nonlinear and inertial terms in the momentum equation and find that nonlinear terms are of ~~relatively-significantly~~ high values initially within 2 km away from the land boundary (Fig 8b6bc), where the inertial term is ~~smaller-weak~~ (Fig 8a6a). For the time-averaged values (Fig 8d6d), the vertical nonlinear term is two times more than the horizontal nonlinear term. The inertial term drops sharply near the boundary, and rises gradually with the distance away from the boundary. At $x > 15$ km, it keeps an almost constant value which is much greater than nonlinear terms. Thus it is concluded that the significant decrease of inertial oscillations near the boundary is due to influence of nonlinear terms, especially the

vertical nonlinear term.

4. Near-inertial internal waves

In addition to inertial oscillations, near-inertial internal waves are usually generated along when the vertical stratification is present. However, due to their close frequencies inertial oscillations and near-inertial internal waves are difficult to be separated. Thus we run a second simulation with the presence of stratification to investigate the differences that near-inertial internal waves introduce. ~~The temperature is 20°C in the upper layer ($-30\text{ m} < z < 0$), and 15°C in the lower layer ($-60\text{ m} < z < -30\text{ m}$). The salinity is constant, so the density is determined by the temperature.~~

4.1 Temperature distributions

Fig. 9-7 shows the evolution of temperature profiles with time. One can see an internal wave packet is generated at the west coast, and then propagates offshore. The wave phase speed is around 1 km/h, ~~consistent with~~ close to the theoretical value (1.4 km/h) ~~computed using the stratification~~. Before the arrival of internal waves, the temperature at mid-depth diffuses gradually due to vertical diffusion in the model. For a fixed position at $x=20\text{ km}$ (Fig. 108), the temperature varies with the inertial period (34.9 hours) and the amplitude of fluctuation declines gradually with time. At $x=60\text{ km}$ and $x=100\text{ km}$, the strength of internal waves is much reduced. And wave periods are shorter initially, followed by a gradually increase to the inertial period. At $x=140\text{ km}$, the internal wave becomes as weak as the background disturbance.

A spectral analysis of the temperature at mid-depth ($z=-30\text{ m}$) is shown in Fig. 11a9a. The strongest peak is at near the inertial frequency (0.69 cpd), but only confined to the region close to the boundary ($x < 40\text{ km}$). In the region $20\text{ km} < x < 70\text{ km}$, the energy is also large at higher frequencies of 0.8-1.7 cpd. This generally agrees with properties of Poincaré waves. During a Rossby adjustment, the waves with higher frequencies propagate offshore at greater group speeds, thus for places further offshore the waves have higher frequencies (Millot and Crepon, 1981). While the wave with a frequency closest to the inertial frequency moves at the slowest group velocity, and it takes a relatively long time to propagate far offshore, thus it is mostly confined to near the boundary. By solving an idealized two-layer model equation, the response of Rossby adjustment can be expressed in form of Bessel functions (Millot and Crepon, 1981; Gill, 1982; Pettigrew, 1981), as in Fig. 11ed-9cd showing the spectra of mid-depth elevation. The

difference from our case is obvious. The frequency of theoretical near-inertial waves increase gradually with the distance from the coast, while in our case this property is absent. And the theoretical inertial energy has a e-folding scale of ~~almost the Rossby radius~~ (54 km), while in our case the e-folding scale is much smaller (~15 km).

4.2 Velocity distributions

With presence of near-inertial internal waves, the contours of velocities near the thermocline tilt slightly (Fig. ~~42d~~10d), and indicates an upward propagation of phase, thus a downward energy flux. This can also be seen in vertical spirals of velocities (Figs. ~~42e-10e~~ and ~~42f~~10f). With only inertial oscillations, current vectors mostly point toward two opposite directions (Figs. 10b and 10c). Once the near-inertial wave is included, the current vectors gradually rotate clockwise with depth.

The spatial distribution of the near-inertial energy is also slightly changed compared to the case with only inertial oscillations (Fig. ~~43-11~~ and Fig. 75). It is also greatly reduced to zero in the boundary layer (0-20 km) like the case without stratification. But at ~50 km away from the boundary the inertial energy reaches a peak. Further away (>100 km) it becomes a constant. This spatial distribution of inertial energy is similar to that observed in shelf seas, with a maximum near the shelf break (Chen et al., 1996; Shearman, 2005). In our case, the boundary layer effect which induces a sharp decrease to zero makes a major contribution, and near-inertial internal waves which bring a small peak further offshore ~~make-have~~ a secondary influence.

5. Dependence on the water depth

In coastal regions, near-inertial motions are rarely reported. It is speculated that the strong dissipation and bottoms friction in coastal region suppress the development of near-inertial motions. However, Chen (2014) found the water depth is also a sensitive factor, with significant reduction for the case with smaller water depth. Here we will run cases with different water depths and clarify why the near-inertial energy changes with water depth. Homogeneous cases with water depths of 50 m, 40 m, 30 m, 20 m are simulated. The vertical interval for all cases is 1 m. All the other parameters including viscosities are the same as the homogeneous case of 60 m.

