

Papers published in *Ocean Science Discussions* are under open-access review for the journal *Ocean Science*

A comparison between vertical motions measured by ADCP and inferred from temperature data

H. van Haren

Royal Netherlands Institute for Sea Research (NIOZ), P.O. Box 59, 1790 AB Den Burg, The Netherlands

Received: 6 March 2008 - Accepted: 27 March 2008 - Published: 14 April 2008

Correspondence to: H. van Haren (hansvh@nioz.nl)

Published by Copernicus Publications on behalf of the European Geosciences Union.



OSD

5, 103–121, 2008

Measurement of vertical motions in ocean





Abstract

Combined vertical current (w) and thermistor string data demonstrate that high-frequency internal "wave" trains along a pycnocline in a flat-bottom shelf sea consist for 2 periods of a dominant mode-1 non-linear part, while thereafter mainly of linear [mode-

- ⁵ 2, quadrupled frequency] waves, to first order. In a simple [linear] heat budget, the use of unfiltered temperature gradient or its time mean changes results by only 10%. The observations also demonstrate that temperature is not always adequate to estimate vertical motions using the linear 1-D heat equation. In shallow seas, tidal-*w* estimated from temperature data can be an order of magnitude weaker than directly observed
- *w*, and thus do not represent free internal waves. In the open ocean, tidal motions represent linear waves and are well described by temperature-inferred *w*. There however, the internal wave continuum is not well-described: near the buoyancy frequency it is dominated by non-linear waves and near [sub]inertial frequencies by eddies and gyroscopic waves.

15 **1** Introduction

20

The recognition of the importance of internal wave breaking for ocean mixing, with relevance for redistribution of suspended matter, justifies some detailed study of motions near the buoyancy frequency *N*. At this high-frequency limit of the internal wave band, motions are considered nearly vertical, so that they can be studied by monitoring vertical currents (*w*), see, e.g., Inall et al. (2000). This current component is not often measured in the ocean or shelf seas, because the aspect ratio is usually $O(10^{-2}-10^{-3})$ and when it is O(1) like near *N* spatial scales tend to be small.

Thus, a common method for monitoring w is using more easily measurable temperature variations under the assumption of a reduced heat equation that is dominated by

OSD

5, 103-121, 2008

Measurement of vertical motions in ocean



only two terms (e.g., Krauss, 1966),

$$\frac{\partial T}{\partial t} = -\mathbf{w} \frac{\partial \overline{T}}{\partial z},$$

where the overbar denotes a time mean. Other advection, non-linear and diffusive terms are considered small and temperature must be a conservative quantity. As in ⁵ a stably stratified sea, in regions where salinity contributions are small, the vertical derivative of slowly varying temperature is positive, *w* and *T* describing free wave motions will always be $\pi/2$ out of phase following Eq. (1), with *w* leading *T*. The use of Eq. (1) to estimate w requires vertical profiles of temperature besides sufficient temporal resolution.

- ¹⁰ Although this use requires a full sequence of thermistor string data, which is not always available, the mean vertical temperature gradient may be estimated from a single CTD-profile using a suitable vertical length-scale for smoothing. This has recently been used for open ocean data in a comparison between *w* inferred from Eq. (1) and w directly measured by acoustic Doppler current profiler (ADCP) (van Aken et al., 2007;
- ¹⁵ Fig. 1). In general, the agreement between the two data sets is reasonably good, with some statistically significant discrepancies near *N* and in the continuum near the low-frequency part of the internal wave band, near the inertial frequency *f* and around the semidiurnal tidal band (" D_2 ") harmonic frequencies like M_2 and S_2 . The best agreement is observed for the tidal harmonic peaks and for the continuum near frequencies
- σ =15–20 cpd, or just below *N* (Fig. 1). In the time domain some periods show misfits (Fig. 1b), but others show rather good comparison down to the fastest near-*N* motions (Fig. 1c). The larger discrepancies, that is weaker values for temperature-inferred *w*, at σ <*f* and σ >*N* were attributed by van Aken et al. (2007) to ADCP-noise. It is noted here that this noise is only partially instrumental white noise for the latter frequencies.
- It is even partially non-white "noise" due to current inhomogeneity for the former, as inferred using the redundant fourth beam providing the "error velocity" (Fig. 1). This is somewhat curious as one would not expect dominant motions at scales smaller than the ADCP's beam spread at sub-inertial frequencies.

