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Towards high resolution mapping of 3-D mesoscale dynamics from observations: preliminary comparison of retrieval techniques and models within MESCLA project

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Discussion Paper OSD 9, 1045-1083, 2012 **High resolution** mapping of 3-D mesoscale dynamics Discussion Paper B. Buongiorno Nardelli et al. **Title Page** Introduction Abstract Discussion Paper Conclusions References Figures Tables Back Close **Discussion** Paper Full Screen / Esc Printer-friendly Version Interactive Discussion



Abstract

Within the MyOcean R&D project MESCLA (MEsoSCale dynamical Analysis through combined model, satellite and in situ data), different estimates of the vertical velocities derived from observations have been compared. Two main approaches have been considered, one based on the retrieval of 3-D fields from the observations alone and one based on the analyses provided by MyOcean MERCATOR models. The motivation for this double approach is that, while data assimilation in numerical models is crucial to obtain more accurate analyses and forecasts, its results might be significantly influenced by specific model configurations (e.g. forcing, parameterization of smaller scale processes and spatial resolution). On the other hand, the purely observation-based approach is limited by the underlying assumptions of simplified dynamical models and by the relatively low resolution of present products. MESCLA tested innovative methods for the high resolution mapping of 3-D mesoscale dynamics from observations, developing new products that might be used to gradually build the next generations of

¹⁵ operational observation-based products.

1 Introduction

The MESCLA project (MEsoSCale dynamical Analysis through combined model, satellite and in situ data, 2010–2012) is devoted to the retrieval and analysis of the vertical velocities in the oceans from a combination of observations and models. The project

- has been funded in the framework of the MyOcean 2009 Open Call for Research and Development and its rationale lies in the fundamental role played by mesoscale in modulating the ocean circulation and the fluxes of heat, freshwater and biogeochemical tracers between the surface and the deeper layers. Indeed, while mesoscale has a crucial role in water mass distribution and mixing below the upper mixed layer, it is not established wat how its interaction upper bility may affect the energy descent and simulation
- established yet how its interannual variability may affect the ocean general circulation and modulate the marine ecosystem functioning (e.g. Levy, 2008; Gruber et al., 2011;





Farneti et al., 2010; and references therein). In fact, significant variations in the vertical exchanges could cause a reduction of the atmospheric CO_2 absorption and sequestration in the deep ocean, as well as a decrease in nutrient availability for phytoplankton growth and reduced sinking of organic matter (biological pump). These variations might thus have an impact on global climate and marine ecosystem. In turn, it is still not fully

⁵ thus have an impact on global climate and marine ecosystem. In turn, it is still not fully assessed how mesoscale activity and associated vertical motions are influenced by observed interannual/climatic changes.

In this context, the main MESCLA objective is the analysis of the interannual variability of the vertical exchanges associated to mesoscale dynamics, from a combination of

- observations and models. However, while the vertical component of ocean currents can be diagnosed in primitive equation numerical models by solving the continuity equation, the same technique is not applicable to direct observations. This is due, on one hand, to the few current measurements available, and, on the other hand, to the high error that would result from the computation of the divergence from measured horizontal
- velocities, that may include significant instrumental errors. It is also clearly impossible to use the continuity equation to estimate the vertical velocities from dynamic heights (computed from temperature and salinity profiles), as the geostrophic velocities are non-divergent by definition. On the other hand, simplified diagnostic models can be applied to retrieve the vertical velocity field from three-dimensional (3-D) estimates of
- 20 geostrophic currents and density fields (e.g. Tintoré et al., 1991; Allen and Smeed, 1996; Buongiorno Nardelli et al., 2001; Pascual et al., 2004; Ruiz et al., 2009). Nevertheless, it must be stressed that sufficiently high spatial resolution must be reached to obtain accurate estimates of the vertical exchanges from 3-D observation-based systems. In fact, in order to correctly retrieve the vertical velocities associated with
- ²⁵ mesoscale features, one should be able to resolve very small scales, i.e. up to less than 10 (for a complete review on the topic, see Klein and Lapeyre, 2009). Actually, 3-D observation-based systems are far enough from being able to correctly reproduce the global variability at these scales (Willis et al., 2003; Roemmich and Gilson, 2009; Von Schuckmann et al., 2009; Guinehut et al., 2004, 2012; Larnicol et al., 2006). In





this framework, the first step of MESCLA project was the improvement of the existing MyOcean observation-based products (namely MyOcean ARMOR3D, Guinehut et al., 2012) and the development and test of new high resolution horizontal interpolation and vertical extrapolation techniques (Buongiorno Nardelli, 2012; Buongiorno Nardelli et

- al., 2006; Buongiorno Nardelli and Santoleri, 2004, 2005). As a second step, a quasi-geostrophic diagnostic numerical model (the Q-vector formulation of the Omega equation) has been used to estimate the vertical velocities (Pascual et al., 2004; Ruiz et al., 2009). The Omega equation was applied to different MyOcean products (both model and observation-based) in order to quantify the limitations in the diagnostic tools used
 and the impact of the resolution on the retrieved velocity. The preliminary results of
 - these first two steps are the subject of the present paper.