For each case, the currents are band-pass filtered to obtain near-inertial currents. Then near-inertial kinetic energy can be calculated. As seen in Fig. 12, the near-inertial energy gradually declines with

decreasing water depth. In this dynamical system, the other dominant process is the seiches induced by barotropic waves. As the elevation induced by seiches is anti-symmetric in such a basin, the potential energy is little. The kinetic energy of seiches can also be calculated by the band-pass filtered currents. We find the energy of seiches, by contrast, increases gradually with decreasing water depth. For the case of 60 m, the near-inertial energy is much greater than the seiches energy. But for the case of 20 m, the energy of seiches has exceeded the near-inertial energy slightly. The total energy of these two processes almost keeps constant for all cases. For a shallower water depth, the reduction of near-inertial energy equals the increase of seiches energy. The initial current is wind-driven and only distributes in the surface layer. The unbalanced across-shelf flow generates elevation near the land boundary which propagates offshore as barotropic waves and form seiches. Part of the energy goes to form inertial oscillations. For a shallower water depth, the elevation is enlarged, and more energy is transferred to form seiches, thus with weakened near-inertial motions. Therefore, in coastal regions with water depth less than 30m, the near-inertial motion is weak, due to the suppression of barotropic waves.

As seen in Section 3.1, inertial oscillations behave in a two-layer structure, with currents in the upper layer in opposite phase with those of lower layer. In terms of kinetic energy, for the case of 60 m (Fig. 13), the near-inertial motion is maximized in the very surface, minimized near the depth of 20 m, and then gradually increases with depth to form a much smaller peak at 40 m. Near the bottom, the near-inertial energy gradually reduces to zero due to bottom friction. When we set the bottom boundary condition from nonslip to slip, such a boundary structure vanishes, and near-inertial energy become constant in the lower layer. For other cases of 20 m and 40 m, their vertical profile are almost the same as the 60 m case. The minimum positions are all located at 1/3 of the water depth. This implies the vertical distribution of near-inertial energy is independent of water depth. Note that in our cases, the vertical viscosity is set as a constant value. In practice, the viscosity in the thermocline is usually significantly reduced, thus the minimum position of near-inertial energy is located just below the mixed layer.

5.—

6. Summary and discussion

Two sets of idealized simple two-dimensional (x-z) simulations are conducted to examine the response

of a shallow closed basin ~~—(600 km×60 m)—~~ to a wind pulse. The first case is homogeneous, in which ~~properties the near-inertial motion is a pure inertial oscillation of seiches and inertial oscillations are investigated. Barotropic waves are generated at two coastal boundaries which then propagate and reflect to form seiches. The seiche has the horizontal structure and frequencies consistent with the theory. Seiches of even number modes are absent, which has been rarely reported. By using the Laplace transform to solve the equations, Csanady (1973) found even mode seiches absent. We interpret it as superposition of two seiches, which are formed by barotropic waves originating from east and west boundaries. They have anti-symmetric elevation and a phase lag of $n\pi$, thus their even mode cancels each other. The mechanism we propose is more physical, and thus a good supplement to explain this phenomenon. Note that for the even modes to be absent the wind forcing and the topography are required to be uniform spatially to keep these two seiches having anti-symmetric elevation.—~~

~~The inertial oscillation is energetic in the homogeneous case.~~ It has a two-layer structure, with currents in the surface and lower layers being opposite in phase, which has been reported frequently in shelf seas. We find that the inertial current is confined in the surface layer initially. The induced depth-integrated transport generates barotropic waves near the boundaries which propagates quickly offshore. The flow driven by the barotropic wave is independent of depth and opposite to the surface flow. Thus the surface flow is reduced but the flow in the lower layer is increased, as a result the transport diminishes. This feedback between barotropic waves and currents continues and ends up with the depth-integrated transport ~~vanishes~~vanishing, i.e., inertial currents in the upper and lower layers having opposite phases and comparable amplitudes. In our simulation, within just one inertial period the typical structure of inertial currents has been established. By solving a two-layer analytic model using the Laplace transform, Pettigrew (1981) also found the vertical structure of opposite currents associated with inertial oscillations. He argued that the arrival of a barotropic wave for a fixed location cancels half of the inertial oscillation in the surface layer, and initiates an equal and opposite oscillation in the lower layer. However, in our simulation the arrival of the first barotropic wave cannot cancel half of the surface flow. The balanced state of upper and lower flows takes more time to reach. Our simulations further demonstrate the role of barotropic waves in forming this feature, and shows some more realistic details during this process.—

The second case is a set-up with idealized two-layer stratification, thus near-inertial internal waves are generated. For a fixed position, velocity contours show clear obvious tiltings near the thermocline, and

velocity vectors display clearly anti-cyclonic spirals with depth. These could be useful clues to examine occurrence of near-inertial internal waves. Near the land boundary the vertical elevation generates fluctuations of thermocline that propagate offshore. The energy of near-inertial internal waves is confined to near the land boundary ($x < 40$ km). At positions further offshore, the waves have higher frequencies. This is generally consistent with properties of a Rossby adjustment process. However, our simulated results also show evident discrepancies from theoretical values obtained in the classic solutions of Rossby adjustment problem, which— are probably attributed to nonlinearity of the model.

