Ocean Science Discussions

Evaluating two numerical advection schemes in HYCOM for eddy-resolving modelling of the Agulhas Current

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Abstract

A 4th order advection scheme is applied in a nested eddy-resolving Hybrid Coordinate Ocean Model (HYCOM) of the greater Agulhas Current system for the purpose of testing advanced numerics as a means for improving the model simulation for eventual
⁵ operational implementation. Model validation techniques comparing sea surface height variations, sea level skewness and variogram analyses to satellite altimetry measurements quantify that generally the 4th order advection scheme improves the realism of the model simulation. The most striking improvement over the standard 2nd order momentum advection scheme, is that the Southern Agulhas Current is simulated as a
¹⁰ well-defined meandering current, rather than a train of successive eddies. A better vertical structure and stronger poleward transports in the Agulhas Current core contribute toward a better southwestward penetration of the current, and its temperature field, implying a stronger Indo-Atlantic inter-ocean exchange. It is found that the transport, and hence this exchange, is sensitive to the occurrences of mesoscale features origi-
¹⁵ nating upstream in the Mozambique Channel and Southern East Madagascar Current, and that the improved HYCOM simulation is well suited for further studies of these inter-actions.

1 Introduction

Modelling of the greater Agulhas Current regime, in particular of the very energetic
²⁰ retroflection region, is challenging. Ocean circulation models usually simulate the Southern Agulhas Current as a train of large eddies extending from the Agulhas Plateau to the retroflection, rather than a continuous, well-defined current (e.g. Barnier et al., 2006; Backeberg et al., 2008). Consequently the simulated dynamics in the retroflection area with the periodic shedding of Agulhas Rings and maintenance of the
²⁵ return flow may be hampered.

Advances in model development, combined with more adequate model validation

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is necessary to limit this deficiency. In essence there are three ways in which ocean models can be improved (Bleck, 2006), notably by: increasing the model resolution, incorporating better model physics and implementing more adequate model numerics. Increasing the grid resolution would, in theory, allow the numerical solution to resolve finer scales. But at the border between resolved and unresolved scales of motion, the interaction of physical processes needs to be parameterised, and therefore truncation errors continue to be problematic. Improving the model physics implies better parameterisation of the physical processes which are not resolved in the model grid. Improving the model numerics, as with higher grid resolution, would lower the truncation error of the finite difference scheme used in the ocean model.

There are several ways in which model numerics can be improved. One approach is to transform the finite difference equations into a coordinate system so that they become easier to solve, and as a result the accuracy of the solutions may be improved. This approach has been adopted in isopycnic coordinate models such as the Miami Isopycnic Coordinate Ocean Model (MICOM; Bleck and Smith, 1990). In the case of isopycnic coordinate models, potential density has become the independent variable, instead of depth, which is used in Cartesian coordinate models. The advantage of using potential density as the vertical coordinate is that adiabatic flow, which is 3-dimensional in Cartesian space, becomes 2-dimensional in potential density space. This makes it easier to satisfy adiabatic constraints of temperature and salinity when estimating their lateral flow. There are two main disadvantages of having potential density as the vertical coordinate. Firstly, what is known as the outcropping problem, isopycnic coordinate surfaces intersect the sea surface and secondly, there is a lack of vertical resolution when simulating unstratified water columns. The Hybrid Coordinate Ocean Model (HYCOM; Bleck, 2002) was developed to combat these problems. It does so by reverting to fixed-depth (z-level or bottom-following) coordinates in unstratified waters, and when outcropping occurs, the layer thickness tends to zero but remains isopycnal in nature.

Model numerics may also be improved by applying higher-order finite difference ap-

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proximations. This would reduce the truncation error, much like increasing the model grid resolution, but at a lower computational cost (Sanderson, 1998). One such scheme is the quadratic upstream interpolation for convective kinematics (QUICK; Leonard, 1979). It was shown that implementing the QUICK scheme in realistic applications of

5 ocean models generally improves their realism (Webb et al., 1998). In particular, in a case study for the Agulhas Current, where the QUICK scheme was applied to both tracer and momentum advection, the narrow, warm Agulhas Current core was significantly improved, resulting in a much better southwestward penetration of the temperature field, a deficiency noted in an application of HYCOM to the greater Agulhas Current

10 system (Backeberg et al., 2008).

Depending on the process of interest, it is not necessary to approximate all terms to the higher-order (Sanderson, 1998). Studies have shown that applying the 4th order scheme only to momentum advection improves the potential vorticity dynamics and conservation (e.g. Morel et al., 2006; Winther et al., 2007). Winther et al. (2007)

15 conclude that with model grid spacing which is smaller than the Rossby radius of deformation, higher-order approximation need only be applied to the momentum scheme in order to yield beneficial results. An application of HYCOM for the Agulhas Current has been thoroughly evaluated in Backeberg et al. (2008). It was concluded that the simulation, using a second order momentum advection scheme, provided an adequate

20 representation of the general circulation and mesoscale variability for the region, although some inaccuracies were recognised. Notably, a train of eddies extending from the Agulhas Plateau to the retroflection, instead of a well-defined current core.

Barnier et al. (2006) in their experiments with NEMO argue for a stronger focus on improving model numerics, rather than increased resolution, as a means to improve

25 the realism of ocean general circulation models (OGCM). In particular they highlight the numerical treatment of momentum advection and as one of the key factors for advancing the development of eddy permitting ocean models. In light of this, the QUICK scheme (4th order, hereafter referred to as O4) was applied to momentum advection in the Agulhas HYCOM, and compared to the 2nd order advection scheme (hereafter

referred to as O2). A similar study using a high resolution model of the North Sea is documented in Winther et al. (2007). In the Agulhas Current, the regular availability of data, in particular satellite altimetry data, supports a more detailed statistical study, using skewness and spatial variograms. Although these statistical tools are very simple and classical, their use in oceanography is still marginal. We will show that they are selective tests for model validation.

Applying and validating model improvements provides a better quantitative understanding of the role and influence of mesoscale variability and dynamics in the Agulhas Current and hence the retroflection region with its frequency of eddy shedding is obtained. Advancing the knowledge of this mesoscale variability and dynamics will in turn yield better grounds for model validation, which is essential in order to gradually progress towards establishing and implementing an operational monitoring and forecasting system for the greater Agulhas Current regime.

A description of the observations and model is outlined in Sect. 2, followed by a qualitative assessment of the two simulation experiments (Sect. 3). Mesoscale variability is studied in both simulations (Sect. 4), and compared to satellite altimetry measurements considering sea surface height variations (Sect. 4.1), sea level skewness (Sect. 4.2) and variogram analyses (Sect. 4.3). The main findings of the inter-comparisons are summarised in the conclusion.

2 Description of observations and model

2.1 Satellite altimetry

The satellite altimetry data is a very important global data set for ocean circulation studies as well as validation of models. It spans a period of more than 15 years and provides measurements of sea surface height variations or sea level anomalies (SLA) at a spatial and temporal scale of about 40 km and 7 days. This is adequate for the Agulhas Current, where the mesoscale signals are very distinct.

The absolute dynamic topography is the sum of SLA and the mean dynamic topography from Rio05 (Rio and Hernandez, 2004; Rio et al., 2005). These data are available from Ssalto/Duacs and distributed by Aviso, with support from the Centre National d'Etudes Spatiales (CNES; www.aviso.oceanobs.com).

Recently Aviso has developed better algorithms for data retrieval in coastal areas, where the measurement corrections are more demanding. This is very valuable for studies of the Agulhas Current, which flows very close to the coast between 30–34° S.

2.2 Sea surface temperatures (SSTs)

Reynolds SSTs (Reynolds et al., 2002) are produced weekly on a one degree grid by the Climate Diagnostic Centre. The data are optimally interpolated, incorporating in situ and satellite SSTs and are adjusted for sea-ice cover. Before the analysis the satellite data are bias-corrected using the method described in Reynolds (1988) and Reynolds and Marsico (1994).

The Reynolds SST data is provided by the NOAA/OAR/ESRL PSD, Boulder, Colorado, USA, and is available freely from their Web site at www.cdc.noaa.gov.

More recently, with the launch of NASA's AQUA satellite, higher resolution ($\sim$25 km) near-global SST data have become available on a daily basis. These are obtained by interpolating SST measurements from the Tropical Rainfall Measuring Mission (TRMM) Microwave Imager (TMI) and the Advanced Microwave Scanning Radiometer for EOS (AMSR-E, onboard AQUA). For these sensors, missing data only occurs in regions near land or where they are influenced by sun-glitter and rain. Although these microwave SST products (hereafter referred to as MW SST) have a lower spatial resolution than full SST measurements from infrared sensors, they represent a significant improvement over the widely used weekly, one degree ($\sim$100 km) NCEP OI (Reynolds) SST product.

Microwave OI SST data are produced by Remote Sensing Systems and sponsored by National Oceanographic Partnership Program (NOPP), the NASA Earth Science Physical Oceanography Program, and the NASA REASoN DISCOVER Project. The

MW SSTs are available at www.remss.com.

2.3 Hybrid Coordinate Ocean Model (HYCOM)

The Hybrid Coordinate Ocean Model (HYCOM) is a primitive equation model, that combines the optimal features of isopycnic-coordinate and fixed-grid ocean circulation models within one framework (Bleck, 2002).

