

## Reference case 0

Length  $b = 100$  km (exponential variation); Strickler coefficient  $K = 45 \text{ m}^{1/3}\text{s}^{-1}$ ; nonlinear friction.

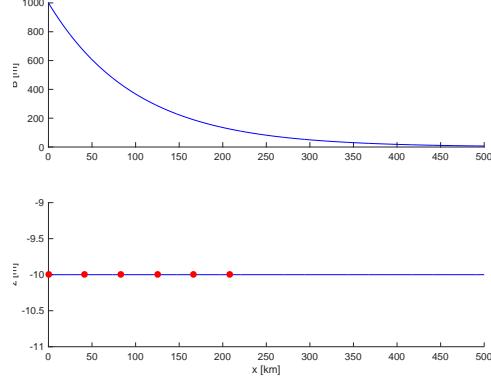


Figure 1: Longitudinal profiles of width and bottom. Dots indicates the locations where the temporal behaviour is shown in figure 3.

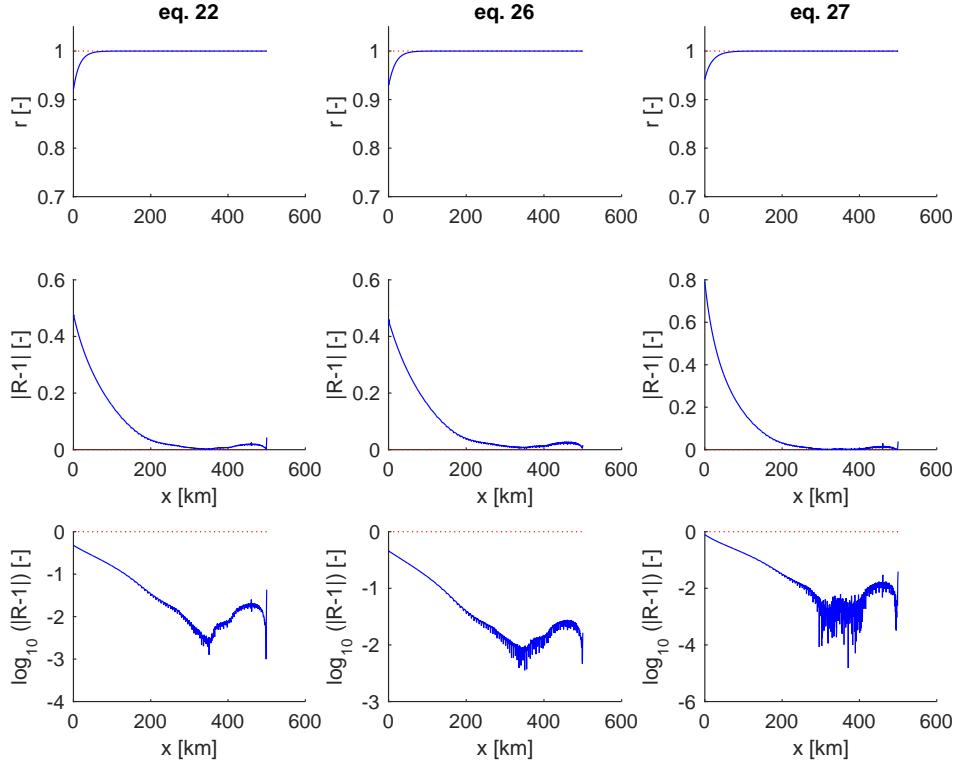


Figure 2: Longitudinal variation of the correlation coefficient  $r$  (first row) and of the two different functions of the ratio  $R$  between right hand side and left hand side of equations 22, 26 and 27 in the manuscript, respectively  $|R - 1|$  and  $\log_{10}(|R - 1|)$ .

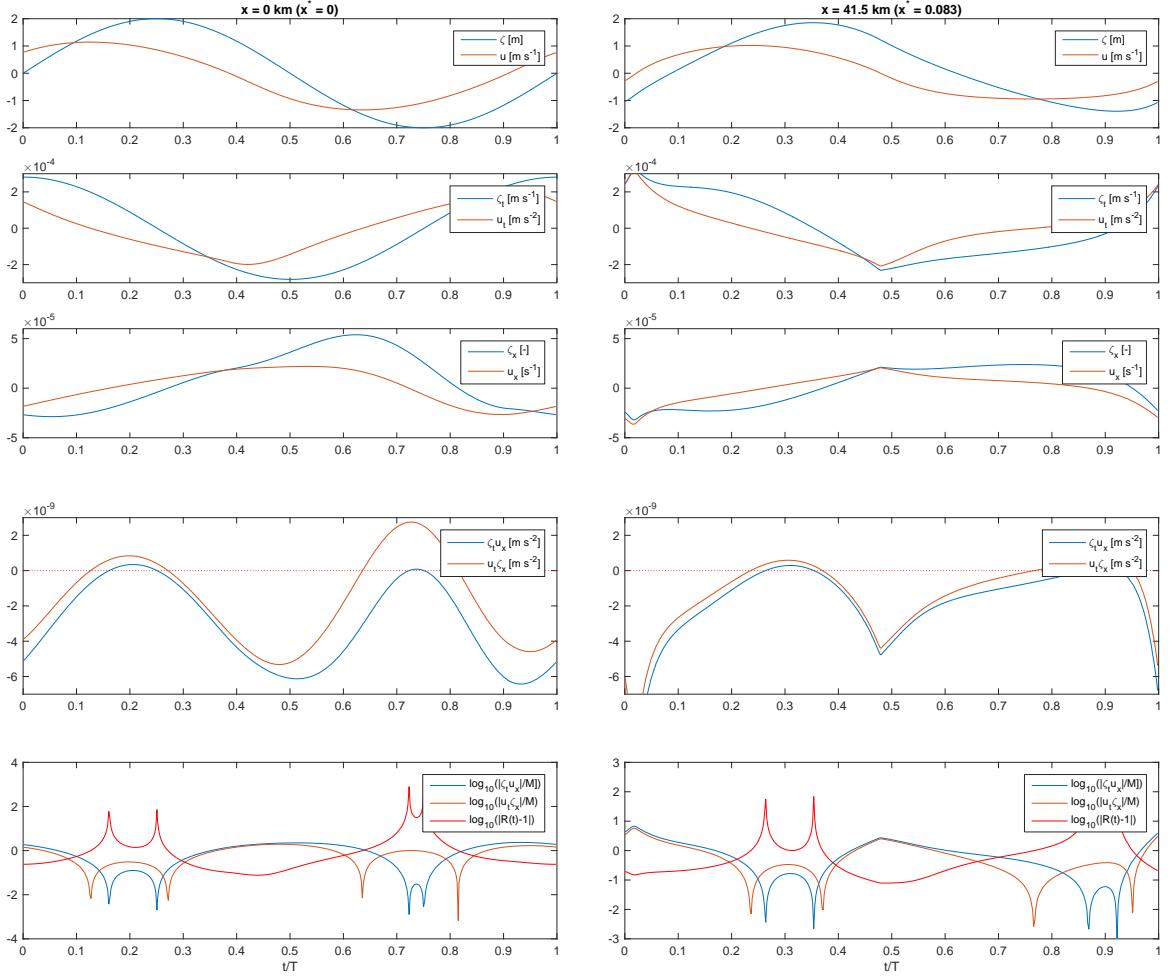


Figure 3: Temporal variation of  $\zeta$  and  $u$  (first plot),  $\zeta_t$  and  $u_t$  (second plot),  $\zeta_x$  and  $u_x$  (third plot),  $\zeta_t u_x$  and  $u_t \zeta_x$  (fourth plot), and  $\log_{10}(|\zeta_t u_x|/M)$ ,  $\log_{10}(|u_t \zeta_x|/M)$ ,  $\log_{10}(|R(t)-1|)$  (fifth plot, where  $R(t) = (u_t \zeta_x)/(\zeta_t u_x)$  and  $M$  is the mean of the tidally averages of  $|\zeta_t u_x|$  and  $|u_t \zeta_x|$ ), in  $x = 0$  km and  $x = 41.5$  km.

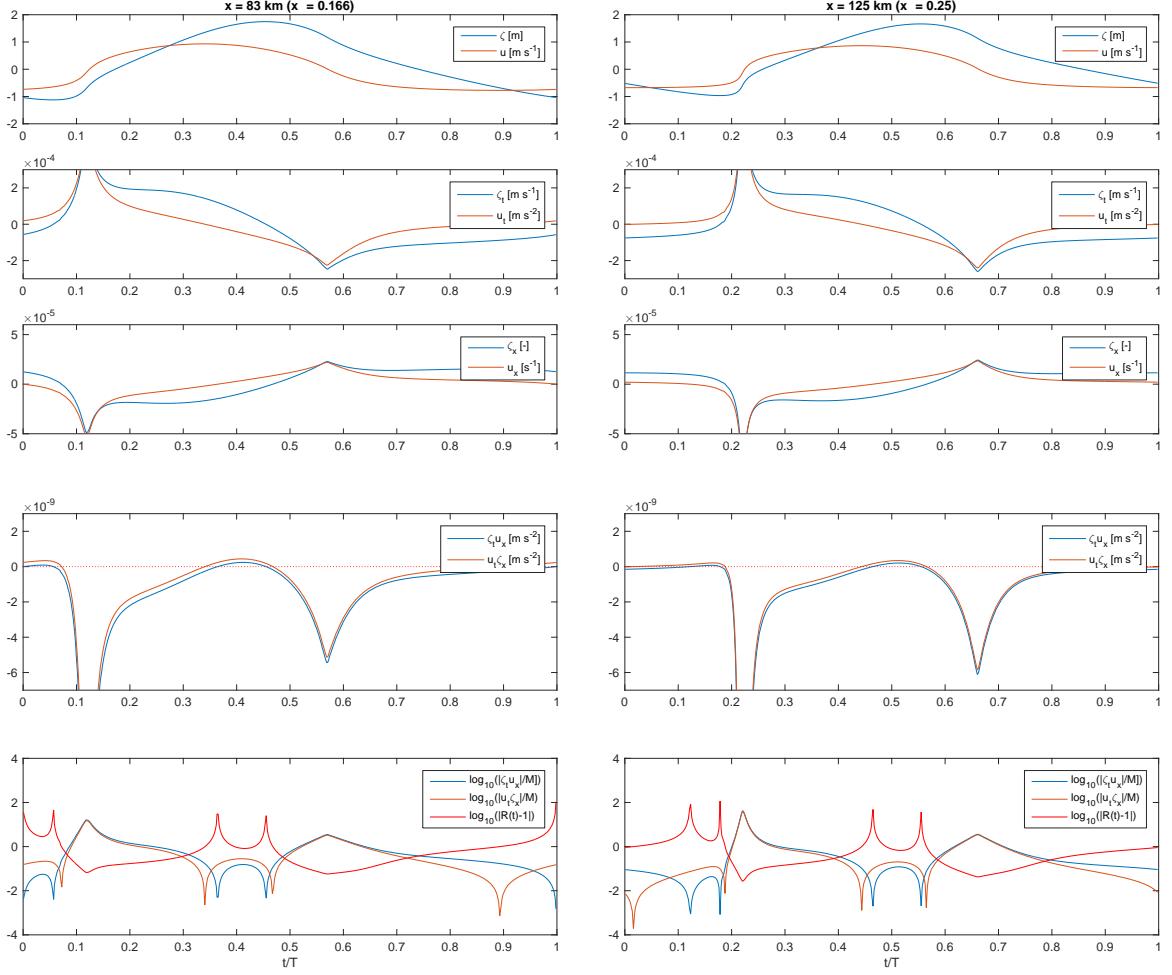


Figure 4: Temporal variation of  $\zeta$  and  $u$  (first plot),  $\zeta_t$  and  $u_t$  (second plot),  $\zeta_x$  and  $u_x$  (third plot),  $\zeta_t u_x$  and  $u_t \zeta_x$  (fourth plot), and  $\log_{10}(|\zeta_t u_x|/M)$ ,  $\log_{10}(|u_t \zeta_x|/M)$ ,  $\log_{10}(|R(t)-1|)$  (fifth plot, where  $R(t) = (u_t \zeta_x)/(\zeta_t u_x)$ ) (fifth plot, where  $R(t) = (u_t \zeta_x)/(\zeta_t u_x)$  and  $M$  is the mean of the tidally averages of  $|\zeta_t u_x|$  and  $|u_t \zeta_x|$ ), in  $x = 83$  km and  $x = 125$  km.

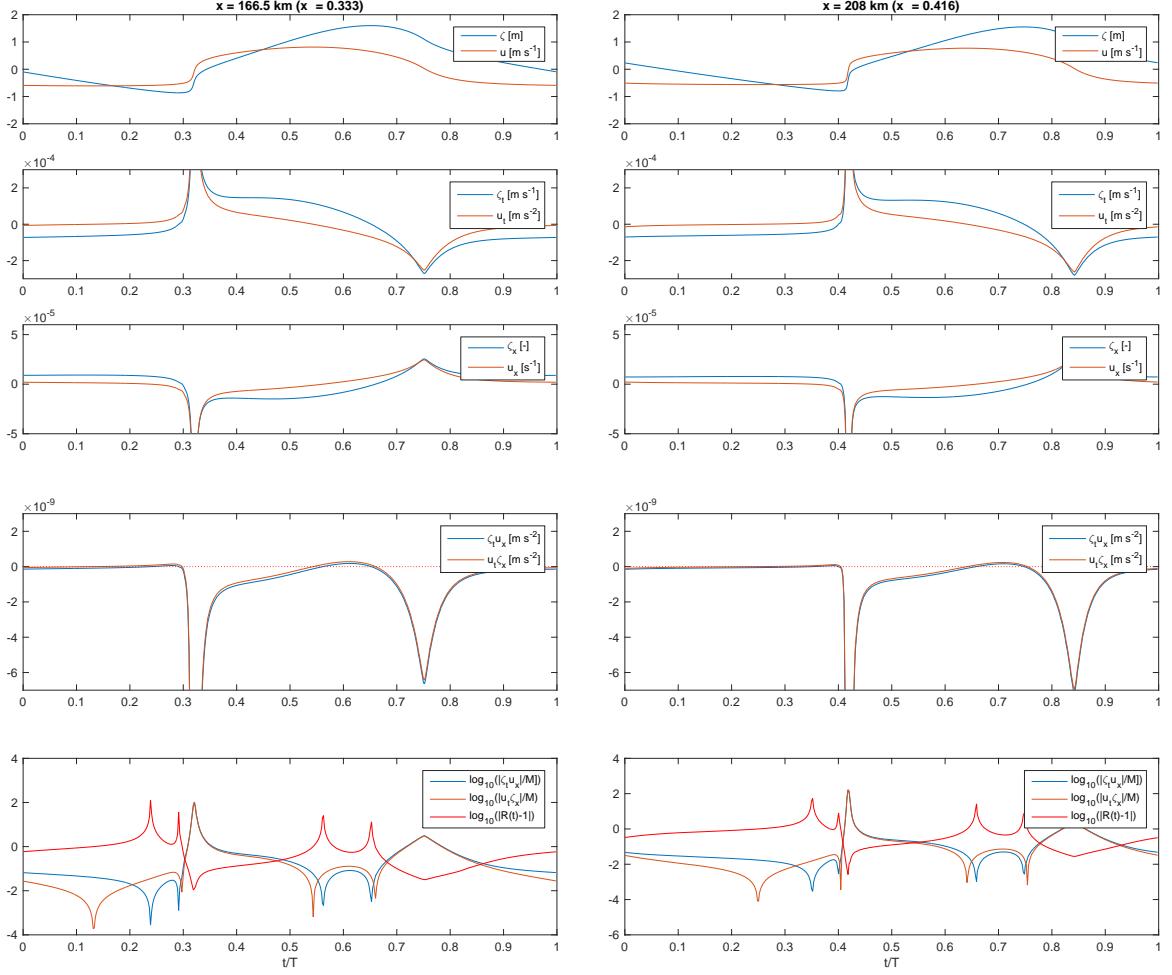


Figure 5: Temporal variation of  $\zeta$  and  $u$  (first plot),  $\zeta_t$  and  $u_t$  (second plot),  $\zeta_x$  and  $u_x$  (third plot),  $\zeta_t u_x$  and  $u_t \zeta_x$  (fourth plot), and  $\log_{10}(|\zeta_t u_x|/M)$ ,  $\log_{10}(|u_t \zeta_x|/M)$ ,  $\log_{10}(|R(t)-1|)$  (fifth plot, where  $R(t) = (u_t \zeta_x)/(\zeta_t u_x)$  and  $M$  is the mean of the tidally averages of  $|\zeta_t u_x|$  and  $|u_t \zeta_x|$ ), in  $x = 166.5$  km and  $x = 208$  km.

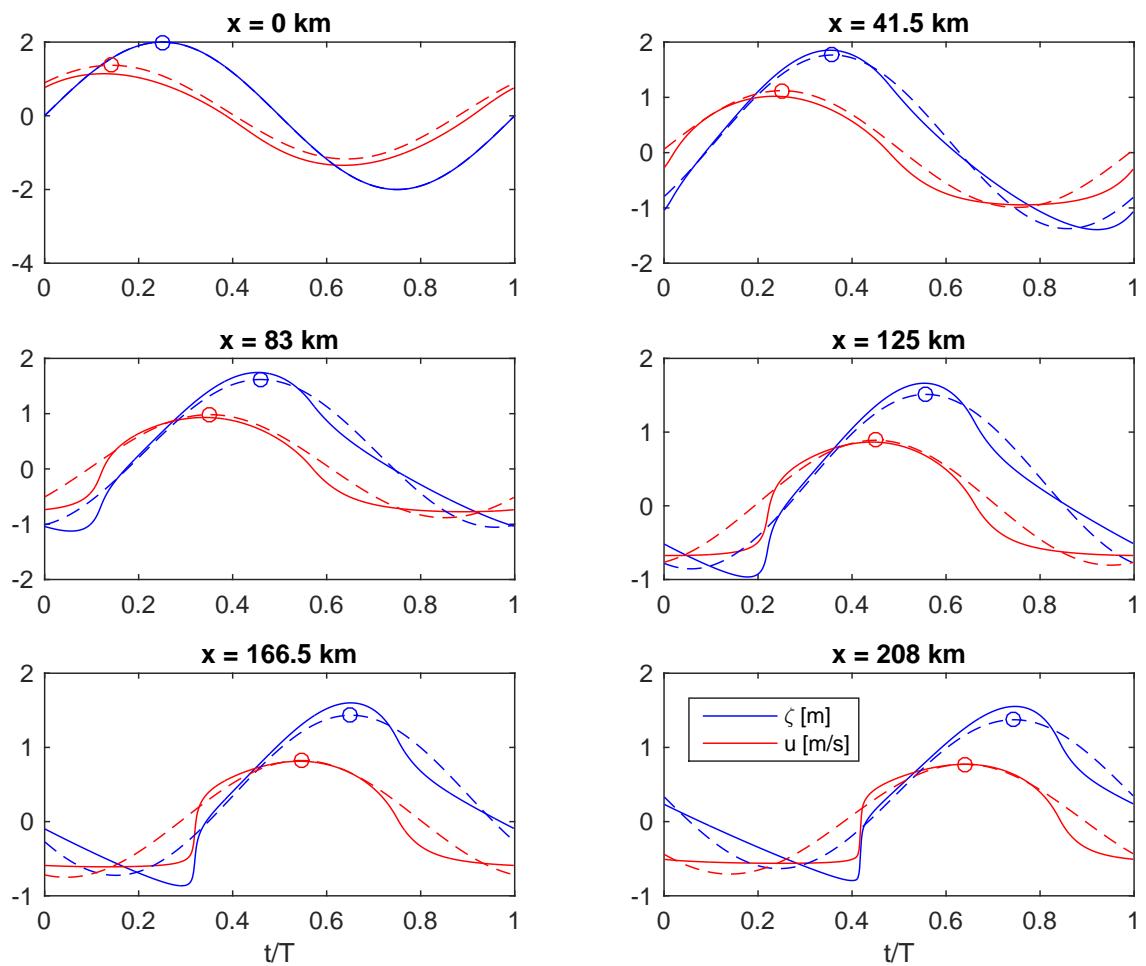


Figure 6: Tidal waves and Fourier series truncated at the first harmonic. Circles indicate the maxima of the dominant tidal component, from which it is possible to detect the phase lag  $u-\zeta$ .

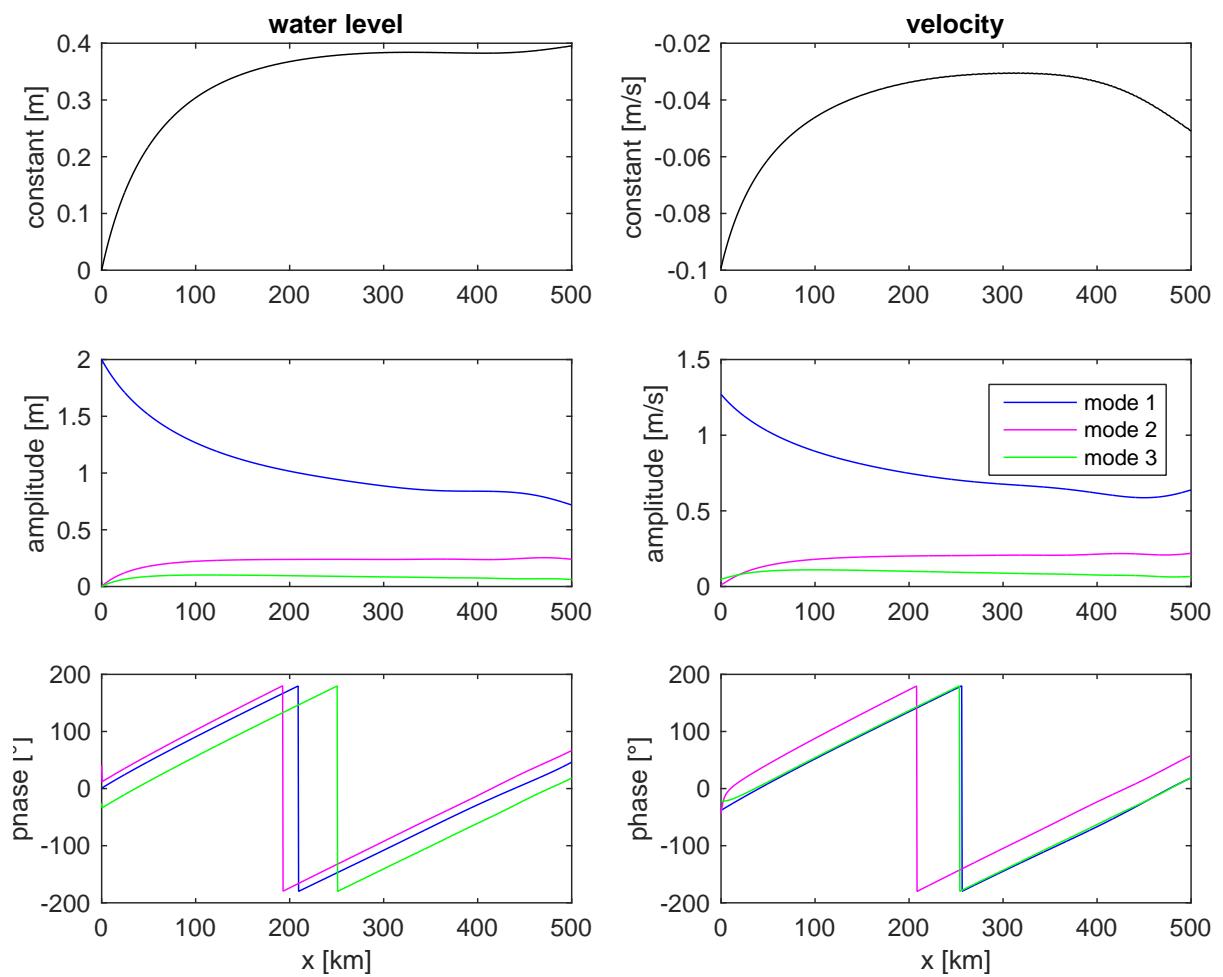


Figure 7: Fourier analysis of tidal wave. From top to bottom: constant term, amplitudes, phases of first three modes. Left column: water level  $\zeta$ ; right column: velocity  $u$ .

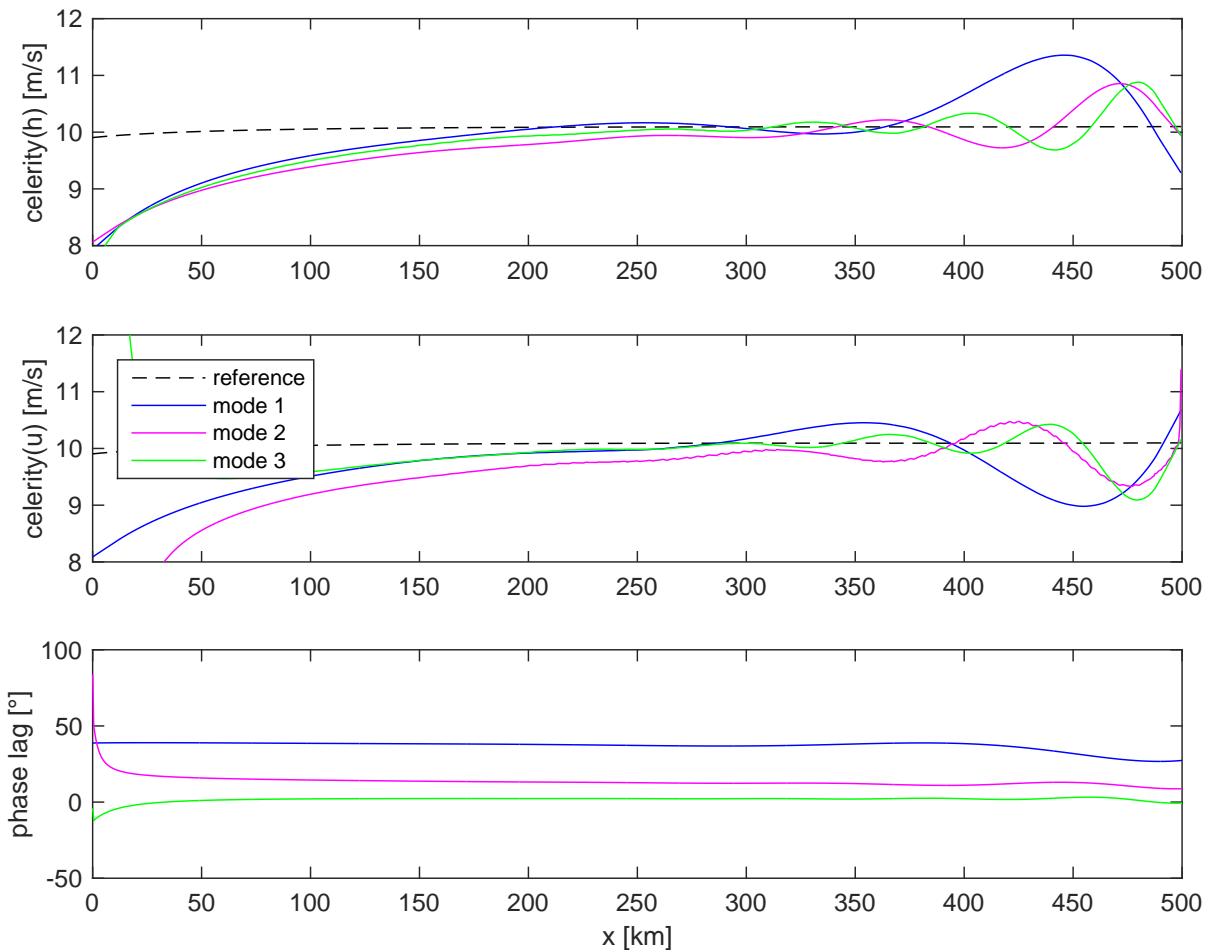


Figure 8: Wave celerity for water level  $\zeta$ , for velocity  $u$ , phase lag  $u-\zeta$ . Colors refer to the first three modes; black dashed line to wave celerity in a frictionless prismatic channel.