The comparison of both model/assimilation and purely observation-based data is expected to provide a more robust analysis of mesoscale vertical velocity variability. In fact, the observation-based products are obtained through relatively simple statistical

- analyses and simple approximations. Conversely, it is evident that data assimilation into models allows to obtain more accurate analyses and forecasts, especially at the shorter time scales, but one must be aware of the fact that model results can be greatly influenced by the specific model configurations and by the uncertainties in the boundary condition imposed (e.g. atmospheric forcing used, parameterization of smaller scale
- ²⁰ processes, spatial resolution, etc.). Comparing the two approaches might thus help to better understand the vertical exchanges associated with mesoscale processes. To summarize, in this paper we will thus describe:
 - the strategies adopted to improve the observation-based products resolution, namely the ingestion of different high resolution Sea Surface Temperature level
 - 4 products (SST L4, i.e. interpolated data) and of a high resolution Sea Surface Salinity product developed within MESCLA in the ARMOR3D processing (Sect. 4.1.1);





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- The implementation of new extrapolation methodologies to obtain experimental higher resolution 3-D re-analyses based on a high resolution Sea Surface Salinity product developed within MESCLA, on one selected high resolution SST L4 product (Sect. 4.1.2) and standard altimeter products;
- the diagnostic model used to retrieve the quasi-geostrophic vertical velocity field from the previously described observation-based density and geostrophic velocities fields (Sect. 4.2);
 - a preliminary evaluation of the 3-D reconstruction methods performances (Sects. 5.1–5.2);
- the comparison of the MyOcean MERCATOR PSY3V2R2 and PSY2V3R1 model vertical velocities (see Sect. 3) with the quasi-geostrophic currents obtained from the model density field (Sect. 5.3);
 - the impact of the increased resolution on the estimation of the vertical velocity field from the 3-D observation-based products (Sect. 5.4).
- Given the lack of independent (direct) measurements of the vertical velocities, a full validation of the new products is clearly not possible. Consequently, the approach followed here relies on the comparison between several different products, concentrating on a well-known area of intense mesoscale activity (the Gulf Stream) and on a specific day (the 17 October 2007), and on the analysis of the impact of the new techniques
 on the vertical velocity field estimation. Additional investigations, including longer time series and more detailed dynamical analyses are left for future work.

2 Observations

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Any vertical extrapolation method requires, on one hand, an historical in situ dataset to estimate the direct correlations between the parameters of interest (namely, temperature, salinity and steric height) or to identify their main statistical or empirical modes





of variability, and, on the other hand, surface measurements of at least two of these parameters to be able to extrapolate their vertical profiles. In the following, the datasets used within MESCLA project are briefly described.

2.1 In situ data

- ⁵ The operational ARMOR3D and the experimental ARMOR3D-MESCLA systems (Sect. 4.1) are trained with the profiles of temperature (*T*) and salinity (*S*) coming from Coriolis/ARGO for more recent data (http://www.coriolis.eu.org), and from the EN3 dataset for the historical data (Ingleby and Huddleston, 2007). Similarly, the dataset used within MESCLA to test the new vertical extrapolation techniques mEOF-R consists of the quality controlled *T* and *S* profiles measured by ARGO and CTD sensors and distributed by the MyOcean In Situ Thematic Assembly Centre (more precisely, these are the profiles used by CORIOLIS In Situ Analysis System (ISAS) to produce their global temperature and salinity 3-D fields). The same dataset served also to de-
- velop the MESCLA high resolution SSS product (Buongiorno Nardelli, 2012). These observations are pre-processed according to ARGO recommendations for data quality control (Wong et al., 2012).

2.2 Surface data

2.2.1 SSS

The Sea Surface Salinity (SSS) L4 data used in input to the mEOF-R 3-D reconstruction (Sect. 4.1.2) was developed as an experimental product in the framework of MESCLA project. Its space-time resolution is 1/10°, daily. The method used to retrieve this SSS field is based on an Optimal Interpolation (OI) algorithm that interpolates in situ salinity including satellite high-pass filtered sea surface temperature (using 1/10° ODYSSEA SST L4) in the determination of the weights used to interpolate SSS
 observations. The covariance function parameters (i.e. spatial, temporal and thermal





decorrelation scales) and the noise-to-signal ratio have been determined empirically, as fully described in Buongiorno Nardelli (2012).

2.2.2 SLA/ADT

The altimeter Sea Level Anomalies (SLA) and Absolute Dynamic Topography (ADT) gridded data used for the 3-D retrieval are those produced and disseminated by the SSALTO/DUACS centre and represent the MyOcean Sea Level Thematic Assembly Centre intermediate product (AVISO, 2011). They are obtained as daily combined maps from all processed altimeters (currently: Jason-1, Jason-2 and Envisat for the NRT products) with a 1/3° horizontal resolution.

10 2.2.3 SST

Different satellite SST datasets have been used for the different phases of the work. each characterized by different nominal and effective resolution (as summarized in Table 1). In fact, as discussed by Reynolds and Chelton (2010), the true resolution of a L4 product is given by a combination of the grid spacing and of the analysis procedures and configurations applied (e.g. weighting functions and background fields). As 15 a consequence, while combined ARMOR3D product is based on the Reynolds Optimally Interpolated L4 SST both at low (1°, corresponding to MyOcean V0 product) and high (1/4°, corresponding to MyOcean V1 product) resolution (Larnicol et al., 2006; Guinehut et al., 2012), the higher resolution tests on ARMOR3D system have been performed also on the ODYSSEA L4 data produced by Ifremer in the framework of 20 the MERSEA project and maintained as part of MyOcean (Autret and Piollé, 2007), and on the Operational SST and Sea Ice Analysis system (OSTIA, see Donlon et al., 2011) also distributed as part of the MyOcean Sea Surface Temperature Thermatic Assembly Centre. ODYSSEA provides daily SST estimates on a 0.1 × 0.1° grid for the Global Ocean, based on both infrared and microwave measurements, while OSTIA L4 25 is available on a 1/20° horizontal grid and includes also in situ SST measurements.





