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## High frequency fluctuations in the heat content of an ocean general circulation model

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The transport and storage of heat by the ocean is of crucial importance because of its effect on ocean dynamics and its impact on the atmosphere, climate and climate change. Unfortunately, limits to the amount of data that can be collected and stored means that many experimental and modelling studies of the heat budget have to make use of mean datasets where the effects of short term fluctuations are lost.

In this paper we investigate the magnitude of the resulting errors making use of data from OCCAM, a high resolution global ocean model. The model carries out a proper heat balance every timestep so any imbalances that are found in the analysis must result from the use of mean fields.

The study concentrates on two areas of the ocean affecting the El Nino. The first is the region of tropical instability waves north of the equator. The second is in the upwelling region along the equator.

It is shown that in both cases, processes with a period of less than five days can have a significant impact on the heat budget. Thus analyses using data averaged over five days or more are likely to have significant errors. It is also shown that if a series of instantaneous values is available, reasonable estimates can be made of the size of the errors. In model studies such values are available in the form of the datasets used to restart the model. In experimental studies they may be in the form of individual unaveraged observations.

#### Introduction

Quantifying the heat budget of the ocean, and its ability to store and transport heat, is a key element in understanding the mechanisms that drive the ocean circulation and its role in climate and climate change. The ocean has the largest heat capacity of any single component of the climate system and for this reason it is essential that we have an accurate understanding of the global and regional oceanic heat budgets at all time scales.

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Over the past 40 yr the ocean has been responsible for major changes in global heat content (Levitus et al., 2001). But despite the developments in global ocean observing system, the problems of quantifying heat budgets and their variability at regional and global scales remains difficult. Errors in such estimates can be large and usually go unreported in the literature (Willis et al., 2004).

A number of papers have focussed on generating accurate estimates of heat content. Willis et al. (2004) combined satellite altimetric height and historically available in situ temperature data to produce global estimates of upper ocean heat content, thermosteric expansion, and temperature variability over a 10.5 yr period.

Dong et al. (2007a) studied the relative role of the air-sea heat flux and oceanic processes in the heat balance in the Southern Ocean. Their study identified an imbalance in the heat equation which they attributed partly to the complex feedback processes of the coupling system in these regions. These are not well resolved by existing measurements. They also found that the air-sea heat flux datasets for the Southern Ocean showed large differences during the winter months, most probably due to the sparseness of the basic raw data.

Using in-situ and altimetry data for the Western North Atlantic, Dong et al. (2007b) studied how the subsurface thermal structure changes correspond to changes in the upper ocean heat content. The residual term in their heat equation was ignored, as previous studies suggest that it is small in gyre regions. In order to balance the heat budget they used an inverse method to adjust velocity estimates in each isothermal layer. They also estimate the residual by computing the RMS difference between the sea surface height and heat content derived from a 3-D model study.

Wells et al. (2009) analyzed the upper ocean heat budget of the North Atlantic using Argo profiling floats and NCEP/NCAR and NOC surface flux data sets. In their work, they considered that high frequency contributions could make a contribution to the heat advection if there were associated high frequency variations in the averaged temperature between the depth of the upper ocean (300 m) and the sea surface. They believed those variations are only likely near frontal zones associated with mesoscale eddies

and these were not resolved in their study. Therefore, the term was ignored.

As a final example of the approaches that have been used, Lee et al. (2004) pointed out the need for caution in identifying the mechanisims controlling the heat content of a region. They explored an alternative scheme for advecting temperature which should make it easier to do this.

Although studies such as these usually justify the use of mean datasets, there is always the possiblity that the fluctuations are making important contributions that are missed when using the mean datsets.

The present study is therefore concerned with learning more about the errors that arise when mean datasets are used to estimate the advection and diffusion of heat within the ocean. We do this using the archived data from a run of the high resolution OCCAM ocean general circulation model to study three regions of the Eastern Tropical Pacific. The latter is a region of energetic variability mainly due to the presence of the Tropical Instability Waves (Fig. 1).

The archive data includes the 5-day average datasets and the instantaneous datasets, from the end of each 5-day period, which are used to restart the model. The model ensures a proper heat balance every model timestep so any errors that arise in the analysis must result from the use of mean datasets.

Section 2 of the paper discusses the heat balance equation and its separation into the mean and fluctuating fields. Section 3 briefly describes the model and the equations it uses. The numerical details, the analysis for a single column and the estimate of the error, or high frequency term, are described in Sect. 4. Section 5 describes the analysis in two larger regions on the Eastern Equatorial Pacific. The paper concludes with a brief summary and discussion of the results.

#### 2 Mean field and fluctuations in time

Changes in the ocean's heat content result from the effects of advection and diffusion within the ocean. If Q is the heat content per unit volume of the ocean, then the

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$$\frac{\partial Q}{\partial t} = \nabla \cdot \mathbf{A} + \nabla \cdot \mathbf{D} + S \tag{1}$$

where the first term in the right hand side represents heat advected by the large scale current field, the second represents the diffusion of heat by small scale oceanic processes and *S* is the surface heat flux.

If the specific heat of sea water is constant, as is assumed in the ocean model, then this can be also written as:

$$\frac{dT}{dt} = \nabla \cdot \boldsymbol{u}T + \nabla \cdot \Lambda \nabla T + S \tag{2}$$

where T is temperature, u is the three dimensional current vector (u,v,w) and  $\Lambda$  the diffusion tensor. In the OCCAM model,  $\Lambda$  is a diagonal tensor, such that,

$$\Lambda \nabla T = A_{\mathsf{h}} \nabla_{\mathsf{h}} T + A_{\mathsf{z}} \partial T / \partial z. \tag{3}$$

 $\nabla_h$  is the horizontal gradient operator.  $A_h$  and  $A_z$  are the horizontal and vertical diffusion coefficients.