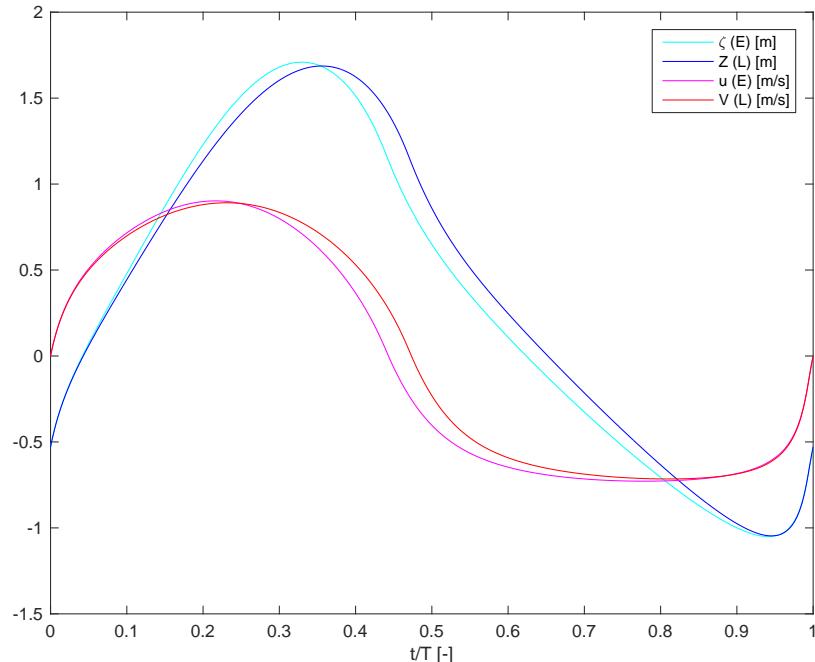


Figure 9: Lagrangean water level  $Z$  and velocity  $V$  compared with Eulerian values  $\zeta$  and  $u$  in  $x = 100$  km.

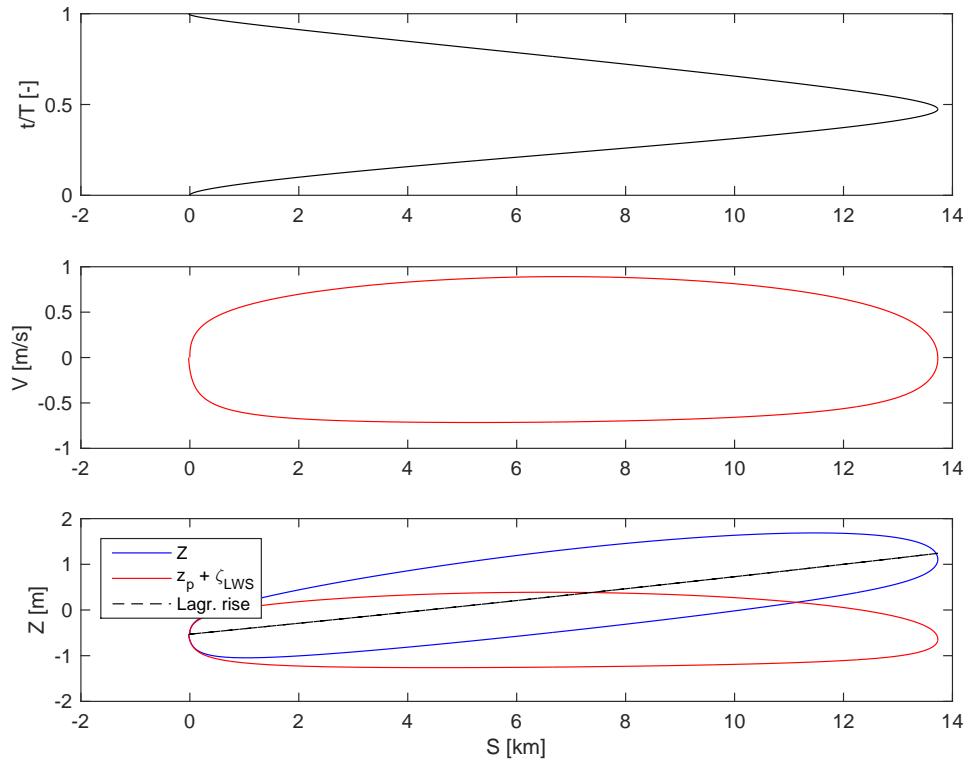


Figure 10: Lagrangean displacement  $S$  in time (first plot) and ellipses  $V$ - $S$  (second plot) and  $Z$ - $S$  (third plot).

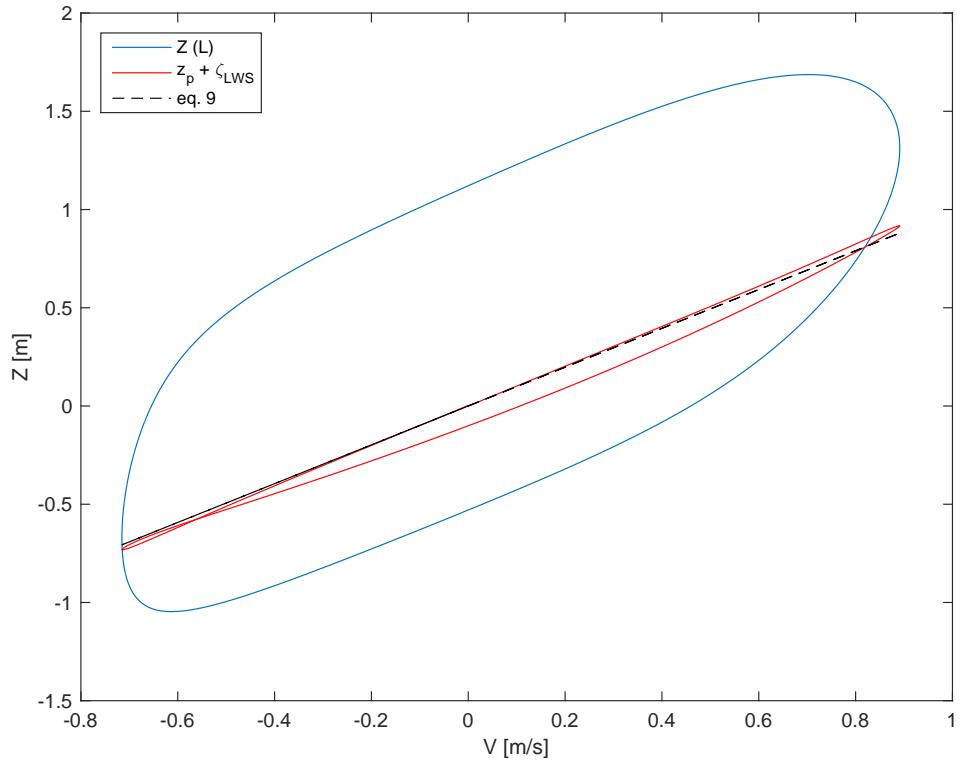


Figure 11: Lagrangean water level against velocity  $V$ :  $Z$  is the actual value,  $z_p + \zeta_{LWS}$  is the transformed water level. Black dashed lines: equation (9).

## Variant 1

Length  $b = 25$  km (exponential variation); Strickler coefficient  $K = 45 \text{ m}^{1/3}\text{s}^{-1}$ ; nonlinear friction.

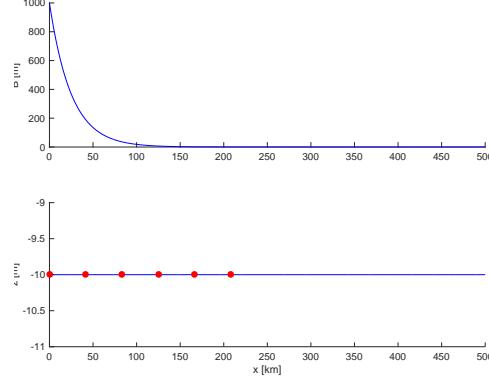


Figure 1: Longitudinal profiles of width and bottom. Dots indicates the locations where the temporal behaviour is shown in figure 3.

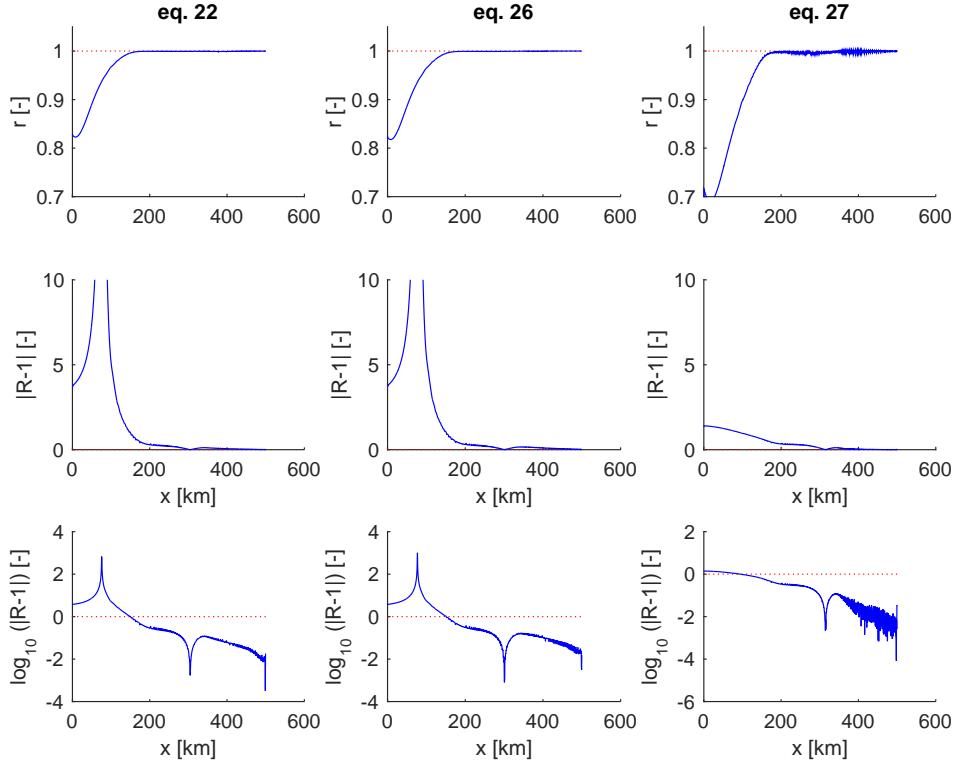


Figure 2: Longitudinal variation of the correlation coefficient  $r$  (first row) and of the two different functions of the ratio  $R$  between right hand side and left hand side of equations 22, 26 and 27 in the manuscript, respectively  $|R - 1|$  and  $\log_{10}(|R - 1|)$ .

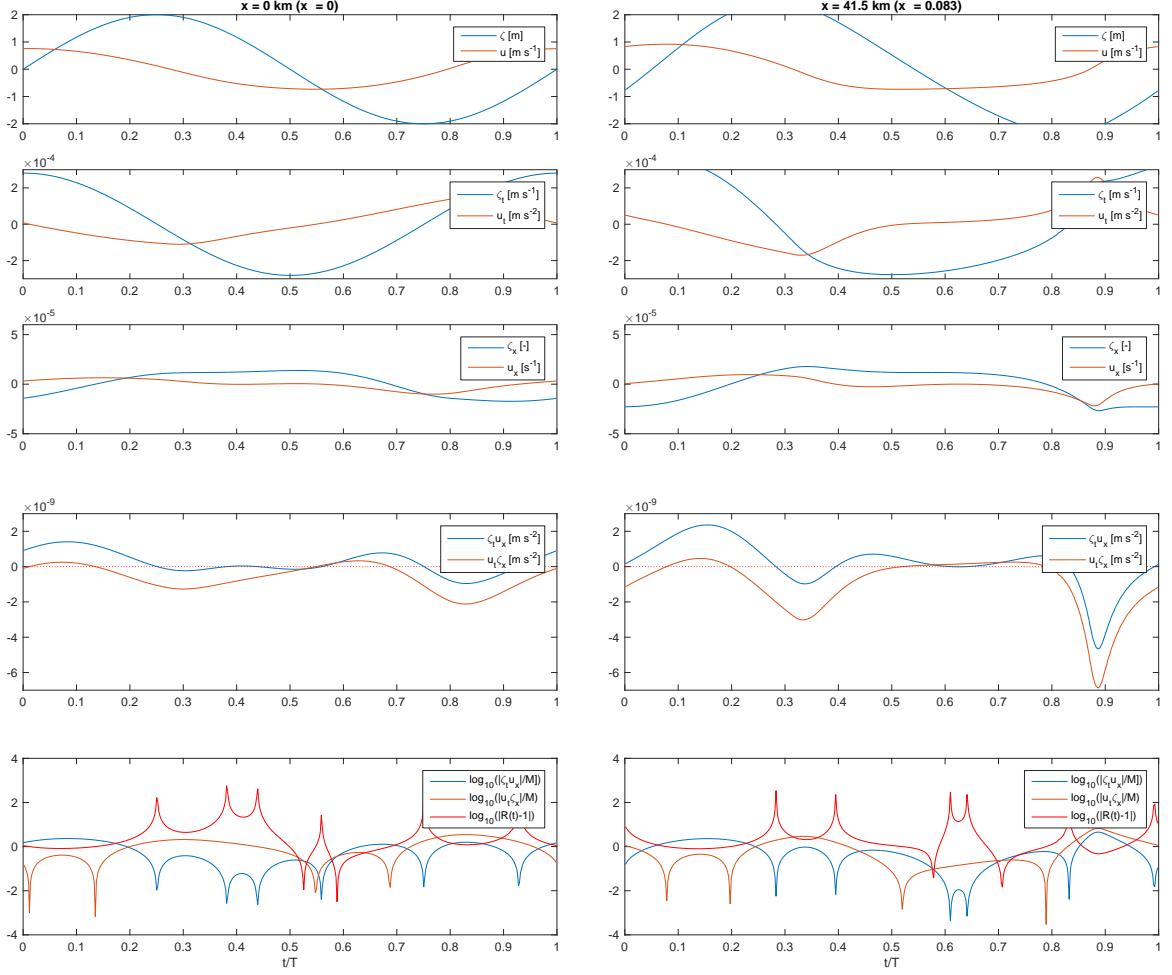


Figure 3: Temporal variation of  $\zeta$  and  $u$  (first plot),  $\zeta_t$  and  $u_t$  (second plot),  $\zeta_x$  and  $u_x$  (third plot),  $\zeta_t u_x$  and  $u_t \zeta_x$  (fourth plot), and  $\log_{10}(|\zeta_t u_x|/M)$ ,  $\log_{10}(|u_t \zeta_x|/M)$ ,  $\log_{10}(|R(t)-1|)$  (fifth plot, where  $R(t) = (u_t \zeta_x)/(\zeta_t u_x)$  and  $M$  is the mean of the tidally averages of  $|\zeta_t u_x|$  and  $|u_t \zeta_x|$ ), in  $x = 0$  km and  $x = 41.5$  km.

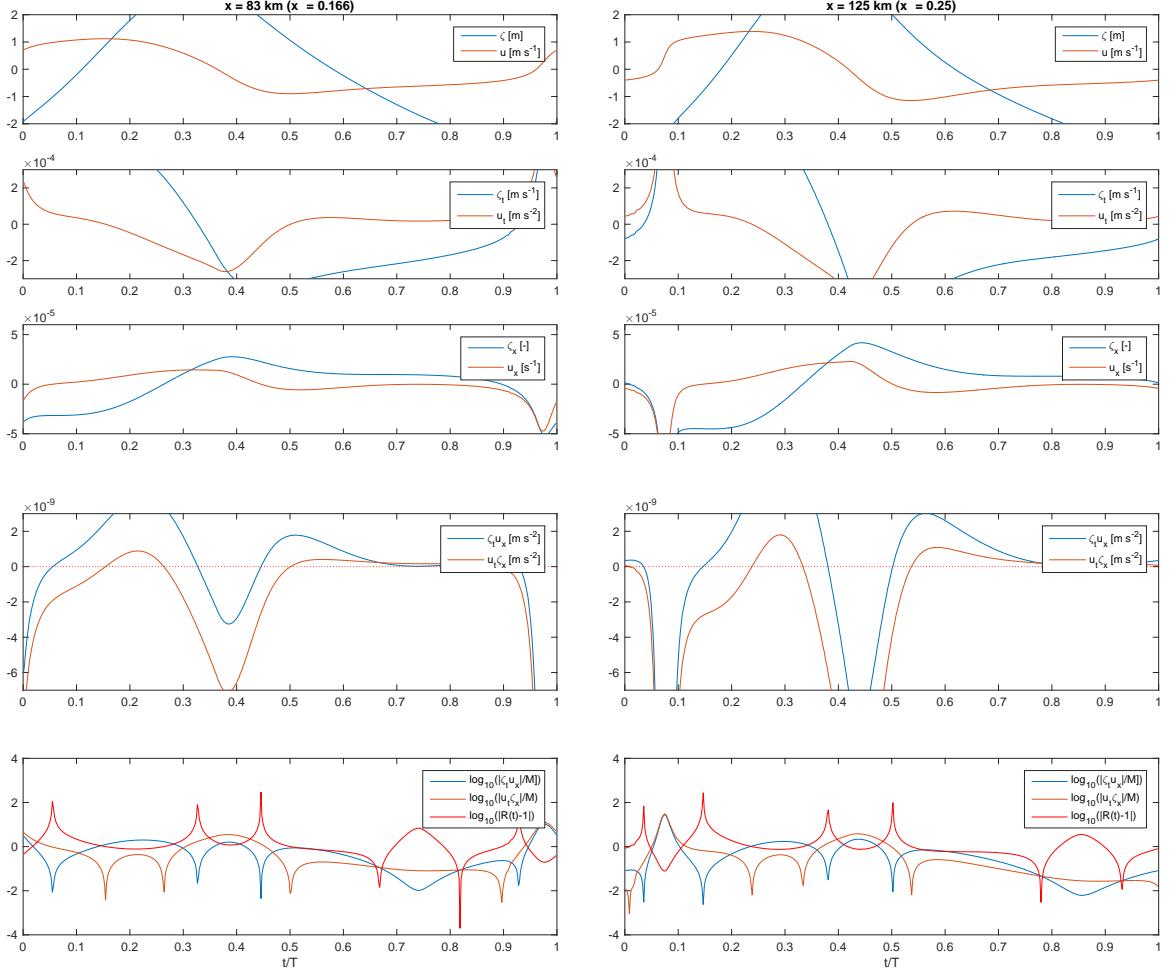


Figure 4: Temporal variation of  $\zeta$  and  $u$  (first plot),  $\zeta_t$  and  $u_t$  (second plot),  $\zeta_x$  and  $u_x$  (third plot),  $\zeta_t u_x$  and  $u_t \zeta_x$  (fourth plot), and  $\log_{10}(|\zeta_t u_x|/M)$ ,  $\log_{10}(|u_t \zeta_x|/M)$ ,  $\log_{10}(|R(t) - 1|)$  (fifth plot, where  $R(t) = (u_t \zeta_x)/(\zeta_t u_x)$ ) (fifth plot, where  $R(t) = (u_t \zeta_x)/(\zeta_t u_x)$  and  $M$  is the mean of the tidally averages of  $|\zeta_t u_x|$  and  $|u_t \zeta_x|$ ), in  $x = 83$  km and  $x = 125$  km.

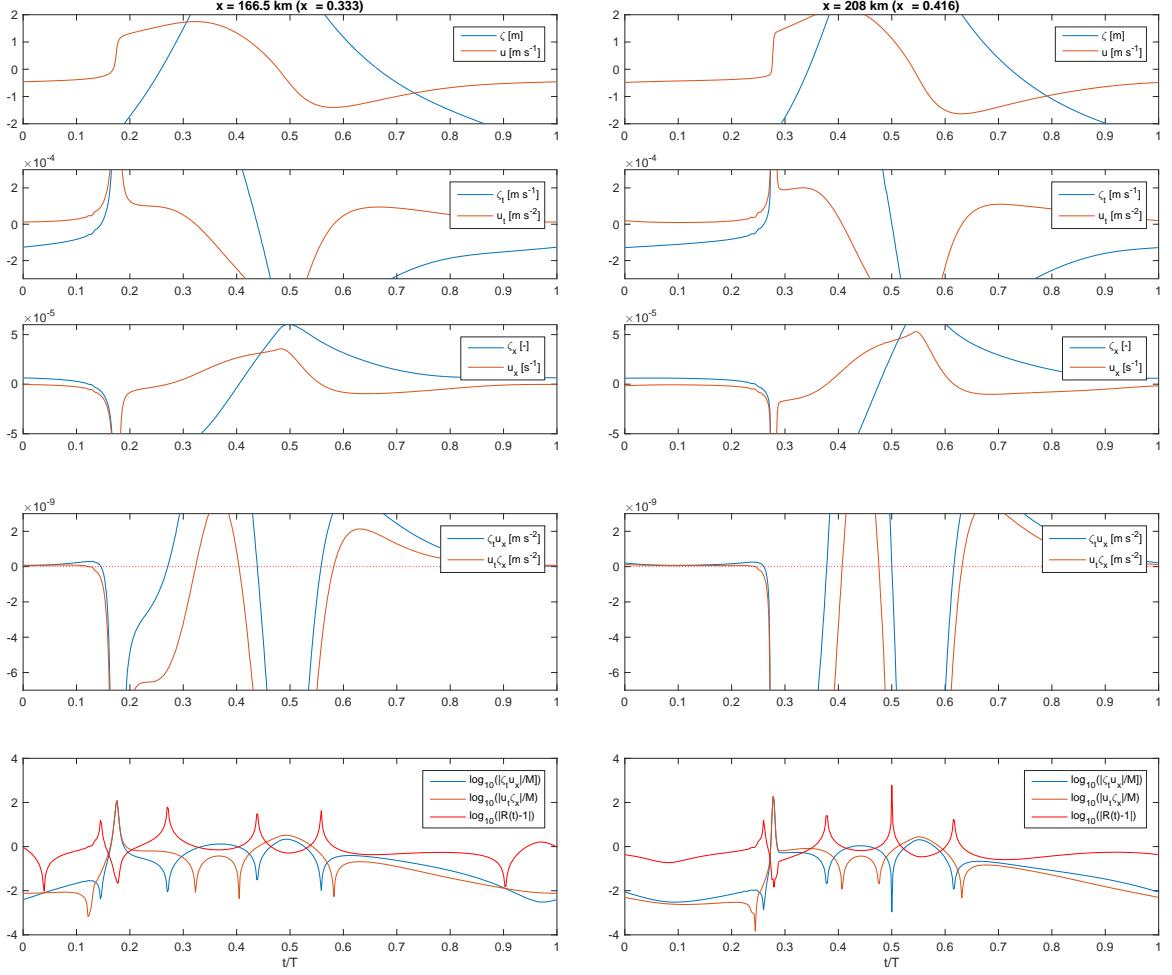


Figure 5: Temporal variation of  $\zeta$  and  $u$  (first plot),  $\zeta_t$  and  $u_t$  (second plot),  $\zeta_x$  and  $u_x$  (third plot),  $\zeta_t u_x$  and  $u_t \zeta_x$  (fourth plot), and  $\log_{10}(|\zeta_t u_x|/M)$ ,  $\log_{10}(|u_t \zeta_x|/M)$ ,  $\log_{10}(|R(t)-1|)$  (fifth plot, where  $R(t) = (u_t \zeta_x)/(\zeta_t u_x)$  and  $M$  is the mean of the tidally averages of  $|\zeta_t u_x|$  and  $|u_t \zeta_x|$ ), in  $x = 166.5 \text{ km}$  and  $x = 208 \text{ km}$ .

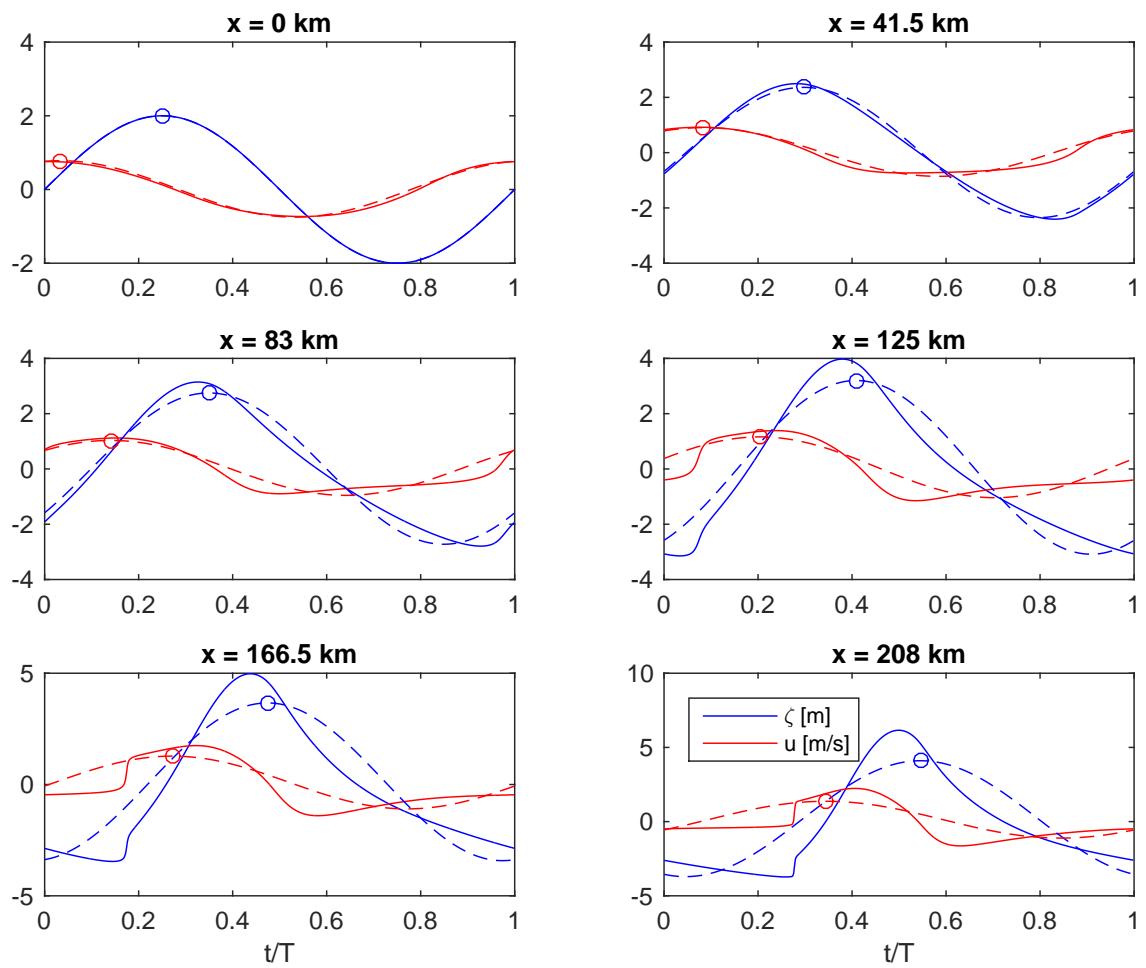


Figure 6: Tidal waves and Fourier series truncated at the first harmonic. Circles indicate the maxima of the dominant tidal component, from which it is possible to detect the phase lag  $u-\zeta$ .

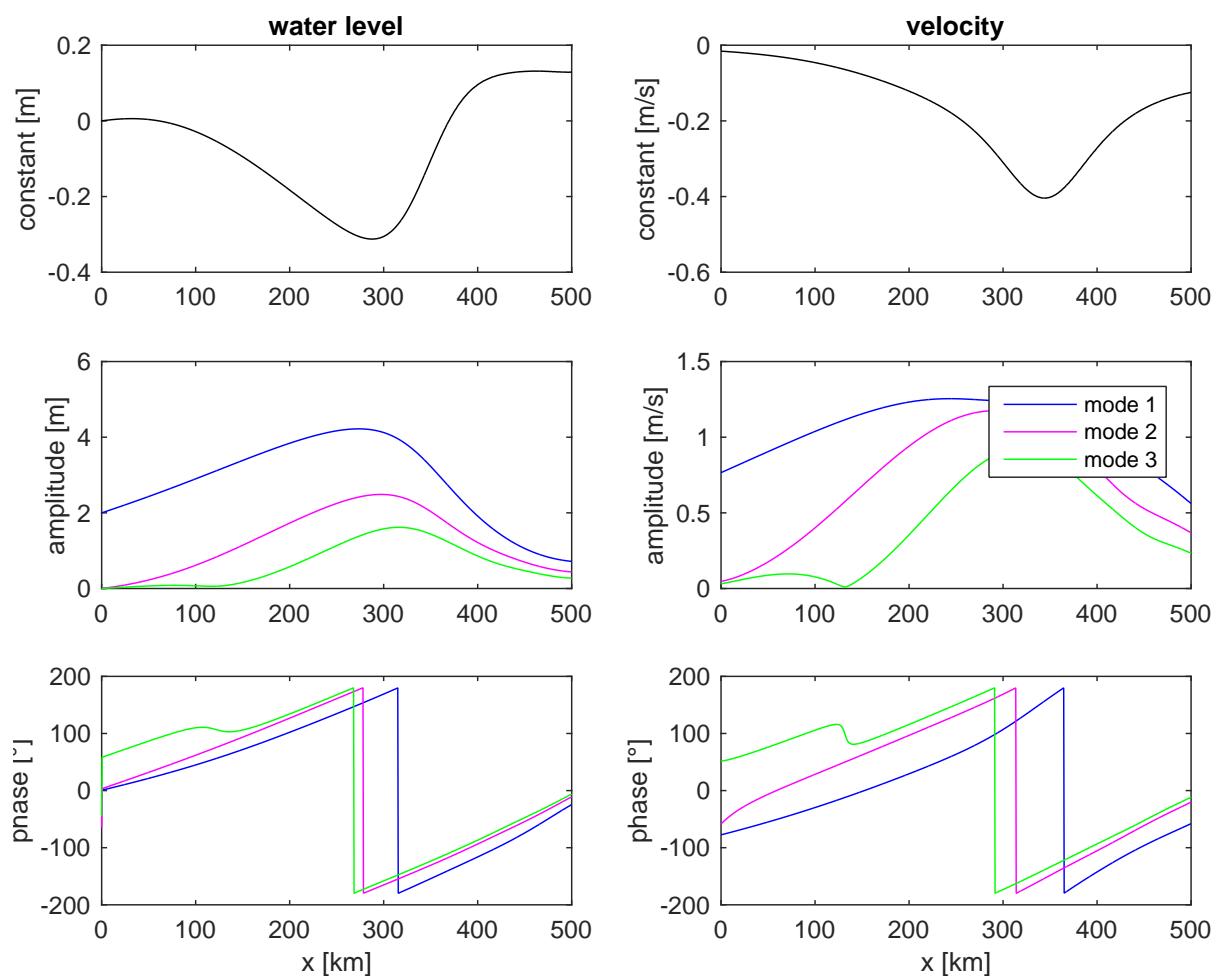


Figure 7: Fourier analysis of tidal wave. From top to bottom: constant term, amplitudes, phases of first three modes. Left column: water level  $\zeta$ ; right column: velocity  $u$ .