OSD 5, 103-121, 2008 Measurement of vertical motions in ocean H. van Haren **Title Page** Introduction Abstract Conclusions References Tables Figures Back Close Full Screen / Esc **Printer-friendly Version** Interactive Discussion

(1)

In this note the focus is on details of the above discrepancies with the aim to learn more about the importance of non-linear internal waves and tidal (frontal) advection and to verify whether the above discrepancies are due to the use of mean temperature gradient from CTD-profiles or other neglected terms in Eq. (1), as noted by Krauss (1966). For this purpose, simultaneous ADCP and thermistor string data from a shelf sea interior and a continental slope will be scrutinized. Hereby, the particular disadvantage of ADCP, the averaging of all three Cartesian current components across horizontal distances O(10–100 m), because its 3–4 beams are slanted at typical angles $\theta=20-30^{\circ}$ to the vertical, is considered as well. This limits the study to phenomena having horizontal scales >100 m.

2 Data

Vertical motions are investigated using four-beam ADCP- and thermistor string data from a site in the central North Sea in summer 1994 (project INP) and from a site in the Faeroe-Shetland Channel "FSC" in spring 1999 (PROCS). Figure 2 shows mooring
locations and Table 1 lists the time intervals of operation. In 1994, Aanderaa thermistor strings are used. It is noted that although the manufacturer of these temperature sensors claims an absolute accuracy of "only" 0.1°C (Table 2), the relative accuracy of Aanderaa's resistors is much better, even below the resolution of digitization. This explains the ability to measure confidently the weak stratification at the top of the bottom
"mixing" boundary layer (Sect. 3). In 1999, a NIOZ-designed high-resolution thermistor string was used.

The flat-bottom INP mooring site in the central North Sea (*H*=45 m water depth) is well within the region of seasonal, predominantly thermal, stratification, and generally away from large frontal zones. The 8 d observational period is characterized by strong stratification mainly supporting large near-inertial motions and shear, strong insolation except for the first day and weak winds. Despite the [tidal] shear-induced turbulent friction, the near-bottom layer is not homogeneous but persistently shows a [minimum]

OSD 5, 103-121, 2008 Measurement of vertical motions in ocean H. van Haren **Title Page** Introduction Abstract Conclusions References Tables Figures Back Close Full Screen / Esc **Printer-friendly Version** Interactive Discussion

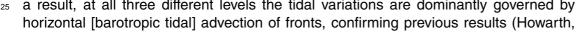
stratification for which the buoyancy frequency $N \approx 5 \cdot 10^{-4} \text{ s}^{-1}$, or $\sim 4f$. In this layer, larger stratification resulting in larger N are observed during particular phases of the tidal current with typical buoyancy periods T_N ranging between 1500 and 2500 s. Similar values are found above the pycnocline. In the pycnocline itself stronger stratification 5 results in $300 < T_N < 500$ s.

Above a smoothly sloping side of the FSC a bottom-lander with ADCP and NIOZ-1 thermistor string was located at H=494 m, an order of magnitude larger than in the central North Sea. Data are discussed from a two-week deployment sampled at a rate of once per 30 s. Main stratification is around 300–500 m, well below mid-depth and with $T_N \approx 1200-1800$ s. This stratification occasionally moves upslope and passes the mooring as a vigorous bore (Hosegood and van Haren, 2004). Outside the main stratification $T_N \approx 3500-7000$ s.