For the test of the new extrapolation techniques (Sect. 4.1.3), only the ODYSSEA L4 has been used. This choice was driven on one hand by the fact that ODYSSEA is among the highest resolution Global SST L4 available and quality controlled operationally (see also Dash et al., 2010), its algorithm is particularly able to retain the smaller spatial scale signals without smoothing too much the original observations (e.g. Maturi et al., 2010) and, on the other hand, by the fact that it is the same product used to retrieve the high resolution SSS by Buongiorno Nardelli (2012).

3 Model output

The model outputs used in this study are daily means computed from the global physical ocean forecasting system delivered as intermediate products by the global Monitoring and Forecasting Centre from MyOcean, namely Mercator Océan. In order to investigate the impact of the horizontal resolution in the vertical velocities reconstruction phase, the two components which compose the global system have been used: the global 1/4° called PSY3V2R2 and the North Atlantic and Mediterranean Sea 1/12°
called PSY2V3R1 (Dombrowsky et al., 2009; Lellouche et al., 2012). Except the horizontal resolution, the two configurations are really close in term of ocean model version, numerical schemes, physical parameterizations, bathymetry, atmospheric forcing, assimilation scheme and assimilated data. The model configuration is based on NEMO1.09 (Madec, 2008) with vertical z coordinates including partial step parameterization and 50 vertical levels from 1 m resolution at the surface to 400 m at the battem. The main numerical schemes used in these applications are set.

- bottom. The main numerical schemes used in these configurations are a TVD advection scheme and an isopycnal laplacian diffusion for the tracers, the energy and enstrophy conserving scheme and a biharmonic diffusion for the momentum. The vertical mixing scheme is TKE with an enhanced convection parameterization in case
- of instability of the water column. All these options are classical and used in global ocean model as mentioned in Barnier et al. (2006). The atmospheric forcing for the real time production is based on daily average of the atmospheric variables or flux





provided by the ECMWF real time forecasting system. The assimilation scheme (Tranchant et al., 2008) used in both configurations is based on the SEEK filter which allows assimilation of the sea level along-track satellite observations delivered by the MyOcean sea level Thematic Assembly Centre., the temperature and salinity profiles

- from the MyOcean insitu Thematic Assembly Centre and the RTG sea surface temperature (http://polar.ncep.noaa.gov/sst/oper/Welcome.html). The model outputs used in this study are based on the "best analysis" which is performed every week with a one week delay in time to assimilate the most of observations over a one week assimilation window. This system was the global forecasting system operated during the V0 phase
- ¹⁰ of MyOcean. The vertical velocity which is used as "reference" in this study to validate the quasi-geostrophic Omega equation is computed by an upward integration of the horizontal divergence from the bottom (Madec, 2008) which is the standard way to compute the vertical velocities in NEMO model in the case of a free surface condition.

4 Methods

15 4.1 3-D reconstruction

Several dynamic, variational, statistical and empirical techniques have been developed in the past to retrieve 3-D fields from a combination of in situ and satellite data (e.g. Carnes et al., 1994; Gavart and De Mey, 1997; Pascual and Gomis, 2003; Meinen and Watts, 2000; Watts et al., 2001; Mitchell et al., 2004). In fact, many of these methods are technically similar to some assimilation schemes (Optimal Interpolation-like), with the difference that the first guess used, i.e. the background analysis, is given by an average over the observations instead of a numerical model forecast. The error associated to this analysis thus represents the actual system variability. In essence, most statistical methods are based on the analysis of covariance relative to a set of in situ data profiles and on the identification of the principal modes characterizing the latter. However, the





accuracy of each technique depends on the choice of the variables characterizing the

1054

state of the system, as well as the number of degrees of freedom which each method absorbs (e.g. Buongiorno Nardelli and Santoleri, 2004).

Univariate techniques such as single EOF *(Empirical Orthogonal Function)* Reconstruction analyze the principal components of each parameter along the water column

- and hypothesize a relationship between the amplitude of such components and a (not necessarily linear) combination of surface parameters (Carnes et al., 1994). Simpler methods, as the one used within ARMOR3D, assume a direct correlation between surface and deep values (Guinehut et al., 2012). The new methods considered within MESCLA are based on multivariate approaches (*Coupled Pattern Reconstruction*-
- ¹⁰ *CPR; multivariate EOF Reconstruction, mEOF-r*). These methods analyze the steric height, temperature and/or salinity covariance and reconstruct the vertical profiles via a combination of a limited number of modes. Following an idea first proposed by Pascual et al. (2003), they include an approximation of the geopotential streamfunction (the steric height profile) in the status vector, thus more directly correlating physical-
- chemical parameter variability to dynamics. The application of these methods already yielded promising results, also compared to empirical methods such as the computation of the Gravest Empirical Modes (Buongiorno Nardelli and Santoleri, 2005).

Within MESCLA a double approach has thus been followed to improve the resolution of the observation-based 3-D fields. The two approaches involve different levels of complexity and might be considered as potential successive store in a gradual im-

of complexity and might be considered as potential successive steps in a gradual improvement of operational products. As a first step, the algorithm used to obtain the MyOcean ARMOR3D product has been adapted to ingest higher resolution SST data. Then mEOF-R technique has then been adapted and tested on a subset of input data.