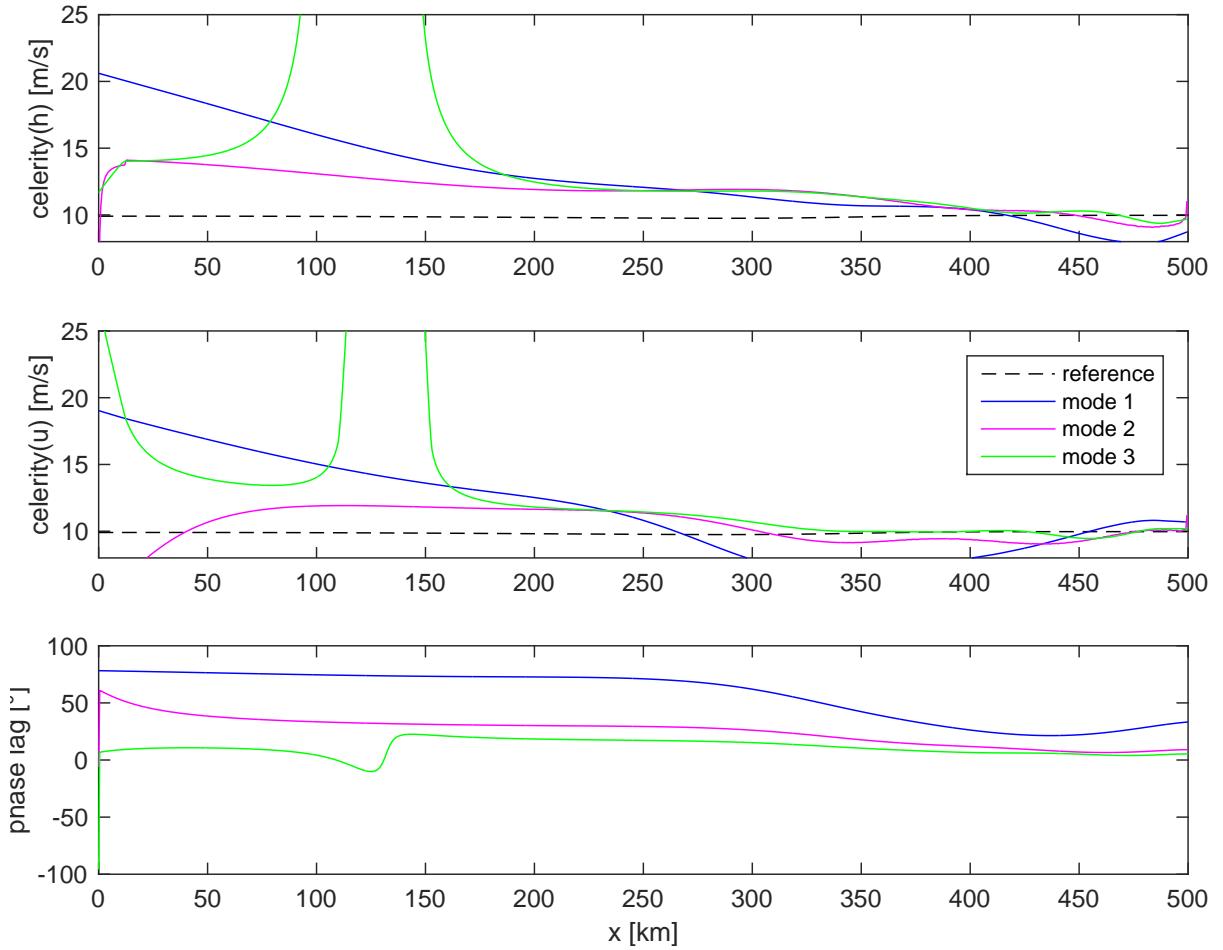


Figure 8: Wave celerity for water level  $\zeta$ , for velocity  $u$ , phase lag  $u-\zeta$ . Colors refer to the first three modes; black dashed line to wave celerity in a frictionless prismatic channel.

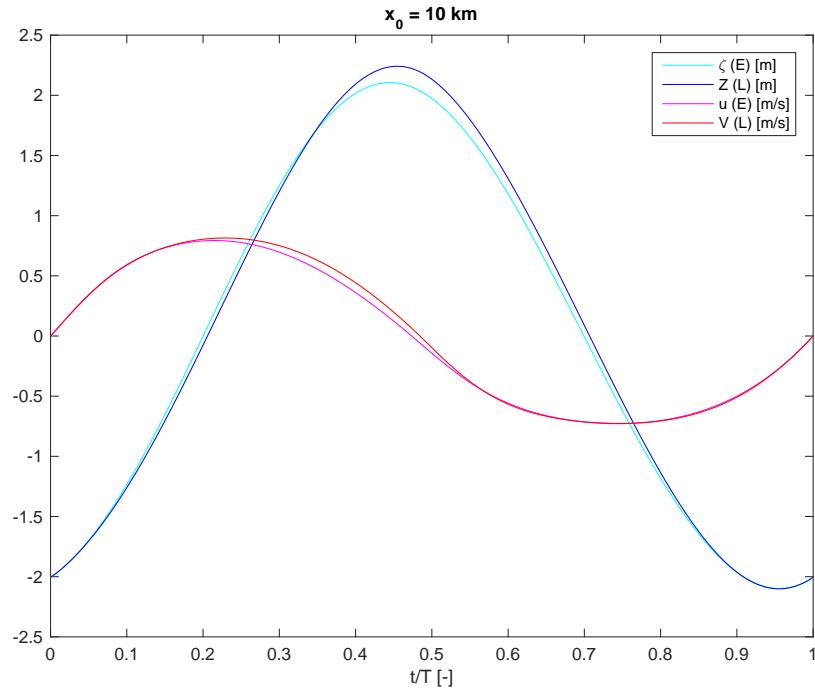


Figure 9: Lagrangean water level  $Z$  and velocity  $V$  compared with Eulerian values  $\zeta$  and  $u$ , for  $x_0 = 10$  km.

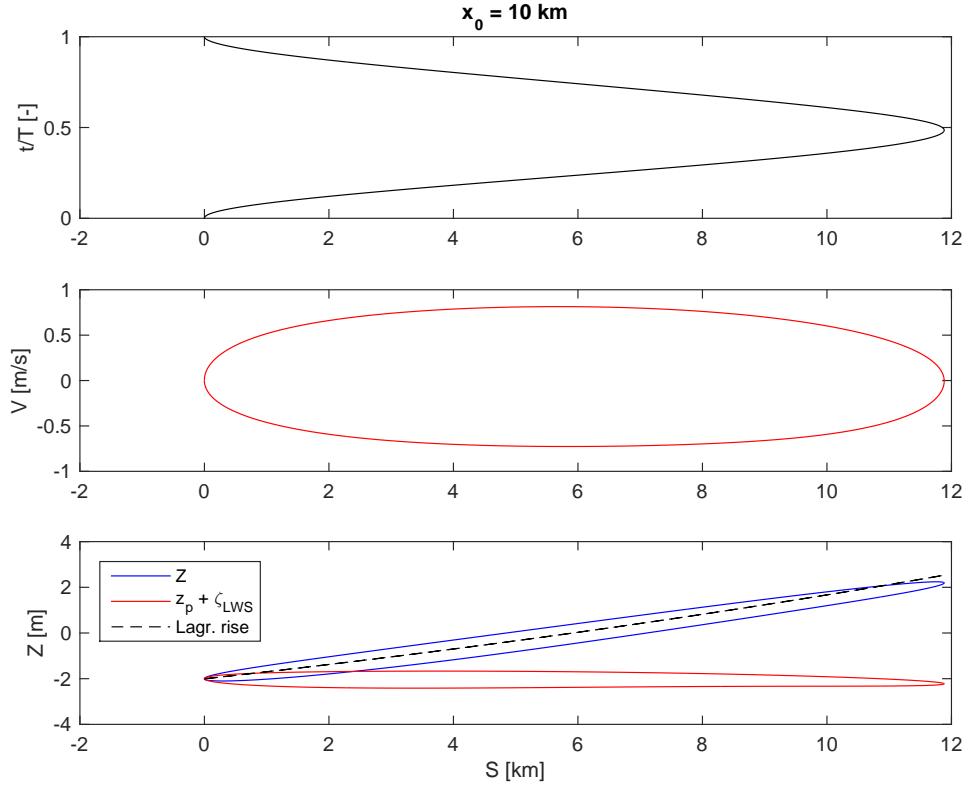


Figure 10: Lagrangean displacement  $S$  in time (first plot) and ellipses  $V-S$  (second plot) and  $Z-S$  (third plot), for  $x_0 = 10$  km.

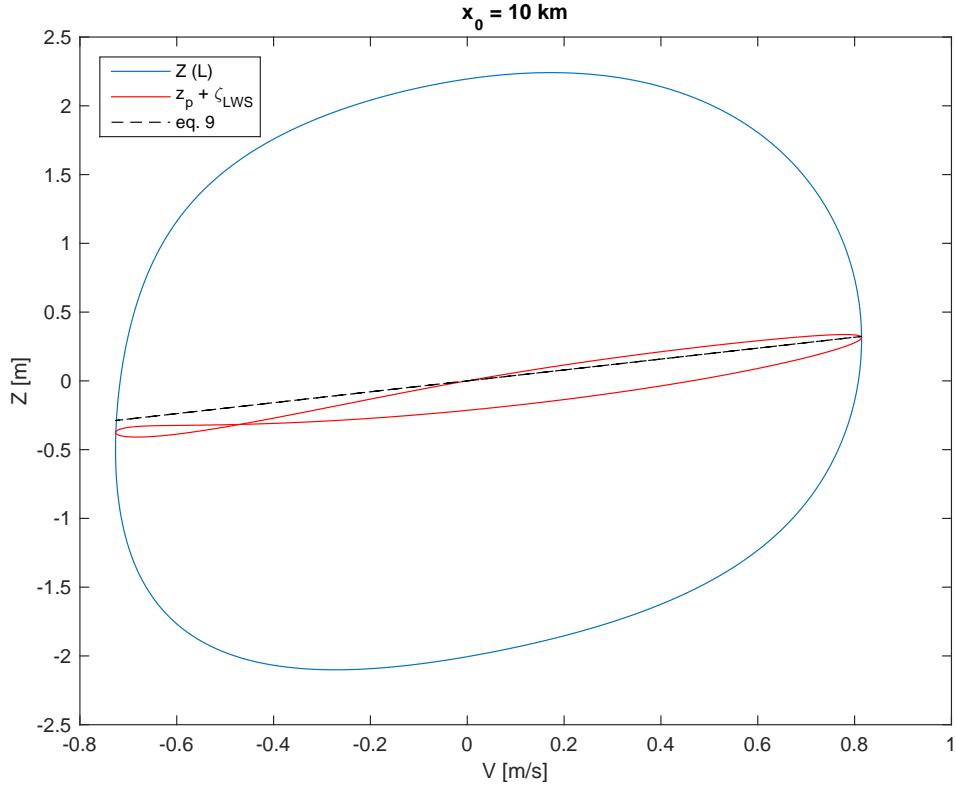


Figure 11: Lagrangean water level against velocity  $V$ :  $Z$  is the actual value,  $z_p + \zeta_{LWS}$  is the transformed water level, for  $x_0 = 10$  km. Black dashed lines: equation (9).

## Variant 2

Length  $b = 300$  km (exponential variation); Strickler coefficient  $K = 45 \text{ m}^{1/3}\text{s}^{-1}$ ; nonlinear friction.

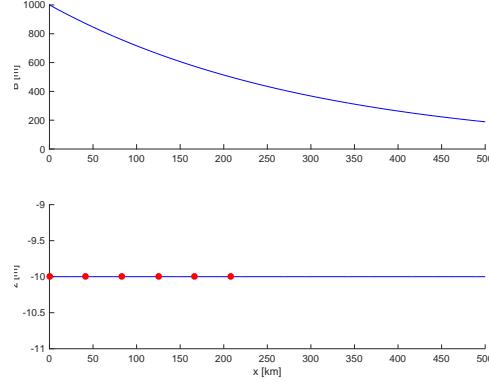


Figure 1: Longitudinal profiles of width and bottom. Dots indicates the locations where the temporal behaviour is shown in figure 3.

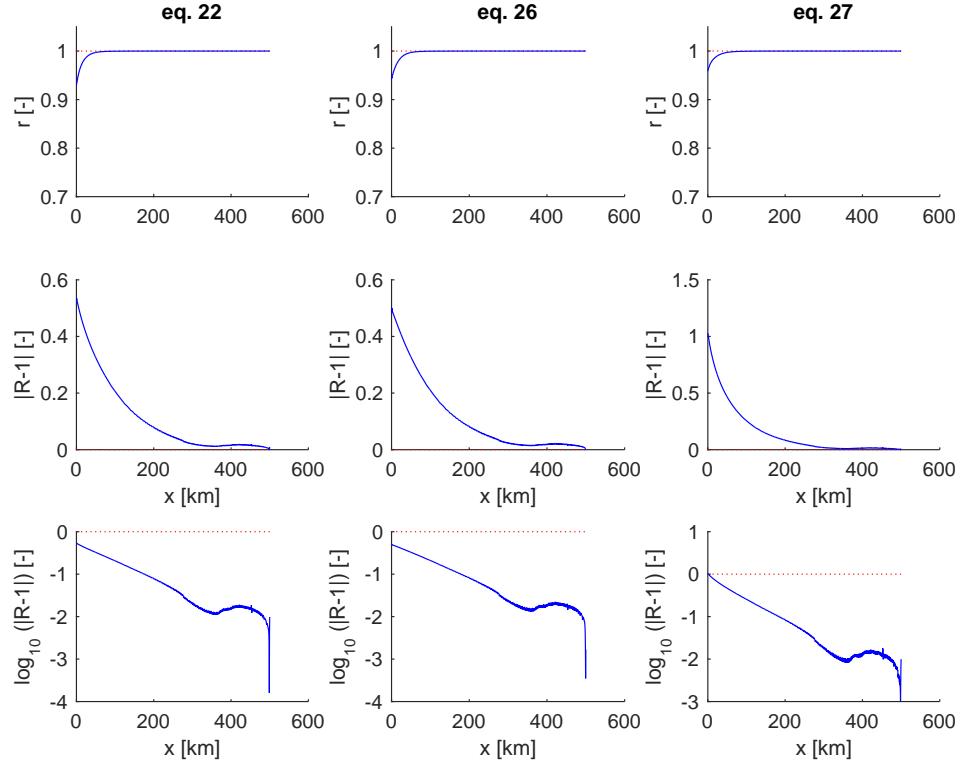


Figure 2: Longitudinal variation of the correlation coefficient  $r$  (first row) and of the two different functions of the ratio  $R$  between right hand side and left hand side of equations 22, 26 and 27 in the manuscript, respectively  $|R - 1|$  and  $\log_{10}(|R - 1|)$ .

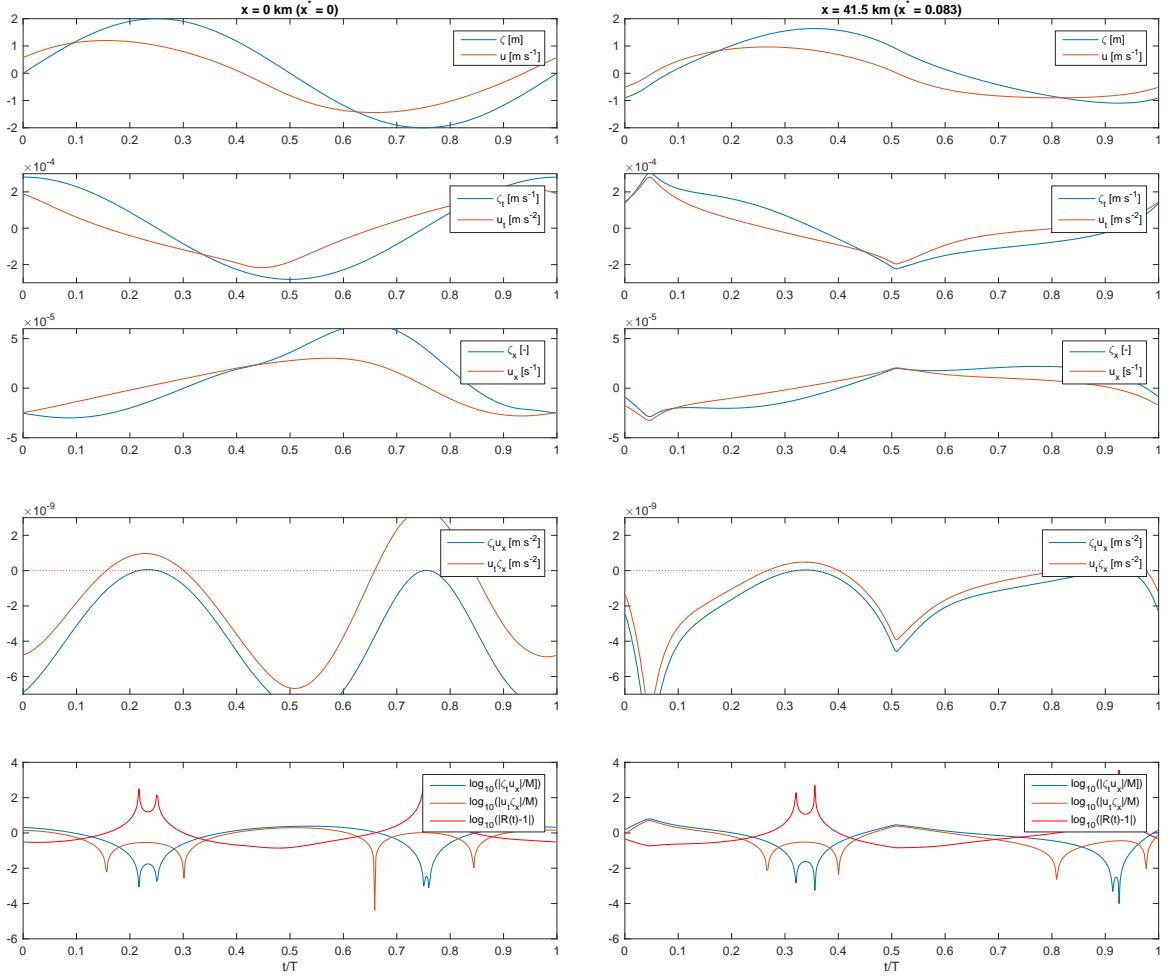


Figure 3: Temporal variation of  $\zeta$  and  $u$  (first plot),  $\zeta_t$  and  $u_t$  (second plot),  $\zeta_x$  and  $u_x$  (third plot),  $\zeta_t u_x$  and  $u_t \zeta_x$  (fourth plot), and  $\log_{10}(|\zeta_t u_x|/M)$ ,  $\log_{10}(|u_t \zeta_x|/M)$ ,  $\log_{10}(|R(t)-1|)$  (fifth plot, where  $R(t) = (u_t \zeta_x)/(\zeta_t u_x)$  and  $M$  is the mean of the tidally averages of  $|\zeta_t u_x|$  and  $|u_t \zeta_x|$ ), in  $x = 0$  km and  $x = 41.5$  km.

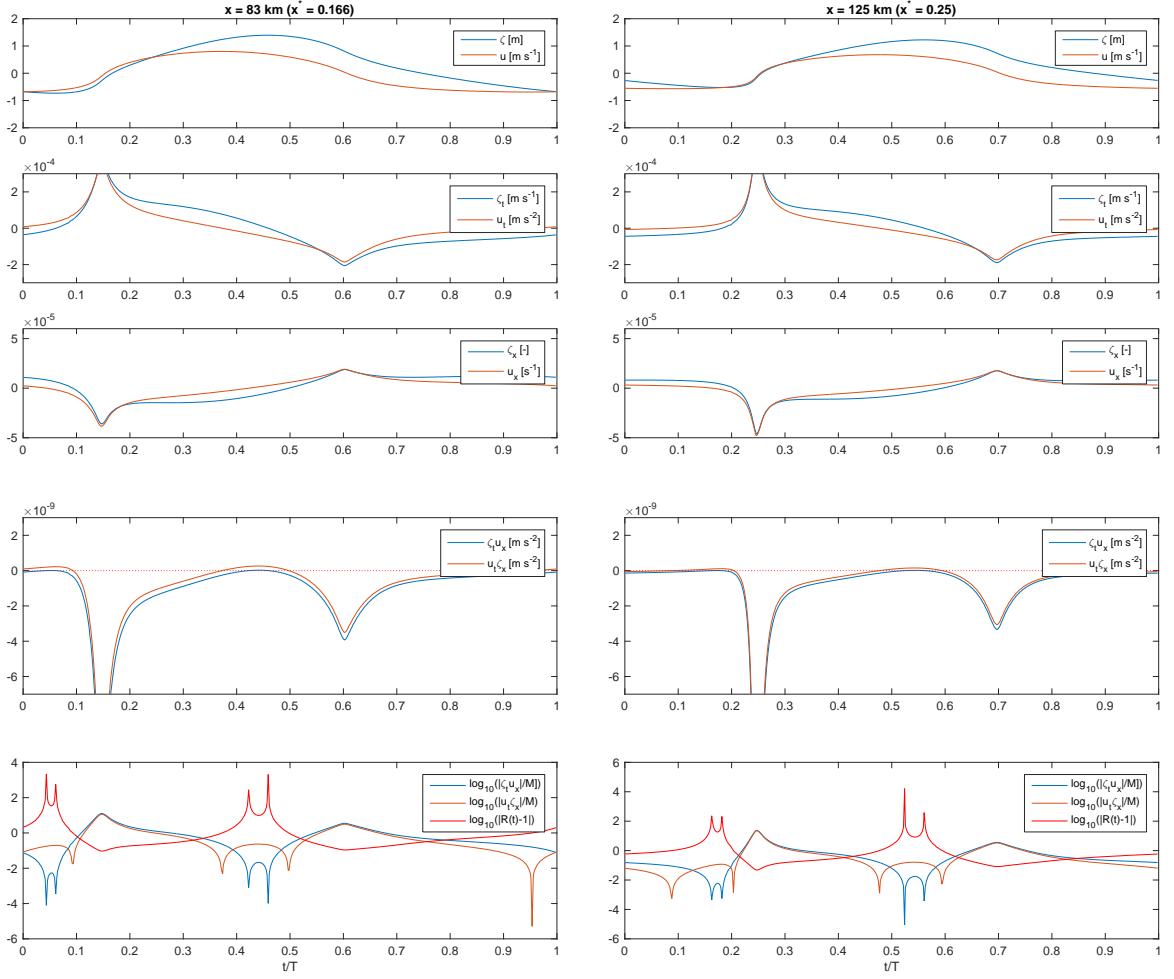


Figure 4: Temporal variation of  $\zeta$  and  $u$  (first plot),  $\zeta_t$  and  $u_t$  (second plot),  $\zeta_x$  and  $u_x$  (third plot),  $\zeta_t u_x$  and  $u_t \zeta_x$  (fourth plot), and  $\log_{10}(|\zeta_t u_x|/M)$ ,  $\log_{10}(|u_t \zeta_x|/M)$ ,  $\log_{10}(|R(t)-1|)$  (fifth plot, where  $R(t) = (u_t \zeta_x)/(\zeta_t u_x)$  and  $M$  is the mean of the tidally averages of  $|\zeta_t u_x|$  and  $|u_t \zeta_x|$ ), in  $x = 83 \text{ km}$  and  $x = 125 \text{ km}$ .

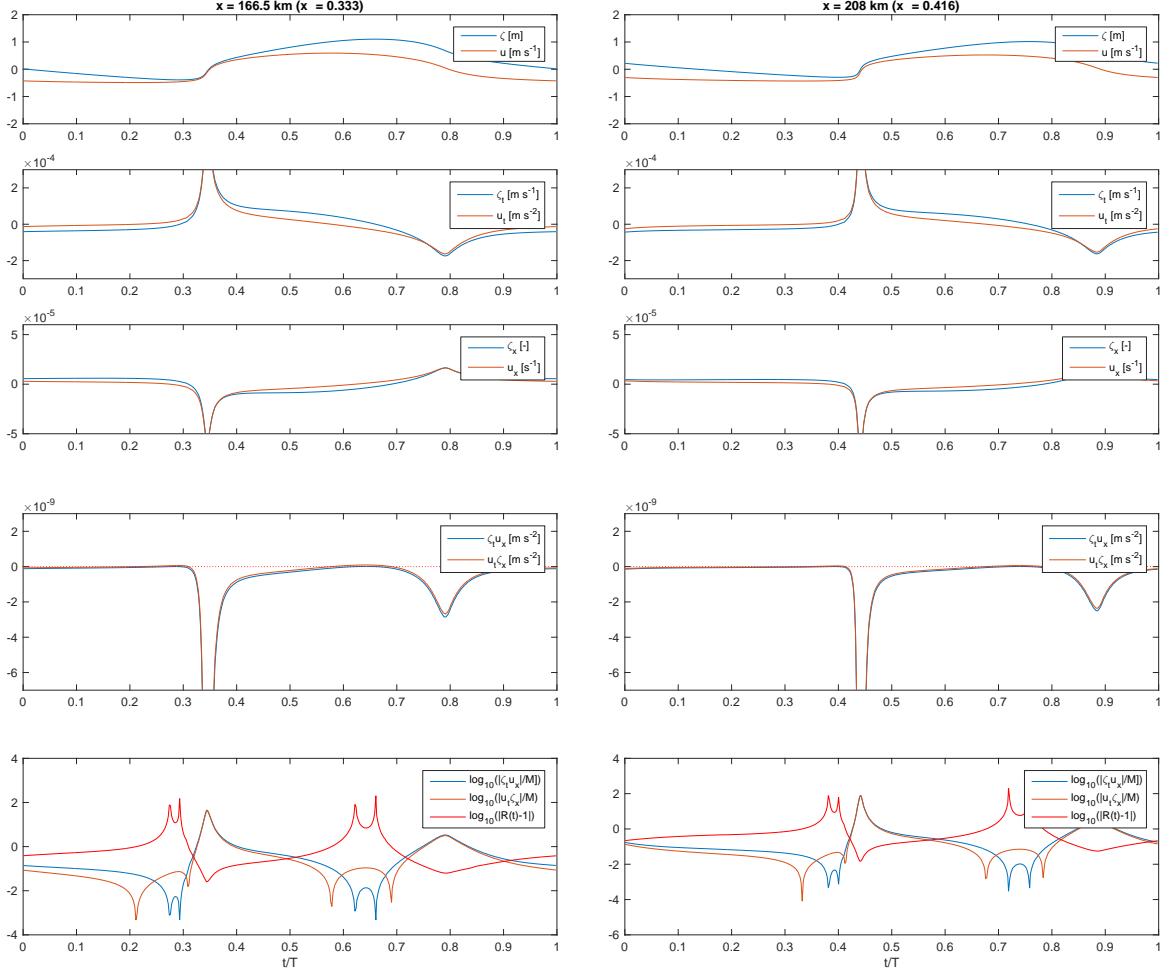


Figure 5: Temporal variation of  $\zeta$  and  $u$  (first plot),  $\zeta_t$  and  $u_t$  (second plot),  $\zeta_x$  and  $u_x$  (third plot),  $\zeta_t u_x$  and  $u_t \zeta_x$  (fourth plot), and  $\log_{10}(|\zeta_t u_x|/M)$ ,  $\log_{10}(|u_t \zeta_x|/M)$ ,  $\log_{10}(|R(t) - 1|)$  (fifth plot, where  $R(t) = (u_t \zeta_x)/(\zeta_t u_x)$  and  $M$  is the mean of the tidally averages of  $|\zeta_t u_x|$  and  $|u_t \zeta_x|$ ), in  $x = 166.5$  km and  $x = 208$  km.