It is convenient to split the temperature and velocity fields into mean and fluctuating parts,

$$T(t) = \overline{T}(t) + T'(t) \tag{4}$$

$$\boldsymbol{u}(t) = \overline{\boldsymbol{u}}(t) + \boldsymbol{u}'(t) \tag{5}$$

where the terms with overbars are the mean during the time period  $\tau$ , i.e.:  $\bar{T} = \frac{1}{\tau} \int_0^{\tau} T dt$  and  $\bar{u} = \frac{1}{\tau} \int_0^{\tau} u dt$ ; the prime terms represent fluctuations during this period. The product uT in the advective term of Eq. (2) then becomes,

$$\mathbf{u}T = (\bar{\mathbf{u}} + \mathbf{u}')(\bar{T} + T'). \tag{6}$$

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Integrating over the period  $\tau$ ,

$$\int_0^{\tau} \mathbf{u} T dt = \int_0^{\tau} \bar{\mathbf{u}} \bar{T} dt + \int_0^{\tau} \bar{\mathbf{u}} T' dt + \int_0^{\tau} \mathbf{u}' \bar{T} dt + \int_0^{\tau} \mathbf{u}' \bar{T}' dt.$$

$$(7)$$

But  $\bar{T}^t \int_0^{\tau} \mathbf{u}' dt = 0$  and  $\bar{\mathbf{u}}^t \int_0^{\tau} T' dt = 0$ . Thus,

$$\int_0^{\tau} \mathbf{u} T dt = \int_0^{\tau} \bar{\mathbf{u}} \bar{T} dt + \int_0^{\tau} \mathbf{u}' T' dt, \tag{8}$$

$$\overline{uT} = (\overline{u}\overline{T}) + \overline{(u'T')}. \tag{9}$$

As a result, the total advective heat flux can be split into a contribution only dependent on the mean values of temperature and velocity plus a contribution only dependent on the fluctuations.

If D represents the diffusive term of Eq. (2), then separating the mean and fluctuation parts in the same way.

$$D = \Lambda \nabla (\overline{T} + T'). \tag{10}$$

If the diffusion tensor is constant, as is often assumed, then when the equation is integrated over a period  $\tau$ , the fluctuation term vanishes so,

$$D = \Lambda \nabla \overline{T}. \tag{11}$$

However in regions where any of the terms of the diffusion tensor vary in time, there will be an extra diffusive contribution from the fluctuations.

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The Ocean Circulation and Climate Advanced Model (OCCAM) is based on the Bryan-Cox-Semtner (Cox, 1984; Bryan, 1969; Semtner, 1974) ocean general circulation model. This is a "primitive equation" model (Bryan, 1969) which differs from other primitive equation models in the use of an Arakawa-B grid in the horizontal (Arakawa, 1966) and level surfaces in the vertical.

The OCCAM model includes a number of important developments in both model physics and model numerics<sup>1</sup>. Physically it replaces the rigid lid of the standard Bryan-Cox-Semtner scheme with a free surface and solves the resulting barotropic equations using a simple tidal model with a time-step of 18 s. It uses the Webb (1995) scheme for the vertical advection of momentum and the split-QUICK scheme (Webb et al., 1998) for the horizontal advection of tracers such as temperature and salinity. It uses the Pacanowski and Philander (1981) scheme for the vertical mixing of tracers.

At the start of the run the potential temperature and salinity fields were initialized from the Levitus (1982) global annual average database. There was then a spin up phase lasting 1440 model days (4 yr), during which the model was forced by the monthly averaged ECMWF wind stress climatology, calculated by Siefridt and Barnier (1993) for the years 1986 to 1988 inclusive. The data was corrected so that when linearly interpolated in time the correct average stress was applied during each model month (Killworth et al., 1991). The surface fluxes of heat and fresh water were calculated so as to relax the surface layer of the model to the Levitus monthly average values (Levitus and Boyer, 1994; Levitus, 1982; Levitus et al., 1994).

Following the spin up phase, the model was forced using six-hourly winds and

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 $<sup>^1</sup>$ OCCAM uses asyncronous message passing, enabling it to be run efficiently on modern multi-processor computers. It also differs from other ocean models in that it is vectorised in the vertical. This arrangement optimises processor usage by limiting main memory transfers when the model is run either on short ( $\backsim$  100) vector processors or on modern Intel type processors with very high speed memory caches.

surface flux data from the ECMWF analyses. The analysis reported here used archive data for the year 1994 and, as in the model tracer calculation, assumes a sea water density of 1 g cm<sup>-3</sup> and a specific heat of 1 cal g<sup>-1</sup> C<sup>-1</sup>. The main model timestep used for the tracer fields is 15 min, but due to storage limitations, archive datasets were only generated every five model days. These consisted in averages over the previous five days plus the instantaneous values from the end of the period kept to restart the model at this point if required.

#### Analysis of the heat equation

The ocean model solves Eq. (1) by first partitioning the ocean into cells whose interfaces lie along lines of constant latitude, longitude and depth (see Fig. 2). Model temperatures are defined at the centre of each cell (or model grid box). The range of depths used in this analysis means that the regions are not immediately affected by surface fluxes but at the same time they may be typical of the upper part of the water column in the Pacific Ocean, therefore S = 0. Integrating Eq. (1) over each grid box gives the flux conserving equation,

$$V_n \frac{\partial T_n}{\partial t} = \sum_m (I_{nm} U_{nm} T_{nm} + I_{nm} D_{nm})$$
 (12)

where the sum is over the cells 'm' surrounding cell 'n'.  $V_n$  is the volume of the cell,  $T_n$ its average temperature,  $I_{nm}$  the area of the interface between cells 'n' and 'm'.  $T_{nm}$ the average temperature on the interface and  $U_{nm}$  the average velocity through the interface. The first term in the right hand side is called the advective term, the second is the diffusive term. The latter represents all the small scale dynamical and molecular diffusive processes not represented by the advective term.