The inertial oscillation has a very large coherent scale of almost the whole basin scale (~~600 km~~). It is uniform in both amplitude and phase across the basin, except near the boundary (~ 20 km offshore). The energy of inertial oscillations declines gradually to zero from $x = 20$ km to the coast. This boundary effect is attributed to influence of nonlinear terms, especially the vertical term ($w \partial \mathbf{u} / \partial z$), which are greatly enhanced near the boundary, and overweighs the inertial term ($f \mathbf{u}$). When near-inertial internal waves are produced in the stratified case, the distribution of total near-inertial energy is modified slightly near the boundary. A small peak appears at ~ 50 km offshore. This is similar to the cross-shelf distribution of near-inertial energy observed in shelf seas (Chen et al., 1996; Shearman, 2005). This energy distribution has been attributed to ~~different reasons, such as~~ downward and offshore leakage of near-inertial energy near the coast (Kundu et al., 1983), the variation of elevation and Reynolds stress terms associated with the topography (Chen and Xie, 1997) and the influence of the baroclinic wave (Shearman, 2005; Nicholls et al., 2012). In our simulations, this horizontal distribution of near-inertial energy is primarily controlled by the boundary effect on inertial oscillations, and the near-inertial internal wave ~~makes~~ has a secondary effect.

Homogeneous cases with various water depths (50 m, 40 m, 30 m, and 20 m) are also simulated. The inertial energy is reduced with decreasing water depth, while the energy of seiches, by contrast, is increased. For the case of 20 m, the seiches energy has slightly exceeds the inertial energy. It is interesting that the reduction of inertial energy just equals the increase of seiches energy, which implies more energy of initial wind-driven currents is transferred to the seiches for the shallower cases, and thus less energy goes to the inertial process. This is probably an important reason why near-inertial motions are weak and rarely reported in shallow coastal regions.

Acknowledgements

We are ~~very~~ appreciated for ~~comments from~~ discussions with John Huthnance and comments from reviewers and the editor. This study is supported by the National Basic Research Program of China (2014CB745002, 2015CB954004), the Shenzhen government (201510150880, SZHY2014-B01-001), and the Natural Science Foundation of China (~~41576008, 41276006, U1405233, and 40976013~~). Shengli Chen is sponsored by the China Postdoctoral Science Foundation (2016M591159).

~~Appendix: the derivation for the general solution of seiches~~

~~The governing equations for seiches can be simplified as:~~

$$\frac{\partial u}{\partial t} - fv = -g \frac{\partial \eta}{\partial x} \quad (\text{A1a})$$

$$\frac{\partial v}{\partial t} + fu = 0 \quad (\text{A1b})$$

$$\frac{\partial \eta}{\partial t} + H \frac{\partial u}{\partial x} = 0 \quad (\text{A1c})$$

~~where u and v are eastward and northward velocities, η the elevation, f the inertial frequency, g the gravity acceleration, H the water depth. Substitutions of η and v by u give~~

$$\frac{\partial^2 u}{\partial t^2} + f^2 u - gH \frac{\partial^2 u}{\partial x^2} = 0 \quad (\text{A2})$$

~~If we assume~~

$$u = X(x)T(t) \quad (\text{A3})$$

~~and substitute (A3) in (A2), we get~~

$$\frac{T''}{T} + f^2 = \frac{gHX''}{X} \quad (A4)$$

If a function of t equals a function of x , they have to both equal a constant,

$$\frac{T''}{T} + f^2 = \frac{gHX''}{X} = -C \quad (A5)$$

The equation of x is then given by

$$gHX'' + CX = 0 \quad (A6)$$

The solution of (A6) can be readily obtained

$$X = C_1 \sin \sqrt{\frac{C}{gH}} x + C_2 \cos \sqrt{\frac{C}{gH}} x \quad (C > 0) \quad (A7)$$

where C_1 and C_2 are arbitrary constants. The across coast velocity must vanish at boundaries, i.e., $u=0$ at $x=0, L$, thus

$$X = C_1 \sin \sqrt{\frac{C}{gH}} x \quad (A8a)$$

$$C = \frac{n^2 \pi^2 gH}{L^2} \quad (A8b)$$

The solution for T is then

$$T = C_3 \sin \omega_n t + C_4 \cos \omega_n t \quad (A9a)$$

$$\omega_n^2 = f^2 + \frac{n^2 \pi^2 gH}{L^2} \quad (A9b)$$

where C_3 and C_4 are arbitrary constants. Therefore the solution for u is

$$u = C_1 \sin \frac{n\pi x}{L} (C_3 \sin \omega_n t + C_4 \cos \omega_n t) \quad (A10a)$$

and the solutions for η and v are

$$\eta = C_1 \frac{n\pi H}{\omega_n L} \cos \frac{n\pi x}{L} (C_3 \cos \omega_n t - C_4 \sin \omega_n t) \quad (A10b)$$

$$v = C_1 \frac{f}{\omega_n} \sin \frac{n\pi x}{L} (C_3 \cos \omega_n t - C_4 \sin \omega_n t) \quad (\text{A10e})$$