3 Observations of directly and indirectly measured w

3.1 North Sea

In the strongly stratified summertime central North Sea vertical motions are generally weak O(10⁻² m s⁻¹) and have a dominant tidal periodicity (Fig. 3a). However, these tidal w-motions do not represent free internal waves. This is evident in Fig. 4a–c, where only below the lower pycnocline, in the near-bottom layer, the first two terms in Eq. (1) have the same magnitude, but with opposing signs and phase. As a result, a heat balance can only be achieved via horizontal advection or other terms. In contrast, at the depth of the lower, most stratified, pycnocline, the first two terms do have equal signs, but the magnitude of the vertical advection term is O(10) times the local temperature time derivative (Fig. 4b). This is also found in the upper pycnocline, where additionally the phase difference between the two terms varies strongly with time (Fig. 4a). As
a result, at all three different levels the tidal variations are dominantly governed by





1998).

This is not so for small-scale internal "waves". In the overall picture (Fig. 3a), occasional very thin lines can be observed in *w*, e.g., around mid-depth at days 194.8 (Fig. 3b) and 198.1, and near the bottom, e.g., at days 200.5 (Fig. 3c) and 201.1. ⁵ Focusing on the time interval with most pronounced w-amplitudes (Fig. 4d), the first two terms of Eq. (1) have the same [order of] magnitude, as far as can be established because the 5-min sampled temperature data do alias the very high frequency motions (e.g., around day 194.82). However, the start of the time interval of substantial high-frequency motions (day 194.7) shows a π -phase difference for motions that have a period of 1900±100 s. This evidences horizontal advection and diffusion or dominant quadratic and triple derivative terms, as in the KdV-equation describing non-linear

- nant quadratic and triple derivative terms, as in the KdV-equation describing non-linear solitary waves (e.g., Helfrich and Melville, 1986), prevailing over free [linear] wave propagation. However, from a sudden transition at day 194.75 onwards the shorter scale motions have periods of 1500 decreasing to 430 s and the first two terms in Eq. (1)
- ¹⁵ have the same sign and magnitude, as far as can be inferred from the shortest period waves that are under-sampled by the thermistor string. As a result, these latter motions describe more or less linear wave propagation for which Eq. (1) can be used to estimate w from temperature data. Data were too noisy to properly evaluate Eq. (1) for the period in Fig. 3c.

²⁰ The above general lack of Eq. (1) describing directly observed *w* is confirmed in the spectral domain (Fig. 5). In contrast with open ocean data (Fig. 1), the overall spectra of temperature-inferred w and ADCP-w poorly match for the North Sea data, especially near the semidiurnal frequency (Fig. 5a). Despite the small amplitudes, ADCP's *w*estimate is significantly exceeding noise levels. Only for the small periods of Fig. 3b some comparison is found between ADCP-*w* and temperature-inferred *w*, albeit mostly for small-scale *N* in the lower pycnocline, T_N =420 s (Fig. 5b). It is noted that the best spectral amplitude comparison for large-scale N is found between pycnocline temperature variations and near-bottom ADCP *w*-estimate. ADCP's *w* in the pycnocline shows 5, 103-121, 2008

Measurement of vertical motions in ocean

H. van Haren





larger amplitudes. This suggests that the bottom boundary layer drives these linear

pycnocline motions, but that the enforcement of the pycnocline w(N) peak is highly non-linear and dominated by the first few periods (see Fig. 4d). Also in the entire record mean spectrum (Fig. 5a) lower-pycnocline temperature-inferred w correspond best with the level of near-bottom ADCP-w, but only for σ >5 cpd≈4 f_h , f_h =2 Ω cos φ the horizontal component of the Earth rotational vector Ω at latitude φ . This suggests linear waves between N and this cut-off and non-linear motions for lower frequencies

linear waves between N and this cut-off and non-linear motions for lower frequencies including tidal and inertial frequencies.