The above equation is stepped forward in time by approximating the time derivation

term.  $\frac{\partial T}{\partial t} = \frac{T(t+dt) - T(t-dt)}{2dt}$ (13) OSD

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where dt is the model timestep. If the forcing on the right of Eq. (12) is represented by F(t), then this gives the equation,

$$T(t+dt) \approx T(t-dt) + 2dtF(t). \tag{14}$$

The approximation is correct to order  $dt^2$ , and if the time step is small enough, it is both accurate and stable when used for the advective term in Eq. (12). Unfortunately diffusive terms make it unstable and so in the model it is modified to.

$$T(t+dt) = T(t-dt) + 2dt(A(t) + D(t-dt))$$
 (15)

This equation is stable for both the advection (A(t)) and diffusion (D(t-dt)) terms.

In the Arakawa B grid used by the model, shown in Fig. 2b, horizontal velocities are defined at the corners of the cells at the same depth as the central tracer (temperature) grid point. The average velocities through the horizontal interfaces, needed for Eq. (12), are thus estimated in the model by averaging the two neighbouring corner values.

As the total flux of water in and out of each grid cell is zero, the ocean being assumed to be incompressible, the horizontal fluxes are then used to calculate the difference in fluxes through the bottom and top of each cell. These differences are summed from the bottom of the ocean, where the vertical flux is zero, to give the velocity flux through each of the levels.

The average tracer at the interface can be estimated in a similar way. Thus replacing 'n' in Eq. (12) by the triplet 'i, j, k', representing the longitude, latitude and depth indices, the mean temperature on the interface between the 'i, j, k' and 'i + 1, j, k' cells can be written (see Fig. 2),

$$T_{i+\frac{1}{2},j,k} = \frac{(T_{i,j,k} + T_{i+1,j,k})}{2}.$$
 (16)

This was the approximation used in the earliest ocean models, and like all the other approximations discussed here is adequate for modelling features with spatial scales much larger than the grid spacing and time scales much longer than a model timestep.

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Unfortunately in ocean models, there are often important features, such as ocean fronts and eddies, which are only a few grid points across. In such cases the approximation involved in Eq. (16) results in such short wavelength features being advected at the wrong speed or even in the wrong direction.

A large number of papers have been written about the problem and possible solutions, one of the most successful solutions being the QUICK scheme devised by Leonard (1979). Farrow and Stevens (1995) adapted QUICK for use in an ocean model, but to ensure stability they replaced Eq. (15) by a time stepping method which was computationally inefficient. Later Webb et al. (1998) showed that the QUICK advective operator included a diffusive-like operator and that if this was treated separately as an extra contribution to the main diffusion term then Eq. (15) could again be used. The same analysis showed that slightly better accuracy could be obtained by changing the term multiplying the second term on the following equation from 1/16 to 1/12. The resulting MSQ (modified split-QUICK) scheme is the one used in the OCCAM model for the run analysed here. Dropping the j and k indices in Eq. (16), the MSQ scheme is,

$$T_{i+\frac{1}{2}} = \frac{T_{i+1} + T_i}{2} - \frac{T_{i+2} - T_{i+1} - T_i + T_{i-1}}{12} + \gamma \frac{|U|}{U} \frac{T_{i+2} - 3T_{i+1} + 3T_i - T_{i-1}}{16},$$
(17)

The second term on the right improves the advection of features with wavelengths of four model grid points or more. The final term is the additional diffusion introduced by the MSQ scheme. Its effect is to damp out the very short waves which, in the model, can generate large errors. Note that MSQ was not used in the vertical. This is because in the presence of realistic surface wind forcing, most of the near-surface vertical velocities are oscillatory, due to the internal waves generated. The oscillations tend to cancel out the errors due to the central difference scheme. At the same time if MSQ is used with a rapidly oscillating current it produces unwanted extra numerical diffusion.

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The main objective here is to quantify the errors that arise when calculating oceanic heat fluxes using averaged datasets. To do this we apply Eq. (12) to closed volumes of ocean and compare the heat flux, calculated using OCCAM 5-day mean datasets for model year 1994, with the rate of change of heat content, calculated from the instantaneous datasets from the beginning and end of the year under study.

Results are presented for three regions in the Equatorial Pacific. The Equatorial Pacific was chosen because of the importance of heat transports there in the development of the El Nino (Halpern, 1987).

#### 4.1 Numerical details

Equation (12) is implemented for each of the regions studied. In terms of the model variables the advective term on an horizontal interface  $i + \frac{1}{2}$  is,

$$A_{i+\frac{1}{2},t_{i}} = \rho I_{i+\frac{1}{2}} C_{p} u_{i+\frac{1}{2},t_{i}} \left[ \frac{\left( T_{i+1,t_{i}} + T_{i,t_{i}} \right)}{2} - \frac{\left( T_{i+2,t_{i}} - T_{i+1,t_{i}} - T_{i,t_{i}} + T_{i-1,t_{i}} \right)}{12} \right]. \tag{18}$$

The first term on the right is the contribution from the central difference approximation and the second is the extra advective component of the MSQ scheme discussed in Sect. 3.1. Vertical fluxes are calculated similarly but with just the central differences term.

The total heat advection into each region at time  $t_i$  is obtained summing Eq. (18) over all the interfaces surrounding the region. Thus if  $\bar{A}_{\text{tot},t_i}$  is the total heat gain by advection in the region at time  $t_i$ ,

$$\bar{A}_{\text{tot},t_i} = \sum_{m} A_{n,m,t_i},\tag{19}$$

where the sum is over all the interfaces surrounding the region.

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$$D_{i+\frac{1}{2},t_{i}} = \Delta y \Delta z \left[ A_{h} \left( \frac{T_{i+1,t_{i}} - T_{i,t_{i}}}{\Delta x} \right) + \gamma \left( \frac{|U|}{U} \left( \frac{T_{i+2,t_{i}} - 3T_{i+1,t_{i}} + 3T_{i,t_{i}} - T_{i-1,t_{i}}}{16} \right) \right) \right], (20)$$

where  $A_h$  represents the horizontal diffusion coefficient and  $\gamma$  is a coefficient set to one (Webb et al., 1998). The last term is the diffusive component of the MSQ scheme. The expression for interfaces above and below the study region is similar except that  $A_h$  is replaced by the vertical diffusion coefficient and again the MSQ term is missing.