4.1.1 Increasing ARMOR3D spatial resolution

The combined ARMOR3D product is computed every week (Wednesday fields) on a 1/3° Mercator horizontal grid, which corresponds to the altimeter SLA grid and from the surface down to 1500-m depth on 24 vertical levels. ARMOR3D method, thoroughly described in Guinehut et al. (2012) this same volume, consists in the improvement of





a climatological first guess using two main steps. At first, synthetic temperature (T) profiles are estimated by extrapolating altimeter and SST data through a multiple linear regression method and covariances computed from historical data. For synthetic salinity (S) profiles, the method uses only altimeter data. Successively, the synthetic profiles (hereafter referred to as *synthetic ARMOR3D* fields) are combined with in situ temperature and salinity profiles using an optimal interpolation method (Bretherton et al., 1976). These fields will be hereafter referred to as *combined ARMOR3D*.

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As a preliminary step, ARMOR3D performs some crucial processing of altimeter data, being able to extract the steric contribution to the sea level variations consistent with the first 1500-m depth (filtering out the eustatic component and the deep steric contribution). This pre-processing is based on regression coefficients deduced from an altimeter/in situ comparison study (Guinehut et al., 2006; Dhomps et al., 2011).

In the present work, the three SST products described in Sect. 2 have been used to test the impact of SST resolution on the synthetic *T* field estimation (step one of the method). Additionally, the use of MESCLA experimental HR SSS fields has also been tested for the reconstruction of the synthetic salinity. While the synthetic ARMOR3D

salinity fields is obtained with a simple linear regression to altimeter SLA, the method has been modified to a multiple linear regression method (as for temperature) to include also the information from SSS.

In order to take into account the higher resolution of the different SST fields two main sets of tests have been performed, from which higher resolution ARMOR3D-MESCLA experimental products have been obtained. The first one consisted in estimating the 3-D fields using the new SST input on the core 1/3° Mercator horizontal grid. These tests required the remapping of each SST product on the 1/3° grid (i.e. sub-sampling), which

²⁵ was performed using a bilinear interpolation of the four nearest points. The second test consisted in computing the 3-D field on each SST native grid (1/4°, 1/10° and 1/20°, respectively). The latter required the computation of the altimeter SLA grid on each SST grid (i.e. upsizing/interpolating the original data). Actually, upsizing has to be performed with particular care in order not to introduce spurious signal. After having





tested different methods (simple bilinear interpolation, Akima spline), a classical spline method has been chosen.

4.1.2 mEOF-Reconstruction

The multivariate EOF reconstruction (mEOF-R) technique is based on the analysis of the "multicoupled" variability of salinity, temperature and steric height profiles through a multivariate EOF decomposition and on the availability of corresponding surface values (Buongiorno Nardelli and Santoleri, 2005).

Here, we will briefly recall how mEOF-R works. A single $3m \times n$ multivariate observation matrix **X** is obtained from the three original sets of data, each of $m \times n$ dimen-

sions, where *n* is the number of measurements (stations) and *m* the number of vertical levels. Data are preliminarily normalized dividing each parameter by its standard deviation (computed for the whole profile). Mean profiles estimated from the whole training dataset are removed in order to obtain anomalies and estimate the covariances. The columns of this matrix consist of the three normalized profiles of *T*, *S* and SH anoma lies, each taken at the same location.

 $\mathbf{X} = \begin{bmatrix} T(0, r_1) & T(0, r_2) & \dots & T(0, r_n) \\ \vdots & \vdots & \dots & \vdots \\ T(z_m, r_1) & T(z_m, r_2) & \dots & T(z_m, r_n) \\ S(0, r_1) & S(0, r_2) & \dots & S(0, r_n) \\ \vdots & \vdots & \dots & \vdots \\ S(z_m, r_1) & S(z_m, r_2) & \dots & S(z_m, r_n) \\ SH(0, r_1) & SH(0, r_2) & \dots & SH(0, r_n) \\ \vdots & \vdots & \dots & \vdots \\ SH(z_m, r_1) SH(z_m, r_2) & \dots & SH(z_m, r_n) \end{bmatrix}$

To compute the multivariate EOF, the Singular Value Decomposition of this new matrix of data is performed. In that way, "multi-coupled" modes are identified, each containing





the three patterns corresponding to the parameters considered. T(z, r), S(z, r) and SH(z,r) can thus be expanded in terms of these three series of patterns. The same coefficient/amplitude (a_k) is found for all parameters, L_k , M_k and N_k being the modes:

$$S(z, r) = \sum_{k=1}^{n} a_k(r) M_k(z)$$
$$S(z, r) = \sum_{k=1}^{n} a_k(r) M_k(z)$$
$$T(z, r) = \sum_{k=1}^{n} a_k(r) L_k(z)$$

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If these expansions are limited to the first three modes, the vertical profiles can be estimated from the surface values (z = 0) of the three parameters solving the system for a_1 , a_2 and a_3 and substituting them in the truncated expansions:

 $\begin{cases} a_1(r)L_1(0) + a_2(r)L_2(0) + a_3(r)L_3(0) = T(0, r) \\ a_1(r)M_1(0) + a_2(r)M_2(0) + a_3(r)M_3(0) = S(0, r) \\ a_1(r)N_1(0) + a_2(r)N_2(0) + a_3(r)N_3(0) = SH(0, r) \end{cases}$

Of course, it is also possible to truncate the expansions to the second mode, which actually means that only two surface parameters are sufficient to retrieve the whole profiles. Similarly, the whole analysis can be performed directly on two sets of parameter.