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Figures

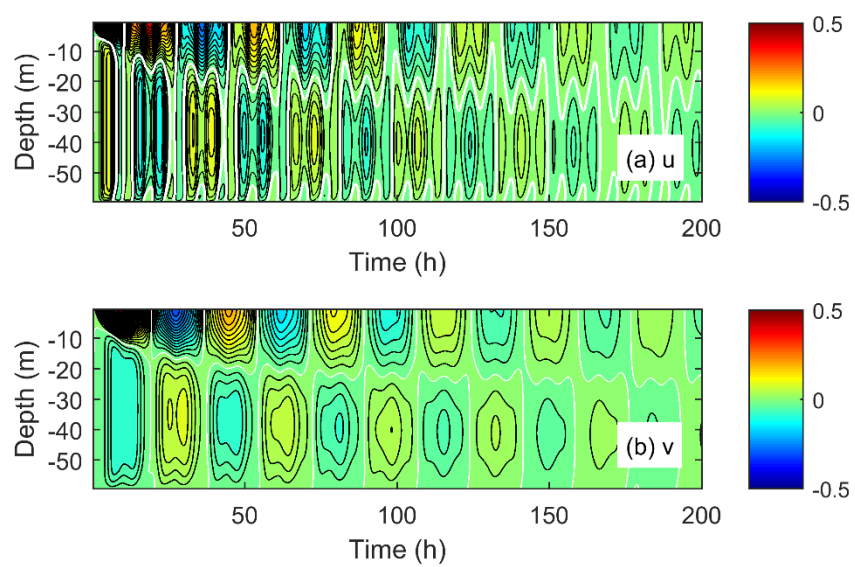


Fig. 1 Velocities (u and v , m/s) at $x=70$ km. The white lines denote the value of zero. The contour

interval is 0.02 m/s for both panels.

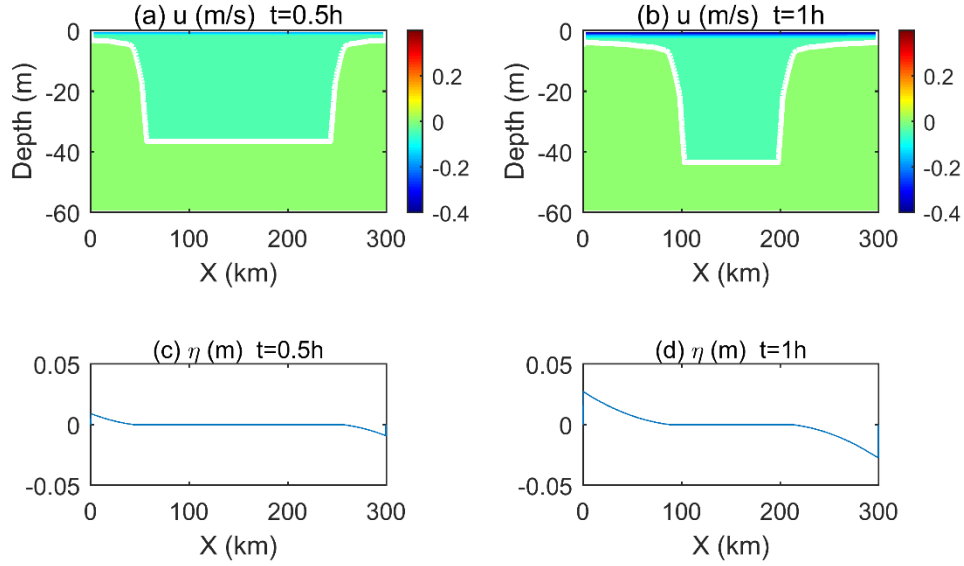


Fig. 2 Snapshots of eastward velocity and elevation (η) at $t=0.5$ and 1 hour. The white lines represent the value of zero.