The total diffusive heat flux into the region is then:

$$\bar{D}_{\text{tot},t_i} = \sum_{m} D_{n,m,t_i},\tag{21}$$

where again the sum is over all the surrounding interfaces. For each analysis period, Eq. (12) can be written as,

$$\frac{\partial Q}{\partial t} = \bar{A}_{\text{tot},t_i} + \bar{D}_{\text{tot},t_i}. \tag{22}$$

#### 4.2 A single vertical column

We first analysed a single vertical column of model grid cells. The south-west corner of the column was at point 150° W, 4.5° N and it extended from a depth of 41.2 m to 146.79 m (see Fig. 1).

The heat content is given by

$$Q_{t_i} = \sum_{n} C_p \rho dx_n dy_n dz_n T_{n,t_i}, \tag{23}$$

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where the sum is over the model cells 'n' within the analysis region. If the averaging time is  $\Delta t$  then the mean rate of change of heat content is,

$$\frac{\Delta Q_{n,t_i}}{\Delta t_i} = C_p \rho dx dy dz \left( \frac{T_{n,t_{i+1}} - T_{n,t_i}}{\Delta t_i} \right). \tag{24}$$

Figure 3 shows the results for the single column for the year studied. The volume of the box is  $8.1 \times 10^{10} \, \text{m}^3$ , so a flux of 1 TW is equivalent to a temperature change of approximately  $0.25\,^{\circ}\text{C}\,\text{day}^{-1}$ . The results show that rates greater than  $0.1\,\text{TW}$  are common and that there is a large amount of short term variability. The differences between the actual heat flux and that calculated from the 5-day mean datasets are small, but they are systematic and may occasionally exceed 10 % of the total flux.

The second part of the figure shows the heat fluxes integrated over a year. In this case a change in heat content of 1 EJ is equivalent to an average temperature change of 2.9 °C.

The figure confirms that the errors are systematic, with the mean fields overestimating the total heat flux into the region during the year by approximately 1 EJ. The flux errors appear to be largest early in the year and from July onwards when Tropical Instability Waves are most developed.

#### 4.3 An independent estimate of the advective error

Figure 3 shows that flux calculations using the mean datasets produces errors, but it does not show whether they are primarily due to errors in calculating the advective or diffusive fluxes. However it is possible to make an estimate of the advective error from the differences between the mean and instantaneous data sets.

For the fluxes through a single model interface, Eq. (9), becomes

$$\overline{uT} = (\overline{u}\overline{T}) + \overline{(u'T')}. \tag{25}$$

 $\bar{T}$  and  $\bar{u}$  are now values from the 5-day mean datasets and the errors in the advective flux calculation correspond to the term u'T'.

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If the fields u(t) and T(t) oscillate many times during each averaging interval then, as discussed in Appendix A, u'T' will have the same statistical properties as  $F_{\rm e}(m)$ , where,

$$F_{e}(m) = (u_{e}(m) - \bar{u}(m))(T_{e}(m) - \bar{T}(m)), \tag{26}$$

<sub>5</sub> and  $u_{\rm e}(m)$  and  $T_{\rm e}(m)$  are the instantaneous values at the end of each interval 'm' available from the restart datasets. The mean value and variance of  $F_{\rm e}(m)$  over a period of time should then be a good approximation to the mean and variance of u'T' during the same period.

In the other limit when the fields u(t) and T(t) are slowly varying, so that they can be approximated as linear functions of time, u' and T' have their maximum amplitudes at the beginning and end of each 5-day period. As shown in Appendix A, Eq. (26), then overestimates u'T' by a factor of three.

Using this independent estimate, the total error in using mean datasets to calculate the advective fluxes into a region of the model ocean is,

$$F_{e,tot} = \sum_{m=1}^{M} (A_m S_m (u_e(m) - \bar{u}(m)) (T_e(m) - \bar{T}(m)))$$
 (27)

where the sum is over the interfaces surrounding the region being considered.  $A_m$ is the area of the mth interface and  $S_m$  equals +1 if u represents inflow and -1 if it represents outflow. The estimate of the advective error will be referred to as the high frequency term.

Figure 4 compares this estimate of the advective error, for the column considered earlier, with the actual error calculated from the difference between the two fluxes in Fig. 3a. At most times the advective estimate is of the same order but slightly larger than the actual error. This confirms that the error estimate  $F_{\rm e}$ , is comparable in magnitude with the error arising from using mean datasets. The average ratio between the two flux magnitudes appears to be larger than the figure of three given above,

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but overall the result shows that the instantaneous datasets can provide useful extra information on the transport of heat within the ocean.

#### 5 The Eastern Equatorial Pacific

#### 5.1 The advection term

We extend this analysis to two regions in the equatorial Pacific. The first lies in the Eastern Equatorial Pacific, between 150° W and 120° W and between 2.25° N and 4.75° N (see Fig. 1), and covers the same range of depths as the single column. This region is characterised by strong horizontal shears due to the North Equatorial Counter Current and the Equatorial Undercurrent. It is also an area of energetic variability due to the presence of Tropical Instability Waves.

Figure 5a shows the rate of change of heat content and the heat flux due to advection and diffusion, calculated from the averaged datasets. For this region a flux of 1 PW is equivalent to a temperature change of 0.21 °C day<sup>-1</sup>. Figure 5b shows the integrated values, a difference of 1ZJ being equivalent to a temperature change of 2.4°C.

The two flux curves follow each other closely for most of the year. However, as shown in Fig. 5b, from July onward the integral over the year, using the mean datasets, produces a much larger increase in the total heat content than is actually observed. By the end of the year the resulting error is as great as the annual variation in the heat content of the region.

Figure 6 compares the error in the flux calculation with the estimate of the advective error calculated using Eq. (27). Both terms have the same overall behaviour and it is noticeable that during July, when the errors are largest, they show a remarkable amount of agreement.

In the OCCAM model, this region north of the equator is one where Tropical Instability Waves are observed. These grow rapidly each June and have their greatest amplitudes between July and January. It seems likely that the waves are advecting heat out of the region and that this process is not being captured by the mean datasets.