Estimates of turbulent diffusion indicate values of about $K=6\cdot10^{-4}$ m² s⁻¹ across the pycnocline during the passage of the high-frequency [non-]linear wave, which gives values of $3-4\cdot10^{-5}$ m² s⁻¹ integrated over a tidal period (van Haren et al., 1999). This overall value is sufficient for nutrient transport generating the summer phytoplankton bloom, and these occasional near-*N* waves also govern the slow heating of the nearbottom layer during spring and autumn. Comparable *K*-values are observed on the Malin Shelf and attributed to non-linear high-frequency waves (Inall et al., 2000).

¹⁵ For all of the above evaluations of Eq. (1), <10% improvement is obtained using instead of $\partial T(t)/\partial z$ its time mean (Fig. 4). However, the influence of the time dependence is larger in a region where strongly turbulent non-linear "waves" or bores prevail, like on a FSC-slope.

3.2 Faeroe-Shetland Channel

horizontal currents.

5

²⁰ Similar vertically striped, generally mode-1, *w*-motions are observed albeit in irregularly occurring groups in the FSC and associated with non-linear wave trains moving up the slope (Hosegood and van Haren, 2004). In the FSC, vertical currents associated with high-frequency motions are larger (by a factor of 3–4) than in the central North Sea, commensurate the equally weaker stratification that supports them. As a result, one could "conclude" that $|w| \sim N^{-1}$, rather than $\sim N^{-1/2}$, which is more common for

Despite the very accurate thermistor string (Table 2 for its characteristics) the vigorous motions cause substantial turbulent overturning, i.e. by definition not linear waves.

OSD

5, 103–121, 2008

Measurement of vertical motions in ocean





This explains the difficulty in evaluating Eq. (1) using these data and spikes are regularly large, especially in temperature-inferred w (Fig. 6c).

However, the frontal upward *w*-jet, exceeding 0.1 m s⁻¹, is detected by both inferred and direct measurements, which is surprising when compared with the first "wave" ⁵ period of small-scale North Sea motions (Fig. 4d). The small phase lag of 30–60 s between the differently observed jet in the FSC (Fig. 6c) is attributable to the ADCP's beam spread in combination with thermistor string motions due to current drag. Regular large-scale, indeed ~1500 s~ T_N period, and occasionally very high frequency motions, are adequately described by Eq. (1). The best comparison with ADCP's w is obtained using $\partial T(t)/\partial z$ rather than its time mean, which implies that a non-linear term is needed to dampen some of the high-frequency spiking, but in the vertical direction

is needed to dampen some of the high-frequency spiking, but in the vertical direction only. Unfortunately, the data do not allow the evaluation of horizontal non-linear terms, responsible for the (turbulent) spikes during other periods. The local turbulent diffusivity is large, $K \sim O(10^{-1} \text{ m}^2 \text{ s}^{-1})$ (Hosegood and van Haren, 2004), but the passage is so rapid that the value integrated over a tidal period is similar to the one above that was estimated for the North Sea.

4 Discussion

It has been shown that direct *w*-observations describe realistic ocean phenomena that have horizontal length scales larger than an ADCP's beam spread, being 10 m here.

- The present data do not [directly] represent free convection, but rather [non-]linear internal waves or frontal advection (cf. Fig. 4). A strong association between the motions' periodicity and depth of maximum amplitude with stratification favours an explanation in terms of internal waves, e.g. Fig. 3b. This has been confirmed using Eq. (1), but it is found that this standard method to compute *w* from *T*-data does not work in a tidal advection area like the North Sea or in an area where non-linear motions provail over
- ²⁵ advection area like the North Sea or in an area where non-linear motions prevail over linear [high-frequency] waves.