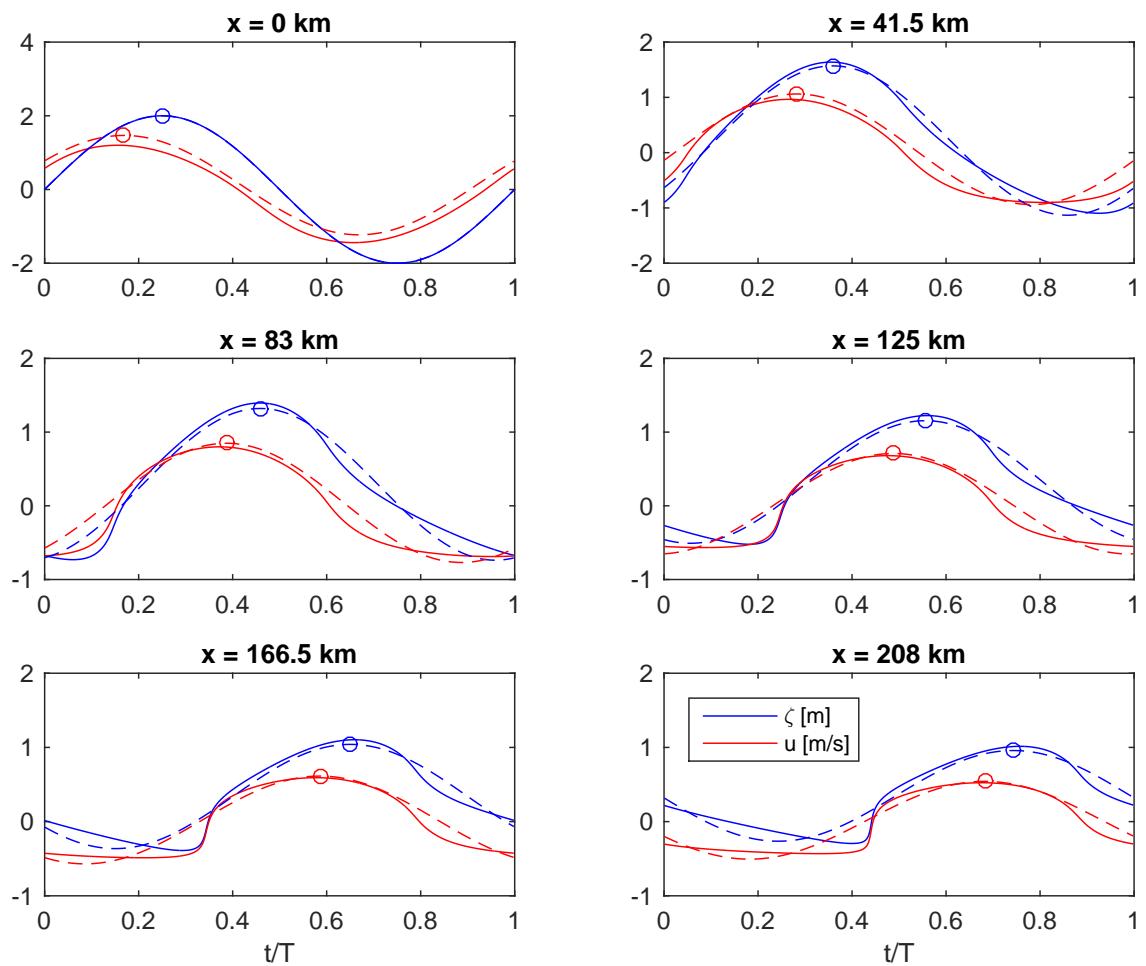


Figure 6: Tidal waves and Fourier series truncated at the first harmonic. Circles indicate the maxima of the dominant tidal component, from which it is possible to detect the phase lag  $u-\zeta$ .

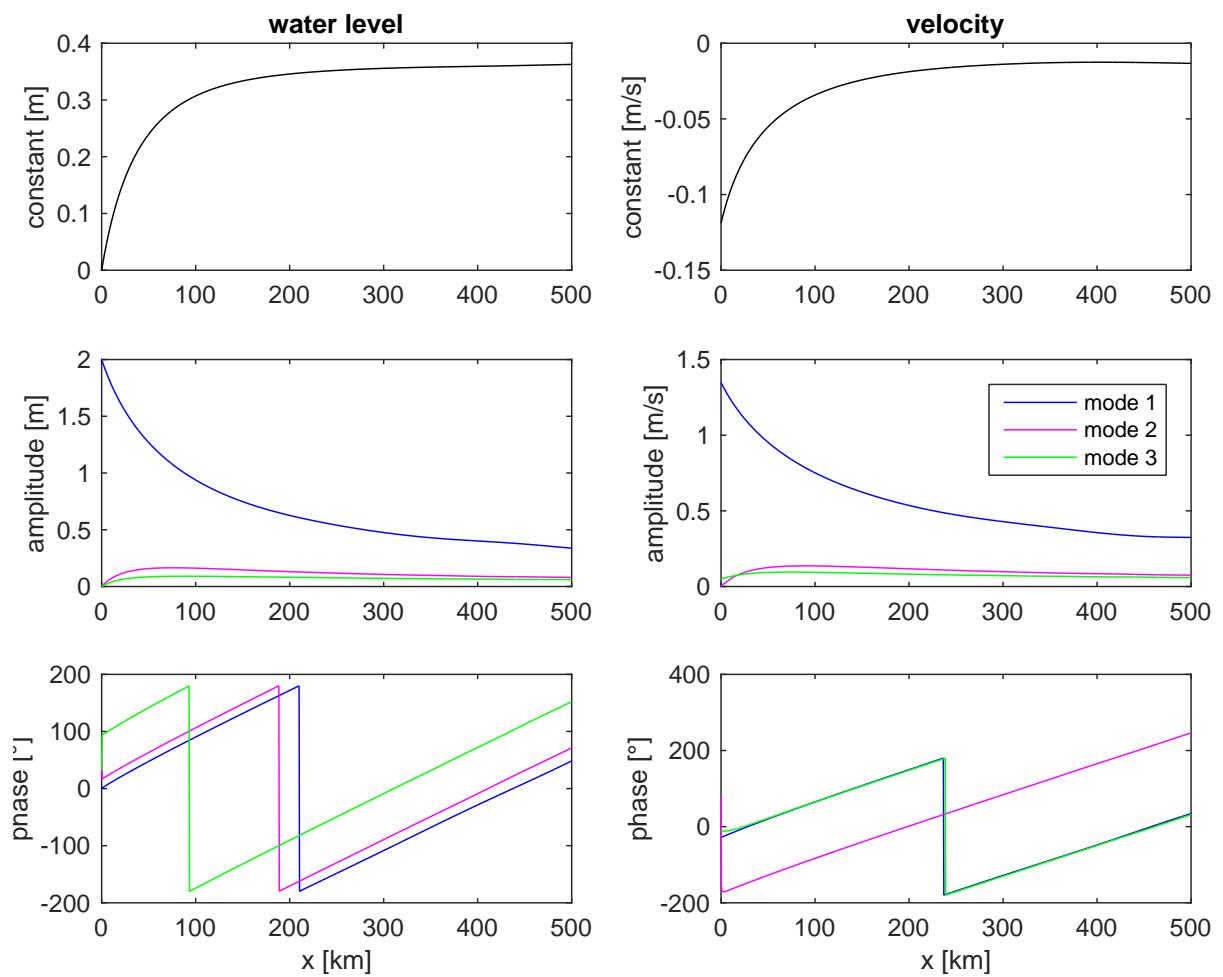


Figure 7: Fourier analysis of tidal wave. From top to bottom: constant term, amplitudes, phases of first three modes. Left column: water level  $\zeta$ ; right column: velocity  $u$ .

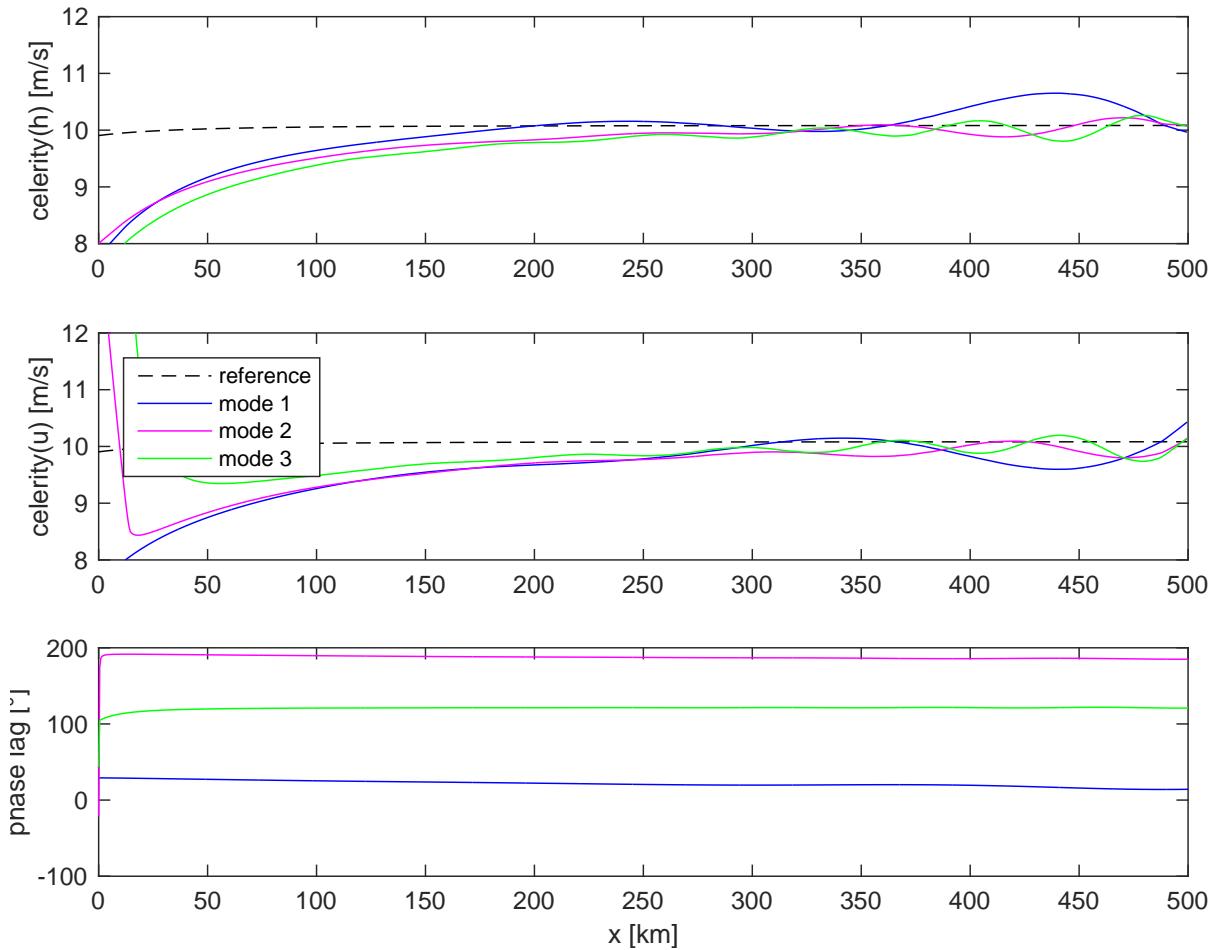


Figure 8: Wave celerity for water level  $\zeta$ , for velocity  $u$ , phase lag  $u-\zeta$ . Colors refer to the first three modes; black dashed line to wave celerity in a frictionless prismatic channel.

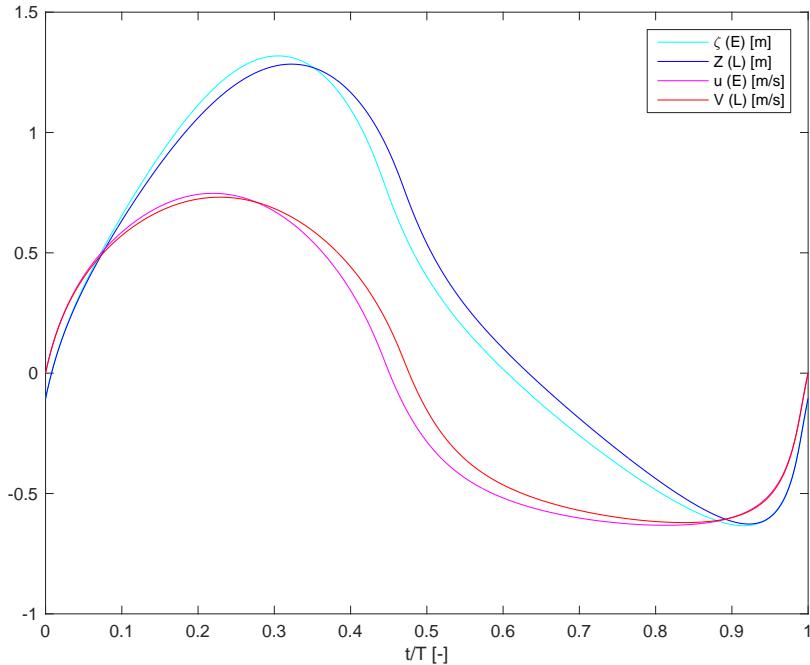


Figure 9: Lagrangean water level  $Z$  and velocity  $V$  compared with Eulerian values  $\zeta$  and  $u$  in  $x = 100$  km.

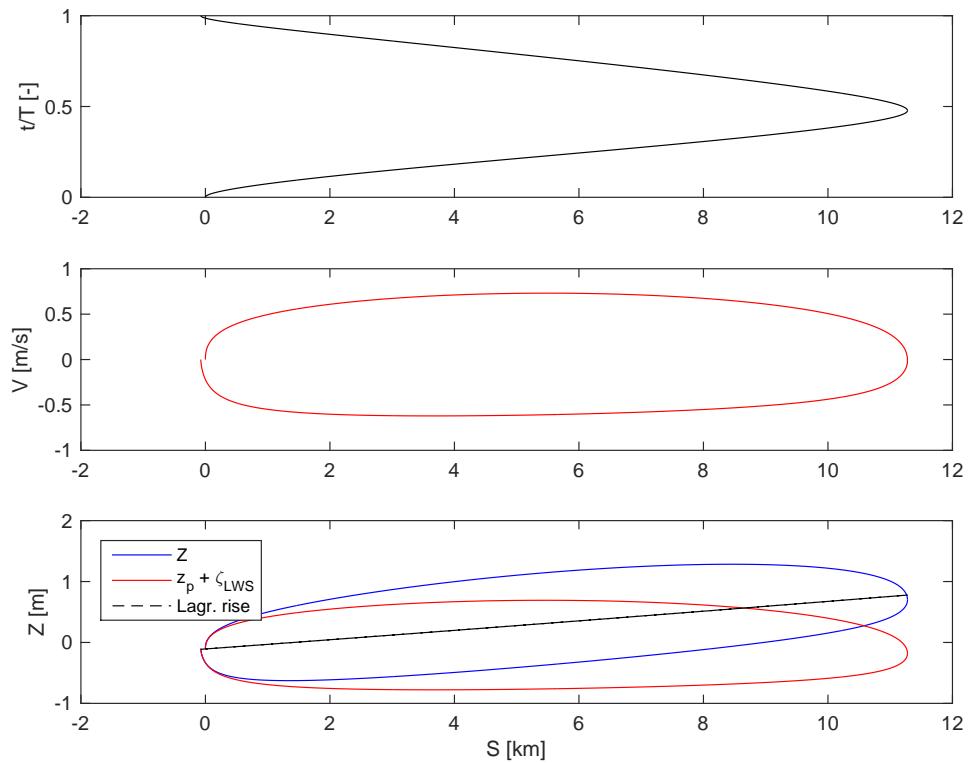


Figure 10: Lagrangean displacement  $S$  in time (first plot) and ellipses  $V$ - $S$  (second plot) and  $Z$ - $S$  (third plot).

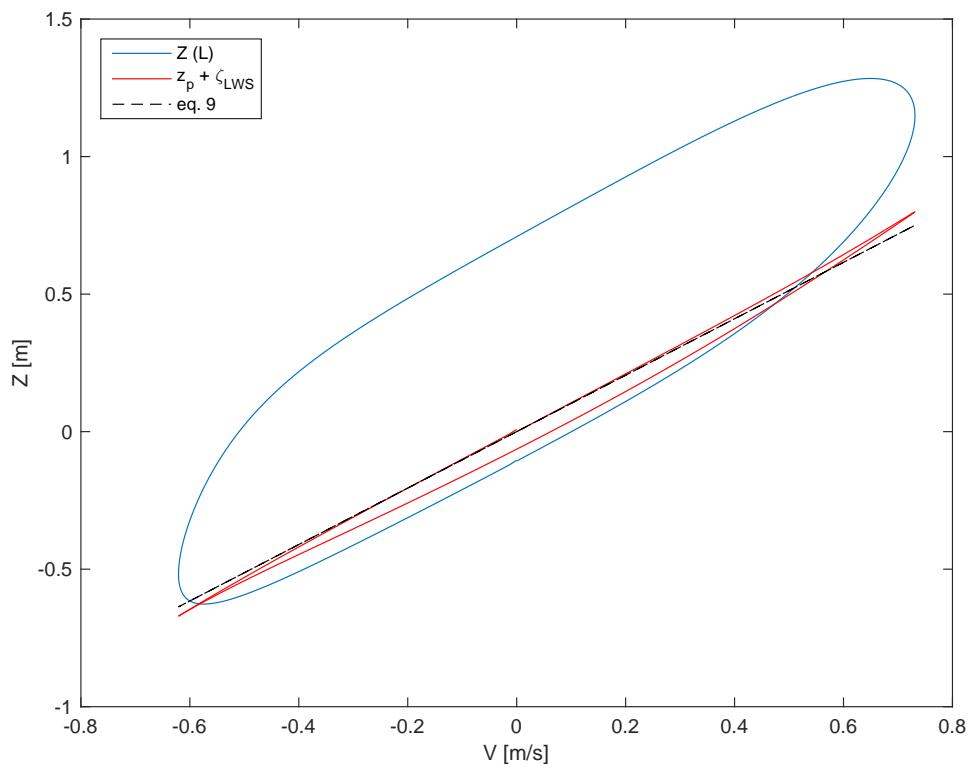


Figure 11: Lagrangean water level against velocity  $V$ :  $Z$  is the actual value,  $z_p + \zeta_{LWS}$  is the transformed water level. Black dashed lines: equation (9).

## Variant 3

Length  $b = 100$  km (exponential variation); Strickler coefficient  $K = 20 \text{ m}^{1/3}\text{s}^{-1}$ ; nonlinear friction.

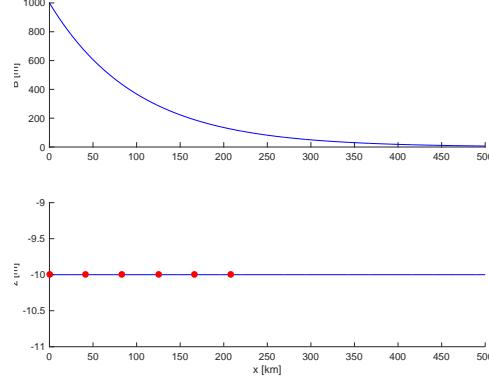


Figure 1: Longitudinal profiles of width and bottom. Dots indicates the locations where the temporal behaviour is shown in figure 3.

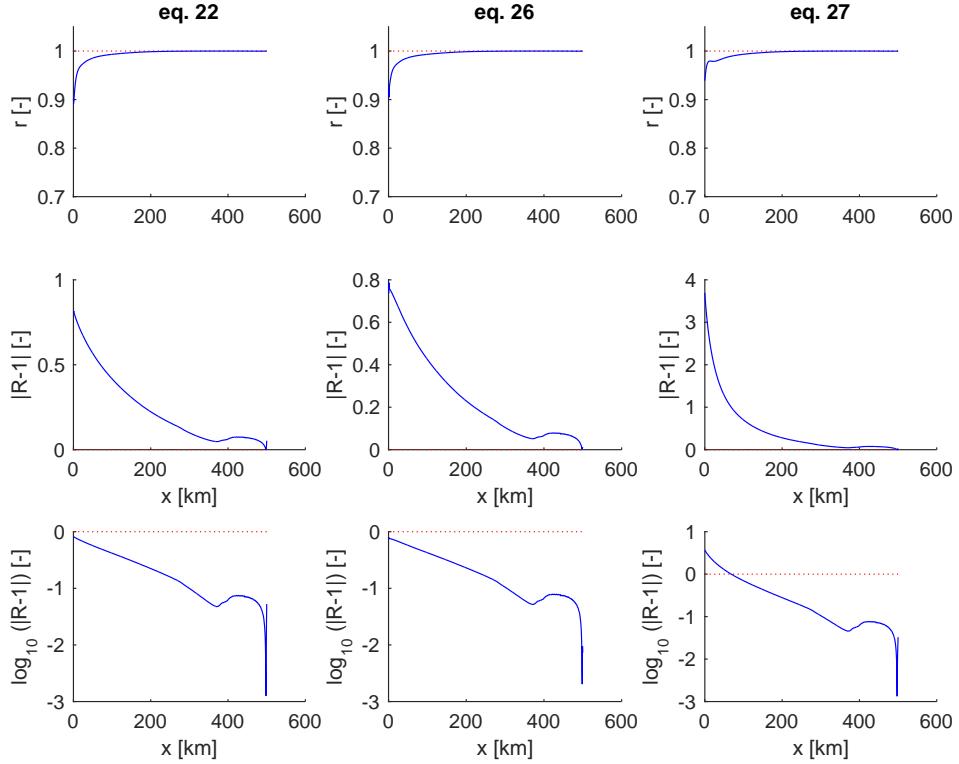


Figure 2: Longitudinal variation of the correlation coefficient  $r$  (first row) and of the two different functions of the ratio  $R$  between right hand side and left hand side of equations 22, 26 and 27 in the manuscript, respectively  $|R - 1|$  and  $\log_{10}(|R - 1|)$ .

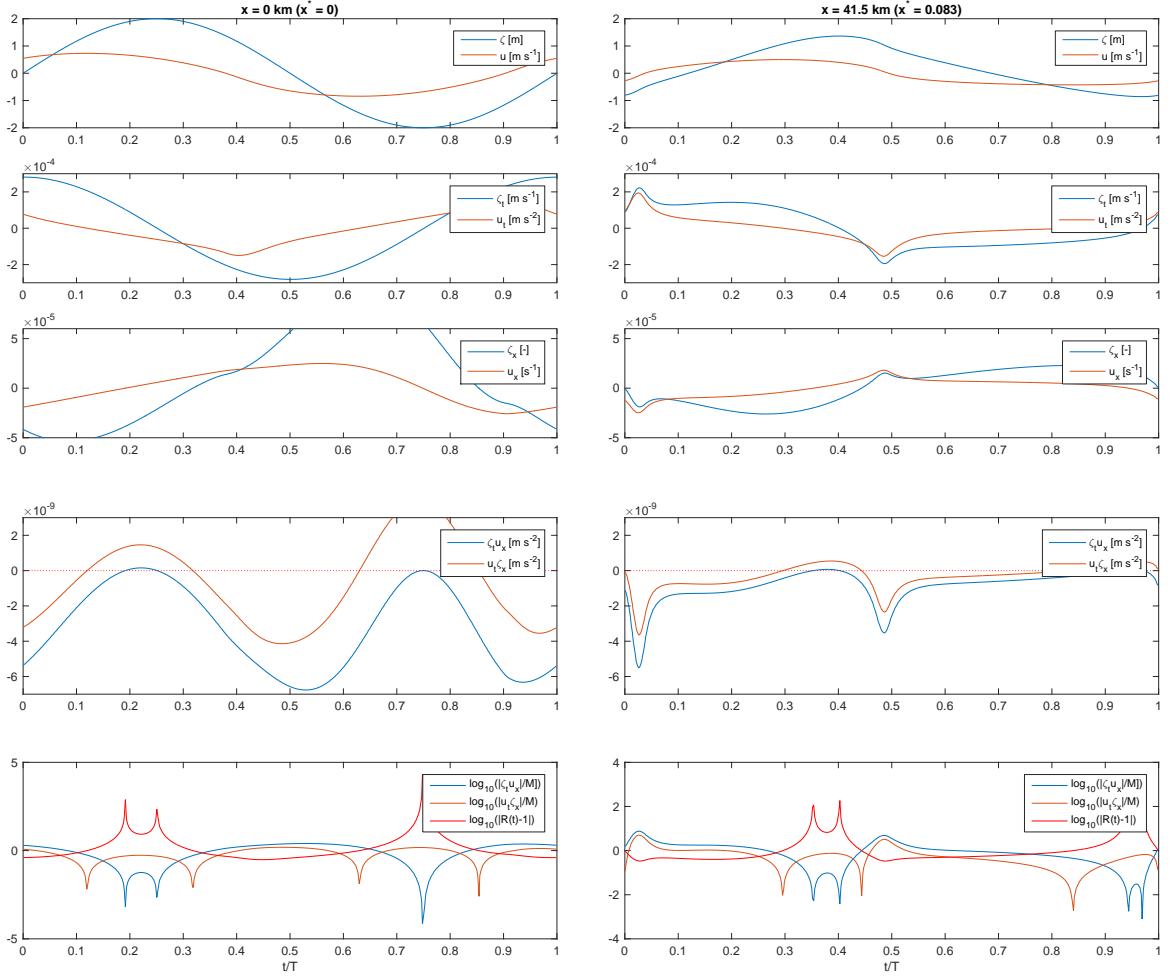


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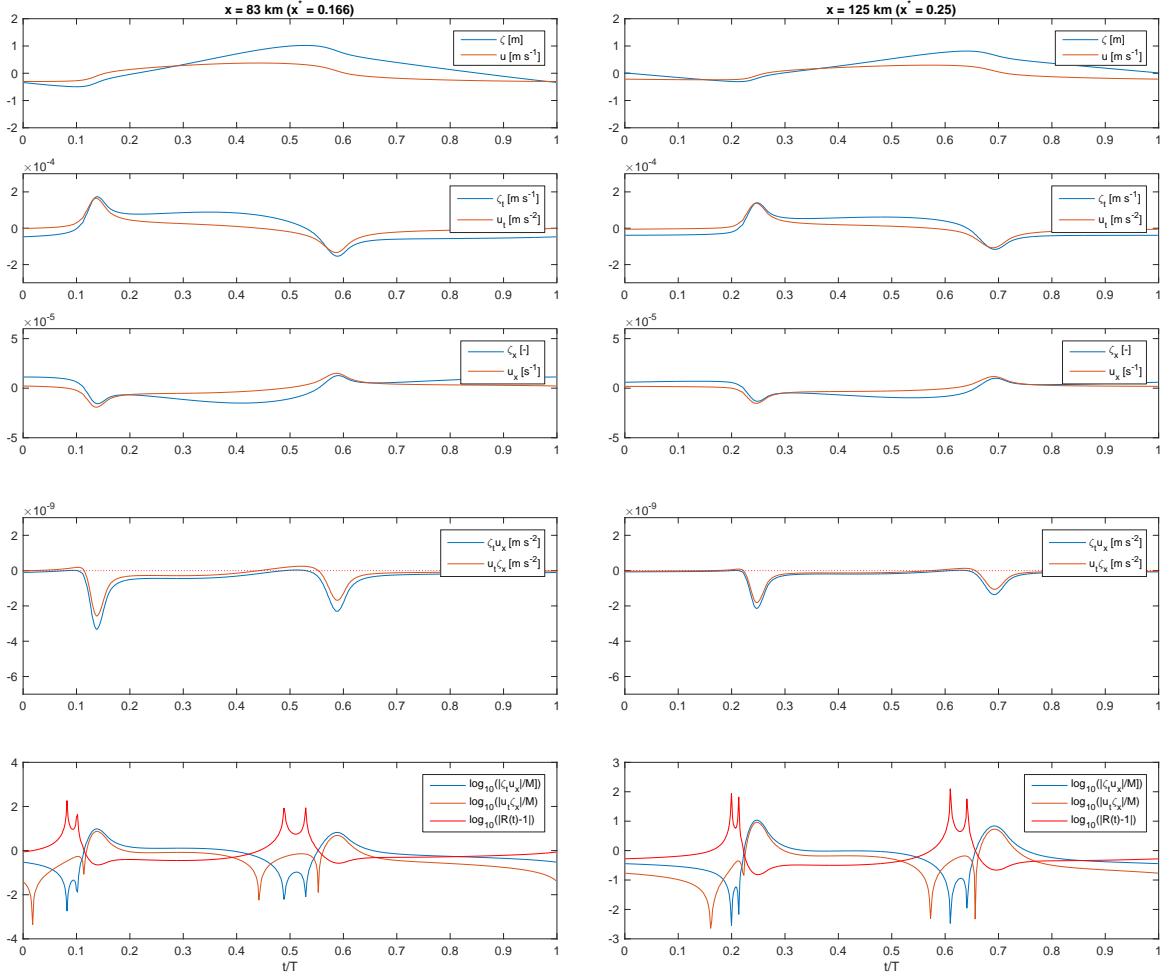


Figure 4: Temporal variation of  $\zeta$  and  $u$  (first plot),  $\zeta_t$  and  $u_t$  (second plot),  $\zeta_x$  and  $u_x$  (third plot),  $\zeta_t u_x$  and  $u_t \zeta_x$  (fourth plot), and  $\log_{10}(|\zeta_t u_x|/M)$ ,  $\log_{10}(|u_t \zeta_x|/M)$ ,  $\log_{10}(|R(t)-1|)$  (fifth plot, where  $R(t) = (u_t \zeta_x)/(\zeta_t u_x)$ ) (fifth plot, where  $R(t) = (u_t \zeta_x)/(\zeta_t u_x)$  and  $M$  is the mean of the tidally averages of  $|\zeta_t u_x|$  and  $|u_t \zeta_x|$ ), in  $x = 83$  km and  $x = 125$  km.