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The second region studied has the same longitude range but spans the equator, running from 1 $^{\circ}$  S to 2.25 $^{\circ}$  N. Advection in the region is dominated by the westward flowing Equatorial Undercurrent but there is also strong equatorial upwelling and meridional convergences and divergences.

Figure 7 shows the rate of change of heat content and the estimated heat flux due to advection and diffusion using the mean datasets. For this region a flux of 1 PW is equivalent to a temperature change of 0.16 °C day<sup>-1</sup>. Figure 7b shows the integrated values, a difference of 1 ZJ being equivalent to a temperature change of 1.9 °C.

The heat flux calculated from the 5-day mean datasets is generally in good agreement with the full model calculation but this time the mean datasets tend to slightly underestimate the fluxes.

This differences shows up more clearly when integrated over a year (Fig. 7b). The differences are less than they were for the northern region but whereas before the mean datasets were overestimating the heat gain, here they overestimate the heat loss. Thus the missing high frequency terms must be warming the region.

Figure 8 shows that the warming may be due to the high frequency advective term. However, especially from September onwards, the estimate of the missing advective contribution is much larger than the actual error. Given the earlier discussion on the different sources of error, this implies that in this region we also need to consider a possible high frequency contribution to vertical mixing.

To summarise the results of this section, in the Eastern Tropical Pacific we find that there are important heat transport processes which are not captured by 5-day mean datasets. In the region of the Tropical Instability Waves we find that over the course of a year the cumulative error can be as large as the seasonal signal. An estimate of the high frequency advective terms indicates that these may be responsible for the discrepancy.

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Near the Equator we find that the cumulative error from using the mean datasets is smaller but that the high frequency advective terms are likely to overcorrect the error. Thus in this region errors due to fluctuations in the diffusion terms also need to be considered.

#### 5.2 The diffusion terms

As discussed earlier, the scheme used to represent horizontal diffusion in the ocean is linear and so is not affected by high-frequency non-linear effects. In the vertical however the model uses the Pacanowski and Philander (1981) scheme and this is non-linear and so will be affected by the high-frequency fluctuations.

The Pacanowski and Philander (1981) vertical mixing scheme depends on the Richardson number which in OCCAM is calculated as:

$$Ri_{k} = g \frac{(z_{k+1} - z_{k})}{\rho} \frac{(\rho_{k} - \rho_{k+1})}{((u_{k} - u_{k+1})^{2} + (v_{k} - v_{k+1})^{2})}$$
(28)

where  $z_k$  is the layer depth,  $\rho$  is the density, u and v are the zonal and meridional velocities and g is gravity.

The vertical mixing coefficient is given by,

$$A_Z = \frac{v_0}{(1 + \alpha Ri)^n} + v_b, \tag{29}$$

where  $\alpha = 5$ , n = 3,  $v_0 = 50$  and  $v_b = 0.5 \,\mathrm{cm}^2 \,\mathrm{s}^{-1}$ .

When the Richardson number is large (Ri > 0.2), the flow is stable to shear instabilities and the vertical mixing coefficient is small ( $\sim 0.5 \, \mathrm{cm}^2 \, \mathrm{s}^{-1}$ ). Conversely, when the Richardson number is small, shear instabilities develop and the mixing coefficient is large ( $\sim 50 \, \mathrm{cm}^2 \, \mathrm{s}^{-1}$ ).

Over most of the ocean the Richardson number is large, so shear instabilities have little effect. However there exist regions, such as the equatorial undercurrent, where

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vertical shear is large and the stratification small. The Richardson number is then small and there is strong vertical mixing.

We investigated this effect by calculating the Richardson number at the top of the cross equatorial region for each analysis time step and grid point, during two time periods – January to May and August to December. This was carried out using both the average and the instantaneous data sets. The region had 1920 grid boxes in the top layer and the calculation was repeated for 28 datasets for both periods, giving a total of 53 760 data points. Points with Richardson number bigger than 0.8 have not been plotted.

The results are shown in Fig. 9. At a Richardson number of 0.8 the vertical mixing coefficient has a value of  $0.9\,\mathrm{cm}^2\,\mathrm{s}^{-1}$ . It increases to  $1.6\,\mathrm{cm}^2\,\mathrm{s}^{-1}$ , at a Richardson number of 0.2, to  $15\,\mathrm{cm}^2\,\mathrm{s}^{-1}$  at 0.1 and  $44\,\mathrm{cm}^2\,\mathrm{s}^{-1}$  at 0.01.

The figure confirms that large Richardson numbers are the most common but more importantly it also shows systematic differences between the values calculated from the instantaneous and 5-day mean datasets. Thus during the first analysis period the number of grid points in the instantaneous datasets with Richardson number less than 0.1 is ten times larger than for the five day data sets. For the second analysis period there is a similar order of magnitude difference for Richardson numbers of less than 0.07.

In both cases the results imply that the mean datasets are missing many of the strong vertical mixing events. For Richardson numbers larger than 0.15, the instantaneous and mean dataset results tend to have similar numbers of points within each of the plotted bands. Thus although there is a strong seasonal signal most of it is captured by the 5-day mean datasets.

Figure 7b compares the integrals of the heat fluxes obtained when using either the mean or instantaneous datsets when calcuating the Richardson number, with the rate of change of the total heat content of the region being studied. It shows that the instantaneous datasets give the better agreement, presumably, as discussed above, they are better at capturing the periods of strong mixing.

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Figure 8 shows the difference between the rate of change of heat content and the total heat flux into the volume using 5-day mean and instantaneous datasets. The figure also shows the estimate of the error, or high frequency term. It can be seen that while both curves follow each other most of the time the use of instantaneous datsets gives stronger fluctuations; at times the latter is closer to the high frequency term than the error produced by the use of the 5-day mean datasets. This is best seen during January and between June and September.

#### Annual average fluxes in the North Equatorial region

Table 1 shows the annual average heat fluxes through each of the interfaces for the region north of the equator for the year under study. As before the advection and diffusion terms are calculated from the 5-day average datasets and the estimate of the high frequency contributions to the advective terms are calculated from the instantaneous restart datasets.