The observation that $\partial T(t)/\partial z$ is better used than its time mean in turbulent near-

OSD 5, 103-121, 2008 Measurement of vertical motions in ocean H. van Haren **Title Page** Introduction Abstract Conclusions References Tables Figures Back Close Full Screen / Esc **Printer-friendly Version** Interactive Discussion

bottom areas and that non-linear near-*N* motions dominate the internal "wave" spectrum near its upper bound in the ocean interior may also explain the discrepancy in *w*-spectra from the Bay of Biscay (Fig. 1). Presumably, weakly non-linear waves likewise dominate the open ocean continuum as well, possibly as interfacial waves like in the North Sea, because the ADCP's w-data exceed noise level and temperature-inferred

⁵ North Sea, because the ADCP's w-data exceed noise level and temperature-inferred *w* at frequencies between tidal harmonics, e.g. between semidiurnal and fourth-diurnal bands in Fig. 1.

The lack of dominant linear high-frequency waves may explain the quarter-wave period discrepancy between T and w observations found by Hallock and Field (2005). It certainly explains East China Sea observations by Lee et al. (2006), who found 3 large "waves" of depression before a group of about 10 higher frequency waves, just like

10

in Fig. 3b. As for the North Sea observations presented here, the sudden change in phase difference between time derivative and vertical advection terms in Eq. (1) after the first two wave periods bears some resemblance with laboratory experiments on

- the generation of mode-2 internal waves following an intrusion in a linearly stratified fluid (Amen and Maxworthy, 1980). Although no *w*-observations were presented by these authors, the gravitational collapse of a mixed region generated two mode-2 solitary waves followed by a train of constant amplitude mode-1 waves of approximately doubled frequency. When sufficiently strong, mode-2 waves can appear as closed partour "waves" with importance for transporting material (Davis and Asrivas, 1067).
- ²⁰ contour "waves", with importance for transporting material (Davis and Acrivos, 1967). Here, they are only observed in limited form, at the top of the bottom-boundary layer (Fig. 3), and, peculiarly, [two] mode-1 waves *precede* mode-2 waves. More modeling is required to establish the generation of such waves, although it has been shown that mode-2 waves can [occasionally] follow a mode-1 wave breaking on a sloping shelf (Helfrich, 1992).

More modeling is also required to establish whether a non-zero limit value exists to diapycnal diffusivity across strong stratification, as suggested by the tidal mean value found in different regions presented here and which are apparently induced by high-frequency non-linear motions.

OSD 5, 103–121, 2008 Measurement of vertical motions in ocean H. van Haren





Similarly, more modeling is required to establish the large discrepancy between directly measured and temperature-inferred w at sub-inertial frequencies. Certainly, the assumption underlying Eq. (1) eliminates gyroscopic waves, which are prevalent in homogeneous layers in the frequency range [0, 2 Ω]. These waves show relatively large w that can be directly measured and which extend spectrally to about $\sigma=4f_b$ before

- dropping into noise (van Haren and Millot, 2005). They are not measured by temperature sensors in homogeneous layers. In contrast in a stratified ocean, the internal wave band drops off for $\sigma < 4f_h$, but faster for temperature-inferred w than ADCP's *w* (Fig. 1a). Apparently also small-scale advection or eddies are not incorporated by 10 Eq. (1), which gives the impression of a strict internal wave band consisting only of
- ¹⁰ Eq. (1), which gives the impression of a strict internal wave band consisting only of tidal harmonic motions dropping off for $\sigma < f$, but which is unrealistic in terms of oceanic low and high-mode w.

Acknowledgements. The assistance of the crew of R/V Pelagia is highly appreciated. I thank T. Hillebrand for mooring preparation. Integrated North Sea Program (INP) and Processes above Continental Slopes (PROCS) were funded in part by the Netherlands Organization for the advancement of Scientific Research (NWO).

References

15

25

- Amen, R. and Maxworthy, T.: The gravitational collapse of a mixed region into a linearly stratified fluid, J. Fluid Mech., 96, 65–80, 1980.
- Davis, R. E. and Acrivos, A.: Solitary internal waves in deep water, J. Fluid Mech., 29, 593–607, 1967.
 - Hallock, Z. R. and Field, R. L.: Internal-wave energy fluxes on the New Jersey Shelf, J. Phys. Oceanogr., 35, 3–12, 2005.