The mEOF-R method requires a training dataset of T, S and SH profiles to extract the main vertical modes of (co)variability. This training dataset might be selected differently at each grid point on the basis of different criteria: fixing a space and/or time search radius (e.g. 1000, week, month, year), keeping only the nearest n profiles, etc. Depending on this choice, one may end up with different reconstruction models (i.e.





different mEOFs) for each grid point or with a single set of modes. After some preliminary hindcast tests (not shown), it was decided to select all the profiles collected in the domain within a monthly window. Given the sparse, even though regular, distribution of data in the *training* set, this was found to be the simplest but also most reliable way to setimate EOFs.

Similarly to the pre-processing performed by ARMOR3D, in order to retrieve the 3-D vertical fields from surface data, a preliminary step is to estimate/extract the surface steric heights from satellite altimeter data. Actually, as there is no way to evaluate the deeper baroclinic and the barotropic contributions from altimeter data and surface measurements alone, in a simple approximation, this estimation is reduced here to an adjustment of the ADT to minimize the differences between the steric height computed from simultaneous (or quasi-simultaneous) in situ profiles and co-located ADT estimates (through a simple regression). Differently to Guinehut et al. (2012), this adjustment has been performed here considering weekly matchups. The in situ *T/S* profiles described in Sect. 2 were re-interpolated at 10 dbar resolution down to 1000 dbar, and

steric height profiles were obtained taking 1000 dbar as reference pressure level. These data have been used as training dataset, while altimeter ADT data ODYSSEA SST L4 and MESCLA SSS L4 data were used as surface input in the test of the mEOF-R technique.

20 4.2 Vertical velocity estimation

Relatively intense vertical exchanges in the oceans are associated to the mesoscale structures. Nevertheless, vertical velocities are generally lower by a factor up to 10⁴ than horizontal ones, and consequently they are not easily measured through direct observations (e.g. Klein and Lapeyre, 2009; Frajka-Williams et al., 2011). Various in-²⁵ direct methodologies have thus been proposed to estimate vertical velocity from observed density and geostrophic velocity fields. Though more complicated techniques such as the semi-geostrophic Omega equation (Viudez and Dritchel, 2004) have been proposed, the most used technique is based on the solution of the quasi-geostrophic





(QG) Omega equation (e.g. Tintoré et al., 1991; Buongiorno Nardelli et al., 2001; Pascual et al., 2004; Ruiz et al., 2009), which has already been shown to give reasonable estimates of the vertical velocities compared to primitive equation models (Pinot et al., 1996).

In this work, the algorithm for the solution *Q* vector formulation of the Omega equation (as originally developed at IMEDEA) was adapted to the specific products that are used/developed within MESCLA project. Actually, the Omega equation requires in input both the geostrophic field and the density stratification. The geostrophic currents have been estimated referencing the thermal wind estimates to the absolute surface altimeter velocities (when applied to observation-based products). Two reference levels for dynamic height computation are considered for models: the surface and 1000 m depth. The code is derived from the QG vorticity and thermodynamic equation (Hoskins et al.,

1978): $\nabla^2 \left(N^2 w \right) + f^2 \frac{\partial^2 w}{\partial z^2} = 2\nabla \cdot Q$

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 $\boldsymbol{Q} = \left[f\left(\frac{\partial V}{\partial x} \frac{\partial U}{\partial z} + \frac{\partial V}{\partial y} \frac{\partial V}{\partial z} \right), -f\left(\frac{\partial U}{\partial x} \frac{\partial U}{\partial z} + \frac{\partial U}{\partial y} \frac{\partial V}{\partial z} \right) \right]$

where (U, V) are the geostrophic velocity components, N is the Brunt-Väisälä frequency and f the Coriolis parameter. In this implementation, N only depends on depth. Different boundary conditions have been tested (i.e. Dirichelet and Neumann conditions), however, given the elliptic nature of the Omega equation, no significant differences were found a few grid points away from the boundaries in the two cases.



5 Results

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5.1 Preliminary hindcast evaluation of the mEOF-R methods

Various mEOF-R products obtained from different configurations have been compared, and a first estimate of their accuracy has been estimated through a hindcast validation.

⁵ This means that the surface values of the in situ profiles used as training datasets were taken as input data for the reconstruction. The hindcast errors were thus estimated as the mean and standard deviation of the differences between the vertically reconstructed (synthetic) profiles and the original measurements. The advantage of this kind of validation is given by the large number of profiles available, while the disadvantage clearly resides in the fact that hindcast is not an independent validation, as

the same data are used to train and test the method.

The hindcast validation was applied to the mEOF-R configurations listed below:

- 1. mEOF-r(*T*-*S*-SH). The mEOFs are computed from *T*, *S* and SH profiles and corresponding synthetic profiles are obtained using SST, SSS and SSH as input data (the amplitude of the first 3 modes is retrieved).
- 2. mEOF-r(*T*-*S*-SH)_{SST-SSH}. The mEOF are computed from *T*, *S* and SH profiles and corresponding synthetic profiles are obtained using only SST and SSH as input data (the amplitude of the first 2 modes is retrieved).
- 3. mEOF-r(*T*-*S*-SH)_{SSS-SSH}. The mEOF are computed from *T*, *S* and SH profiles and corresponding synthetic profiles are obtained using only SSS and SSH as input data (the amplitude of the first 2 modes is retrieved).
- 4. mEOF-r(*T*-SH). The mEOF are computed from *T* and SH profiles only, and corresponding synthetic profiles are obtained using SST and SSH as input data (the amplitude of the first 2 modes is retrieved).