The figures show that the region is warmed by the downward advection of heat and that this is largely balanced by a loss of heat due to meridional advection. A smaller amount of heat is lost to zonal advection. Thus when using the 5-day mean fields, the net effect of advection is to warm the region at a rate of 29.8 TW<sup>2</sup>.

The same mean fields produce a diffusive cooling at a rate of 14.2 TW. This is due primarily to a loss of heat to layers deeper in the water column. The combined effect of advection and diffusion, using the 5-day average values, thus produces a heating at a rate of 15.6 TW. However over the course of the year the model region actually cooled at a rate of 2.2 TW, which means that the mean fields are generating a spurious heating at a rate of 17.8 TW.

The estimates of the contributions to the high frequency advective term show that

<sup>&</sup>lt;sup>2</sup>Other studies are often concerned with the heat flux through the surface of the ocean. To convert TW to the equivalent flux in W m<sup>-2</sup> through the top surface of each volume studied, mutiply by 1.08 for the north equatorial region and 0.83 for the larger equatorial region.

the main contribution comes from advection of heat through the upper surface of the region. There is also a significant southward heat flux but the two terms balance out so the net effect is small. Overall the fluctuations in the advective term are estimated to generate a heat flux cooling of 23.2 TW – close to the value needed to explain the descrepancy when using the 5-day mean fields.

#### 5.4 Annual averaged fluxes in the Equatorial Region

Table 2 shows the corresponding values for the region centred at the equator. The advection terms, calculated using the 5-day mean datasets, generate a net cooling over the year of 32.54 TW. The meridional flows act to heat the region but this is balanced by large vertical and meridional heat losses.

As with the northern region, diffusion is dominated by the vertical terms, but this time they act to warm the region. The total diffusive flux is 12.14 TW as a result of which the advection and diffusion using the 5-day datasets gives a heat flux loss of 20.4 TW. Over the year the model region actually cooled at a rate of 13.8 TW meaning that the mean fields overcooled the region by 6.6 TW.

The estimates of the heat advected by the high frequency fluctuations indicates that they generate a southward flux of heat into the region which is partly compensated by a loss to the surface layers of the ocean. The net heat flux by these terms (8.0 TW) is certainly sufficient to explain the errors when using the 5-day mean datasets.

However the equatorial region is also one where shear instabilities above the equatorial undercurrent are likely to be important. For this reason Table 2 also includes a column showing the estimate of the diffusion obtained when the instantaneous restart values are used to calculate the Richardson number. This shows an increase in the downward diffusion of heat, the net effect being an increase of 4.6 TW in the diffusive heat flux into the region.

If the high-frequency and instantaneous Richardson number contributions are taken together their sum (12.2 TW) is almost double the amount needed to explain the descrepancy when using the mean datasets. However if the high frequency term is being

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overestimated (see Appendix A), which is possible given the long term drift in heat content (see Fig. 7), then its actual value could be nearer 2.7 TW. Together with the Richardson number contribution this would give a net cooling of 13.3 TW, close to the actual change of 13.8 TW.

#### Discussion and conclusions

The overall purpose of this study was to shed light in the limitations of using 5-day mean datasets in heat budget analyses in the ocean. The results show that processes with a period of less than five days can have a significant impact on the heat budget and that model restart datasets can be used to estimate the size of the resulting errors.

In the region studied north of the equator, calculation of the advection and diffusion terms using the 5-day mean datasets showed a net heating of 15.6 TW during the year studied, whereas the model, which conserves heat every timestep, actually cooled at a rate of 2.2 TW. The descrepancy of 17.8 TW is in reasonable agreement with the value of 23.2 TW, estimated as being the contribution of the advective processes with periods of less than 5 days.

In the equatorial region, the 5-day mean datasets produced a net cooling of 20.4 TW. Temperatures in the model did drop during the year but only at a rate of 13.8 TW, leaving a descrepancy of 6.6 TW. Estimates of the high-frequency contributions indicated that the descrepancy may result from both the extra advection and diffusion terms.

Overall the results stress the importance of short period fluctuations in the transport of heat within the ocean. Such advective fluctuations are often called eddy heat fluxes and, as concluded by Bryden and Brady (1989), they make a substantial contribution to the heat balances in the equatorial Pacific Ocean. The model results indicate that in the regions studied the "eddies" are primarily Tropical Instability Waves and that datasets, averaged over periods of only 5 days, are insufficient to fully resolve their effect.

It is possible that such terms have their greatest effect in the tropical regions studied here but, until it is shown otherwise, they need to be treated with care in all regions of the ocean.

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### Estimating the contribution of short period fluctuations

Assume that the model is run for a period of time to estimate uT, the flux through a particular interface. Let the period be made up of M intervals, each involving N model timesteps of length dt. Then if u(i) and T(i) are the values of u and T on an interface at timestep i, the total heat flux,  $F_a$ , through the interfaces is:

$$F_{a} = \sum_{m=1}^{M} \sum_{n=1}^{N} \frac{u(i)T(i)}{MN}$$
 (A1)

where *i* equals (m-1)N + n.

At the end of the model run the data archive includes the instantaneous values  $u_{\rm p}(m)$ and  $T_{\rm e}(m)$  (equal to u(Nm) and T(Nm)) from the last timestep of each of the M intervals, plus  $\bar{u}(m)$  and  $\bar{T}(m)$  the mean values over each of the intervals.

Let u'(i) and T'(i) be defined as the differences between the actual value at the current timestep 'i' and the mean value during the current interval 'm'. Then,

$$u'(i) = u(i) - \bar{u}(m) \tag{A2}$$

$$T'(i) = T(i) - \bar{T}(m) \tag{A3}$$

Then following a similar argument to that used to derive Eq. (9),

$$F_a = \sum_{m=1}^{M} \frac{\bar{u}(m)\bar{T}(m)}{M} + \sum_{m=1}^{M} \sum_{n=1}^{N} \frac{u'(i)T'(i)}{MN}$$
 (A4)

where *i* is related to *m* and *n* as before.