At each time-step HYCOM determines an optimal hybrid layer distribution, interchanging between isopycnic (ρ) vertical coordinates when simulating the stratified open ocean, z-level coordinates when resolving upper-ocean mixed layer dynamic processes and σ-coordinates in the shallow coastal regions. During these vertical coordinate interchanges, emphasis is placed on restoring the grid to isopycnic coordinates.

The HYCOM system set up to simulate the Agulhas Current system involves two models: a coarse resolution, basin-scale model of the Indian and Southern Oceans, which provides boundary conditions for a regional nested high-resolution model of the Agulhas Current system (Fig. 1).

The model grids were created using the conformal mapping tool developed by Bentsen et al. (1999). Realistic ocean bathymetry data, from the 1' resolution General Bathymetric Chart of the Oceans (GEBCO; www.ngdc.noaa.gov/mgg/gebco) was interpolated to each of the model grids.

A $\frac{1}{10}$ of a degree model of the Agulhas Current system (AGULHAS) receives boundary conditions from the coarser model (INDIA) in a one way nesting approach. For the slow varying variables such as baroclinic velocity, temperature, salinity and layer interfaces, the boundary condition calculations are based on the flow relaxation scheme (FRS; Davies, 1983). The barotropic variables are treated in a hyperbolic wave equation for pressure and vertically integrated velocities (Browning and Kreiss, 1982, 1986).

The geographical domain of AGULHAS extends from 0°–60° E and from 10°–50° S, to include the major features of the Agulhas Current system, namely the source regions, the Mozambique Channel and the East Madagascar Current, the Agulhas Current proper, the Agulhas Retroflection, the ring shedding corridor and the Agulhas Re-

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turn Current.

The vertical discretisation in AGULHAS mimics that of INDIA. It has 30 hybrid layers with target densities ranging from 21.0 to 28.3, referenced to σ_0.

INDIA was initialised from Generalised Digital Environmental Model (GDEM; Teague et al., 1990) data, and a spin-up period of 8 years using monthly mean climatological forcing was run to allow it to reach a balanced state prior to beginning the simulation experiments. The forcing data used during the spin-up period is based on the ERA40 re-analysis (Uppala et al., 2005), with a correction applied to dampen the strong precipitation bias of the ERA40 re-analysis in the tropical oceans.

AGULHAS was initialised from a balanced INDIA field interpolated to the high resolution grid.

Two simulation experiments of the nested high resolution model are discussed in this paper. The O2 experiment uses the standard 2nd order advection scheme, while in the O4 experiment a 4th order advection scheme (QUICK scheme; Leonard, 1979) was applied. Both simulations use the same nesting conditions, and in each case the same forcing fields were applied. Namely, synoptic atmospheric forcing fields from ERA40, before 2002 and then operational analyses from the ECMWF, with cloud cover data from the Comprehensive Ocean-Atmosphere Data Set (COADS; Slutz et al., 1985) and precipitation data from Legates and Willmott (1990).

3   Assessment of the simulation results

Figure 2 shows the area averaged mean kinetic energy (MKE; a) and the eddy kinetic energy (EKE; b) for the Agulhas domain.

The simulation study is carried out over a 11-year period from 1996 to 2006, inclusive. Both experiments reveal a rapid increase during the first 2–3 years in MKE (until 1998) and EKE (until 1999). After which they decrease to a stable level in the year 2001. It takes about 1 year longer for the O2 simulation to adjust to its stable state, which in the case of EKE is about $40\,\mathrm{cm}^2.\mathrm{s}^{-2}$ below, or 14% less than that of the

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O4 simulation and the observations.

Both simulations are able to reproduce the inter-annual changes in EKE from 2001 onwards, and the O4 experiment does so in very good agreement to the observed EKE from Aviso. The agreement with the MKE is a bit more sporadic, and both simulations underestimate the overall MKE for the region, although they are able to capture the general changes in the yearly MKE.

When nesting models in regions where strong boundary currents occur, such as the Agulhas Current, a long adjustment time seems to be needed in order to evacuate all the transient modes from the model domain. Further work is needed to address this issue, but does not lie within the scope of this study. For the purposes here, the first 5 years of the simulation are considered to represent the spin-up period. Only the latter period from 2001–2006 will be used in the analysis.

3.1 Mean SST distribution

One of the deficiencies in the O2 model simulation was the extent of the southwestward penetration of the temperature field in the Southern Agulhas Current. Webb et al. (1998) showed that by applying the QUICK scheme to both tracers and momentum a similar deficiency was improved in their simulation experiments. In these experiments with HYCOM, the QUICK scheme was only applied to momentum advection following the arguments by Sanderson (1998).

Figure 3 shows the 3 year mean SSTs (2004–2006, inclusive) from both model simulations, which are compared to the MW SST measurements described in Sect. 2.2.

The contours represent the surface expressions of the extent of the Agulhas Current (20° and 22°C) and the three main frontal regions in the Southern Ocean: the Subtropical Convergence and its northern extent (STC; 14.2° and 17.9°C), the Sub-Antarctic Front (SAF; 7.0°C) and the Antarctic Polar Front (APF; 3.4°C). The surface expressions for the frontal bands were derived from ship-board observations (Lutjeharms and Valentine, 1984).

In general, the agreement between the model and the observations is relatively good

considering that no relaxation toward observed SSTs was applied in the HYCOM simulations. SSTs are very sensitive to localised wind effects, which may not necessarily be represented in the relatively coarse resolution wind forcing used to drive the model. The latitudinal temperature gradient as well as the positions of the frontal bands are in good agreement with the observations. The extent of the Benguela upwelling system is well represented in both model simulations.

The southwestward penetration of the Agulhas Current, as represented by the 20° and 22°C isotherms, extends much further southwestward in the O4 experiment than the in the O2 experiment (Fig. 3). Suggesting a better representation of the Agulhas Current core, but the extent of the southwestward penetration still does not completely agree with the MW SSTs.

In terms of heat transport into the South Atlantic Ocean, the gap between the southern tip of Africa and the 17.9°C isotherm to the southwest is broader in O4, suggesting a significant improvement of the heat flux into the South Atlantic Ocean.

In order to quantify the differences between both model simulations and the SST observations in the retroflection region, weekly data has been averaged for the area 16–21° E and 37–41° S (indicated by the boxes in Fig. 3). The resulting time series were re-gridded to 1°×1° spatial resolution and averaged weekly in the case of the MW-SSTs. The mean and standard deviation are given in Table 1. The area was chosen such that an underestimate of the mean SST reflects a reduced southwestward penetration of the Southern Agulhas Current.

There are some discrepancies between the Reynolds SST and the MW SST (Sect. 2.2). It has been shown that a horizontal resolution the 1°×1° resolution of the Reynolds SST is insufficient to capture the variability of narrow western boundary currents such as the Agulhas Current, and that observations of the Agulhas Current are significantly improved with the MW SSTs (Rouault and Lutjeharms, 2003). Nevertheless, in terms of model validation of SST for long time periods, the Reynolds SST provides a useful data set, especially since the optimally interpolated MW SST only became available in June 2002.

During the period from June 2002 to 2006, there is an average difference of $1.55°C$ between the O2 SST and the Reynolds SST (Table 1), which suggests that the O2 experiment underestimates the southwestward extent of the Agulhas Current significantly. There is a marked improvement in the O4 simulation, which compared to the

5　Reynolds SSTs underestimates the temperatures by only $0.83°C$. Taking into account that the MW SSTs provide better observations of the Agulhas Current, the discrepancy is in fact $2.01°C$ for O2 and $1.29°C$ for O4.

The standard deviation for the O2 simulation is also significantly lower than the observations, 34% lower, and notably is also 17% less than O4, indicating that the 4th

10　order advection scheme improves the variability in the retroflection region.

The improved southwestward penetration of the temperature field in the O4 simulation suggests that the Agulhas Current core is stronger in this simulation experiment. To further investigate this, the vertical structure of the Northern Agulhas Current, where good observations have been made, will be evaluated in the following Section.

15　3.2　The vertical structure of the Northern Agulhas Current

The Agulhas Current near $32°$ S closely follows the narrow continental slope, and is known for its very stable, invariant, flow conditions. Gründlingh (1983) showed that the current, in this northern region, does not meander more than 15 km from its mean path. de Ruijter et al. (1999) in their study of the generation and evolution of Natal

20　Pulses explain that the unusual stability of the current is due to the steepness of the continental slope. Natal Pulses are large cyclonic meanders in the Northern Agulhas Current, which periodically interrupt its stable flow condition.

A year long current meter mooring array was deployed during the World Ocean Circulation Experiment (WOCE; Bryden et al., 1995) southeast of Durban near $32°$ S from

25　February 1995 to April 1996. These measurements provide, to date, the best estimate of the time-averaged volume flux and the vertical structure of the Agulhas Current. Position and depths of the current meter mooring array are summarised in Table 2.

In general the core of the Agulhas Current can be found close to the coast, lying

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within 31 km of the coast 79% of the time. The current penetrates to depths of 2200 m, and at its core, above 100 m, velocities exceeding 100 cm.s^{-1} are observed. The data also indicate that the offshore edge of the Agulhas Current, as determined by the position of the zero isotach, lies 203 km from the coast.