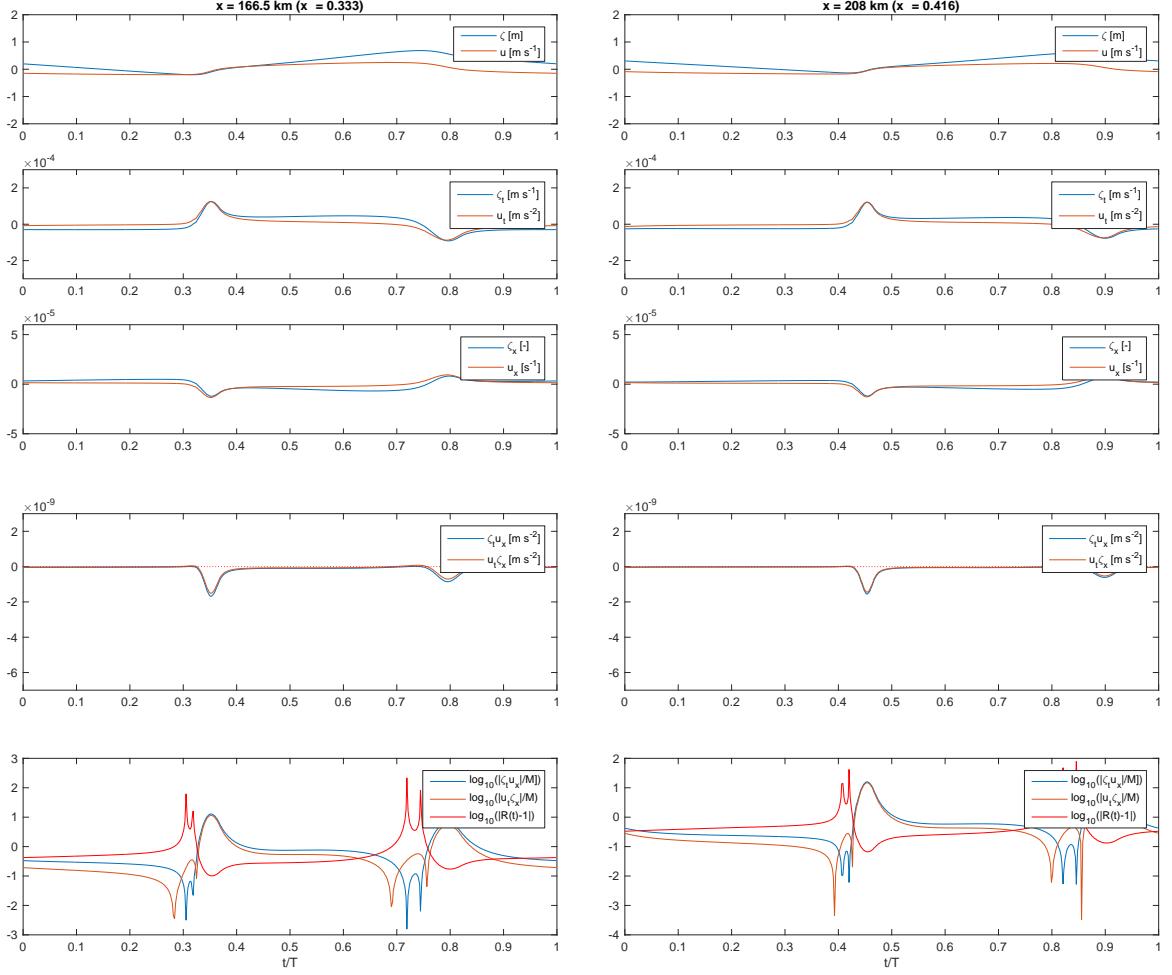


Figure 5: Temporal variation of  $\zeta$  and  $u$  (first plot),  $\zeta_t$  and  $u_t$  (second plot),  $\zeta_x$  and  $u_x$  (third plot),  $\zeta_t u_x$  and  $u_t \zeta_x$  (fourth plot), and  $\log_{10}(|\zeta_t u_x|/M)$ ,  $\log_{10}(|u_t \zeta_x|/M)$ ,  $\log_{10}(|R(t)-1|)$  (fifth plot, where  $R(t) = (u_t \zeta_x)/(\zeta_t u_x)$  and  $M$  is the mean of the tidally averages of  $|\zeta_t u_x|$  and  $|u_t \zeta_x|$ ), in  $x = 166.5 \text{ km}$  and  $x = 208 \text{ km}$ .

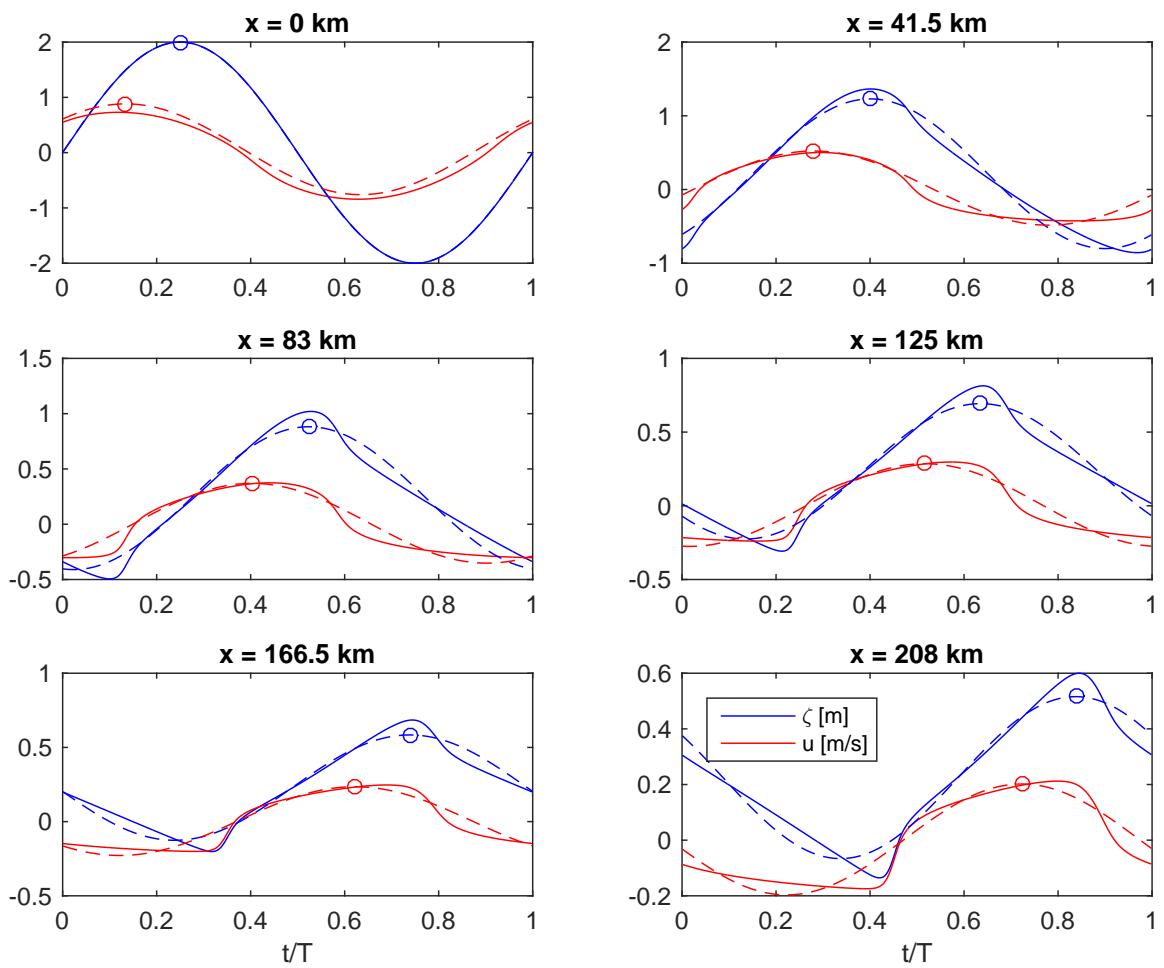


Figure 6: Tidal waves and Fourier series truncated at the first harmonic. Circles indicate the maxima of the dominant tidal component, from which it is possible to detect the phase lag  $u-\zeta$ .

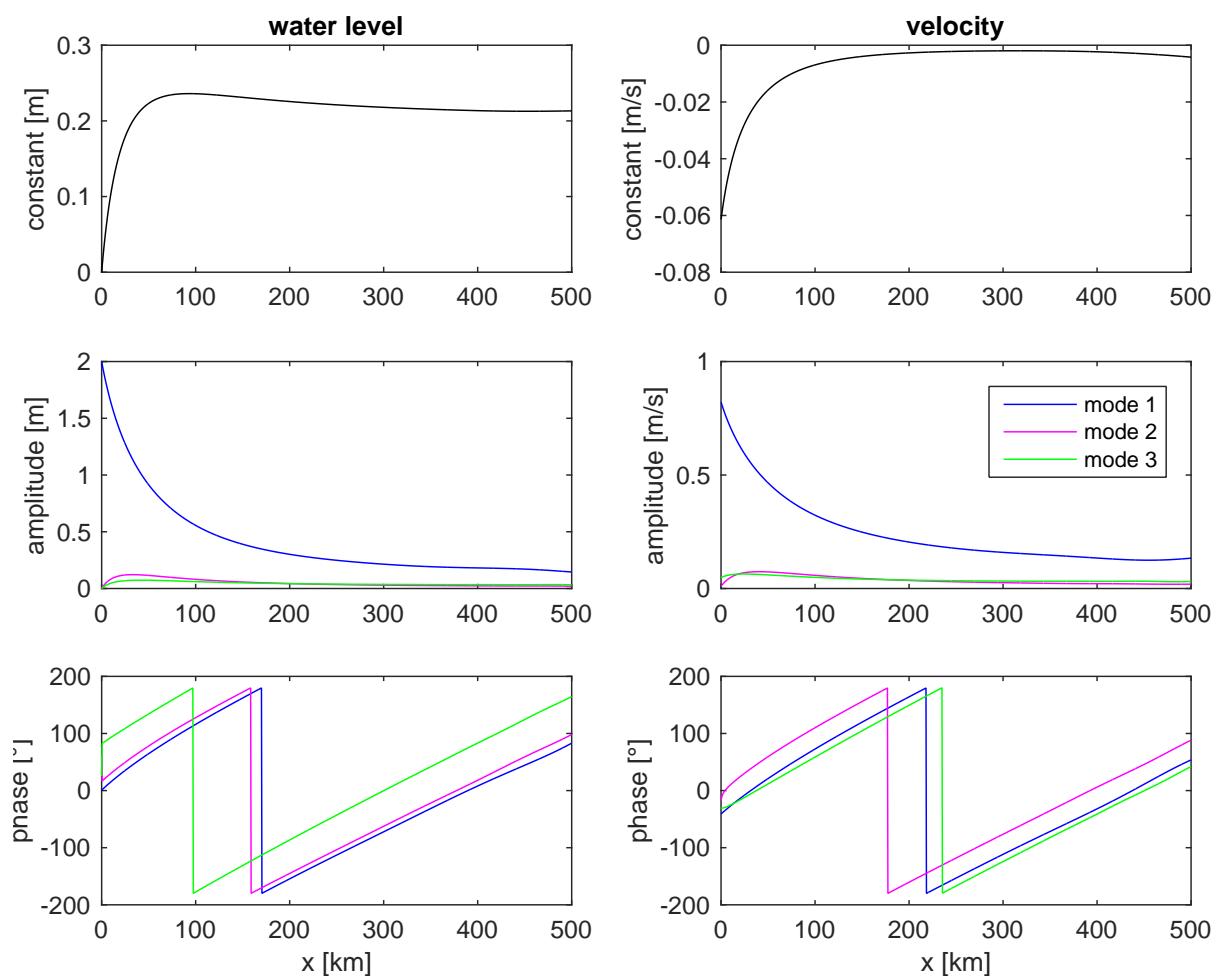


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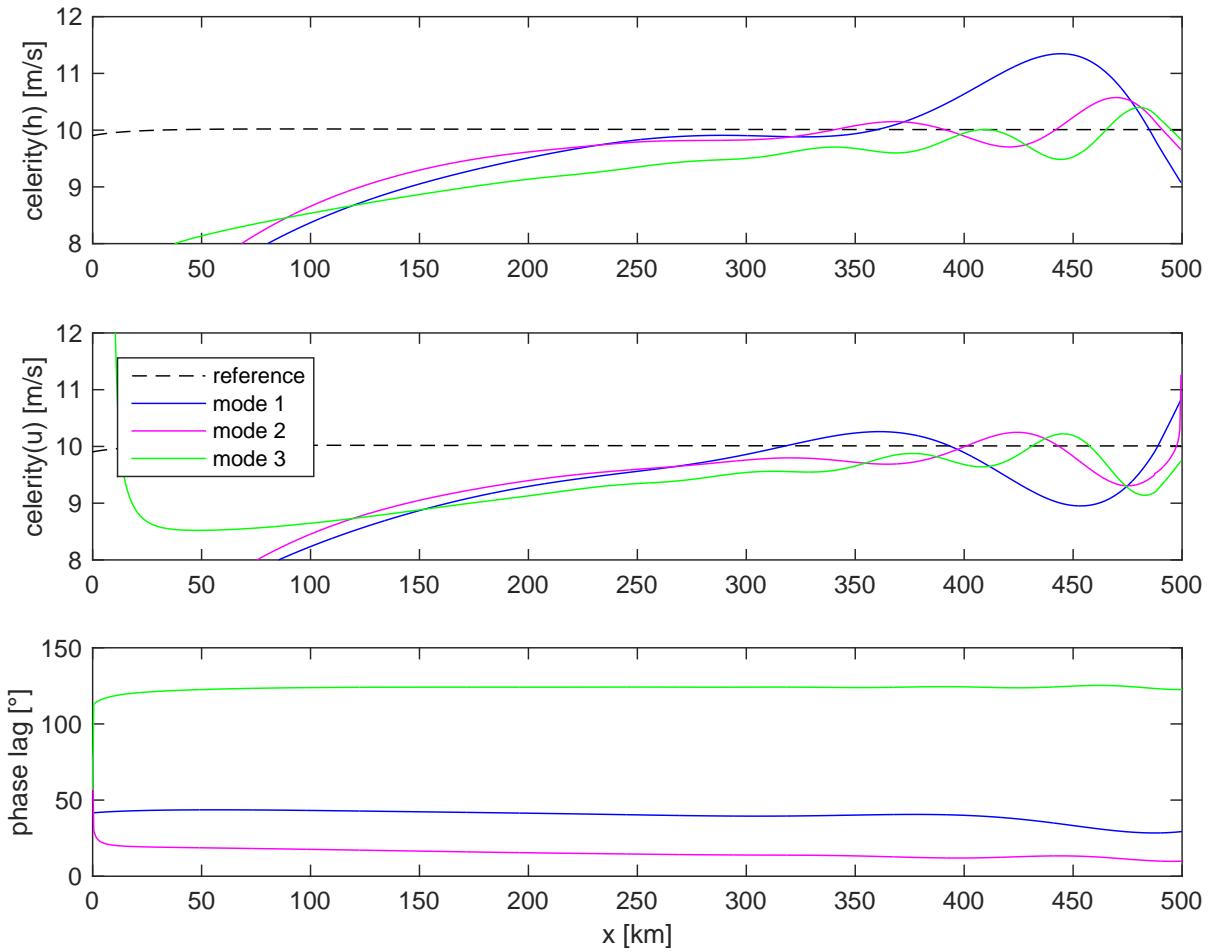


Figure 8: Wave celerity for water level  $\zeta$ , for velocity  $u$ , phase lag  $u-\zeta$ . Colors refer to the first three modes; black dashed line to wave celerity in a frictionless prismatic channel.

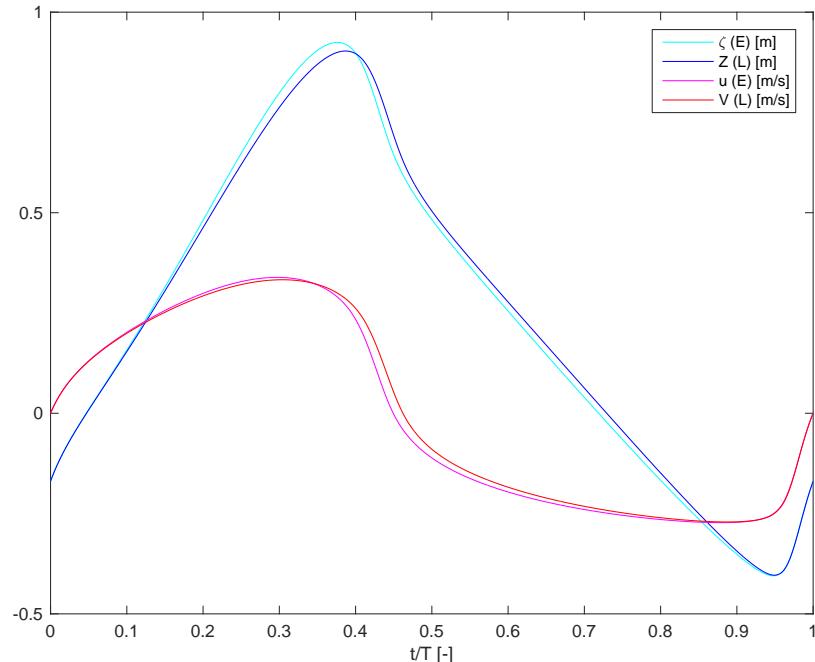


Figure 9: Lagrangean water level  $Z$  and velocity  $V$  compared with Eulerian values  $\zeta$  and  $u$  in  $x = 100$  km.

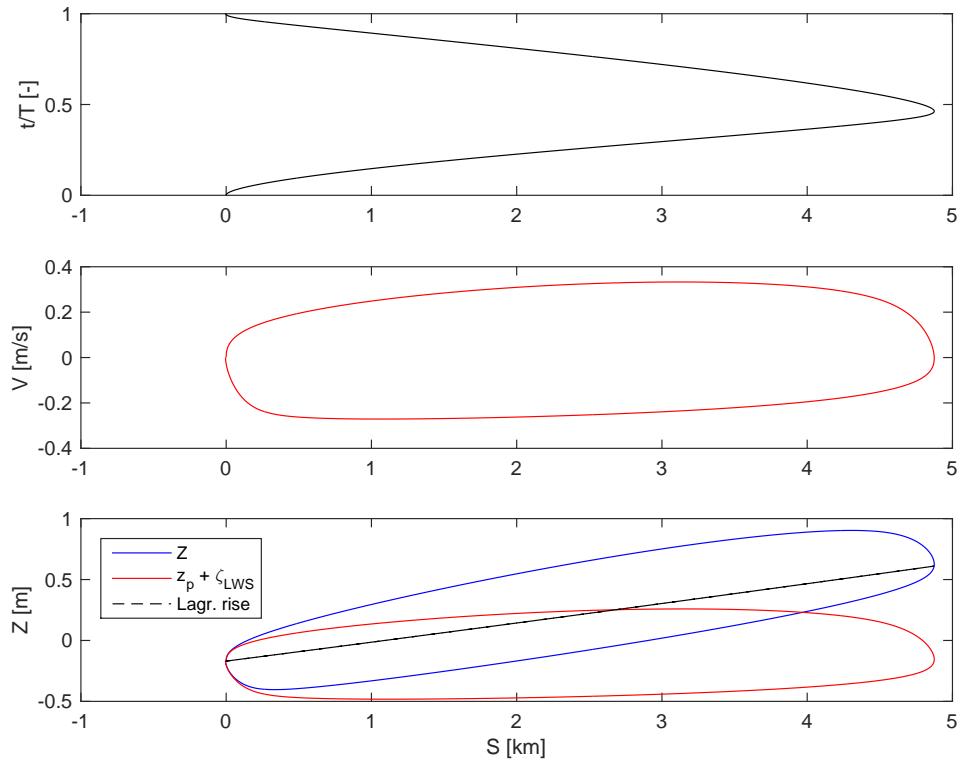


Figure 10: Lagrangean displacement  $S$  in time (first plot) and ellipses  $V$ - $S$  (second plot) and  $Z$ - $S$  (third plot).

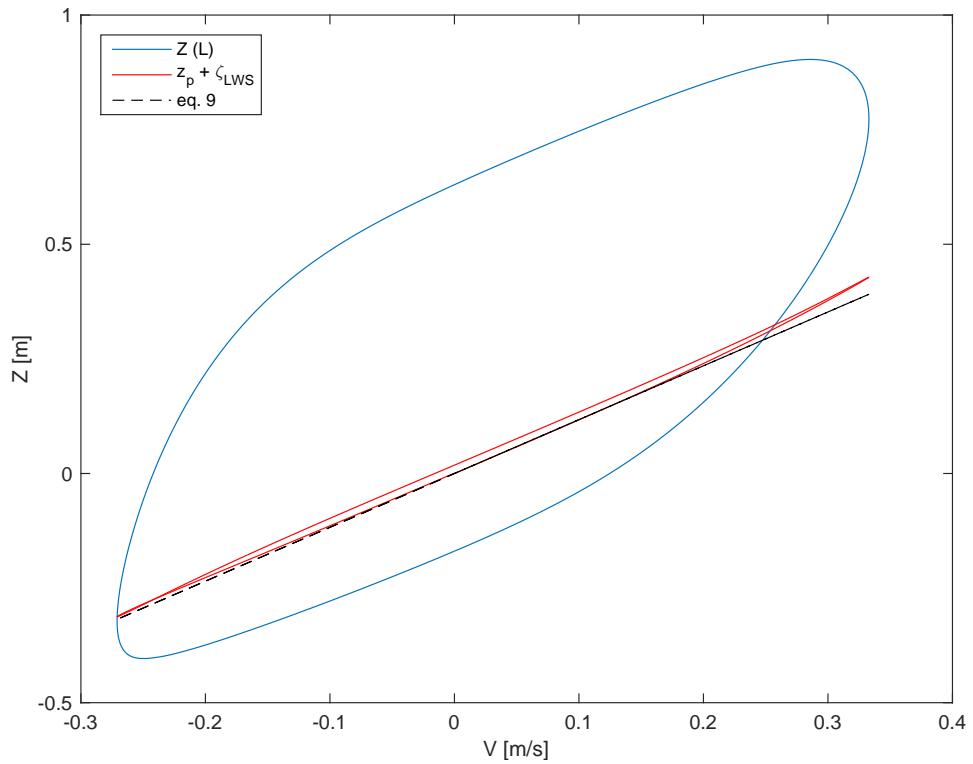


Figure 11: Lagrangean water level against velocity  $V$ :  $Z$  is the actual value,  $z_p + \zeta_{LWS}$  is the transformed water level. Black dashed lines: equation (9).

## Variant 4

Length  $b = 100$  km (exponential variation); Strickler coefficient  $K = 80 \text{ m}^{1/3}\text{s}^{-1}$ ; nonlinear friction.

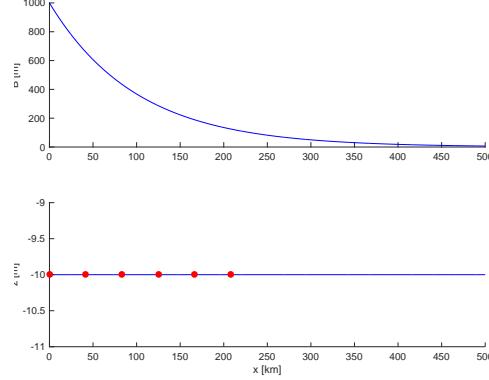


Figure 1: Longitudinal profiles of width and bottom. Dots indicates the locations where the temporal behaviour is shown in figure 3.

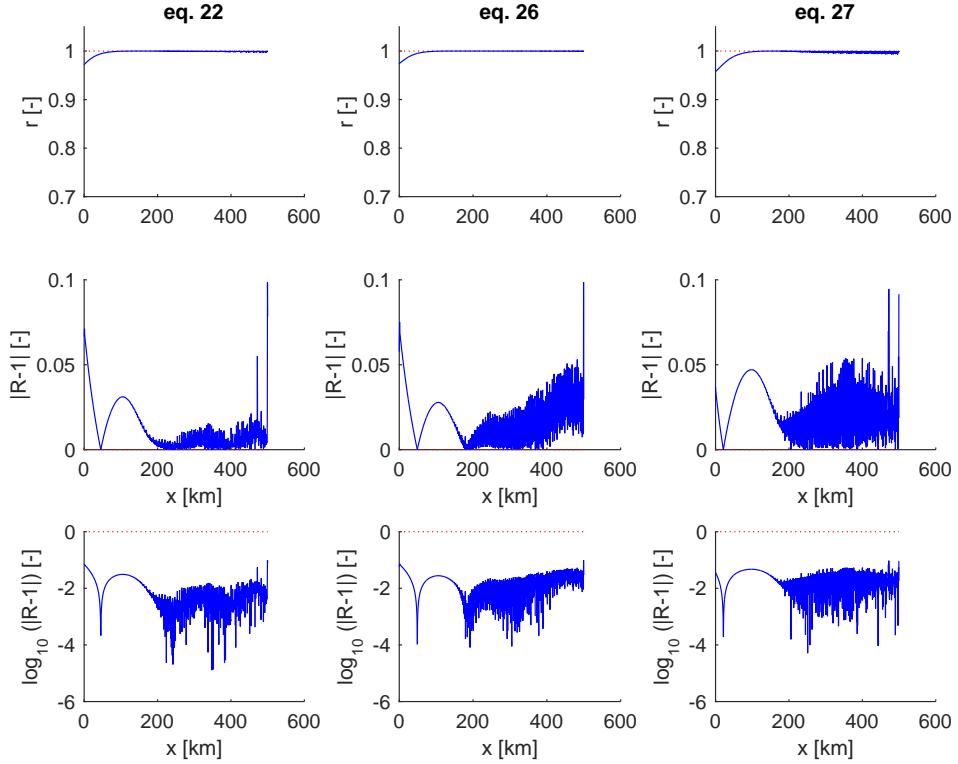


Figure 2: Longitudinal variation of the correlation coefficient  $r$  (first row) and of the two different functions of the ratio  $R$  between right hand side and left hand side of equations 22, 26 and 27 in the manuscript, respectively  $|R - 1|$  and  $\log_{10}(|R - 1|)$ .