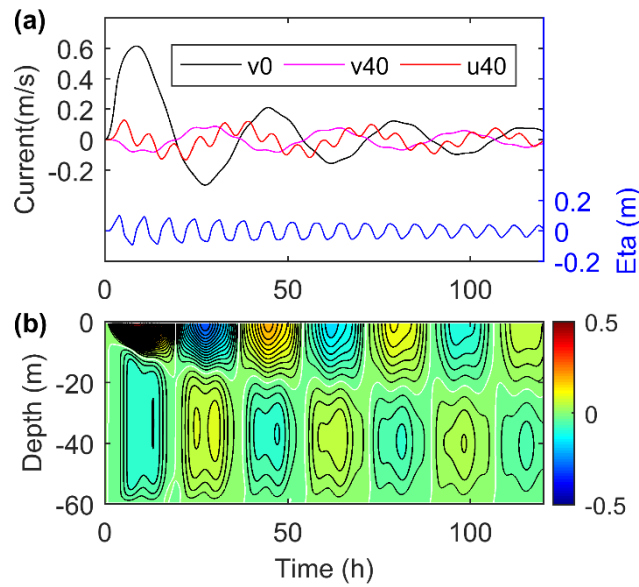


Fig. 3 (a) Time series of velocities and elevation at $x=100$ km. 'v0' and 'v40' mean the northward velocity (v) at depths of 0 m and 40 m, and 'u40' is the eastward velocity (u) at 40 m. (b) Contours of v at $x=100$ km. The white lines denote the value of zero, and the contour interval is 0.02 m/s.

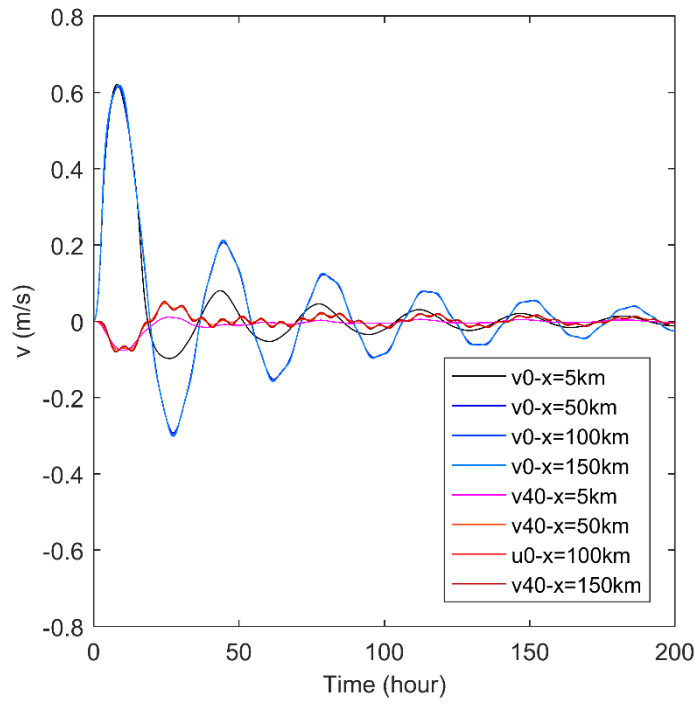


Fig. 4 Time series of the northward velocity (v) at different depths and positions. 'v0' and 'v40' mean v at depths of 0 m and 40 m.

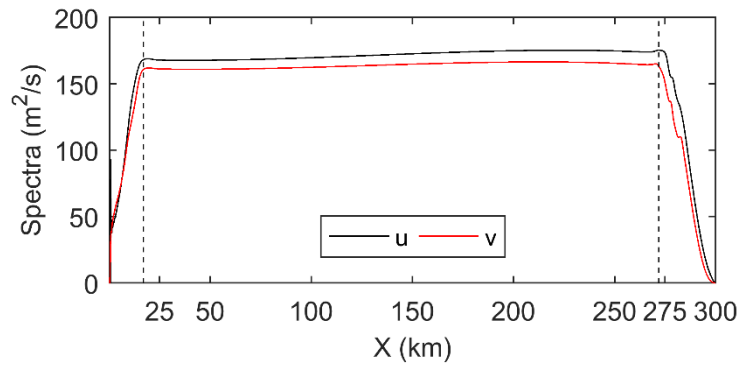


Fig. 5 Spatial variation of depth-mean spectra of velocities in near-inertial band for the homogeneous case.