5   In order to compare the HYCOM simulations to the above described data, a section was defined corresponding to the positions of the year long mooring array, extending from the coast at Port Edward to 220 km offshore, and velocities normal to this section were extracted from the model (Fig. 4). The weekly velocities were averaged over a 9 month period and compared to the mean structure described in Bryden et al. (2005),

10   here shown as Fig. 4b.

From the zero isotach in HYCOM O2, the outer edge of the current lies 200 km from the coast, while in HYCOM O4 the current lies closer, between 150–200 km from the coast.

The characteristic V-shaped structure of western boundary currents is much better

15   represented in the O4 simulation, with the maximum current velocity moving away from the coast with depth. In both HYCOM simulations, the current extends all the way to the bottom, with 10 cm.s^{-1} velocities evident at depths of 3000 m. This is deeper than indicated by the observations by Bryden et al. (2005), where according to the zero isotach the current extends to 2200 m, and this is most likely due to a lack of vertical resolution

20   in the model. Importantly, the 20 cm.s^{-1} isotach lies at 1200–1300 m approximately 60–70 km offshore in HYCOM O4, in very good agreement with the observations. The 20 cm.s^{-1} isotach in the O2 experiment only extends to about 800–900 m depths. The 50 cm.s^{-1} isotach can be found at about 400 m depth in both simulations, while it is 300 m deeper in reality.

25   Velocities exceeding 100 cm.s^{-1} above 100 m are evident in both simulations, but are more strongly defined in the 4th order advection scheme. The outer edge of the 100 cm.s^{-1} velocities extend offshore to 50 km compared to 30 km in the O2 simulation. In general this indicates that the current velocities are weaker in the O2 simulation, which has implications in terms of the southwestward penetration of the Agulhas Cur-

rent, which was shown to be reduced in the SST comparison (Sect. 3.1).

Overall, it is clear that the O4 simulations provides a much better representation of the vertical structure of the Agulhas Current in good agreement with the observations. The transports derived from this section will be discussed in relation to the observations in the following Sect. (3.3).

3.3 Transport in the Northern Agulhas Current

Bryden et al. (2005) calculated the time-averaged volume transport, by integrating the velocities from the coast to 203 km offshore and to a depth of 2400 m. The daily transports were averaged over 267 days from 5 March to 27 November 1995 to yield a mean poleward transport of 69.7 ± 21.5 Sv (1 Sv=1×10^6 m^3.s^{-1}).

For the comparison to HYCOM, the weekly transports were calculated across the same section (Fig. 4a) and integrated to a depth of 2400 m. The mean transports and their standard deviations were calculated for HYCOM for the entire period from the beginning of 2001 to the end of 2006, as well as for 9 months of each year, corresponding to the 267 days over which the mooring data transports were calculated (Table 3).

On average, the O2 simulation underestimates the observed poleward volume transport by 21.4 Sv. This is improved in the O4 experiment, where the transports are only 12.2 Sv less than estimated by Bryden et al. (2005), within one standard deviation of the observed mean.

The yearly running mean transports (Fig. 5) of HYCOM O4 oscillate around ~60 Sv, while in HYCOM O2 they decrease by approximately ~20 Sv between 2001 and 2006, indicating that the second order advection scheme is subject to a degree of model drift throughout the simulation.

In HYCOM there is no indication of a seasonal signal of the transports, although some interannual signals seem to be evident.

The volume flux in the Agulhas Current is always poleward, varying between 8.9 Sv and 121.0 Sv (Bryden et al., 2005). Apart from the last week in April 2006 in HYCOM O2 where the transport is negative, equatorward, both experiments simulate predomi-

nately poleward transports (Fig. 5), ranging from 9.4 Sv to 108.4 Sv (HYCOM O2) and from 6.9 Sv to 124.2 Sv (HYCOM O4). The weekly transports are generally stronger (poleward) in HYCOM O4 than in HYCOM O2, in particular the extremes (confirmed with a Q-Q plot, not shown).

The minimum and maximum velocities in both simulation experiments are always associated with the southwestward passage of anticyclonic eddies. These transport fluctuations occur between 4–6 times per year, in good agreement with the occurrence of southwestward propagating Mozambique Channel eddies. They were previously shown to appear in the Mozambique Channel 5–6 times per year, frequently interacting with the Northern Agulhas Current (Backeberg et al., 2008). The advection of these eddies are clearly responsible for the large fluctuations in Agulhas Current transport.

From these comparisons, it is evident that the O4 simulation provides stronger poleward transports within the Agulhas Current core. Additionally, it seems that these are significantly contributed toward by upstream mesoscale variability. An increase in mesoscale variability in the O4 scheme seems to be the cause of the enhanced transports, considering that the 4th order scheme has been documented to increase the eddy kinetic energy in model simulations (Winther et al., 2007). According to previous studies (e.g. Backeberg et al., 2008) these also have an impact on the dynamics at the retroflection, influencing the heat transport and therefore the Indo-Atlantic inter-ocean exchange. Assuming that these fluxes are predominantly influenced by the mesoscale variability, it is therefore important to examine and quantify the eventual relationship between the upstream and downstream dynamics.

4 Analyses of the mesoscale variability

In this Section mesoscale variability associated with sea surface heights are analysed using the satellite altimetry data as well as the two model simulations. Due to the fact that the mesoscale signals in the greater Agulhas Current region are quite strong the inter-comparison with altimetry measurements yields a good opportunity to validate

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model simulations.

4.1 Sea surface height variations

To convert altimeter measurements into dynamically meaningful quantities, the exact position of the sensor with respect to the geoid is required. To date the precision of the geoid is insufficient to allow for useful dynamical calculations of wavelengths shorter than about 2000 km (Le Traon, 2002). In terms of comparing the mean flow, the mean dynamic topography of the model simulation differs from the observations, there is an offset of about 150 cm between the AGULHAS HYCOM and Rio05 (Rio et al., 2005) mean dynamic topography but the gradients are similar (not shown), therefore they are comparable. From the geostrophic assumption, the mean SSH contour lines (Fig. 6, black) depict the mean circulation pathway.

Altimeter based sea level anomalies and estimation of eddy kinetic energies (resp. standard deviation) are routinely used to assess the performance of eddy-resolving/-permitting ocean models (Treguier et al., 2003). The standard deviation (∇, Eq. (1), Fig. 6, colour scheme) is the variability about the time mean, and hence differences in the mean dynamic topography do not come into play.

$$\nabla = \sqrt{\frac{1}{n}[\sum \eta^2 - \frac{1}{n^2}(\sum \eta)^2]} \tag{1}$$

where n is the number of observation and simulation weeks, and η is the sea surface height.

North of Madagascar, near the open boundary, the jet associated with the South Equatorial Current (SEC) seems to be slightly stronger in the O4 versus the O2 simulation, while the jet in the altimetry observations appears to be stronger than the model experiments. This is most likely due to inherent weaknesses from the parent model.

In the Mozambique Channel, there is no clearly defined current indicated by the streamlines from the altimetry SSH. The high levels of variability indicate, in agreement

with the previous literature, that the flow here is dominated by the passage of eddies. Both model runs are able to simulate these high levels of mesoscale variability. Slightly stronger variability is evident in the O4 experiment, suggesting that the eddies are more frequent and/or more energetic in the 4th order advection scheme.

5   Both model simulations depict the mean path of the southern extension of the East Madagascar Current (SEMC). The mean SSH streamlines retroflect in an anticyclonic direction to flow eastward into the South Indian Ocean. Higher levels of mesoscale variability are encountered due to this retroflecting current, with occurrences of both cyclonic and anticyclonic eddies as reported by Siedler et al. (2009). The variability
10 in the O4 simulation is slightly broader and more energetic but remains lower than observed from altimetry.

In the Northern Agulhas Current, the simulation experiments overestimate the current strength in comparison to the altimetry. In particular north of 34° S, the narrow separation between SSH streamlines indicate a strong gradient and hence an intensifi-
15 cation of the mean geostrophic current. However, as mentioned previously, the quality of the data from Aviso close to the coast is questionable and the Agulhas Current is known to remain within 31 km of the coast 79% of the time in this region (Bryden et al., 2005).

The mesoscale variability in this northern part of the Agulhas Current, is predomi-
20 nantly confined to the offshore side of the current. This is evident from the enhanced variability offshore of the Northern Agulhas Current, in both model simulations as well as the altimetry.

In the Southern Agulhas Current, the current is again sufficiently far away from the coast for the altimetry data to recapture its flow. Comparing the trajectories of the
25 Southern Agulhas Current mean flow, between 20°–28° E and 34°–38° S, the core of the current is too far south in HYCOM O2, suggesting that it separates from the continental shelf prematurely. In the 4th order simulation, the southwestward extent of the Agulhas Current core is much narrower and extends further southwestward than in the 2nd order experiment. Its trajectory is also slightly further north.

As the Southern Agulhas Current separates from the coast, following the continental shelf break, it continues southwestward as an unstable, meandering current. In turn the SSH standard deviation reveals a narrow band of high variability, along the continental shelf break north of 36° S between 22° and 26° E. In the O2 simulation this narrow band is completely masked by excessively high and broad standard deviation values assumed to be caused by the distinct train of eddies extending from the Agulhas Plateau to the retroflection (Backeberg et al., 2008). In the O4 scheme a narrow band of high variability is encountered, suggesting that it is able to simulate the Southern Agulhas Current as a meandering current, rather than a train of eddies. This will be confirmed later using sea level skewness (Sect. 4.2.2).