5. mEOF-r(*S*-SH). The mEOF are computed from *S* and SH profiles only, and corresponding synthetic profiles are obtained using SSS and SSH as input data (the amplitude of the first 2 modes is retrieved).

Mean Bias Error (MBE) and Standard Deviation Error (STDE) profiles for both temperature and salinity are shown in Fig. 1a and b, respectively. It is interesting to observe that the synthetic mEOF-r MBE is generally quite small. The mEOF-r provides the smallest STDE errors when only two modes are considered, both in the trivariate formulation and in the bivariate one.

A simple explanation for this may be given by analyzing the mEOF modes (Fig. 2) and corresponding explained covariance percentage. Similarly to what was found by Buongiorno Nardelli et al. (2006), the first mode is almost certainly driven by the quasigeostrophic dynamics, as the SH pattern closely resembles the typical shape of the first baroclinic mode. However, even if this first mode explains an extremely high percentage of the variance (almost 99%), while only about 0.3% of it is explained by the second mode, some important information is still contained in the second mode. In fact, we also run a single mode mEOF(*T*-*S*-SH) reconstruction (both for temperature and salinity)

- run a single mode mEOF(T-S-SH) reconstruction (both for temperature and salinity) which gave much worse results than the mEOF-r in the two mode configurations (see Fig. 3). Actually, T and S patterns in the first mEOF mode have the same sign, meaning that the surface anomalies with respect to the mean profile driven by this mode reflect
- down to the deep layers. On the opposite, the second mode basically accounts for the presence of *T* and *S* anomalies only in the upper layers, which might, for example, be related to the presence/absence of waters of coastal/riverine origin. More investigations will be needed to better understand which process drives the variability of this second mode. Meanwhile, it is clear that the third mode is related to conditions that apply to an
- extremely low number of profiles. Adding it to the reconstruction, in fact, leads to typical errors associated with an over-fitting of the data. Only the best performing techniques, as evaluated with the previous hindcast validation, have been applied to the SST, SSS and adjusted ADT maps. The selected techniques are the mEOF-r(*T*-*S*-SH)_{SST-SSH} and mEOF-r(*T*-*S*-SH)_{SSS-SSH}.





5.2 Combined ARMOR3D, synthetic ARMOR3D and mEOF-R comparison

A preliminary evaluation of the accuracy of combined and synthetic standard ARMOR3D products, new high resolution synthetic ARMOR3D products and new mEOF-R has been roughly estimated via a weekly matchup comparison, which means

- that the in situ profiles collected in a temporal range of ± 3 days (weekly matchups) have been taken aside as an independent test dataset, and have been compared with the co-located profiles obtained with the different reconstruction methods. The same matchup has been applied to eight different versions of the ARMOR3D product (see Sect. 4.1.1), as listed below:
- 10 1. Combined ARMOR3D (MERCATOR 1/3° grid),
 - 2. Synthetic ARMOR3D (MERCATOR 1/3° grid sub-sampled Reynolds SST),
 - 3. Synthetic ARMOR3D (MERCATOR 1/3° grid sub-sampled Odyssea SST),
 - 4. Synthetic ARMOR3D (MERCATOR 1/3° grid sub-sampled OSTIA SST),
 - 5. Synthetic ARMOR3D (Reynolds SST on original 1/4° grid),
- 6. Synthetic ARMOR3D (Odyssea SST on original 1/10° grid),
 - 7. Synthetic ARMOR3D (OSTIA SST on original 1/20° grid),
 - 8. Synthetic ARMOR3D (MESCLA HR SSS on original 1/10° grid).

The matchup comparison has the advantage of starting from fully independent surface input data, but the number of in situ profiles available within this weekly window was also quite low (actually, 13 matchups were found, see Fig. 4), so that the estimated MBE and STDE may only give an indication on the methods' performance, while a longer test period should be used to get a real validation. Moreover, the estimated difference can possibly also be affected by the temporal variability at scales shorter than 3 days, which might not be negligible in rapidly evolving frontal areas.





The results of the weekly matchup comparison are summarized in Fig. 5. As the differences between the various synthetic ARMOR3D profiles resulted to be practically negligible, we kept only the profiles relative to the synthetic ARMOR3D computed from the Odyssea L4 on its original grid, which displayed very slightly lower matchup differ-

- ⁵ ences than the others, and the profiles relative to the synthetic ARMOR3D including MESCLA HR SSS in input. This also allowed to directly compare the mEOF-r and the high resolution ARMOR3D techniques starting from the same input. Conversely, in the combined ARMOR3D, the synthetic profiles are merged with the observed ones via an OI algorithm, so that this comparison cannot be considered particularly relevant, as
- the in situ profiles used to estimate the differences are included in the analysis (the datasets are not independent). Corresponding mean and standard deviation of the differences are displayed anyway in Fig. 5.

At first sight, it seems that the mEOF-r method (limited to 2 modes) provides the more reliable results with respect to the synthetic ARMOR3D estimates, both for temperature reconstruction and for salinity retrieval with a STDE improvement of about 0.1 psu and 0.5 °C in the layer between 50 m and 800 m. However, it has to be noticed that the inclusion of the MESCLA HR SSS as input for the retrieval of salinity in ARMOR3D reduced the STDE in the upper 100 m to values almost comparable to those obtained with mEOFr, though introducing a small bias at the surface.