Helfrich, K. R.: Internal solitary wave breaking and run-up on a uniform slope, J. Fluid Mech., 243, 133–154, 1992.

Helfrich, K. R. and Melville, W. K: On long nonlinear internal waves over slope-shelf topography, J. Fluid Mech., 167, 285–308, 1986.



- Hosegood, P. and van Haren, H.: Near-bed solibores over the continental slope in the Faeroe-Shetland Channel, Deep-Sea Res. Pt. II, 51, 2943–2971, 2004.
- Howarth, M. J.: The effect of stratification on tidal current profiles, Cont. Shelf Res., 18, 1235–1254, 1998.
- ⁵ Inall, M. E., Rippeth, T. P., and Sherwin, T. J.: Impact of nonlinear waves on the dissipation of internal tidal energy at a shelf break, J. Geophys. Res., 105, 8687-8705, 2000.
 - Krauss, W.: Methoden und Ergebnisse der Theoretischen Ozeanographie. II Interne Wellen. Gebrueder Borntraeger, Berlin, 248 pp., 1966.
 - Lee, J. H., Lozovatsky, I., Jang, S.-T., Jang, C. J., Hong, C. S., and Fernando, H. J. S.: Episodes
- of nonlinear internal waves in the northern East China Sea, Geophys. Res. Lett., 33, L18601, doi:10.1029/2006GL027136, 2006.
 - van Aken, H. M., van Haren, H., and Maas, L. R. M.: The high-resolution vertical structure of internal tides and near-inertial waves, measured with an ADCP over the continental slope in the Bay of Biscay, Deep-Sea Res. I, 54, 533–556, 2007.
- van Haren, H. and Millot, C.: Gyroscopic waves in the Mediterranean Sea, Geophys. Res. Lett., 32, L24614, doi:10.1029/2005GL023915, 2005.
 - van Haren, H., Maas, L., Zimmerman, J. T. F., Ridderinkhof, H., and Malschaert, H.: Strong inertial currents and marginal internal wave stability in the central North Sea, Geophys. Res. Lett., 26, 2993–2996, 1999.
- van Haren, H., Groenewegen, R., Laan, M., and Koster, B.: A fast and accurate thermistor string, J. Atmos. Ocean. Technol., 18, 256–265, 2001.

5, 103-121, 2008

Measurement of vertical motions in ocean

Title Page					
Abstract	Introduction				
Conclusions	References				
Tables	Figures				
	►I				
•	•				
Back	Close				
Full Screen / Esc					
Printer-friendly Version					
Interactive Discussion					



5, 103–121, 2008

Measurement of vertical motions in ocean

H. van Haren

Title Page					
Abstract	Introduction				
Conclusions	References				
Tables	Figures				
14	►I				
Back	Close				
Full Screen / Esc					
Printer-friendly Version					
Interactive Discussion					



Table 1. RDI-broadband uplooking-ADCP mooring details. INP is in the central North Sea,PROCS in the Faeroe-Shetland Channel.

	INP summer	PROCS spring
Data start	13/07/1994	19/04/1999
Data end	21/07/1994	01/05/1999
Latitude	54°25′ N	60°49′ N
Longitude	004°02′ E	–003°00′ W
Water depth (m)	45	494
Vertical slant angle (θ)	20°	20°
Transmit frequency	600 kHz	600 kHz
Transmission length	1.9 m	1.2 m
Instrument depth	0.3 m ab. bottom	1.7 m a.b.
First bin	41.9 m	491 m
# bins×bin size	90×0.5 m	60×0.5 m
Ensemble period	150 s	30 s
Std u, v	0.006 m s ⁻¹ /ens	0.012 m s ⁻¹ /ens
Std w, e	$0.002{ m ms^{-1}/ens}$	$0.004{\rm ms^{-1}/ens}$

Table 2. Thermistor string mooring details. AA=Aanderaa, NIOZ=Netherlands Institue for Sea Research design (van Haren et al., 2001). The modified AA-thermistor string has standard sensors that are connected to aluminium plates cut in the rubber tube that holds the entire string and strength member. This decreases the response time.