Moreover the standard deviation pattern and distribution in the retroflection area in HYCOM O4 agrees better with the altimetry observations.

The Agulhas Ring shedding corridor in HYCOM O2 is confined to a very narrow band extending northwestward from the retroflection. This indicates that eddies and rings shed from the retroflection prefer to travel along this one trajectory. The strength and pattern of the standard deviation distribution is less focused in the northwest direction in the O4 experiment. In comparison this agrees better with the spatial distribution of variability observed from altimetry suggesting that, although the higher-order momentum advection scheme seems to underestimate the variability for the region compared to observations, it is able to simulate more variable eddy trajectories in the ring shedding corridor.

The meandering pathway of the Agulhas Return Current, is represented by the narrowly spaced band of mean SSH contours and high standard deviation at about 40° S between 20° and 60° E in the altimetry. It is known to have three main quasi-stationary meanders (e.g. Boebel et al., 2003) and these are well represented in the simulated mean SSH field. Although slightly lower levels of variability are observed. The second and third meanders, with their northern troughs near 33° and 39° E, are more clearly defined in the O4 experiment.

In summary there are marked improvements from applying the 4th order advection

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scheme in HYCOM for the Agulhas Current simulations. In particular the strength and distribution of the MKE (mean SSH) and EKE (∇) in the Southern Agulhas Current associated with the transition from a more stable current upstream to a strongly meandering and retroflecting current downstream appears to be more reliable in HYCOM O4 when compared to altimetry.

4.2 Sea level skewness

The above comparisons are qualitative, and more quantitative analyses need to be performed in order to objectively assess these simulation results.

Sea level skewness has been proposed by Thompson and Demirov (2006) as a new method for using SSH measurements from altimetry in model validation and mesoscale variability studies.

Skewness is a measure of the asymmetry of the distribution of a variable, or just the normalised third moment about the mean. It is given by γ_1 (Eq. 2), of which we will consider the classical unbiased estimate (Eq. 3).

$$\gamma_1 = \frac{\frac{1}{n}\sum_{i=1}^{n}(x_i - \overline{x})^3}{[\frac{1}{n}\sum_{i=1}^{n}(x_i - \overline{x})^2]^{\frac{3}{2}}} \tag{2}$$

$$\gamma_\eta = \frac{\sqrt{n(n-1)}}{n-2}\gamma_1 \tag{3}$$

γ_η denotes the unbiased skewness of SSH (η) for a sample of n values, x_i is the ith value and $\overline{x}$ the sample mean.

Thompson and Demirov (2006) show that in an idealised example of a meandering current, standard deviation of SSH is a function of position, with the maximum variability occurring at the mean position of the current, where the sea surface gradient is greatest.

Similarly, skewness is also a strong function of the cross current position. It is zero at its mean position, where changes in the sea surface height induced by the meandering current are symmetric. Therefore in a meandering current it is possible to infer its mean position from the zero line of the skewness. Moreover, as the skewness increases toward lower mean sea levels, a geostrophic flow to the left (right) can be inferred in the Southern (Northern) Hemisphere.

In regions with an abundance of eddies, the skewness field allows for the preferred sense of rotation to be determined. Consider the following two situations: (1) one large anticyclonic eddy and one large cyclonic eddy of the same dimension, and (2) one large anticyclonic eddy and two small cyclonic eddies. For the two situations, the mean SSH and its standard deviation may be the same but the skewness will be zero in situation (1) and negative in situation (2). Therefore negative (positive) skewness indicates a preference for cyclonic (anticyclonic) rotation.

Thompson and Demirov (2006) conclude that the skewness analysis is a useful statistical method for validating high resolution ocean models. In the following Section sea level skewness determined from altimetry is assessed for greater Agulhas Current region and then used to assess the model simulations. To our knowledge, this is the first time that sea level skewness is used in model validation.

4.2.1 Assessment from altimetry measurements

In order to evaluate the sea level skewness field it is compared to the mean geostrophic currents derived from altimeter SSH measurements (Fig. 7a) and to the fraction contribution of anticyclonic eddies toward the total EKE (Fig. 7b). The method of distinguishing between cyclonic and anticyclonic rotation by calculating the fraction from total EKE was used in the study of the southern extension of the East Madagascar Current (Siedler et al., 2009), but here was applied to the entire greater Agulhas Current domain.

The zero skewness line seems to indicate the mean positions of meandering currents northwest of Madagascar, in the Southern Agulhas Current, and in the Agulhas Return

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Current (Fig. 7a). The fraction of anticyclonic EKE from the total seems to explain most of the pattern evident in the sea level skewness field (Fig. 7b).

The flow in the Mozambique Channel is dominated by southward moving anticyclonic eddies (e.g. Sætre and da Silva, 1984; Biastoch and Krauss, 1999; de Ruijter et al., 2002), and most of the variability associated with these eddies is located toward the centre of the channel (Fig. 6a), contributed to mostly by anticyclonic eddies (Fig. 7b). The skewness field (Fig. 7a) is predominantly positive here in good agreement with the fraction of anticyclonic EKE. Near the Mozambican coast there is a preference for cyclonic rotation, consistent with cyclonic shear edge eddies forming from friction at the continental shelf edge. However, the skewness field does not indicate the presence of cyclonic shear. This may be related to the fact that skewness cannot distinguish between an eddy field with an equal mix of cyclonic and anticyclonic eddies of the same intensity and a region with no eddies.

The two modes of the southern extension of East Madagascar Current (SEMC) described by Siedler et al. (2009) are clearly evident in the skewness field. The current consistently retroflects southwest of Madagascar near 42° E, with anticyclonic motion (and eddies) favoured during a southwestward extension of the SEMC, while cyclonic motion (and eddies) occurs during westward flow along the south Madagascar continental shelf edge. For the SEMC the zero skewness line (Fig. 7a) does not seem to indicate the mean position of the westward outflow. The mean geostrophic currents are located within the area of negative skewness, indicating that the SEMC outflow is not a meandering current.

The tongue of positive sea level skewness, extending from south of Madagascar toward the Agulhas Current, was suggested to represent anticyclonic eddies propagating westward (Thompson and Demirov, 2006). Moreover, these are thought to be one of the mechanisms by which Natal Pulses are triggered in the Northern Agulhas Current (Schouten et al., 2002). The occurrence of anticyclonic eddies in this region has been confirmed by (e.g. Siedler et al., 2009), and is also clearly evident in the fraction of anticyclonic EKE (Fig. 7b).

Natal Pulses are large cyclonic meanders, that form at the Natal Bight, on the east coast of South Africa near 29° S. Their average offshore extent is 170 km and they form approximately 6 times per year (Lutjeharms and Roberts, 1988). These periodically interrupt the stable flow conditions of the Northern Agulhas Current as they propagate
5 southwestward along the South African east coast.

The band of negative skewness extending about 150 km offshore along the east coast of South Africa from 26°–35° S indicates that there is a preference for cyclonic disturbances in the mean current, consistent with what is known of Natal Pulses. The fraction of anticyclonic EKE (Fig. 7b) is low, and confirms that up to 80% of the variance
10 is from cyclonic meanders. However the total EKE (cyclonic + anticyclonic; Fig. 6a) is very low, suggesting a rather stable current with relatively infrequent occurrences of Natal Pulses. In fact, most of the EKE, between 26° and 35° S is located on the offshore side of the Agulhas Current, and is mainly due to anticyclonic eddies. These EKE maxima might be connected with anticyclonic eddies frequently originating at the
15 SEMC and the Mozambique Channel.

Upon approaching the Agulhas retroflection, between 21°–27° E and 35°–40° S, the skewness field as well as the fraction of anticyclonic eddies in total EKE, indicate predominantly cyclonic rotation in the Southern Agulhas Current. This might be related to the arrival of Natal Pulses in combination with westward propagating cyclonic eddies
20 pinched off from the northern extremities of the meandering Agulhas Return Current.

The zero skewness line in the Southern Agulhas Current closely follows the mean position of the current. In particular southwestward of 22° E/37° S, at the southern termination of the Agulhas Bank, where the current separates from the continental shelf break and continues southwestward as a meandering current. As such the skewness
25 field is able to determine the mean position of a meandering current, and approaching the Agulhas retroflection region, is in good agreement with the fraction of anticyclonic EKE.

In the ring shedding corridor the tongue of positive skewness extending into the South Atlantic Ocean, indicates a preference for anticyclonic eddies. Thompson and

Demirov (2006) discuss that it has been shown that cyclonic eddies which occur closer to the South African west coast travel west-southwest from this position, while anticyclonic Agulhas Rings travel west-northwest from the Agulhas retroflection (e.g. Richardson and Garzoli, 2003; Matano and Beier, 2003; Treguier et al., 2003). They argue that if the relative contributions of cyclonic and anticyclonic eddies are equal, the skewness will be zero (as in situation 1, Sect. 4.2). It may be possible that these cancel each other out closer to the coast and hence cause the southward displacement of the ring shedding corridor.

In the meandering Agulhas Return Current the zero skewness line provides a really good indication of the mean position of the current, and its quasi-stationary meanders.