In addition to the quantitative comparisons presented above, we also made a qualitative comparison between the horizontal patterns of the various synthetic reconstructed fields at depth. As SST field resolution impacts mainly the first few hundred meters of the ocean, input fields (SLA/ADT and SST) and deep structures at 100 m depth are compared. When computed on the 1/3° Mercator grid, the new experimental AR-MOR3D temperature synthetic fields are very similar using any of the three SST as

input. When computed on each of the original SST grids, the synthetic fields display stronger differences (Fig. 6a). They show the smallest scale structures using Odyssea SST. Conversely, results are very similar at 100 m using Reynolds (either on the original 1/4° SST grid, or on the 1/3 Mercator ARMOR3D grid (not shown), since the two





grids have very similar resolution at these latitudes) and Ostia SST, as Ostia SST effectively resolves structures at much larger scales than its nominal resolution (1/20°). Similarly, the mEOF-R temperature fields at depth present quite different and smaller scale structures with respect to those obtained with the synthetic ARMOR3D prod-

- ⁵ ucts calculated from Reynolds and OSTIA. mEOF-r temperature at 100 m also displays slightly smaller scale structure and more intense gradients than those from synthetic ARMOR3D Odyssea. Concerning the salinity field, it has to be stressed that MESCLA HR-SSS and the ARMOR3D SSS fields computed from the first guess and covariances at the surface between altimeter SLA and salinity are quite different (Fig. 6b). In par-
- ticular, the MESCLA HR-SSS field shows a very sharp gradient along the front of the Gulf Stream with much fresher SSS than those present in the ARMOR3D field. Both the mEOF-r and the ARMOR3D salinity reconstruction methods propagate this sharp gradient and the small scale structures retrieved by MESCLA HR SSS down to 100 m.

5.3 Comparison of the MyOcean model PE and QG vertical velocities

A comparison of the QG-vertical velocities (*qgw*) obtained by applying the Omega equation to Mercator model output with corresponding primitive equation solutions has been performed. The impact of the spatial and temporal resolution on the vertical velocity estimation has been assessed and the sensitivity to the choice of the reference level on the geostrophic and ageostrophic (vertical component) velocities have also been investigated. As for Sect. 5.2, all the plots refer to 100 m depth, which is a particularly interesting level as it corresponds approximately to the base of the euphotic

layer in the Gulf Stream area (Oschlies and Garçon, 1998).

The different dynamic height patterns and corresponding Omega estimates show a high sensitivity, both in terms of shape and intensity, to the spatial resolution of the model (Fig. 7). Vertical velocities obtained from the 1/12° (PSY2w) model (Fig. 7c–

²⁵ model (Fig. 7). Vertical velocities obtained from the 1/12° (PSY2w) model (Fig. 7c– d) are a factor of 2–3 larger than the 1/4° (PSY3w) (Fig. 7a–b) version (maximum upward and downward velocities of the order of 40–60 m day⁻¹ vs. 20–30 m day⁻¹, respectively). On the other hand, the comparison between PE and QG vertical velocities





shows a reasonable agreement in both model simulations, even if model QG's values underestimate the PE velocities at low resolution (Fig. 7). These differences can be better quantified looking at the scatter plot and computing correlation coefficients, as displayed in Fig. 8 (similar results were also found for deeper layers, not shown). In fact, QG velocities displayed maximum upward and downward values of the order of $40-60 \text{ m day}^{-1}$ and $10-15 \text{ m day}^{-1}$, in the high resolution and low resolution tests, with correlation with PE (Pearson coefficient) reaching almost 0.8 and 0.7, respectively.

The results indicate that resolution is a key factor in the estimate of the vertical component of the ageostrophic velocity through the quasi-geostrophic omega (compared to

PE estimates). If sufficient resolution is kept, velocities are more correctly reproduced even in the quasi-geostrophic approximation and, even though the patterns in the QG solution may slightly be smoother, the estimated values compare reasonably well. In the following, the QG method will thus be applied to the observation-based experimental 3-D products, providing a fully observational estimate of the vertical velocities over the Gulf Stream area.

5.4 Vertical velocities estimates from experimental 3-D products

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Similarly to what was found for the tracer fields in Sect. 5.2, very similar *qgw* estimates were obtained from the synthetic experimental ARMOR3D using the SST L4 sub-sampled on the 1/3° Mercator grid (not shown). Conversely, vertical velocity intensity increased significantly when experimental synthetic ARMOR3D fields were computed on the (higher) original SST grid resolution and with mEOFr. A qualitative com-

- parison of the vertical velocities retrieved by applying the Omega equation to the synthetic ARMOR3D products (listed as 4–8 in Sect. 5.2) and mEOF-r field is thus illustrated in Fig. 9. The lowest velocities were estimated from the synthetic ARMOR3D
- ²⁵ using the Reynolds L4 SST (peak qgw ~32 m day⁻¹, horizontal velocities peak ~1.5 m s⁻¹). Coherently with the findings of the Sect. 5.2, synthetic ARMOR3D qgw from OSTIA, though having the highest nominal resolution, do not display the highest average and peak velocities, though they are still significantly higher than those obtained





from Reynolds (peak $qgw \sim 52 \text{ m day}^{-1}$, peak horizontal velocities $\sim 1.7 \text{ m s}^{-1}$). Slightly higher values were computed from synthetic ARMOR3D using Odyssea SST, with peak qgw values of $\sim 54 \text{ m day}^{-1}$ and peak horizontal velocities of $\sim 1.7 \text{ m s}^{-1}$. The most intense velocities, however, were estimated from the two products using both Odyssea

- SST and MESCLA SSS in input, with *qgw* peak values of 58 m day⁻¹ and 66 m day⁻¹ in the synthetic ARMOR3D and mEOFr, respectively. More pronounced differences in both the geostrophic velocities and vertical velocity structures are found along the main Gulf Stream jet, where the mEOF-r field displays higher values than synthetic AR-MOR3D. More investigations on the observed differences and on the dynamical anal-10 ysis of the three-dimensional velocity fields retrieved from these observation-based
- products is beyond the scope of the present paper and left for future studies.