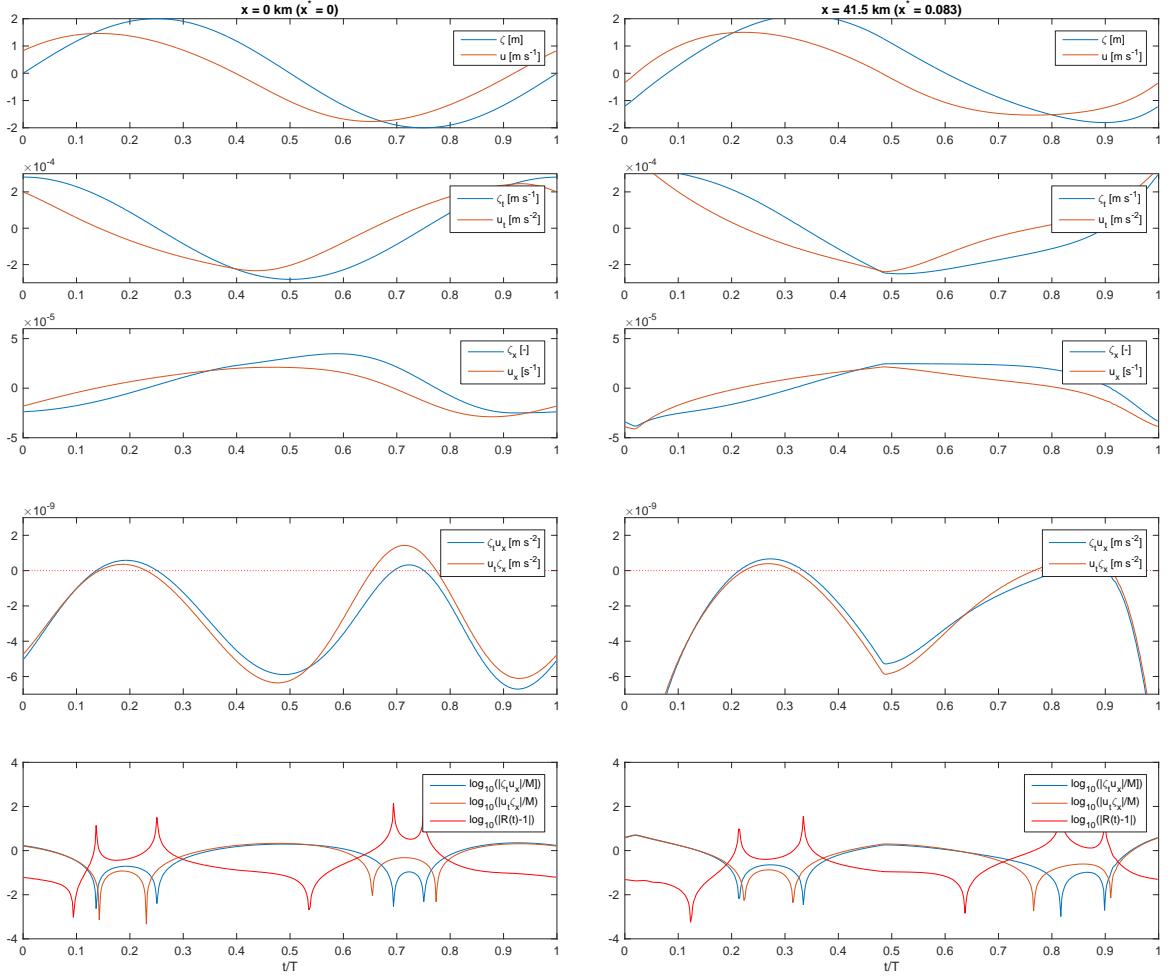


Figure 3: Temporal variation of  $\zeta$  and  $u$  (first plot),  $\zeta_t$  and  $u_t$  (second plot),  $\zeta_x$  and  $u_x$  (third plot),  $\zeta_t u_x$  and  $u_t \zeta_x$  (fourth plot), and  $\log_{10}(|\zeta_t u_x|/M)$ ,  $\log_{10}(|u_t \zeta_x|/M)$ ,  $\log_{10}(|R(t)-1|)$  (fifth plot, where  $R(t) = (u_t \zeta_x)/(\zeta_t u_x)$  and  $M$  is the mean of the tidally averages of  $|\zeta_t u_x|$  and  $|u_t \zeta_x|$ ), in  $x = 0$  km and  $x = 41.5$  km.

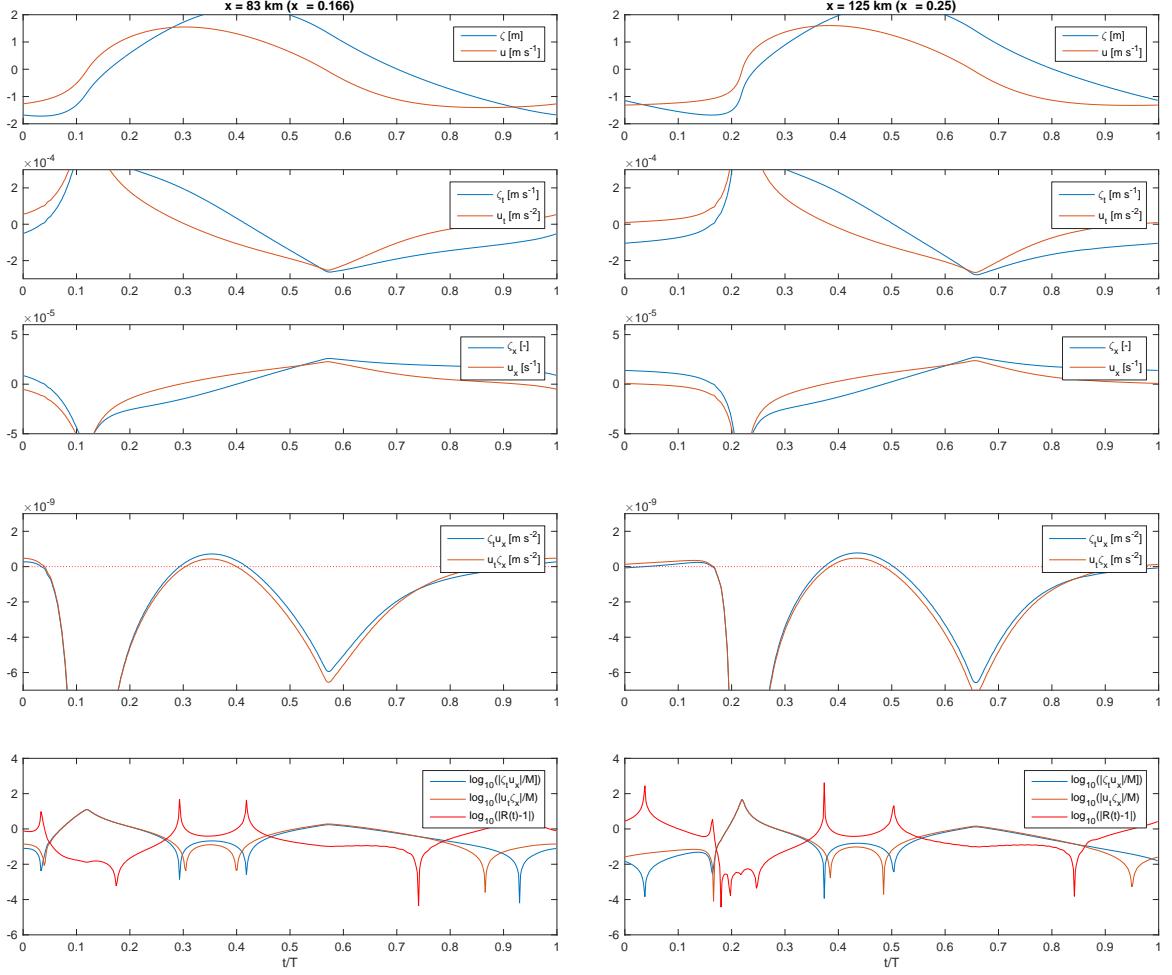


Figure 4: Temporal variation of  $\zeta$  and  $u$  (first plot),  $\zeta_t$  and  $u_t$  (second plot),  $\zeta_x$  and  $u_x$  (third plot),  $\zeta_t u_x$  and  $u_t \zeta_x$  (fourth plot), and  $\log_{10}(|\zeta_t u_x|/M)$ ,  $\log_{10}(|u_t \zeta_x|/M)$ ,  $\log_{10}(|R(t)-1|)$  (fifth plot, where  $R(t) = (u_t \zeta_x)/(\zeta_t u_x)$ ) (fifth plot, where  $R(t) = (u_t \zeta_x)/(\zeta_t u_x)$  and  $M$  is the mean of the tidally averages of  $|\zeta_t u_x|$  and  $|u_t \zeta_x|$ ), in  $x = 83$  km and  $x = 125$  km.

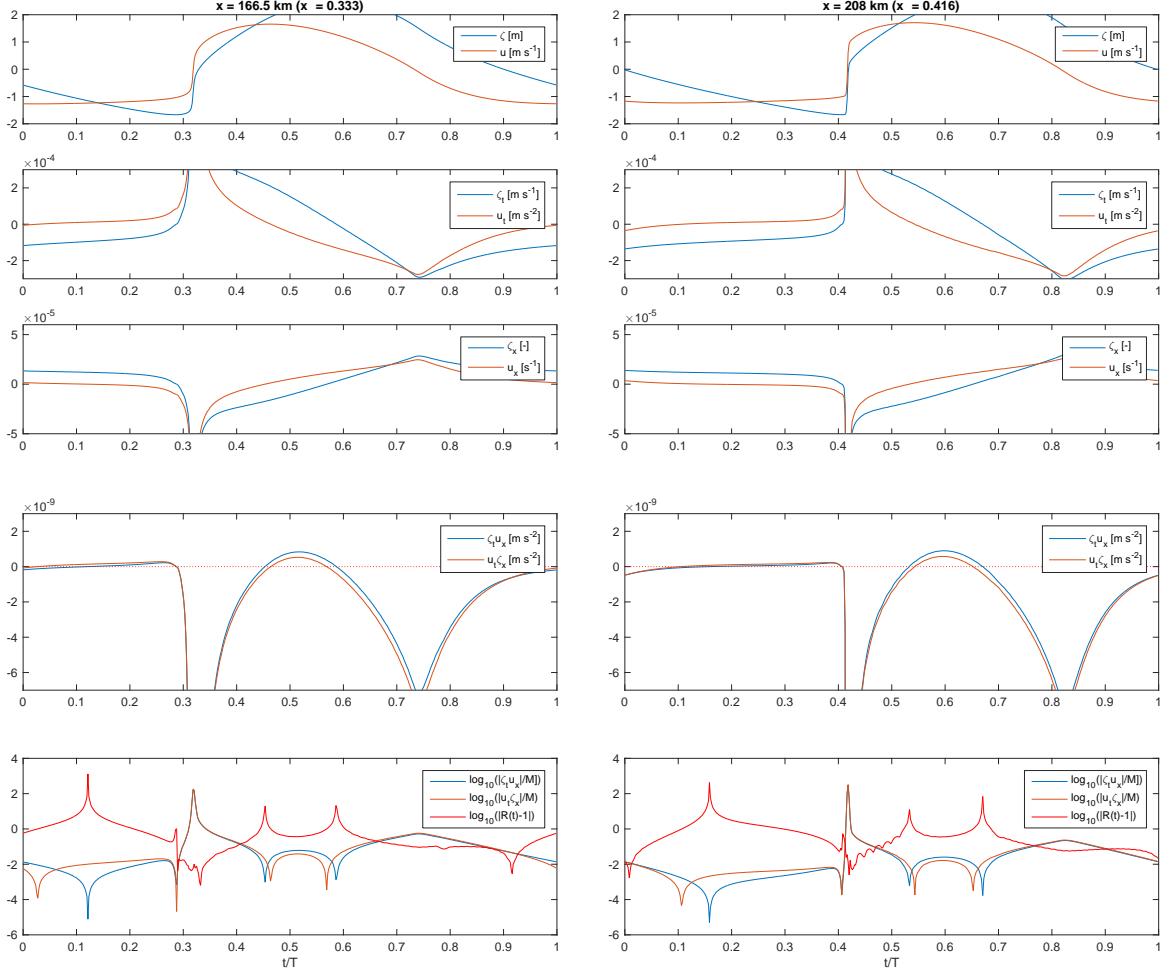


Figure 5: Temporal variation of  $\zeta$  and  $u$  (first plot),  $\zeta_t$  and  $u_t$  (second plot),  $\zeta_x$  and  $u_x$  (third plot),  $\zeta_t u_x$  and  $u_t \zeta_x$  (fourth plot), and  $\log_{10}(|\zeta_t u_x|/M)$ ,  $\log_{10}(|u_t \zeta_x|/M)$ ,  $\log_{10}(|R(t)-1|)$  (fifth plot, where  $R(t) = (u_t \zeta_x)/(\zeta_t u_x)$  and  $M$  is the mean of the tidally averages of  $|\zeta_t u_x|$  and  $|u_t \zeta_x|$ ), in  $x = 166.5 \text{ km}$  and  $x = 208 \text{ km}$ .

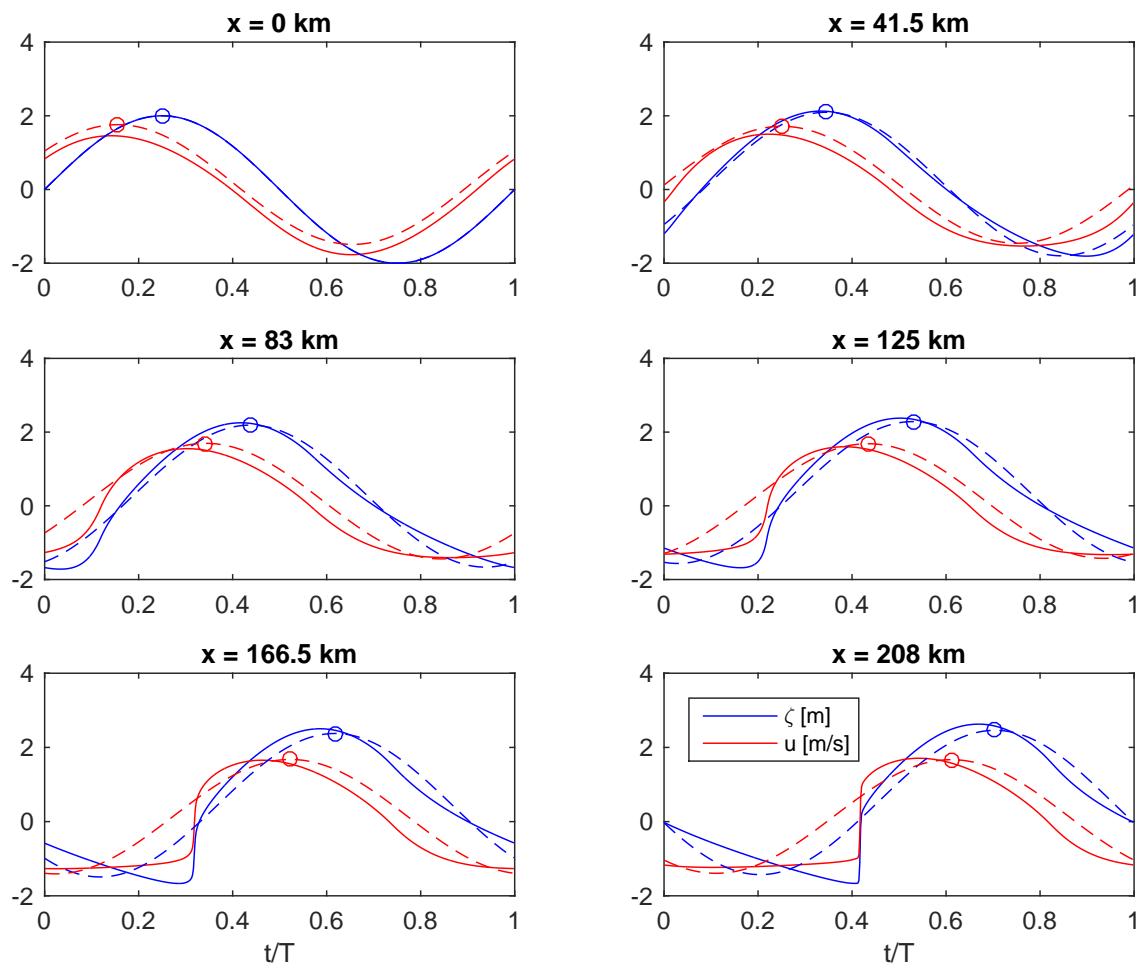


Figure 6: Tidal waves and Fourier series truncated at the first harmonic. Circles indicate the maxima of the dominant tidal component, from which it is possible to detect the phase lag  $u-\zeta$ .

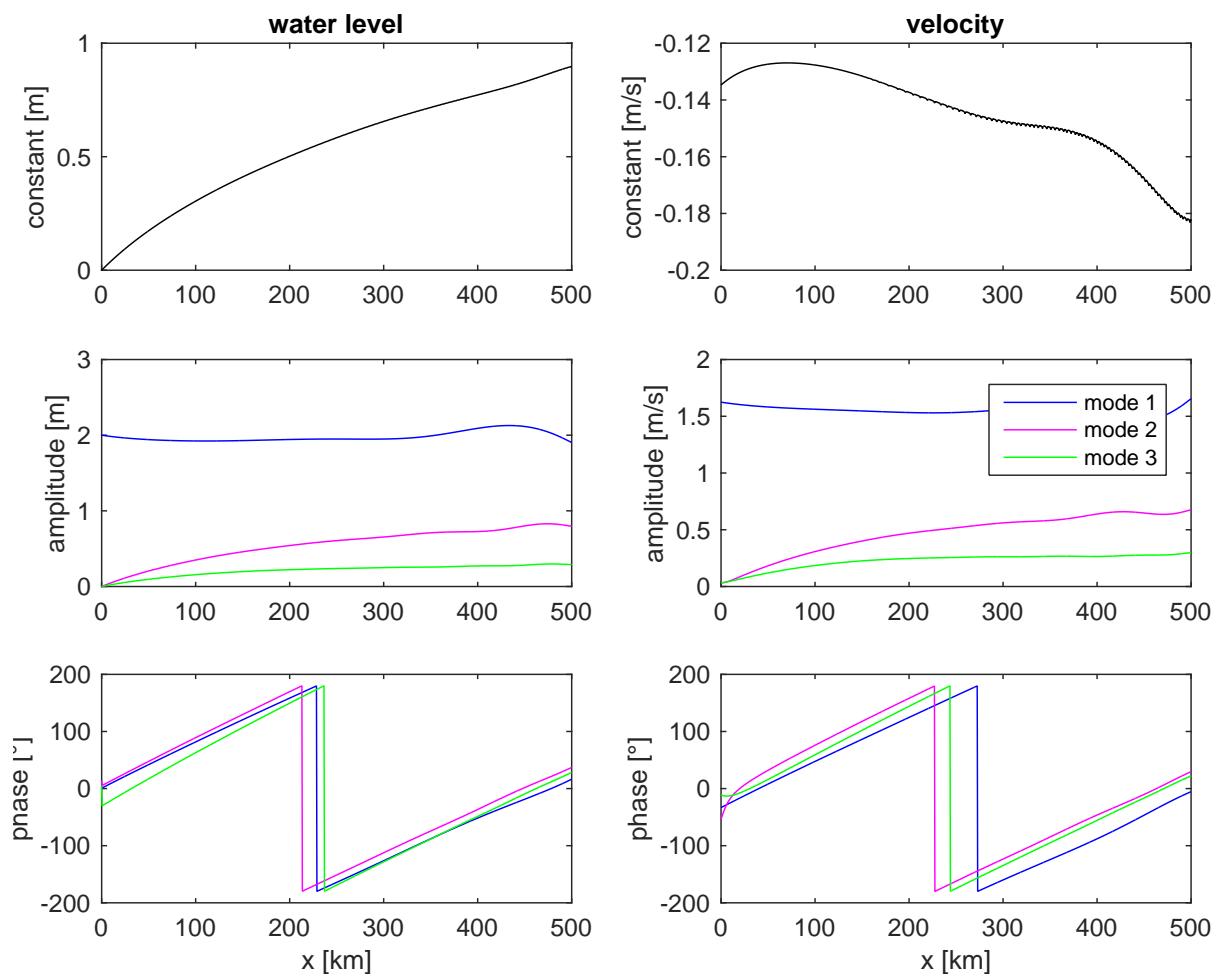


Figure 7: Fourier analysis of tidal wave. From top to bottom: constant term, amplitudes, phases of first three modes. Left column: water level  $\zeta$ ; right column: velocity  $u$ .

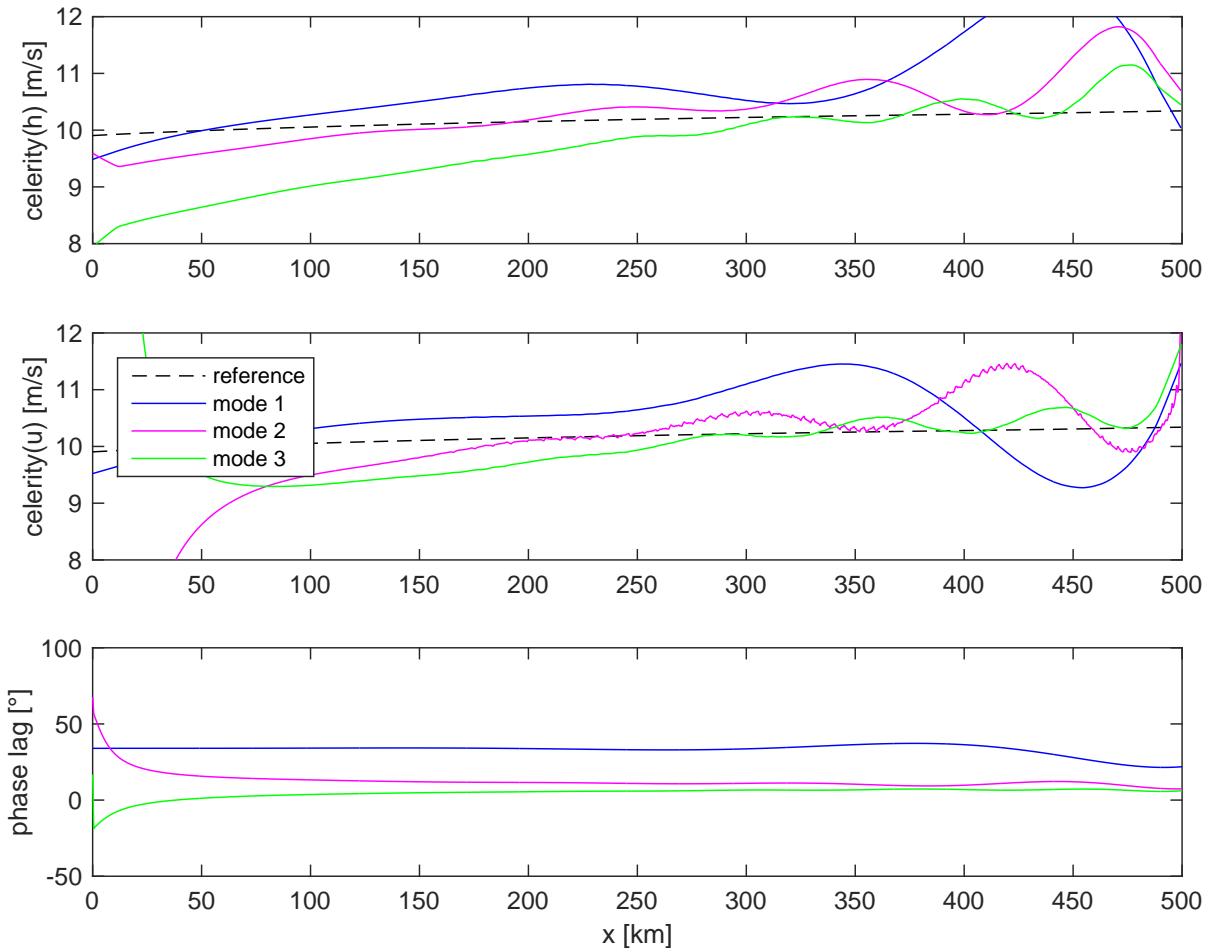


Figure 8: Wave celerity for water level  $\zeta$ , for velocity  $u$ , phase lag  $u-\zeta$ . Colors refer to the first three modes; black dashed line to wave celerity in a frictionless prismatic channel.

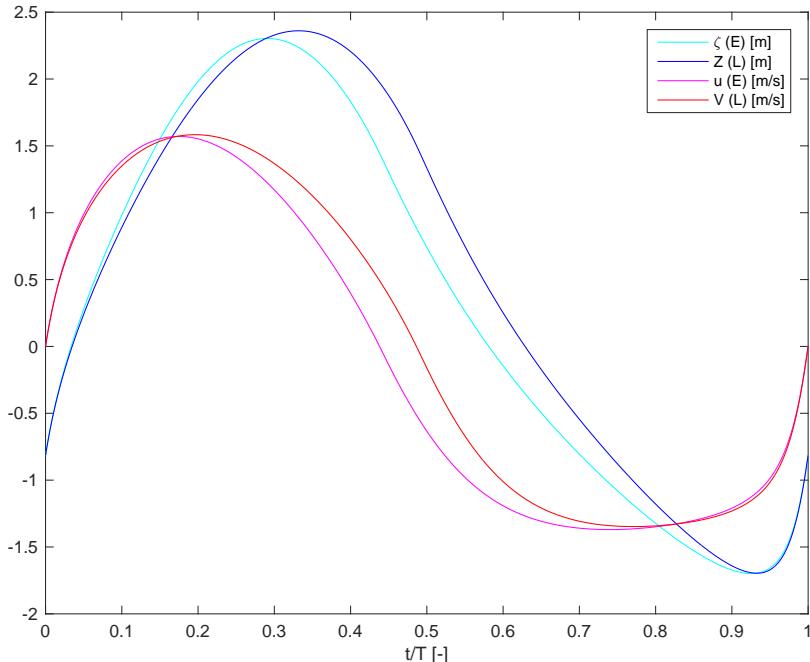


Figure 9: Lagrangean water level  $Z$  and velocity  $V$  compared with Eulerian values  $\zeta$  and  $u$  in  $x = 100$  km.

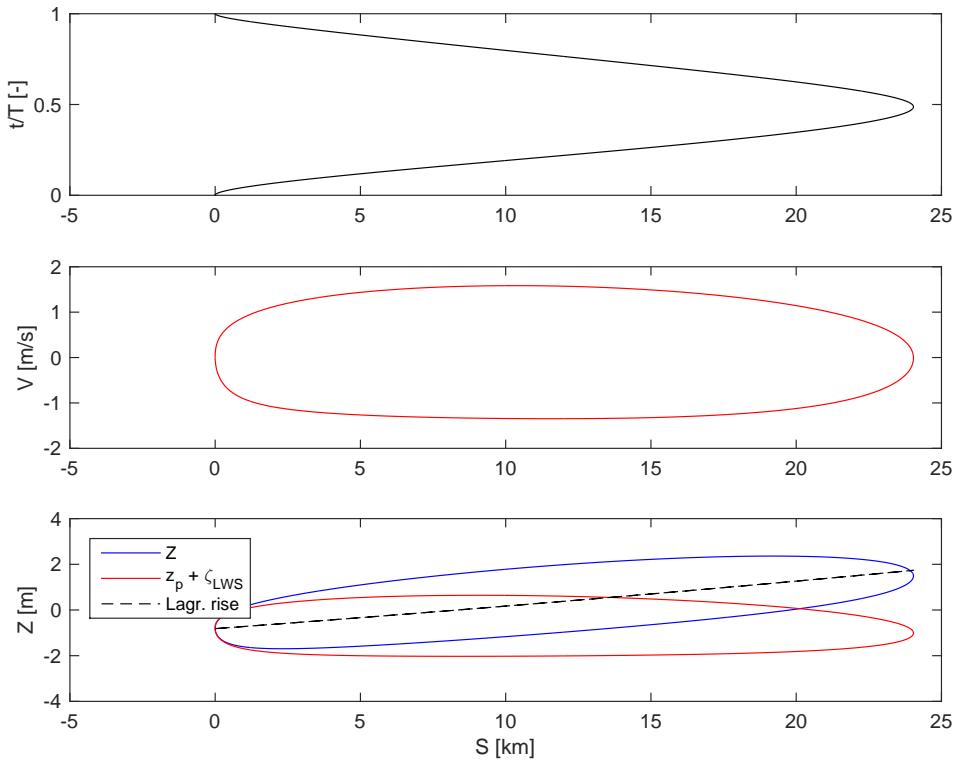


Figure 10: Lagrangean displacement  $S$  in time (first plot) and ellipses  $V$ - $S$  (second plot) and  $Z$ - $S$  (third plot).