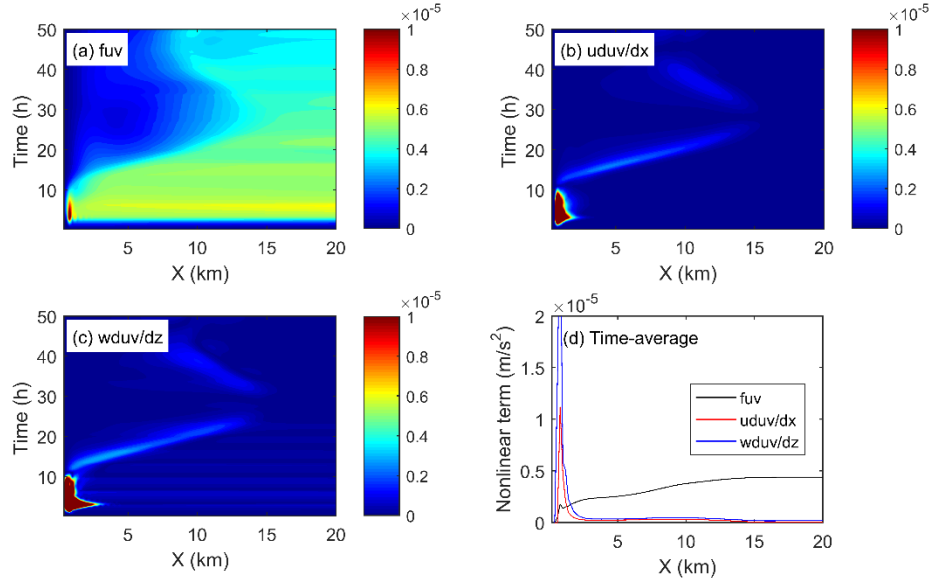


Fig 6. Variation of depth-mean inertial and nonlinear terms (m/s^2). The inertial term (a) is calculated as $|f(u + iv)|$, the horizontal nonlinear term (b) is $|u(\partial u / \partial x + i \partial v / \partial x)|$, and the vertical nonlinear term (c) is $|w(\partial u / \partial z + i \partial v / \partial z)|$. (d) Time averaged value for the first 50 hours.

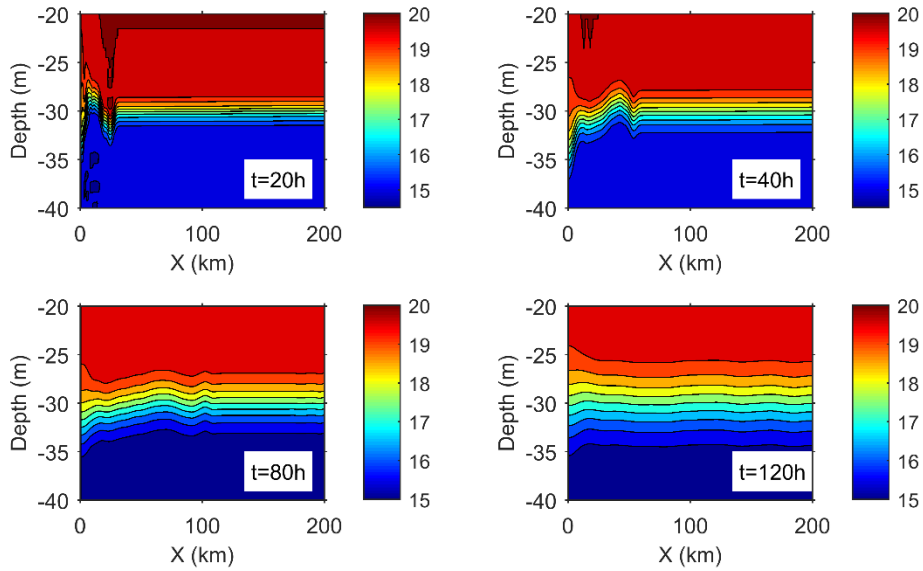


Fig. 7 Snapshots of temperature profiles at t=20h, 40h, 80h and 120h. The contour interval is 0.5 °C.

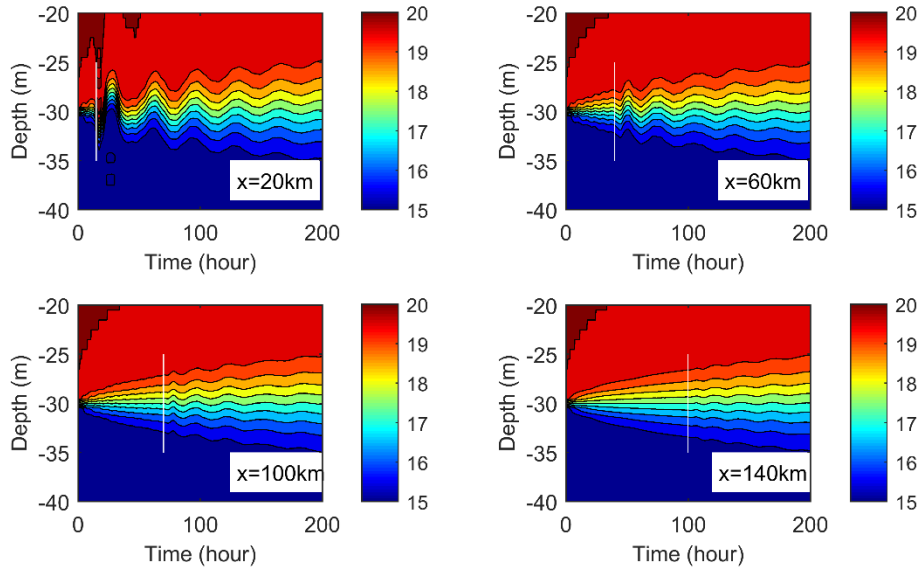


Fig. 8 Time series of temperature at $x=20, 60, 100$ and 140 km. White lines denote arrival of internal waves. The contour interval is 0.5 $^{\circ}\text{C}$.