4.2.2 Comparison to HYCOM simulations

The skewness field has been calculated from HYCOM O2 and O4 SSH fields (Fig. 8) as a means to validate and compare the two simulations as well as provide new insight into mesoscale dynamics simulated in the model.

The current to the northwest of Madagascar is well represented in both simulations, the zero skewness line indicating the mean path at 10° S, in agreement with the altimetry skewness field (Fig. 7).

Moreover, a preference for anticyclonic eddies in the Mozambique Channel is well represented in both HYCOM simulations, in good agreement with the observations.

In the SEMC, contrary to the altimetry sea level skewness, there is a preference for anticyclonic rotation in the model simulations. However, a band of negative skewness extending toward Mozambique west of Madagascar's southern tip in the O4 scheme suggests that it is able to reproduce the bimodal pattern discussed in Siedler et al. (2009). Although this pattern is not as pronounced as in the altimetry skewness field, it is completely absent in HYCOM O2.

The most striking improvement from applying the 4th order advection scheme can be seen in the Agulhas Current proper. The band of negative skewness along the east coast of South Africa extends all the way to the retroflection region, near 40° S, in good

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agreement with the observations from altimetry. This indicates that the O4 scheme is able to simulate the Agulhas Current as a well defined current core, with the periodic occurrence of cyclonic disturbances or Natal Pulses. This band of negative skewness is much shorter in O2 extending from 32° E/29° S to 25° E/35° S, the northern tip of the Agulhas Plateau.

In the Southern Agulhas Current the zero skewness line from the O4 scheme lies within the centre of the mean position of the current. According to Thompson and Demirov (2006), the zero skewness line will only indicate the mean position of a current, when it freely meanders. The O4 simulation results therefore suggest that the Southern Agulhas Current is represented as a meandering current, as opposed to a train of eddies evident in the O2 scheme (Backeberg et al., 2008).

The skewness distribution of the O4 scheme at the Agulhas retroflection is generally in better agreement with the altimetry skewness field. Along the continental shelf of the Agulhas Bank, for instance, there is a narrow band of positive skewness north of the negative skewness band, which continues westward at the southern termination of the Agulhas Bank. The ring shedding corridor is less focussed in O4, indicating a more realistic representation of the variability associated with the Agulhas retroflection ring shedding.

In both simulations the meandering Agulhas Return Current is only represented by the zero skewness line east of 30° E, which seems to indicate that not enough flow is returning eastward from the retroflection. In particular, the second meander, with its southern trough near 35° E extends too far south in the O4 simulation, while it seems to be more realistically portrayed in the 2nd order advection scheme. Moreover, the negative (positive) skewness north (south) of the mean position of the return current is well pronounced in both simulation experiments, although not as strong or persistent as found in the altimetry analyses.

In summary, the 4th order advection scheme significantly improves the dynamic characterisation of the Southern Agulhas Current, revealing a well-defined meandering current, with distinct bands of cyclonic and anticyclonic eddies.

4.3 Variogram analysis

In this Section the spatial scales of mesoscale features are discussed. The (semi-)variogram, is a geostatistical technique which characterises the spatial correlation within a data set and quantifies variability as a function of scale (Wackernagel, 1998).

Dissimilarities (γ) between sample pairs are calculated by computing the squared difference between the values (Eq. 4), and these are plotted against the separation of the sample pairs in geographical space, or lag (h), to form the variogram cloud. The lag distances are grouped into classes (H_k), and within each class the dissimilarities are averaged to form the sequence of values of the experimental variogram. The dissimilarities depend on the spacing and on the orientation of the point pair described by the lag vector, and because it is a squared quantity, the order in which the points in space are considered does not come into play. Therefore the variogram is symmetric with respect to h.

$$\gamma(H_k) = \frac{1}{2n_c} \sum_{\alpha=1}^{n_c} (\eta(x_\alpha + h) - \eta(x_\alpha))^2 \text{ with } h \in H_k \tag{4}$$

n_c are all the point pairs that can be linked by a vector, h. The average dissimilarity with respect to a vector class within a specific interval H_k, is a value of the experimental variogram $\gamma(H_k)$.

Usually the average dissimilarity between values increases with distance between point pairs, as near samples tend to be more alike. If the variable is stationary, at large distances between point pairs the experimental variogram may reach a sill, its maximum. When this occurs the expression converges to twice the variance, therefore dividing by 2 means that the sill approximates the variance within the data. At scales exceeding the natural scale of the phenomena in question, harmonic effects may be noted, in which the variogram peaks and dips at lag distances that are multiples of the natural scale, this is known as cyclicity.

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An abrupt change of the slope of the dissimilarity function at a specific scale indicates that an intermediate level of variation has been reached, this is known as the range. It identifies the distance from the origin where the variogram reaches its maximum value (the sill), at which point the sampled variable exhibits its maximum variance.

The behaviour of the variogram near the origin is important to note, it characterises the very small scales within a dataset and indicates the type of continuity of the variable: differentiable, continuous but not differentiable, or discontinuous. A discontinuous variogram at the origin is known as a nugget effect, which indicates that the values of the variables change abruptly at very small scales, it may also arise when data is sparse or from measurement error.

A theoretical curve is fitted to the variogram in order to attribute a physical meaning to them. The fit is done by eye, because emphasis is not placed on how well the variogram function fits the the sequence points, but rather what type of continuity is assumed near the origin. The fit therefore implies an interpretation of the behaviour of the variogram at the origin and its behaviour at large lag distances.

4.3.1 Comparison to a spatial Fourier analysis

A spatial Fourier and variogram analysis of modelled SLA data (HYCOM O2) are compared in order to confirm for an oceanographic application, that the variogram indicates the scale up to which a spatial correlation exists between data points, thus giving an indication of the size of mesoscale features. The comparison is done for modelled SLA data along a section in the Mozambique Channel where large anticyclonic eddies, up to 300 km in diameter, are known to occur frequently (HYCOM O2; Backeberg et al., 2008).

Figure 9a is the time averaged spatial FFT spectrum for the modelled SLA data along the section indicated in Fig. 8a. Notice the peak near $L_w \cong 560$ km, which for a Fourier analysis typically corresponds to two eddies (cyclonic and anticyclonic) with diameters of about 280 km, in agreement with the simulated eddies observed in HYCOM O2 for the Mozambique Channel (Backeberg et al., 2008).

The blue curve (Fig. 9b) indicates the corresponding experimental variogram calculated using Eq. (4), and the red curve is the theoretical variogram fitted to the sequence (Eq. 5), which in this case is a combination of a Gaussian and a cosine function. Other functions were tested (cardinal sine, cubic, exponential) with less success.

$$\gamma(h) = C_g[1 - \exp(-\frac{h^2}{a_g^2})] + C_c[1 - \cos\frac{2\pi h}{a_c}] \tag{5}$$

where C is the amplitude, h the distance vector and a the range, or radius. The subscript g and c refer to the Gaussian and cosine variables respectably.

The range (radius) a_g is 110 km, and in a Gaussian model, this corresponds to a length scale of 275 km ($a_g \times 2.5$).

Mozambique Channel eddies in HYCOM O2 are all of very similar sizes. Therefore, the typical mesoscale size indicated by the Fourier analysis should be of a similar size to the maximum mesoscale estimated by the variogram. In this case, the mesoscale estimate from the variogram is 275 km and the estimate from the Fourier analysis is 280 km, in good agreement with each other as expected.

In addition to this, the combined Gaussian and cosine fit indicates a mixture of periodic (cosine) and other (Gaussian) signals. Here the periodic signal suggests a succession of eddies. The cosine range (a_c=90 km) indicates that successive eddies are typically ~560 km ($a_c \times 2\pi$) apart.

Both the spatial Fourier and variogram analyses reflect the whole range of spatial scales related to mesoscale currents for a given region. Therefore it may be prudent to refer to "mesoscale features" rather than "eddies" when discussing these results. However, due to the dominance of anticyclonic eddies (in HYCOM O2) in the Mozambique Channel it may be safe to conclude that these results provide an indication of the of typical (Fourier) and maximum (variogram) eddy diameters. For consistency, discussions hereafter will refer to "mesoscale features" only, and these are defined to include both eddies and meanders in mesoscale currents.

The information contained in a variogram is in principle equivalent to that contained in a Fourier transform, but the variogram is more practical for testing the stationarity of a variable and for examining small scales. In addition to this Fourier transform relies on the assumption that the data domain is periodic rather than infinite. Furthermore, when
5 calculating the experimental variogram the data does not need to be preprocessed. Before calculating the Fourier transform, trends in the data have to be removed, and tapering functions need to be applied at the edges. Moreover, the physical meaning of the semivariance is easy to interpret. In the case of mesoscale variability in the ocean, it represents the amplitude of the differences, and like eddy kinetic energy, high
10 values represent regions with high mesoscale variability. The major advantage of the variogram, is that it is easy to calculate, requiring only a few lines of code.

These results confirm that the variogram indeed provides an indication of the size of mesoscale features for a given region, and in addition to this is able to determine the presence of periodic signals, as well as comparable magnitudes of the variance.

15 4.3.2 Quantifying spatial scales of mesoscale variability

To quantify the spatial scale of mesoscale variability in key regions of the greater Agulhas Current system, three sections were defined along which SLA data from Aviso, HYCOM O2 and HYCOM O4 was extracted (see Figs. 7 and 8).