6 Conclusions

While several operational systems have demonstrated the importance of assimilating observations in high resolution numerical models to better simulate the ocean dynamics at mesoscale (e.g. Stammer et al., 2010, and references therein), a purely observation-based approach, aiming to retrieve the 3-dimensional structure of the oceans at mesoscale from a combination of in situ and satellite observations, has received until now only a limited recognition. This is most probably related to the general tendency to look at the observations as a source of information for the retrieval of a

- single parameter at a time. Conversely, different multivariate approaches have been proposed until now to retrieve 3-D fields of temperature and salinity, even though very few of these translated into operational products (e.g. Fox et al., 2002; Guinehut et al., 2004, 2012). However, while data assimilation in numerical models is crucial to obtain more accurate analyses and forecasts, its results might be influenced by specific model
- ²⁵ configurations (e.g. forcing, parameterization of small scale processes and spatial resolution). The availability of high resolution observation-based 3-D fields might thus help in model validation through more advanced comparisons than those based on simple





climatologies or sparse observations of temperature, salinity or velocities. On the other hand, the limits of present observation-based products are correctly identified in their relatively low resolution and by the difficulties to provide any estimate of the ocean currents beyond the geostrophic approximation.

- ⁵ Within the MyOcean R&D project MESCLA, a step towards a more efficient combination and more complex analysis of existing observations has been made. MESCLA tested innovative methods for the high resolution mapping of 3-D mesoscale dynamics from a combination of in situ and satellite data (as described in Sect. 4.1), developing new products that might be used as prototypes to gradually build the next generations of operational observation-based products. In order to demonstrate the new tech-
- tions of operational observation-based products. In order to demonstrate the new techniques' potential, different estimates of the vertical velocities derived from different 3-D synthetic fields through a quasi-geostrophic diagnostic model have been compared (Sect. 5). Resolution confirmed to be an important factor for the retrieval of the currents. However, even in the limits of a simplified dynamical framework, and knowing
- that most of the analysis could not necessarily go beyond a simple qualitative comparison (vertical velocities cannot be measured directly at sea), realistic estimates of the vertical field could be retrieved, at least as compared to those diagnosed through primitive equation numerical models. The ocean observation-based products tested within MESCLA might thus open a wide range of possible applications for both Operational Ope
- ²⁰ Oceanography and Ocean Climate Monitoring studies.

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Table 1. Description of the L4 SST products used.

SST	Spatial Res.	Time series available	Sensors	Method
Reynolds HR AVHRR- AMSR	1/4°	Since 2002/06/01	AVHRR + AMSR + in situ observations	Bias correction, Sea ice to SST conversion algo- rithm, First guess = previ- ous analysis (Reynolds et al., 2007)
Ostia	1/20°	Since 2006/01/01	AATSR (Envisat), AMSR- E (Aqua), AVHRR-LAC (NOAA 17 & 18), AVHRR- GAC (NOAA 18), InSitu observations, Sea ice, primarily SSM/I (DMSP), SEVIRI (MSG1), TMI (TRMM).	Bias correction, First guess = previous analysis (Donlon et al., 2011)
Odyssea	1/10°	From 2007/10/01 to 2009/11/23	AATSR, AVHRR (NOAA 17 & 18), GOES/VISSR, MSG-1/SEVIRI; AMSRE, TMI	Sampling or averaging, First guess: reference daily climatology (Autret and Piollé, 2007)



Discussion Paper

Discussion Paper

Discussion Paper

Discussion Paper













Fig. 2. Trivariate (*T*-*S*-SH) mEOF modes.





Fig. 3. Hindcast temperature and salinity mean bias errors (blue) and standard deviation errors (red) when using only the first mode in the mEOF-r trivariate reconstruction.







Fig. 4. Matchups location superimposed on 17 October 2007 Odyssea SST L4.







Fig. 5. Mean (dotted lines) and standard deviation (solid lines) of the difference between: – in situ temperature profiles and corresponding data from mEOF-r and combined ARMOR3D (a); in situ temperature profiles and corresponding data from mEOF-r and synthetic ARMOR3D using Odyssea SST (b); – in situ salinity profiles and corresponding data from mEOF-r and combined ARMOR3D (c); in situ salinity profiles and corresponding data from mEOF-r and synthetic ARMOR3D on Odyssea SST grid (d); in situ salinity profiles and corresponding data from mEOF-r and synthetic ARMOR3D using MESCLA SSS (e).















Fig. 6b. SSS and salinity at 100 m from the three reconstruction methods selected (see details in the text). The color scale range from 30 to 37, every 0.2 for the SSS and from 31 to 37, every 0.2 for the S at 100 m.







Fig. 7. Vertical velocity fields at 110 m as obtained from primitive equation and quasigeostrophic Omega equation for PSY3 ($1/4^{\circ}$) and PSY2 ($1/12^{\circ}$) Mercator models.













mEOF-r fields.