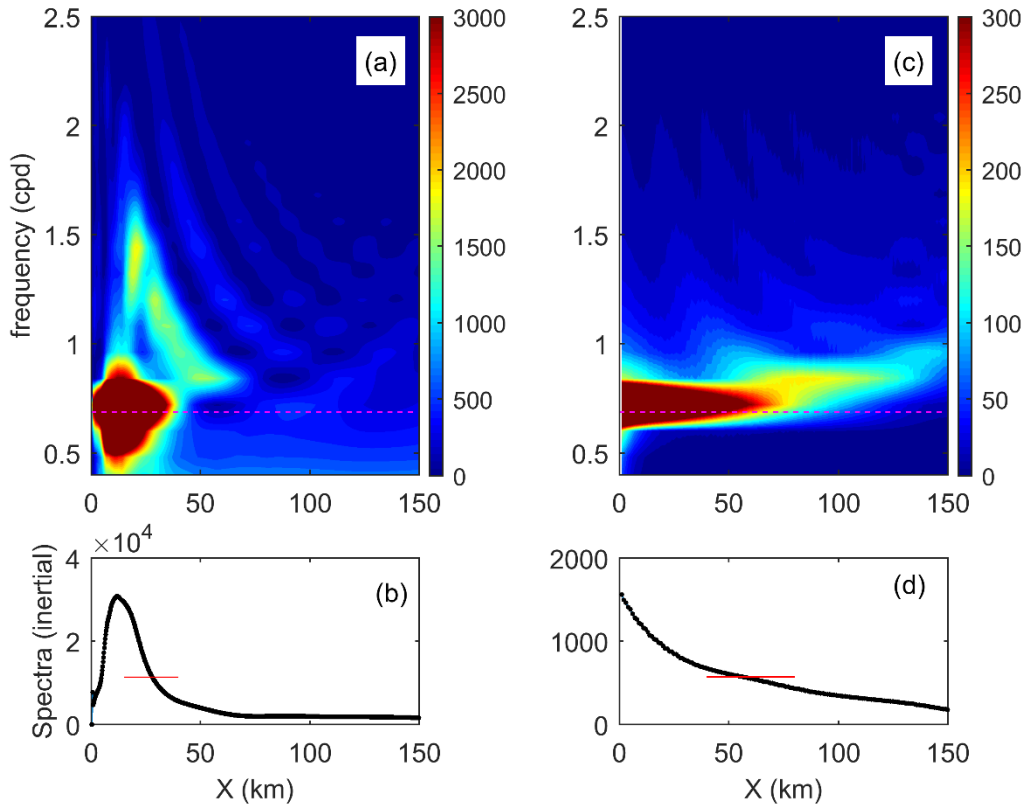


Fig. 9 (a) Spectra of the temperature at the mid-depth ($z=-30$ m). The pink dash line represents the

inertial frequency. (b) Sum of spectra in inertial band with a red line denoting the e-folding value of the peak. (c) Theoretical spectra of mid-depth elevation calculated from the solution in the form of a Bessel function as in Eq. 3.16 of Pettigrew (1981). (d) Same as (b) but for theoretical spectra.

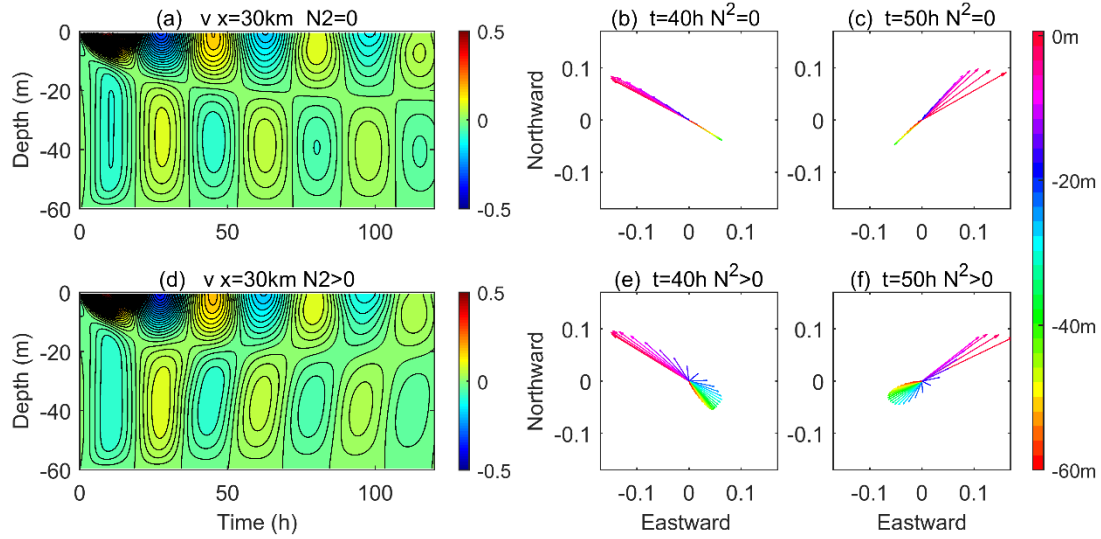


Fig. 10 Distribution of near-inertial currents (v , m/s) and current spirals for the cases without (a, b, c) and with (d, e, f) stratification at $x=30$ km. The near-inertial currents are obtained by applying a band-pass filter. The contour interval is 0.02 m/s.