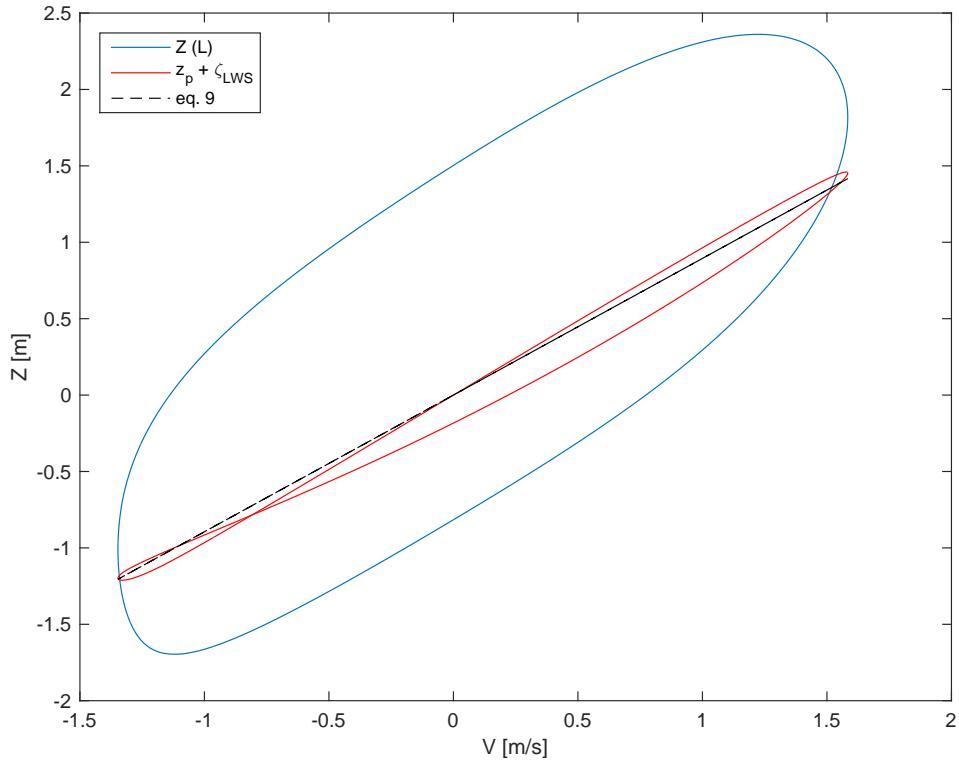


Figure 11: Lagrangean water level against velocity  $V$ :  $Z$  is the actual value,  $z_p + \zeta_{LWS}$  is the transformed water level. Black dashed lines: equation (9).

## Variant 5

Length  $b = 100$  km (exponential variation); Strickler coefficient  $K = 45 \text{ m}^{1/3}\text{s}^{-1}$ ; linear friction.

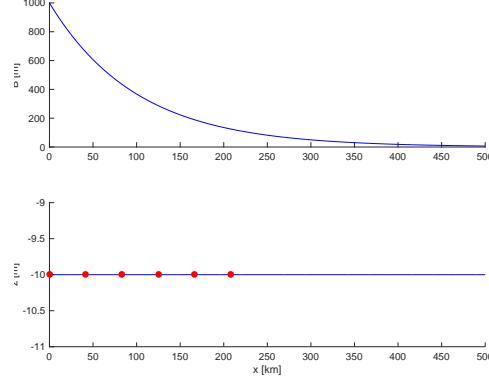


Figure 1: Longitudinal profiles of width and bottom. Dots indicates the locations where the temporal behaviour is shown in figure 3.

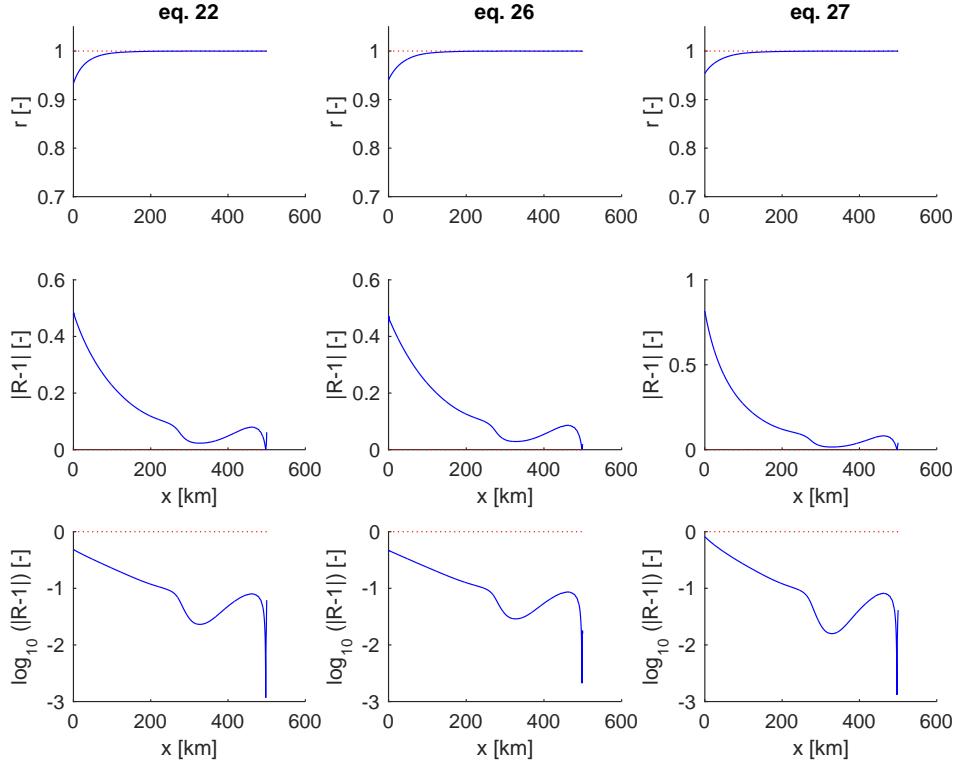


Figure 2: Longitudinal variation of the correlation coefficient  $r$  (first row) and of the two different functions of the ratio  $R$  between right hand side and left hand side of equations 22, 26 and 27 in the manuscript, respectively  $|R - 1|$  and  $\log_{10}(|R - 1|)$ .

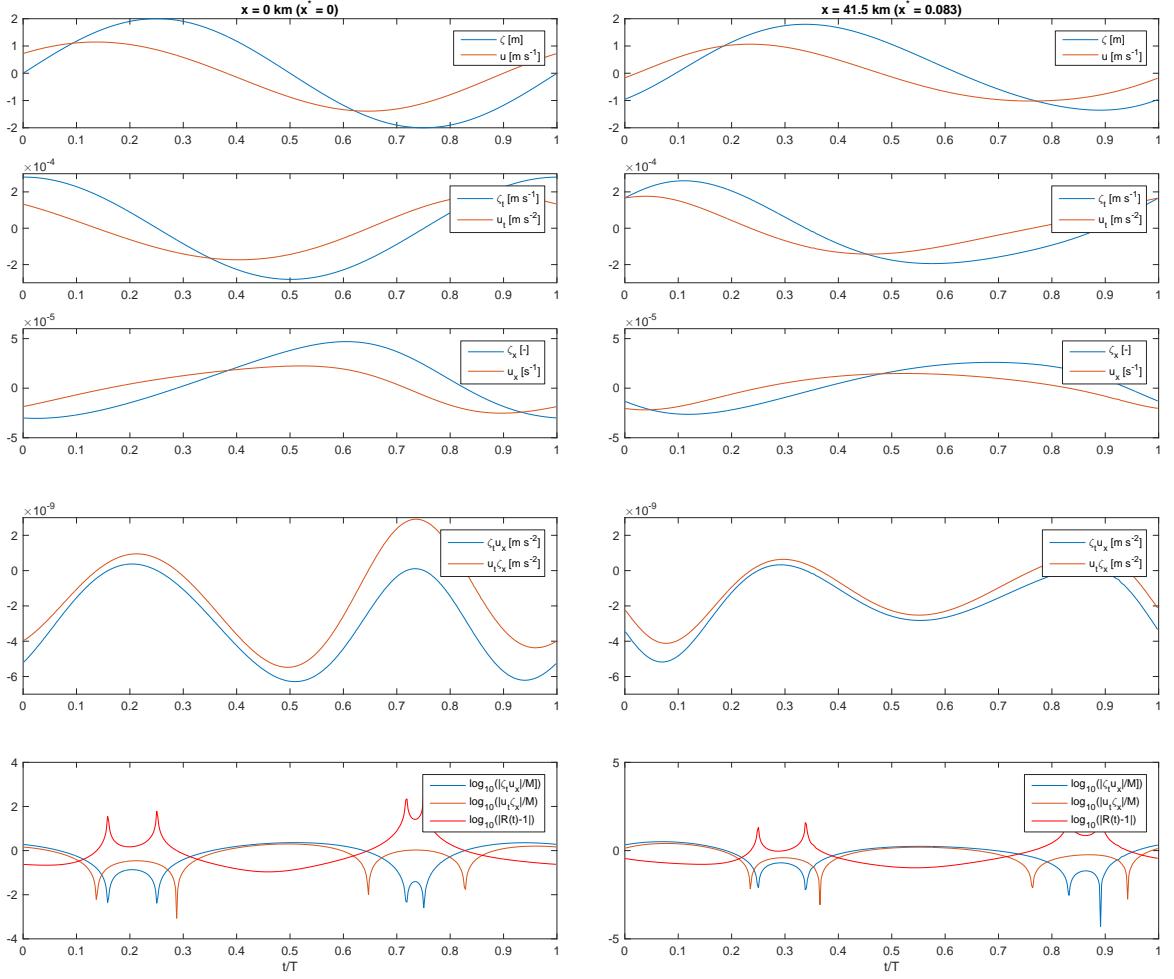


Figure 3: Temporal variation of  $\zeta$  and  $u$  (first plot),  $\zeta_t$  and  $u_t$  (second plot),  $\zeta_x$  and  $u_x$  (third plot),  $\zeta_t u_x$  and  $u_t \zeta_x$  (fourth plot), and  $\log_{10}(|\zeta_t u_x|/M)$ ,  $\log_{10}(|u_t \zeta_x|/M)$ ,  $\log_{10}(|R(t)-1|)$  (fifth plot, where  $R(t) = (u_t \zeta_x)/(\zeta_t u_x)$  and  $M$  is the mean of the tidally averages of  $|\zeta_t u_x|$  and  $|u_t \zeta_x|$ ), in  $x = 0$  km and  $x = 41.5$  km.

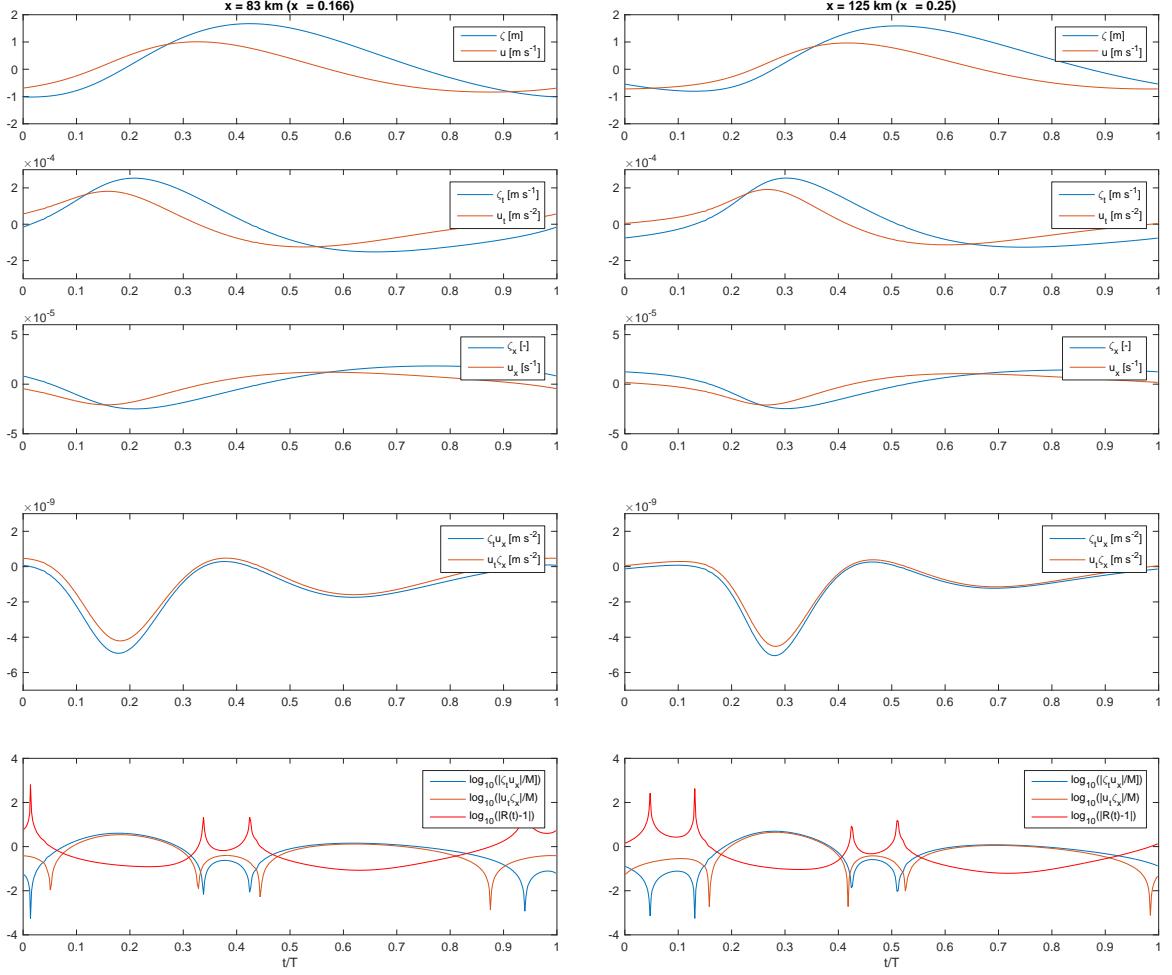


Figure 4: Temporal variation of  $\zeta$  and  $u$  (first plot),  $\zeta_t$  and  $u_t$  (second plot),  $\zeta_x$  and  $u_x$  (third plot),  $\zeta_t u_x$  and  $u_t \zeta_x$  (fourth plot), and  $\log_{10}(|\zeta_t u_x|/M)$ ,  $\log_{10}(|u_t \zeta_x|/M)$ ,  $\log_{10}(|R(t)-1|)$  (fifth plot, where  $R(t) = (u_t \zeta_x)/(\zeta_t u_x)$ ) (fifth plot, where  $R(t) = (u_t \zeta_x)/(\zeta_t u_x)$  and  $M$  is the mean of the tidally averages of  $|\zeta_t u_x|$  and  $|u_t \zeta_x|$ ), in  $x = 83$  km and  $x = 125$  km.

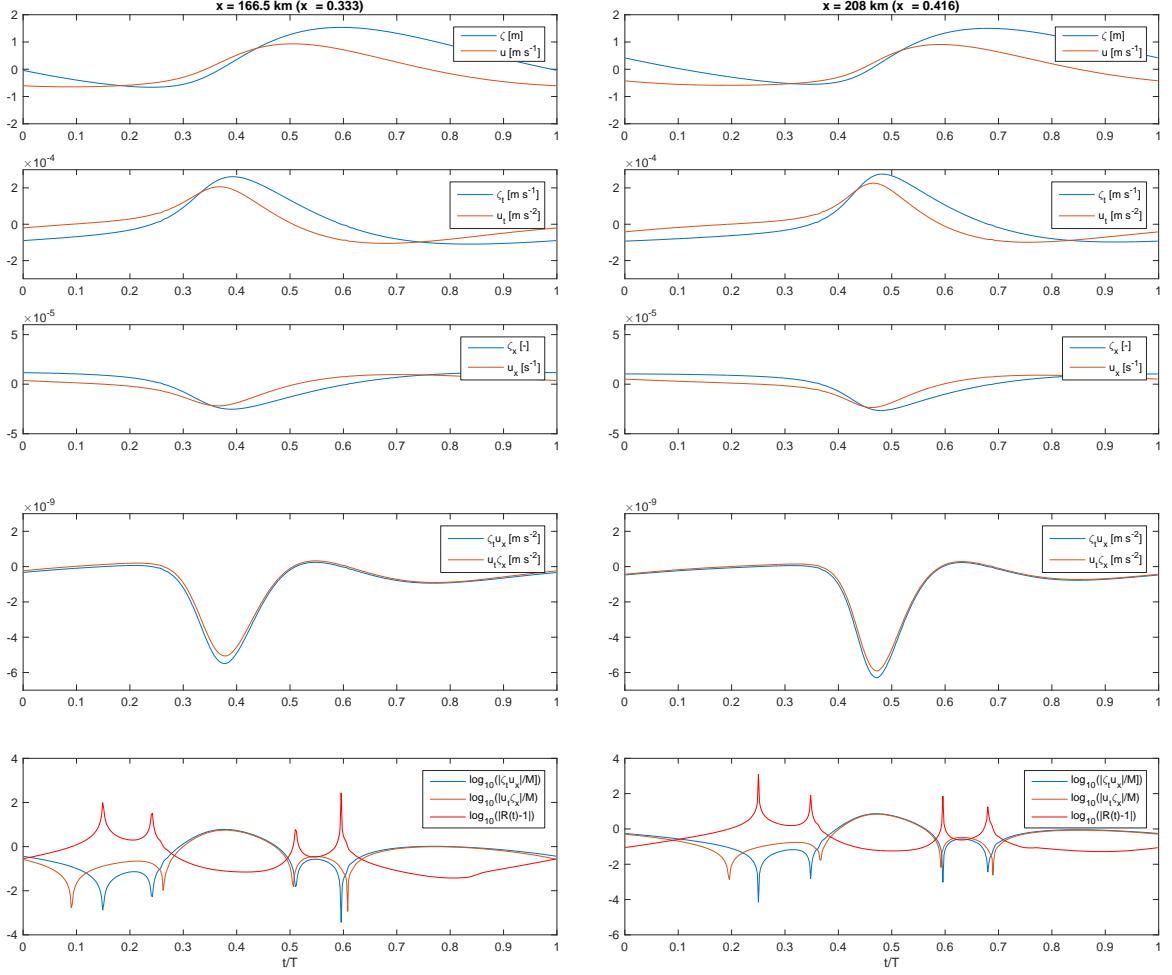


Figure 5: Temporal variation of  $\zeta$  and  $u$  (first plot),  $\zeta_t$  and  $u_t$  (second plot),  $\zeta_x$  and  $u_x$  (third plot),  $\zeta_t u_x$  and  $u_t \zeta_x$  (fourth plot), and  $\log_{10}(|\zeta_t u_x|/M)$ ,  $\log_{10}(|u_t \zeta_x|/M)$ ,  $\log_{10}(|R(t)-1|)$  (fifth plot, where  $R(t) = (u_t \zeta_x)/(\zeta_t u_x)$  and  $M$  is the mean of the tidally averages of  $|\zeta_t u_x|$  and  $|u_t \zeta_x|$ ), in  $x = 166.5 \text{ km}$  and  $x = 208 \text{ km}$ .

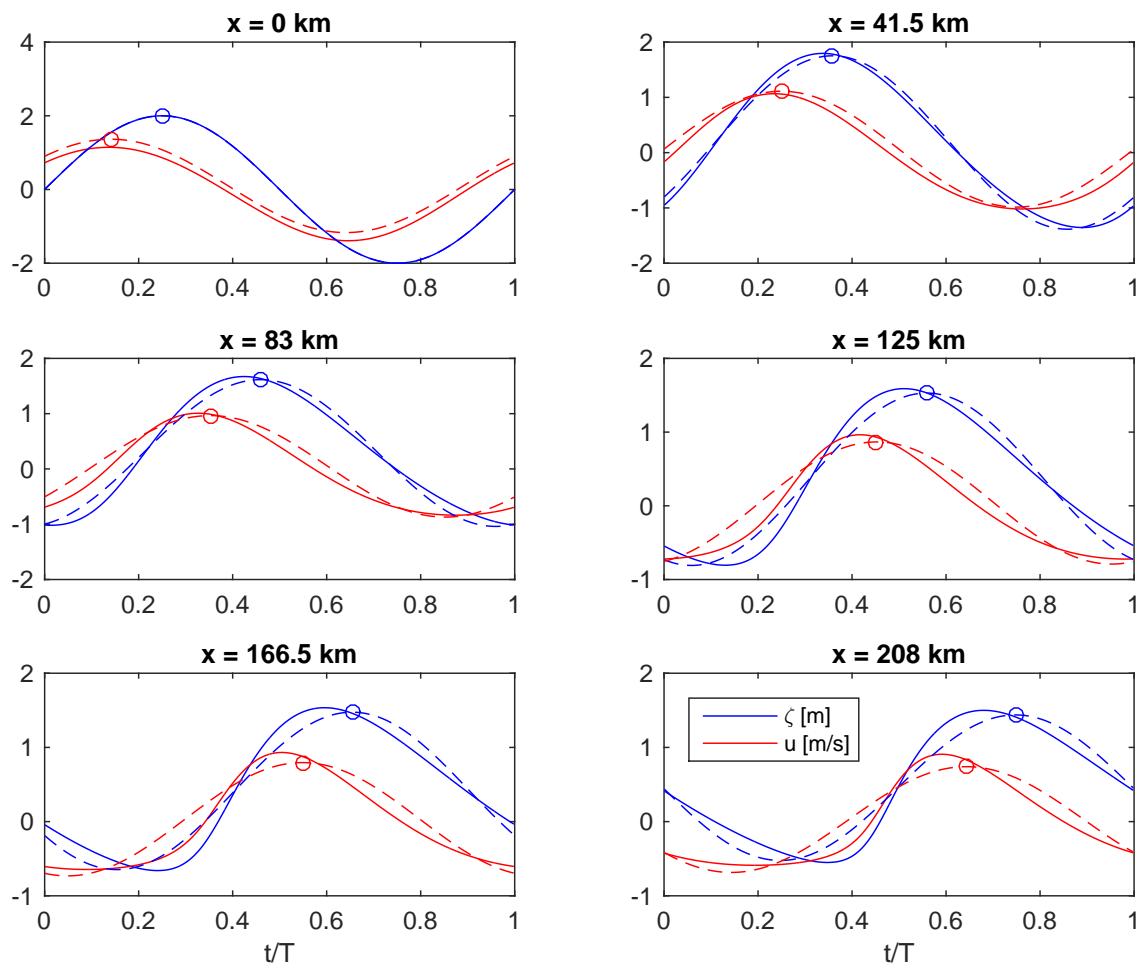


Figure 6: Tidal waves and Fourier series truncated at the first harmonic. Circles indicate the maxima of the dominant tidal component, from which it is possible to detect the phase lag  $u-\zeta$ .

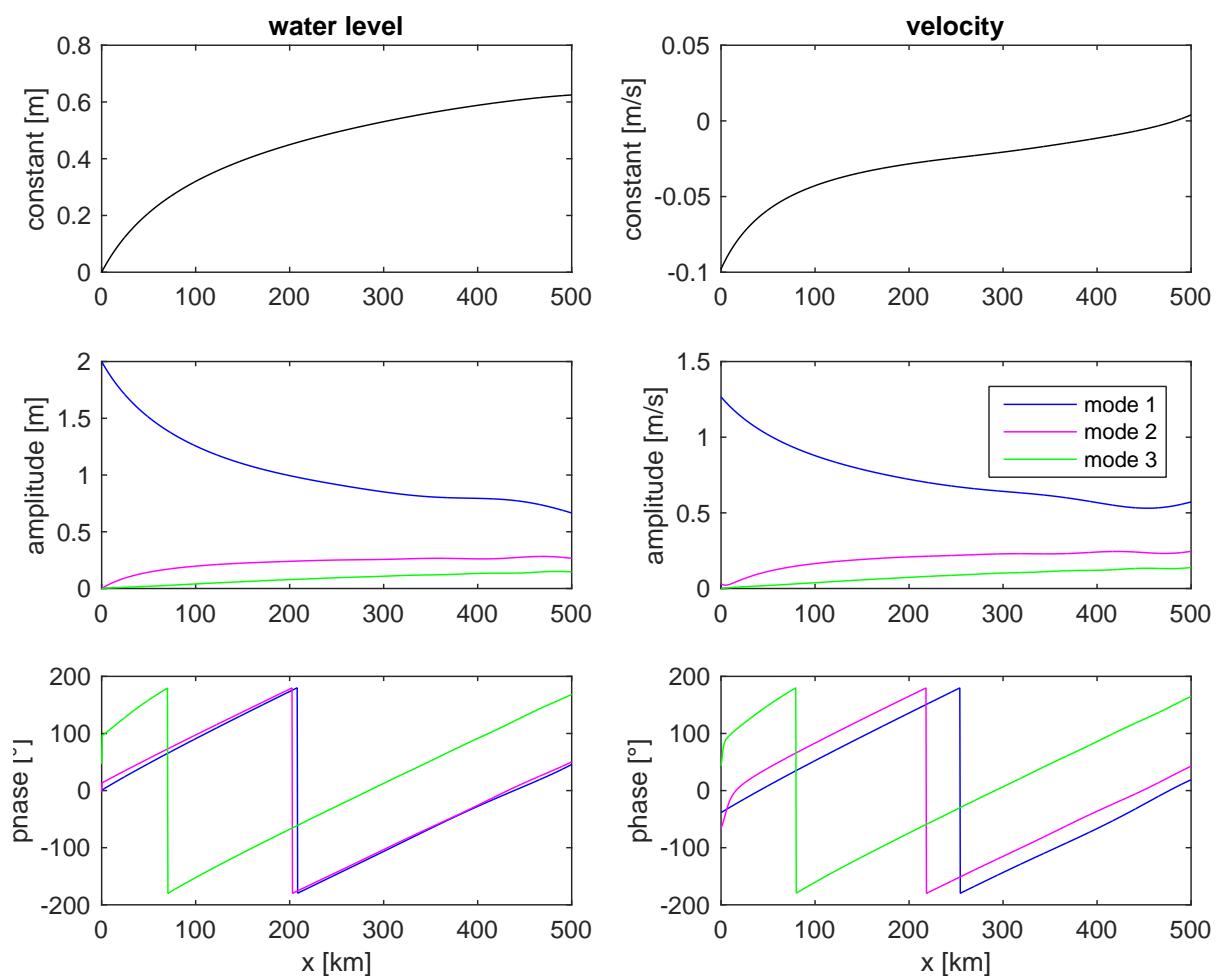


Figure 7: Fourier analysis of tidal wave. From top to bottom: constant term, amplitudes, phases of first three modes. Left column: water level  $\zeta$ ; right column: velocity  $u$ .

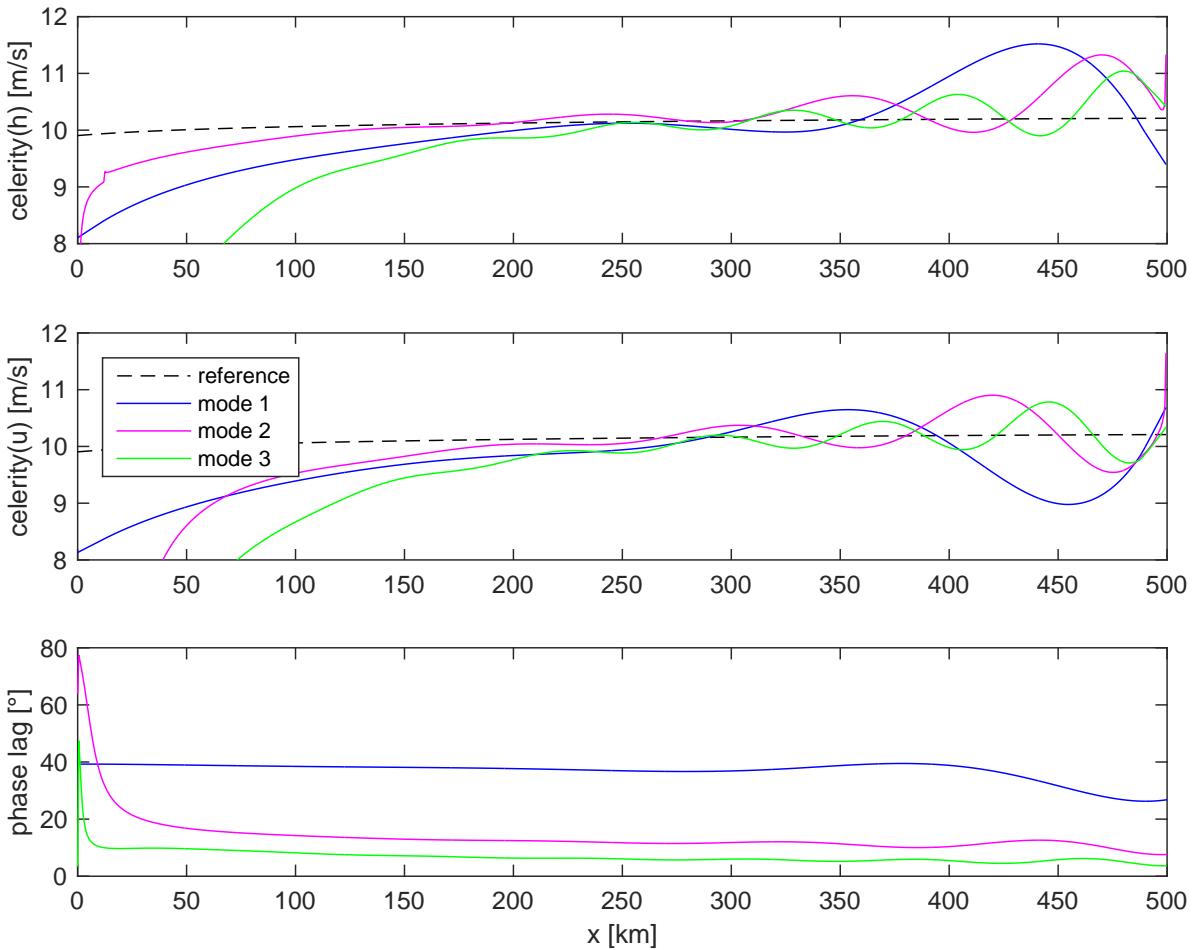


Figure 8: Wave celerity for water level  $\zeta$ , for velocity  $u$ , phase lag  $u-\zeta$ . Colors refer to the first three modes; black dashed line to wave celerity in a frictionless prismatic channel.