The Mozambique Channel section, extending southward from $43°$ E/$14°$ S to
20 $30°$ E/$33.5°$ S, was chose to represent the path along which predominantly anticyclonic eddies propagate southward from the Mozambique Channel toward the Northern Agulhas Current. This path can be clearly identified in both HYCOM O2 and O4 simulations, and is also evident in the altimetry field.

The Aviso SLA experimental variogram (Fig. 10a, left) was fitted with a Gaussian
25 function (the first term in Eq. 5), indicating that a maximum variance (or sill) of $355\,\mathrm{cm}^2$ is reached at a radius (or range) of 150 km. This suggests that mesoscale features (eddies or meanders) along this section have diameters up to 375 km, somewhat larger than previously documented.

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As discussed previously (Sect. 4.3.1), the HYCOM O2 variogram (Fig. 10, middle) was fitted with a curve combining a Gaussian and cosine function (Eq. 5). The respective Gaussian and cosine ranges, (a_g and a_c) indicate that, contrary to previous findings (Backeberg et al., 2008), the Mozambique Channel eddies in HYCOM O2 are smaller and less intense than in reality, with diameters of 275 km, and a semivariance 60% less than observed from altimetry. In addition to this the periodicity, with successive eddies ~560 km ($a_c \times 2\pi$) apart, is not evident in the altimetry SLA section, indicating that the formation of eddies in the O2 simulation is too regular/periodic.

Applying the 4th order advection scheme in HYCOM improves some of the deficiencies of the O2 scheme in the Mozambique Channel. The amplitude of the Gaussian sill (C_g) is much higher, and the range has increased to 140 km, corresponding to a diameter of 350 km, in better agreement with the altimetry observations. There is also some improvement in the (artificial) periodicity, in that the amplitude of the cosine function (C_c) is slightly lower, suggesting a reduction of the periodicity.

The second section extends from 32° E/30° S along the South African east coast toward the retroflection region at 20° E/39° S and lies within a band of negative skewness thought to be associated with periodic cyclonic disturbances or Natal Pulses.

The Aviso variogram analysis, with C_c=220 cm^2 and a_c=125 km, here indicates mesoscale diameters of up to 312.5 km, in agreement with the documented scale of the Agulhas retroflection loop (340 km; Lutjeharms and van Ballegooyen, 1988).

The amplitude of the sill in O2 is much higher (C_c=450 cm^2), with a shorter range (a_g=100 km) corresponding to diameters of 250 km. A periodicity of 80 km (corresponding to eddies ~500 km apart) confirms the successive train of eddies simulated in O2.

The HYCOM O4 variogram is in much better agreement with the altimetry, and no periodicity is evident. A Gaussian function provides the theoretical fit. The amplitude of the sill is slightly higher, but the range of 125 km is in good agreement with the altimetry. A train of eddies (as in O2) will result in a variogram with a higher variance at the sill, due to the enhanced variability associated with an eddy field, but with a

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smaller spatial scale compared to a well defined current extending southwestward with a large retroflection loop at its termination, as in Aviso and O4. This result presents an additional indication that the O4 scheme provides a much more realistic simulation of the Southern Agulhas Current.

From the skewness analysis two sections were defined in the altimetry for the north-westward passage of Agulhas Rings. The first (solid line, Fig. 10c, left) corresponding to the track along which rings seem to preferentially propagate in HYCOM (Fig. 8) and the second where according to the skewness field from altimetry (Fig. 7), predominantly anticyclonic eddies are found in the observations (dashed line).

The Aviso variogram shows that the northern section has a variance of $620\,cm^2$, with a scale of 140 km, corresponding to diameters of 350 km. The variance in the southern section is 40% lower, but the length scales are similar (135 km corresponding to a diameter of 337.5 km). This indicates, that eddies shed from the retroflection tend to preferentially propagate along the northern track, and that the altimetry skewness field is unable to indicate this path as pointed out by Thompson and Demirov (2006). Note that Agulhas Rings have been documented to have diameters of up to 320 km (Lutjeharms and van Ballegooyen, 1988), in good agreement with the variogram analysis.

While in both model simulations the spatial scales are in good agreement with the altimetry observations, the amplitude of the variance in O2 is too large. A periodic (cosine) signal is also evident in both simulations, suggesting an artificial regularity of Agulhas Ring shedding. This amplitude is somewhat lower in the O4 scheme.

In conclusion, using the variogram tool, the spatial scales of mesoscale features for three sections in the greater Agulhas Current system were quantified. In addition to this, the variogram analysis, provides an objective tool for comparing and validating the two model simulations. It was able to identify (unrealistic) periodic signals in the model simulations, as well as provide a good quantitative comparison of the scales of the ocean features. A major improvement of the O4 simulation is that the periodicity evident in all the sections for the O2 scheme, is reduced in the Mozambique Channel and ring shedding corridor, and significantly, absent for the section through the Agulhas

Current. Moreover, the spatial scales and amplitudes of the variances in HYCOM using the 4th order advection scheme are much more realistic, and in better agreement with the altimetry observations.

5 Conclusions

From this inter-comparison of the two numerical advection schemes in HYCOM it was clearly shown that applying higher order numerics (the 4th order QUICK scheme) significantly improve the model simulation of the greater Agulhas Current regime. Moreover, this is achieved at a fraction of the computational cost of increasing the grid resolution.

The most significant improvement in the O4 simulation is the change in the Southern Agulhas Current, from a train of successive eddies, to a well-defined meandering current. Stronger poleward transports and a much improved vertical structure of the Agulhas Current near 32° S in HYCOM O4 is evident. These improvements may contribute toward a better southwestward penetration of the temperature field, and implies a stronger leakage of warm, saline Indian Ocean waters into the South Atlantic Ocean vital for the Meridional Overturning Circulation.

Satellite altimetry measurements of the sea surface are used in model validation techniques. The sea surface height variations, sea level skewness and variogram analyses quantify the improvements evident in the simulation, as well as providing some new perspectives in terms of studying mesoscale variability in the ocean.

Sea level skewness was shown to be an ideal tool for studying flows with meanders that become unstable and change into eddies. In an eddy field it is able to distinguish between a preference for cyclonic or anticyclonic rotation. The zero skewness line in the Southern Agulhas Current confirms that throughout the O4 model simulation, the current is represented as a well defined meandering current.

The variogram analysis confirms that the O4 scheme simulates more realistic scales and variances of mesoscale features. Additionally, it is able to identify (unrealistic) peri-

odic signals such as too regular Mozambique Channel eddies and successive eddies in the Southern Agulhas Current, which are pronounced deficiencies of the O2 scheme.

Finally, the Agulhas Current transport, and hence the Indo-Atlantic inter-ocean exchange, is sensitive to mesoscale features that originate upstream in the source regions. HYCOM O4, in particular with the improved simulation of the Southern Agulhas Current, is well suited for application in further studies of this exchange.

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Table 1. Statistics from the SST time series calculated for the period from June 2002 until December 2006, corresponding to the availability of the MW SST data with the launch of NASA's AQUA satellite.

	Mean	Standard deviation
HYCOM O2	16.83	1.05
HYCOM O4	17.55	1.26
Reynolds SST	18.38	1.75
MW SST	18.84	1.59

Table 2. Mooring positions and current meter depths deployed during the RRS Discovery Cruise 214 (Bryden et al., 1995).

Mooring	A	B	C	D	E	F
Latitude (° S)	31 05.03	31 05.30	31 10.38	31 20.55	31 34.46	31 54.51
Longitude (° E)	30 22.08	30 25.44	30 32.22	30 46.60	31 06.00	31 28.24
Current meter depths (m)	138	384	403	353	353	388
	238	790	809	753	753	789
	439.5	1190	1209	1154	1154	1189
	740	1391	2010	1963	1963	1997
Water depth (m)	849	1480	2498	2900	2900	3446

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Table 3. Northern Agulhas Current transport statistics. Note the inverted convention from Bryden et al. (2005), the maximum transport was considered to be positive and poleward.