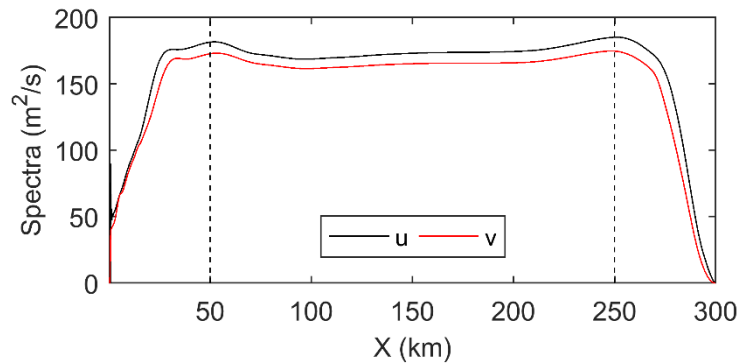


Fig. 11 Spatial variation of depth-mean spectra of velocities in near-inertial band for the stratified case.

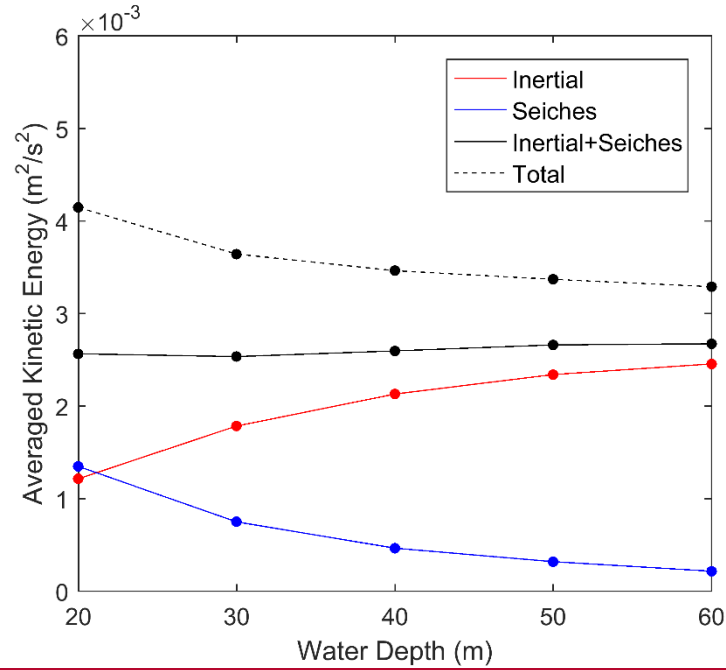


Fig. 12 The kinetic energy of near-inertial motions and seiches for different water depths. For each case, the currents are band-pass filtered to get currents for each type of motions which are then averaged over time and integrated over space to obtain a final value.

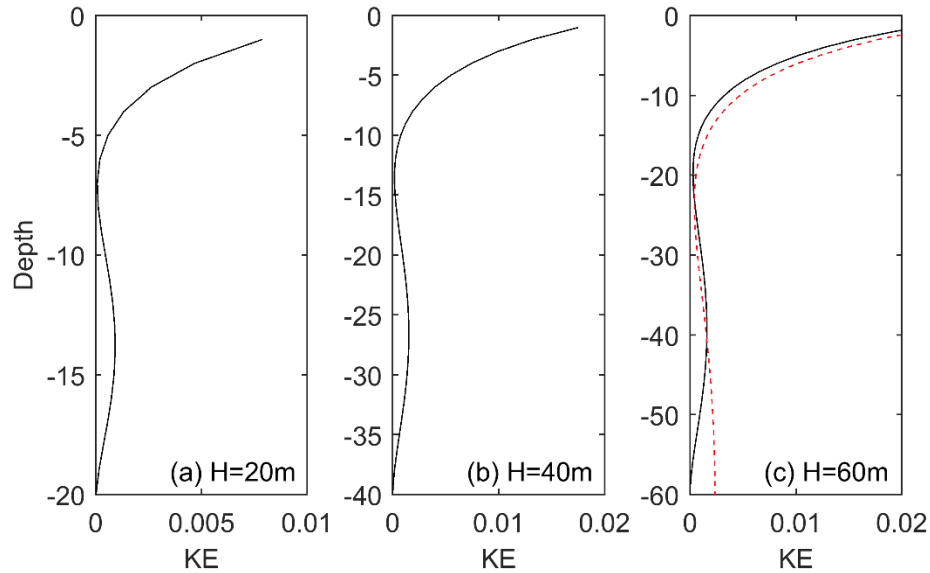


Fig. 13 Vertical profile of averaged inertial kinetic energy for the homogeneous cases with water depths of 20 m, 40 m and 60 m. The red dash line in (c) denotes the slip case.