If heat fluxes are calculated from just the mean values during each interval, then the first term is the resulting estimate of the heat flux. The second term, the contribution 9, 25-61, 2012

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$$F_{e} = \sum_{m=1}^{M} \sum_{n=1}^{N} \frac{u'(i)T'(i)}{MN}$$
 (A5)

If there are a large number of fluctuations of u and T within each averaging interval and the amplitude of the fluctuations are large compared with changes in the mean values, then the set of archived instantaneous values  $u'_{\rm e}(m)$  and  $T'_{\rm e}(m)$  (equal to u'(mN)) and T'(mN)), should have similar statistics as the full set of values, u'(i) and T'(i).

If this is so then a good approximation to  $F_e$  is given by,

$$E(F_{e}) = \frac{1}{M} \sum_{m=1}^{M} u'_{e}(m) T'_{e}(m), \tag{A6}$$

where,

$$u'_{e}(m) = u_{e}(m) - \bar{u}(m),$$
 (A7)

$$T_{\mathrm{e}}'(m) = T_{\mathrm{e}}(m) - \bar{T}(m). \tag{A8}$$

 $E(Q_e)$  is easily calculated from the restart data.

Also if  $F_{\rm e}(m)$  is the contribution from interval m, and  $\varepsilon$  is r.m.s. amplitude of such contributions over the period studied then,

$$\varepsilon = \sqrt{\frac{\sum (u_{\rm e}'(m)T_{\rm e}'(m))^2}{n-1}} \tag{A9}$$

where n is the number of data sets during one year.

If instead u' and T' vary slowly with time, then the product u'T' will tend to be largest near the beginning and end of each averaging interval. In this case Eq. (A6) will overestimate the contribution of fluctuations to the total heat flux.

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$$u'(i) = (u_e(m) - \bar{u}(m)) \frac{i - (N+1)/2}{(N-1)/2},$$
(A10)

$$T'(i) = (T_{e}(m) - \bar{T}(m)) \frac{i - (N+1)/2}{(N-1)/2}.$$
(A11)

5 The error in using  $u_m$  and  $T_m$  alone during the period is,

$$F_{\rm e}(m) = u_{\rm e}'(m)T_{\rm e}'(m)\frac{1}{N}\sum_{i=1}^{N} \left(\frac{i - (N+1)/2}{(N-1)/2}\right)^2. \tag{A12}$$

Using standard formula for the sum of integers and their squares, it is straightforward to show that,

$$F_{\rm e}(m) = u'_{\rm e}(m)T'_{\rm e}(m)\left(\frac{1}{3}\frac{N-1}{N+1}\right).$$
 (A13)

When N is large,

$$F_{\rm e}(m) = \frac{1}{3} u'_{\rm e}(m) T'_{\rm e}(m)$$
 (A14)

Thus a good estimate of the error in the flux arising from the use of mean values is given by,

$$E(F_{\rm e}) = \frac{1}{3M} \sum_{m=1}^{M} u'_{\rm e}(m) T'_{\rm e}(m). \tag{A15}$$

This shows that, in the worst case, Eq. (A6) overestimates the error by a factor of three. In general we may expect the factor to lie between 1 and 1/3, although the error in any one of the averaging intervals may be greater or less than that estimated using the above equations.

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**Table 1.** Heat fluxes averaged over the year at each interface of the region north of the Equator. The columns show the heat fluxes due to advection and diffusion, both calculated from the 5-day mean datasets, and the estimate  $F_{\rm e}$  of the error in the advective flux due to ignoring high frequency fluctuations. The last column shows the actual mean rate of change of heat content during the period. Positive signs indicate flux into the region. Units are TW (10<sup>12</sup> W).

interface	advection	diffusion	$F_{\mathrm{e}}$	$\frac{\partial Q}{\partial t}$
top	417.61	7.66	-26.16	
bottom	83.62	-21.33	1.15	
east	340.28	0.01	0.59	
west	-398.69	-0.01	-0.17	
north	697.51	0.39	12.27	
south	-1110.50	-0.93	-10.84	
Total	29.83	-14.20	-23.15	-2.20

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**Table 2.** As Table 1 but for the region centred at the Equator. In addition the table shows the vertical diffusive flux when using the restart datasets when calculating the Richardson number. Flux in TW.

interface	advection	diffusion		$F_{ m e}$	$\frac{\partial Q}{\partial t}$
		5-day	restart		01
top	-2298.29	29.81	34.17	-2.92	
bottom	429.55	-18.68	-18.69	-0.25	
east	-1002.88	0.01	0.01	0.48	
west	911.50	0.02	0.02	0.08	
north	1110.50	0.93	0.93	10.84	
south	817.08	0.05	0.05	-0.25	
Total	-32.54	12.14	16.50	7.98	-13.84

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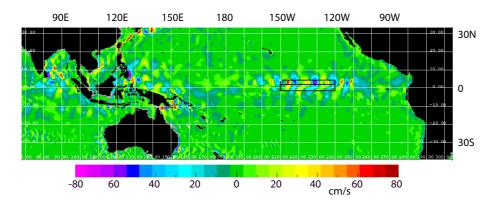
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**Fig. 1.** Meridional velocity (cm s<sup>-1</sup>) at 30 m depth in September 1993 (from an OCCAM restart dataset). The rectangular areas outline the regions used for the flux study described later in this paper.

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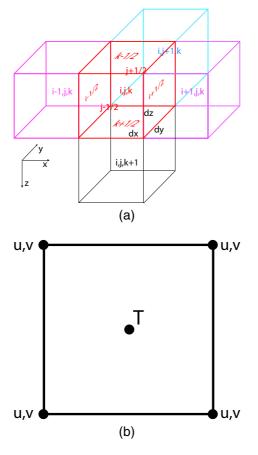
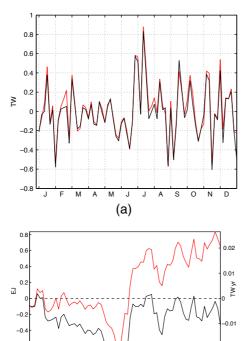


Fig. 2. (a) Model grid box around the point i/k; i increases with longitude, j with latitude and k with model depth. The length of each side of the box are given by dx, dy and dz, and interfaces between boxes are represented by  $i + \frac{1}{2}$ ,  $i - \frac{1}{2}$ , etc. (b) Hozizontal arrangement of tracer (temperature) and velocity compnents in the Arakawa B-grid.