	#sensors	depths	samp.int	au-resp	resolution	accuracy
INP summer						
AAstandard "upp"	10	3–21 m	600 s	60 s	0.02°C	0.1°C
AAmodified "mid"	11	21–31 m	300 s	10 s	0.02°C	0.1°C
AAstandard "low"	11	23–43 m	1800 s	60 s	0.02°C	0.1°C
PROCS spring						
NIOZ-1	32	461–492 m	30 s	0.25 s	50 μK	< 0.5 mK

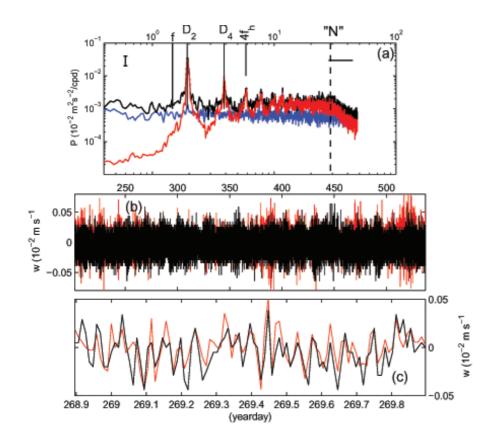
OSD

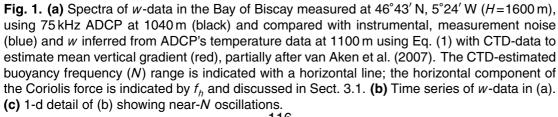
5, 103–121, 2008

Measurement of vertical motions in ocean

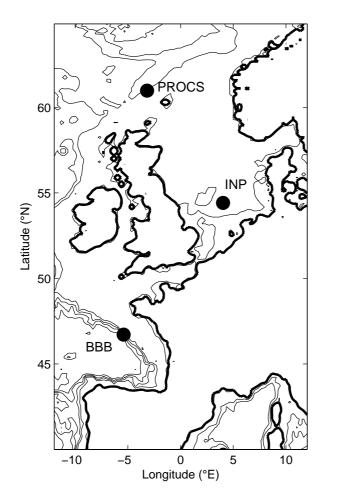












5, 103–121, 2008

Measurement of vertical motions in ocean

H. van Haren





Fig. 2. Mooring locations (•) in North Sea (INP), Faeroe-Shetland Channel (PROCS) and Bay of Biscay (BBB).

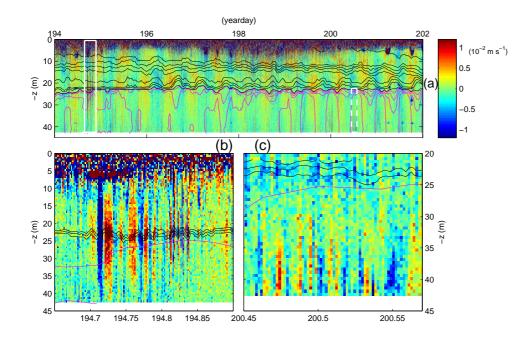


Fig. 3. Summertime INP time series. **(a)** Vertical current data with hourly smoothed temperature contours every 1°C between 10-18°C (black) and every 0.2°C between 9.1-9.9°C (purple). The solid rectangle indicates the period of panel **(b)**, the dashed rectangle that of panel **(c)**. (b) Detail of (a) with high-frequency waves near mid-depth and only one purple contour (9.5°C), (c) Detail of (a) with high-frequency waves near the bottom and only one purple contour (9.3°C). Note different *z*,*t* scales compared to (b). In (a–b) the brown band between 0 and about -7 m represents bad (surface reflection side-band) ADCP-data.

OSD

5, 103–121, 2008