	Period	Mean	Std
Bryden et al. (2005)	05/03–27/11/1995	69.7	21.5
HYCOM O2	2001–2006	48.3	19.6
	2001	52.9	19.7
	2002	52.4	17.7
	2003	52.3	21.7
	2004	48.3	16.8
	2005	42.4	13.3
	2006	37.7	17.8
HYCOM O4	2001–2006	57.5	19.9
	2001	56.9	22.2
	2002	54.1	17.7
	2003	60.7	18.1
	2004	64.4	27.5
	2005	55.6	19.6
	2006	51.8	17.56
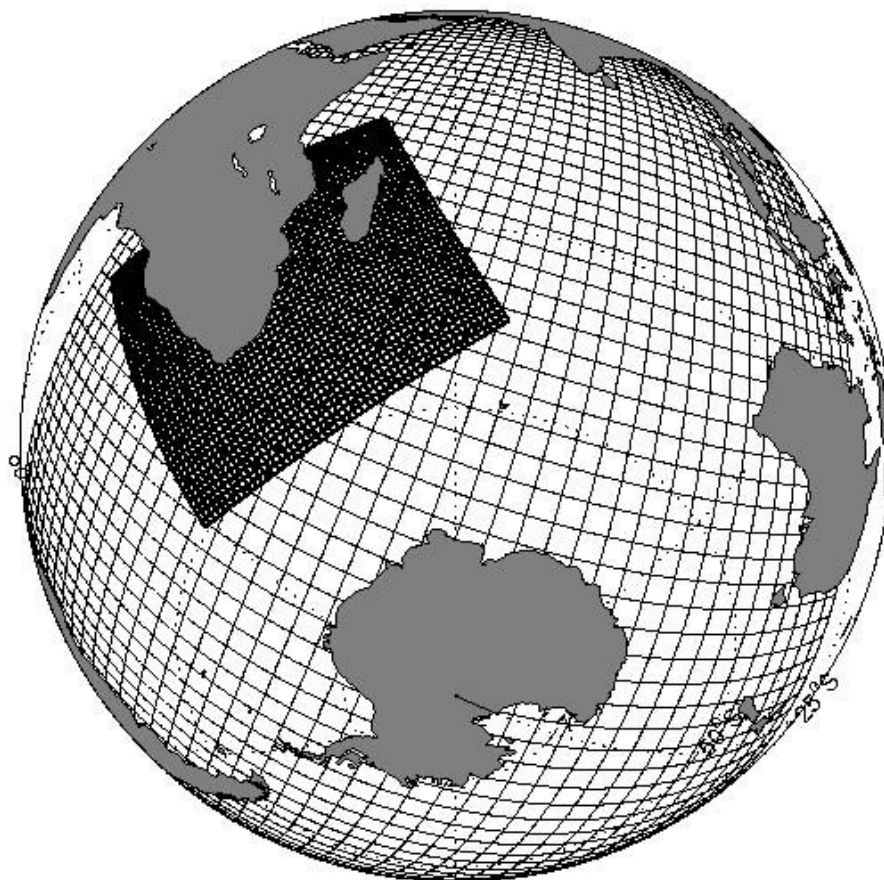
Fig. 1. Illustration of the HYCOM model system: coarse resolution basin-scale (INDIA) model grid, provides boundary conditions for a high-resolution nested regional (AGULHAS) model grid. Every 10th grid cell was plotted to produce the mesh grid.
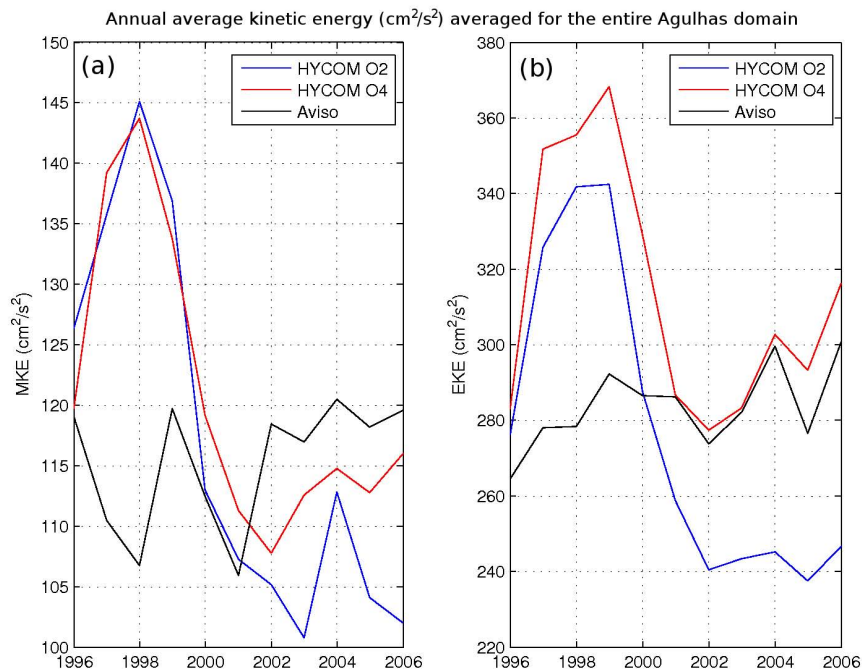
Fig. 2. Annual averages of the mean kinetic energy **(a)** and eddy kinetic energy **(b)** for the Agulhas domain. HYCOM O2 (blue), HYCOM O4 (red) and calculated from Aviso geostrophic currents (black).
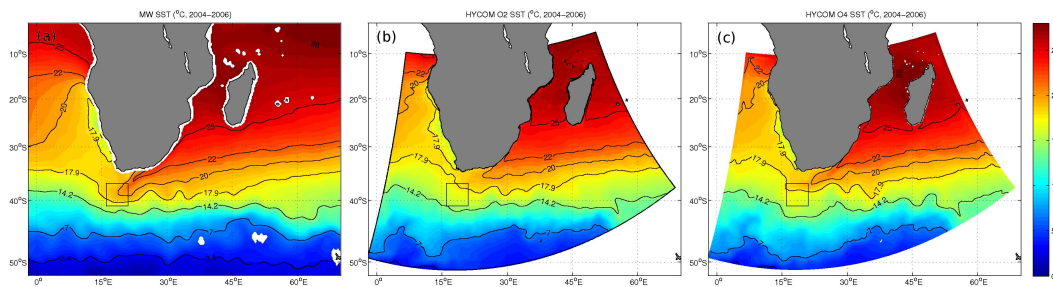
Fig. 3. Mean sea surface temperatures (SSTs) from MW SST **(a)**, HYCOM O2 **(b)** and HYCOM O4 **(c)**.
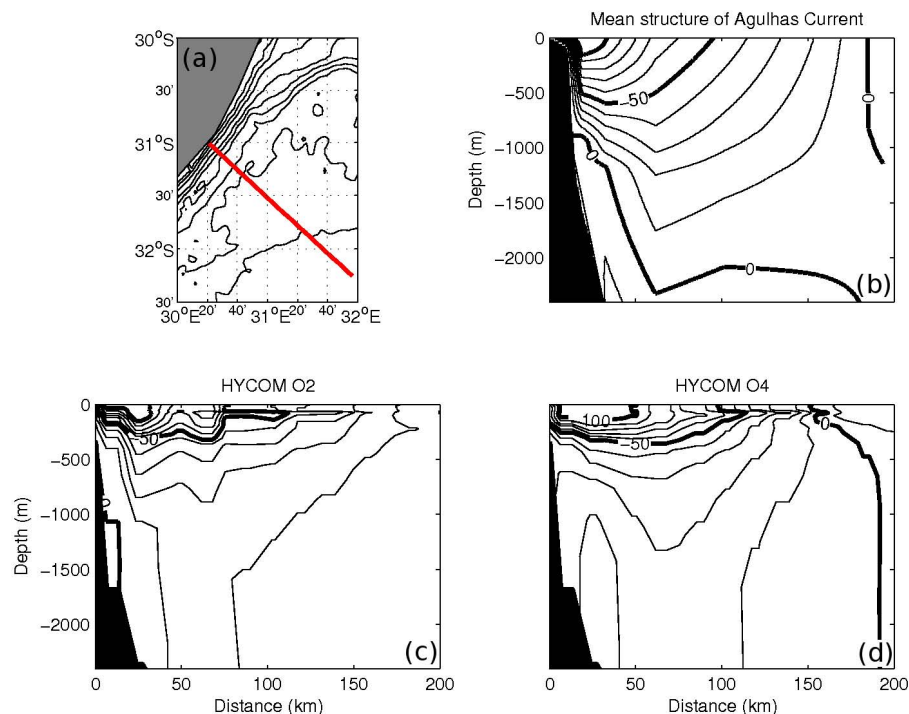
Fig. 4. Mean vertical structure of the Northern Agulhas Current from Bryden et al. (2005) **(b)**, HYCOM O2 **(c)** and HYCOM O4 **(d)**. The velocities normal to the section are given in cm.s^{-1} and are plotted at 10 cm.s^{-1} intervals. The section is indicated on the map **(a)** with the depth contours 100 m, 250 m, and 500 m to 4000 m at 500 m intervals from etopo2 bottom topography (http://www.gfdl.noaa.gov/products/vis/data/datasets/etopo2_topography.html) indicated.
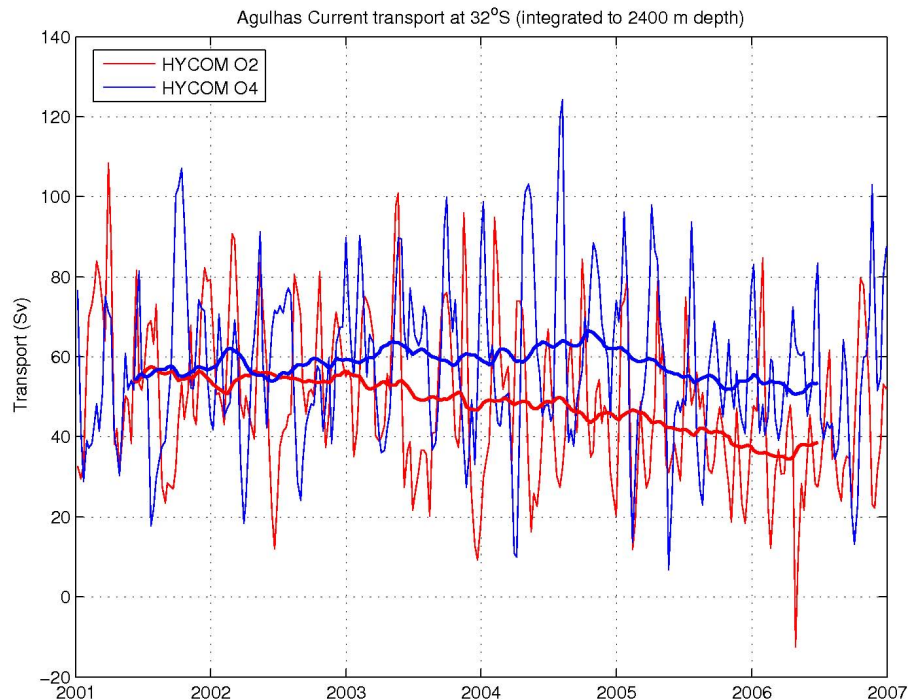
Fig. 5. Agulhas Current weekly transports at 32° S from HYCOM O2 and O4, with the corresponding yearly running means. The running means for the first and last 6 months have been excluded due to edge effects of the running mean window.