**Fig. 3.** Results for the single column of model cells at  $150^{\circ}$  W,  $4.5^{\circ}$  N during model year 1994. **(a)** Sum of the advection and diffusion terms (red – calculated from the 5-day mean datasets) and rate of change of heat content (black – calculated from the instantaneous datasets). Heat flux in TW ( $10^{12}$  W). **(b)** Cumulative integrals of both terms. Heat content in EJ ( $10^{18}$  J).

(b)

-0.02

-0.03

0

-0.6

-0.8

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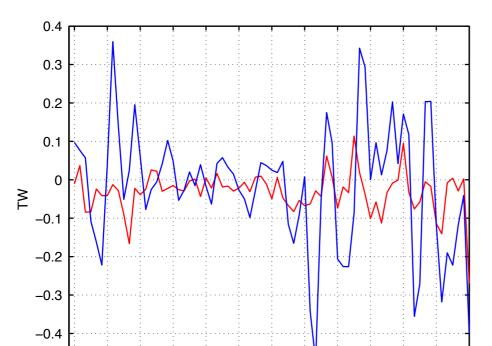
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**Fig. 4.** Estimates of the heat flux error (in TW) due to neglecting short term fluctuations (blue – Eq. A6) compared with, in red, the difference between the actual change in model heat content and that estimated from the 5-day mean datasets.

S

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-0.5

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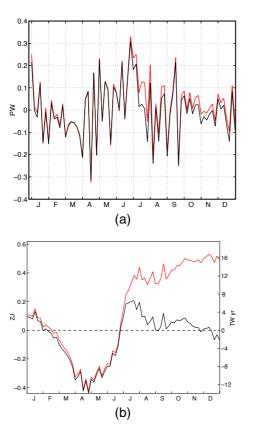
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**Fig. 5.** Results for the northern region during model year 1994: **(a)** Rate of change of heat content (black – calculated from the instantaneous datasets) and sum of the advection and diffusion terms (red – calculated from the 5-day mean datasets). Heat flux in PW (10<sup>15</sup> W). **(b)** Cumulative integrals of both terms. Heat content in ZJ (10<sup>21</sup> J), also shown as TW years.

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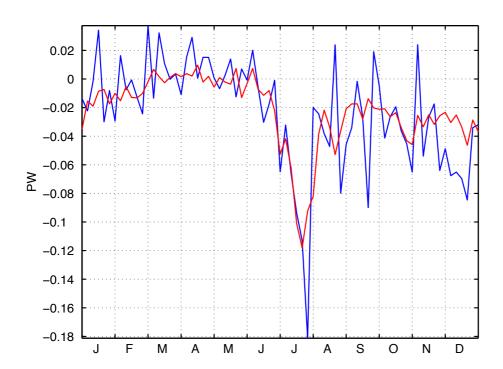


Fig. 6. Results for the northern region: Estimates of the heat flux error (in PW) due to neglecting short term fluctuations (blue - Eq. A6) compared with, in red, the difference between the actual change in model heat content and that estimated from the 5-day mean datasets.



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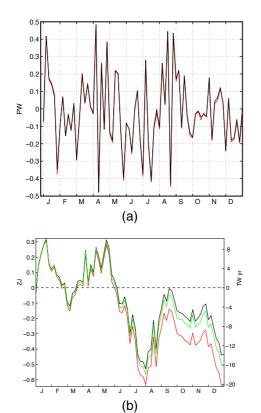
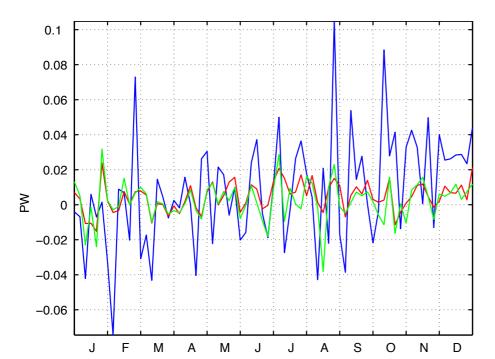


Fig. 7. Results for the equatorial region: (a) Rate of change of heat content (black - calculated from the instantaneous datasets) and sum of the advection and diffusion terms (red - calculated from the 5-day mean datasets). Heat flux in PW. (b) Total heat content (black from instantaneous datasets) plus cumulative integrals of heat fluxes calculated using mean datasets (red) and instantaneous datasets (green). Heat content in ZJ (10<sup>21</sup> J), also shown as TW years.



**Fig. 8.** Result for the equatorial region: Estimate of the heat flux error (in blue) resulting from ignoring the high frequency fluctuations compared with (red) the difference between rate of change of the model heat content and the fluxes calculated using the 5-day mean datasets and (green) the same but using the instantaneous datasets to calculate Richardson numbers.

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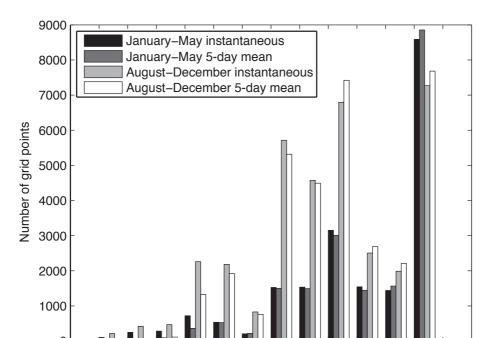
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**Fig. 9.** Number of grid points at 41.20 m (model level three) with values of the Richardson number within the interval shown, see legend.

0.4 0.45 0.5

Ri

0.0010.01 0.07 0.1 0.15 0.18 0.19 0.25 0.3

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