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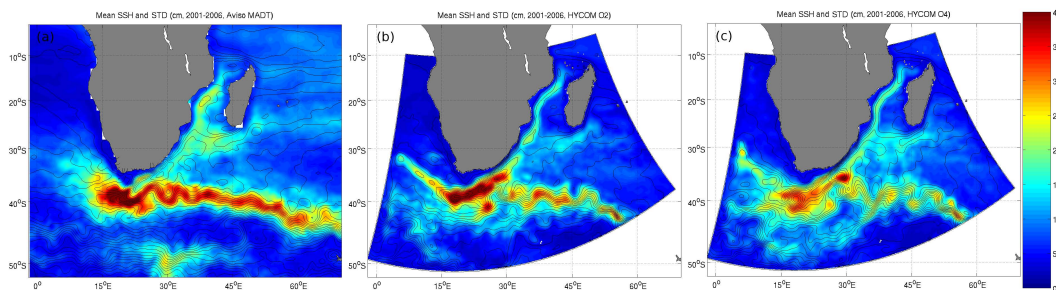
Fig. 6. Sea surface height (SSH) mean (black contours, spaced every 7.5 cm) and standard deviation (∇, colour scheme in cm) from Aviso MADT **(a)**, HYCOM O2 **(b)** and HYCOM O4 **(c)** for the period from 2001 to 2006, inclusive.

Fig. 7. **(a)** Sea level skewness (colour scheme indicates positive and negative) with mean geostrophic currents derived from altimetry SSH measurements (vectors). **(b)** The fraction of anticyclonic EKE from the total EKE. The solid black contour indicates zero skewness.
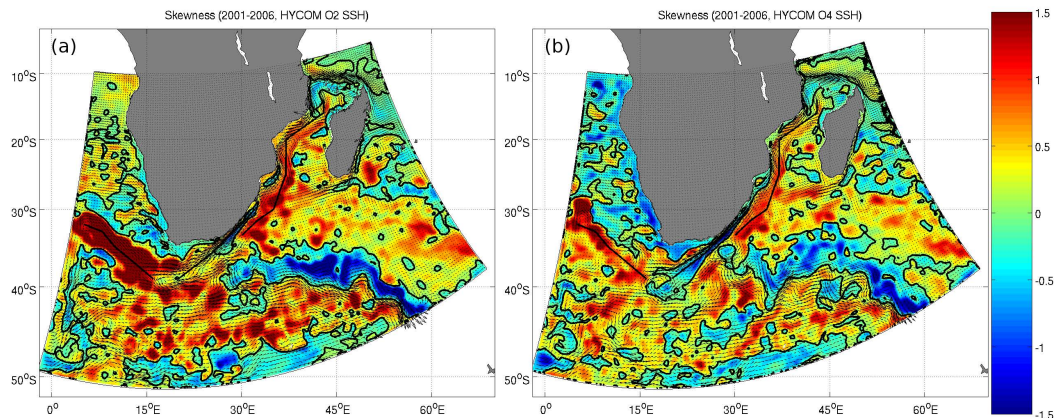
Fig. 8. Mean surface currents (vectors), with the colour scheme indicating the skewness, and the black contour indicating zero skewness. HYCOM O2 **(a)** and O4 **(b)**. The data period spans from 2001 to 2006, inclusive.

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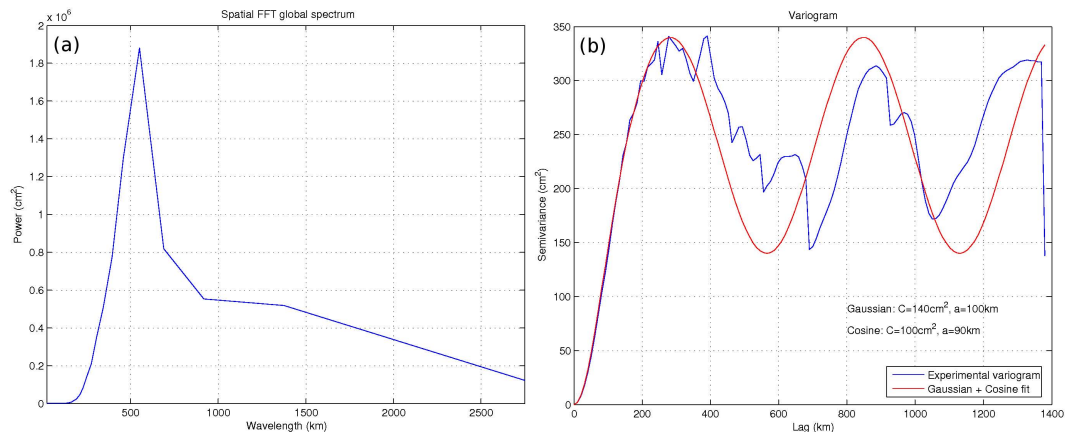
Fig. 9. Spatial FFT spectrum **(a)** and variogram analysis **(b)** of model SLA data from HY-COM O2 along a section in the Mozambique Channel. The section data was extracted from gridded data and interpolated to 10 km.
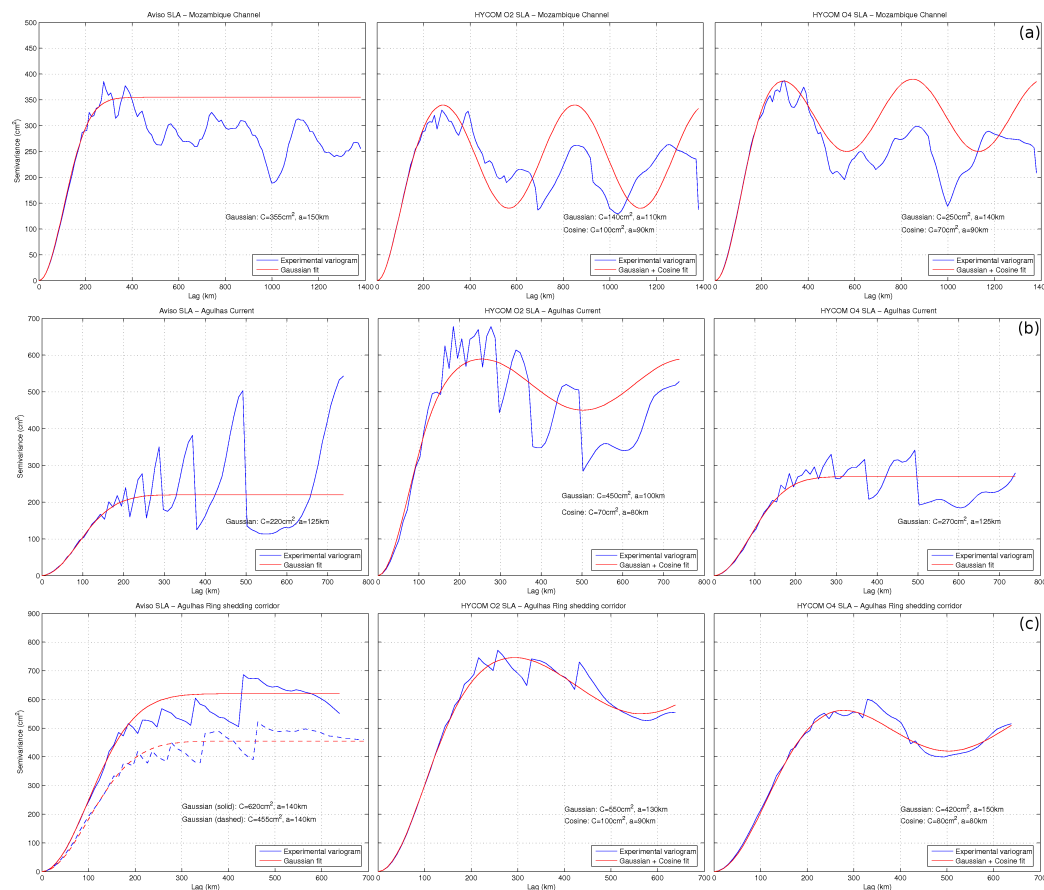
Fig. 10. Variogram analysis for Aviso (left), HYCOM O2 (middle) and HYCOM O4 (right). SLA data was extracted from gridded data along sections for the Mozambique Channel **(a)**, Agulhas Current **(b)** and Agulhas Ring shedding corridor **(c)** and interpolated to 10 km. See straight black lines in Figs. 7a and 8.

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