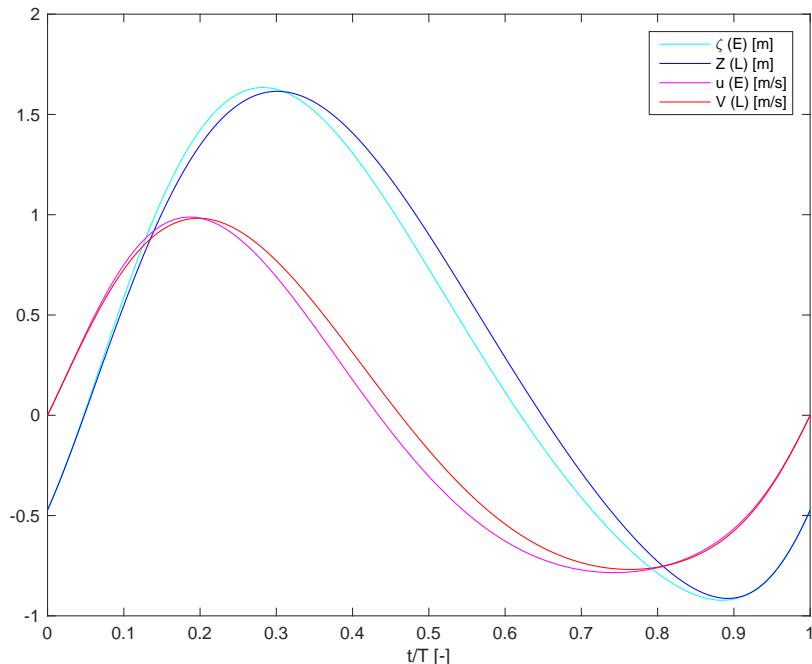


Figure 9: Lagrangean water level  $Z$  and velocity  $V$  compared with Eulerian values  $\zeta$  and  $u$  in  $x = 100$  km.

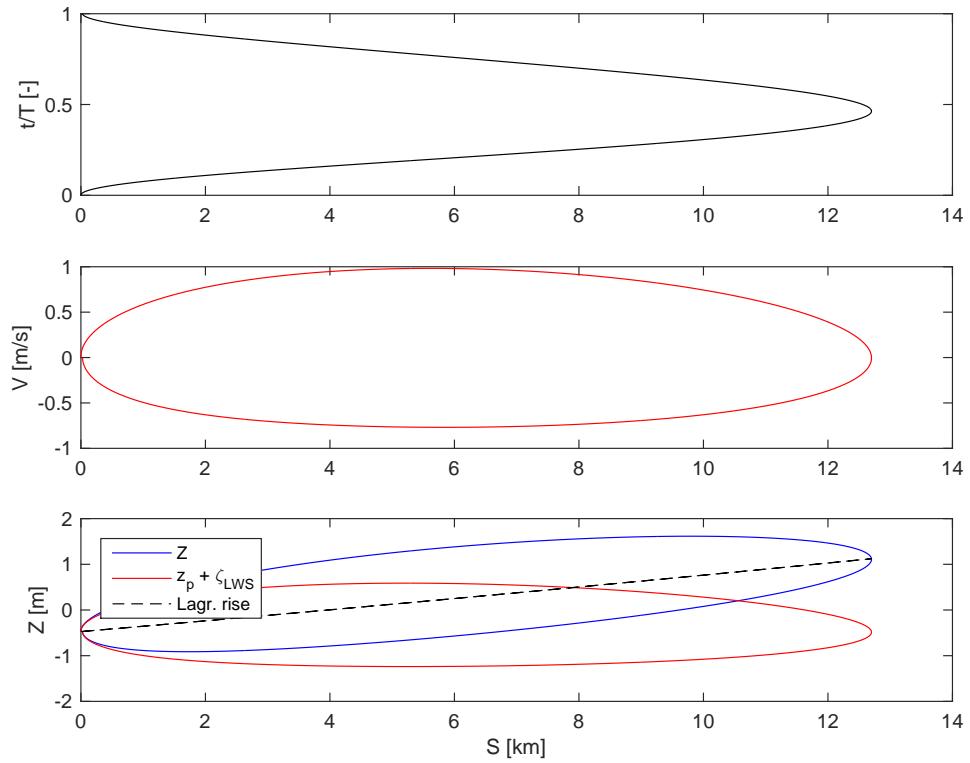


Figure 10: Lagrangean displacement  $S$  in time (first plot) and ellipses  $V$ - $S$  (second plot) and  $Z$ - $S$  (third plot).

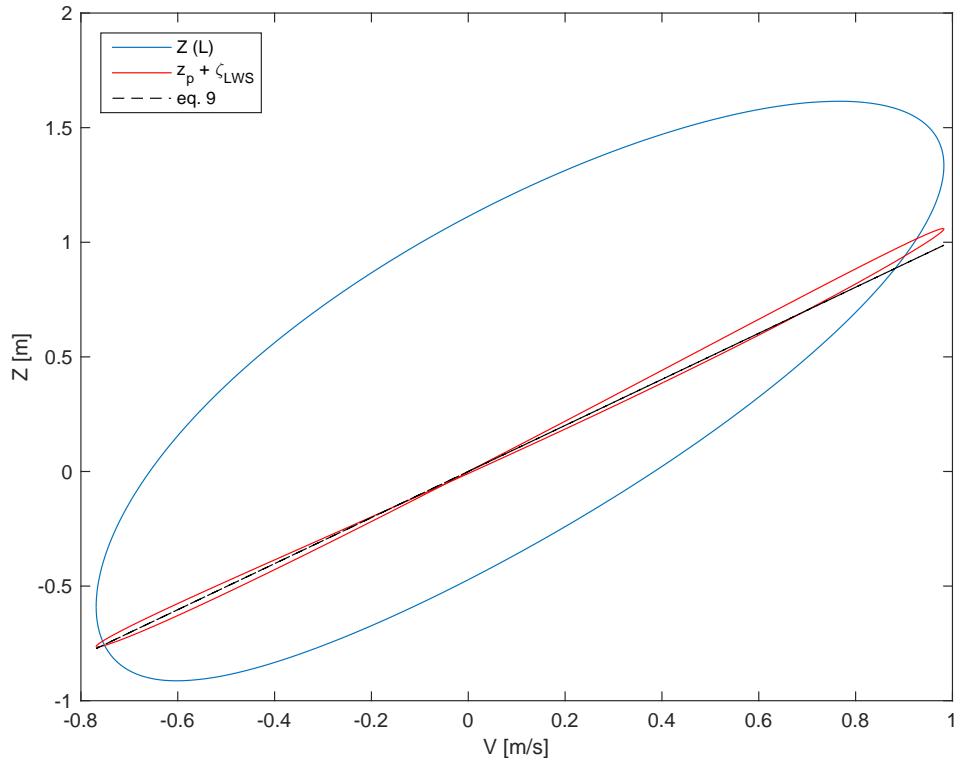


Figure 11: Lagrangean water level against velocity  $V$ :  $Z$  is the actual value,  $z_p + \zeta_{LWS}$  is the transformed water level. Black dashed lines: equation (9).

## Variant 6

Length  $b = 25$  km (exponential variation); Strickler coefficient  $K = 45 \text{ m}^{1/3}\text{s}^{-1}$ ; nonlinear friction; asymptotic width  $B_\infty = 10$  m.

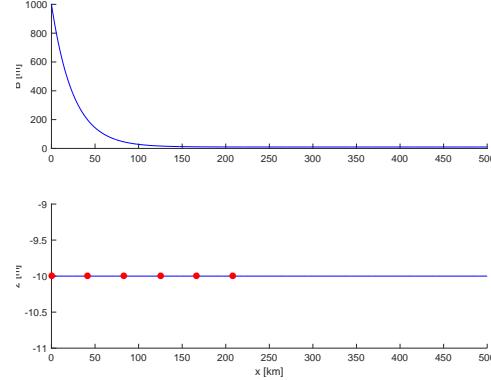


Figure 1: Longitudinal profiles of width and bottom. Dots indicates the locations where the temporal behaviour is shown in figure 3.

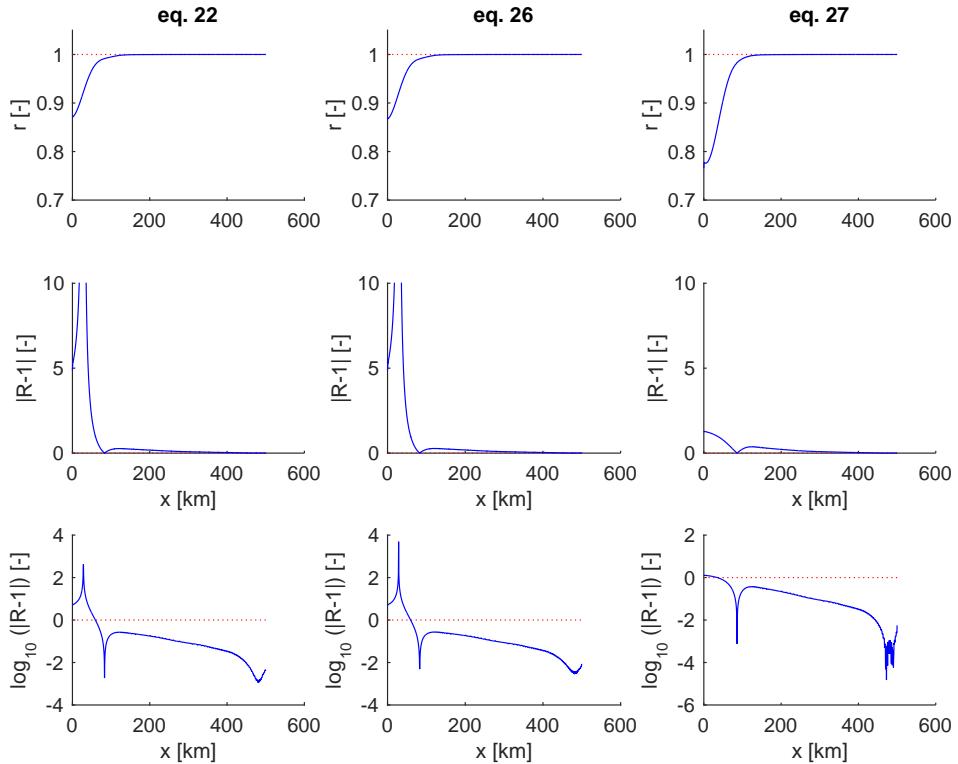


Figure 2: Longitudinal variation of the correlation coefficient  $r$  (first row) and of the two different functions of the ratio  $R$  between right hand side and left hand side of equations 22, 26 and 27 in the manuscript, respectively  $|R - 1|$  and  $\log_{10}(|R - 1|)$ .

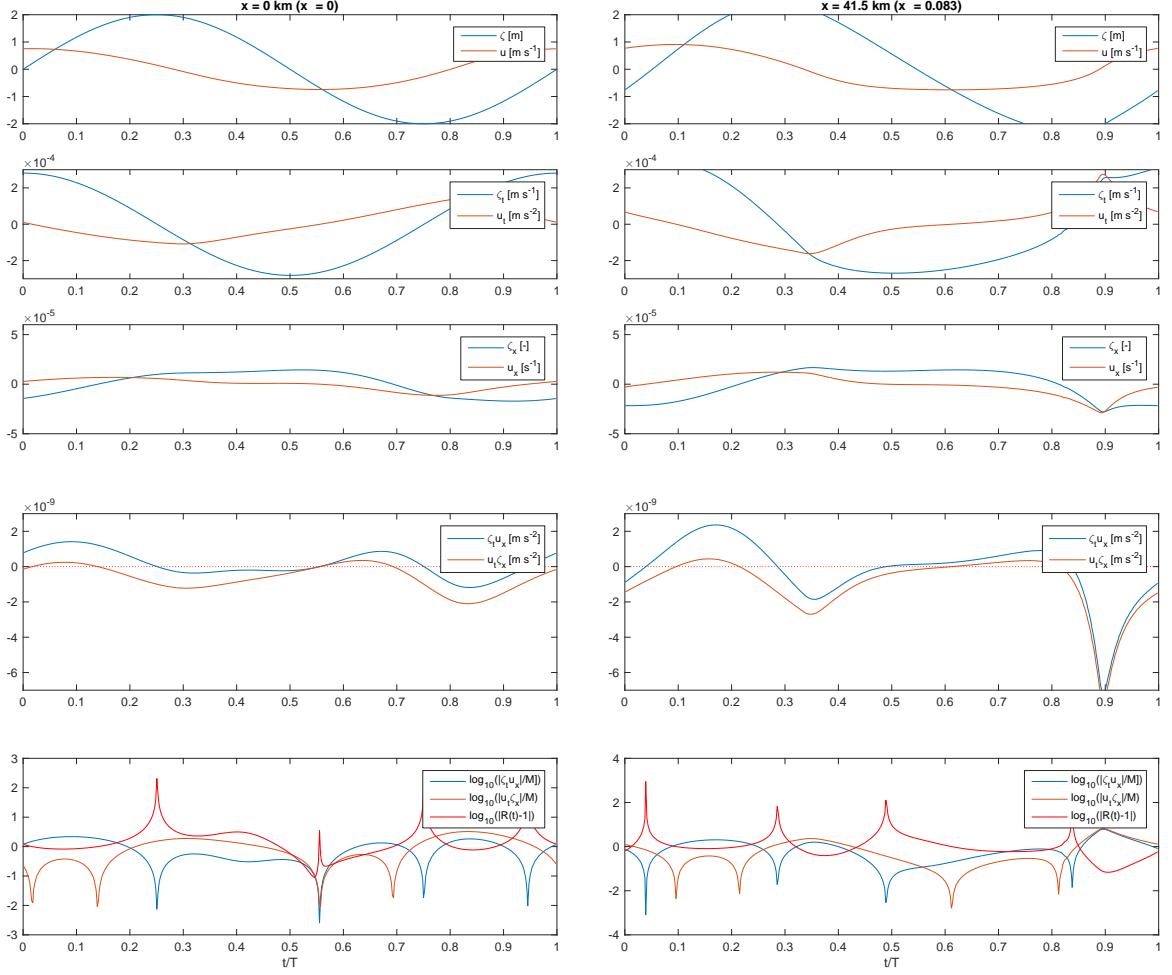


Figure 3: Temporal variation of  $\zeta$  and  $u$  (first plot),  $\zeta_t$  and  $u_t$  (second plot),  $\zeta_x$  and  $u_x$  (third plot),  $\zeta_t u_x$  and  $u_t \zeta_x$  (fourth plot), and  $\log_{10}(|\zeta_t u_x|/M)$ ,  $\log_{10}(|u_t \zeta_x|/M)$ ,  $\log_{10}(|R(t)-1|)$  (fifth plot, where  $R(t) = (u_t \zeta_x)/(\zeta_t u_x)$ ) and  $M$  is the mean of the tidally averages of  $|\zeta_t u_x|$  and  $|u_t \zeta_x|$ ), in  $x = 0$  km and  $x = 41.5$  km.

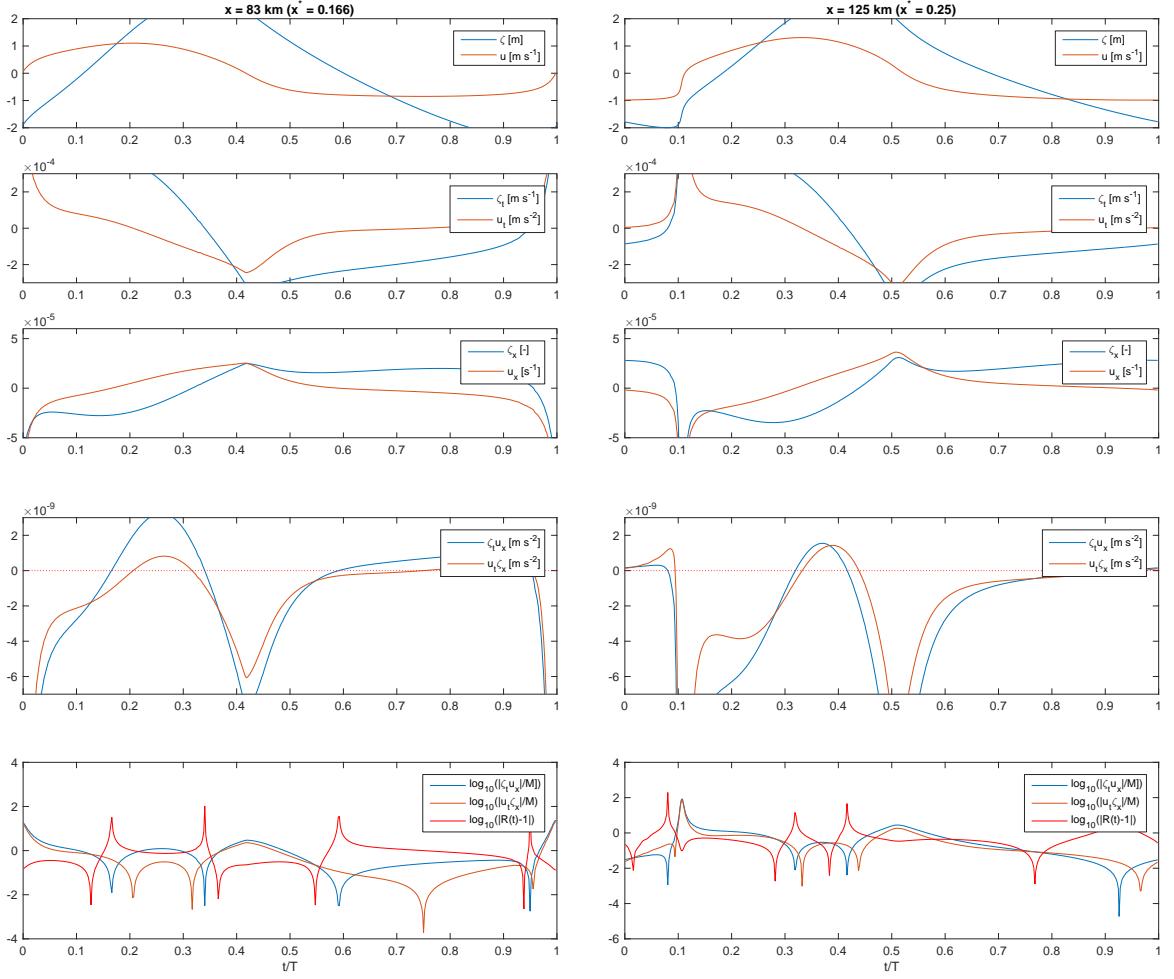


Figure 4: Temporal variation of  $\zeta$  and  $u$  (first plot),  $\zeta_t$  and  $u_t$  (second plot),  $\zeta_x$  and  $u_x$  (third plot),  $\zeta_t u_x$  and  $u_t \zeta_x$  (fourth plot), and  $\log_{10}(|\zeta_t u_x|/M)$ ,  $\log_{10}(|u_t \zeta_x|/M)$ ,  $\log_{10}(|R(t)-1|)$  (fifth plot, where  $R(t) = (u_t \zeta_x)/(\zeta_t u_x)$ ) (fifth plot, where  $R(t) = (u_t \zeta_x)/(\zeta_t u_x)$  and  $M$  is the mean of the tidally averages of  $|\zeta_t u_x|$  and  $|u_t \zeta_x|$ ), in  $x = 83$  km and  $x = 125$  km.

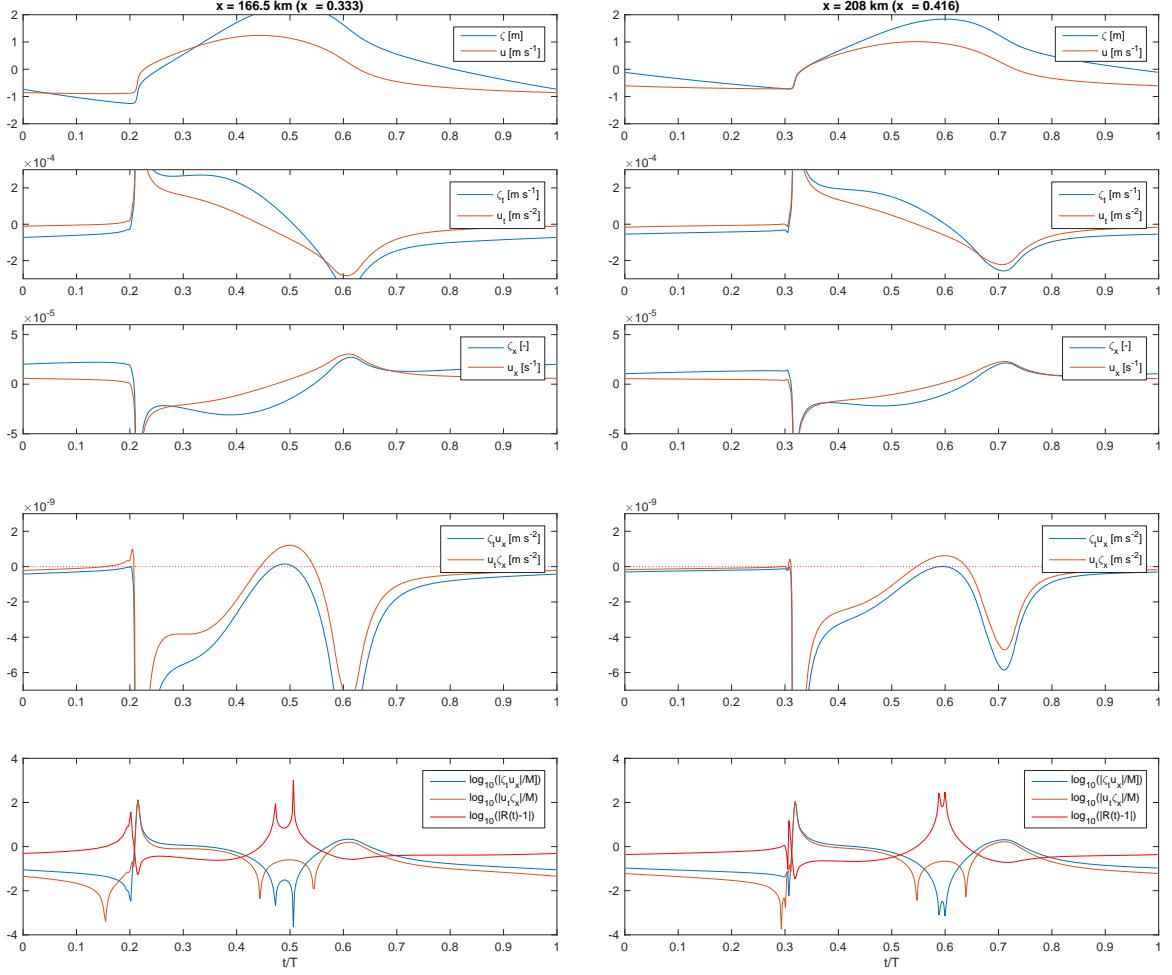


Figure 5: Temporal variation of  $\zeta$  and  $u$  (first plot),  $\zeta_t$  and  $u_t$  (second plot),  $\zeta_x$  and  $u_x$  (third plot),  $\zeta_t u_x$  and  $u_t \zeta_x$  (fourth plot), and  $\log_{10}(|\zeta_t u_x|/M)$ ,  $\log_{10}(|u_t \zeta_x|/M)$ ,  $\log_{10}(|R(t)-1|)$  (fifth plot, where  $R(t) = (u_t \zeta_x)/(\zeta_t u_x)$ ) in  $x = 166.5$  km and  $x = 208$  km.

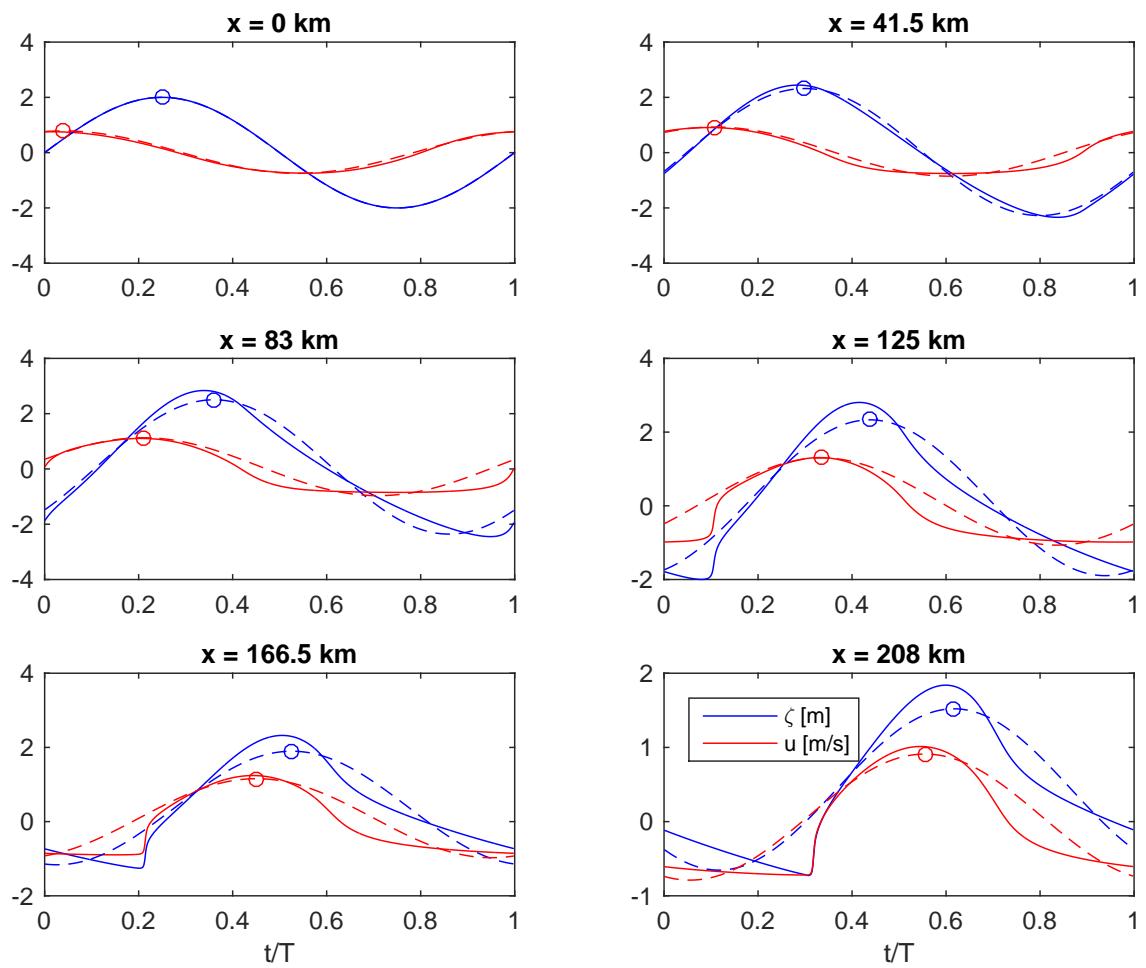


Figure 6: Tidal waves and Fourier series truncated at the first harmonic. Circles indicate the maxima of the dominant tidal component, from which it is possible to detect the phase lag  $u-\zeta$ .

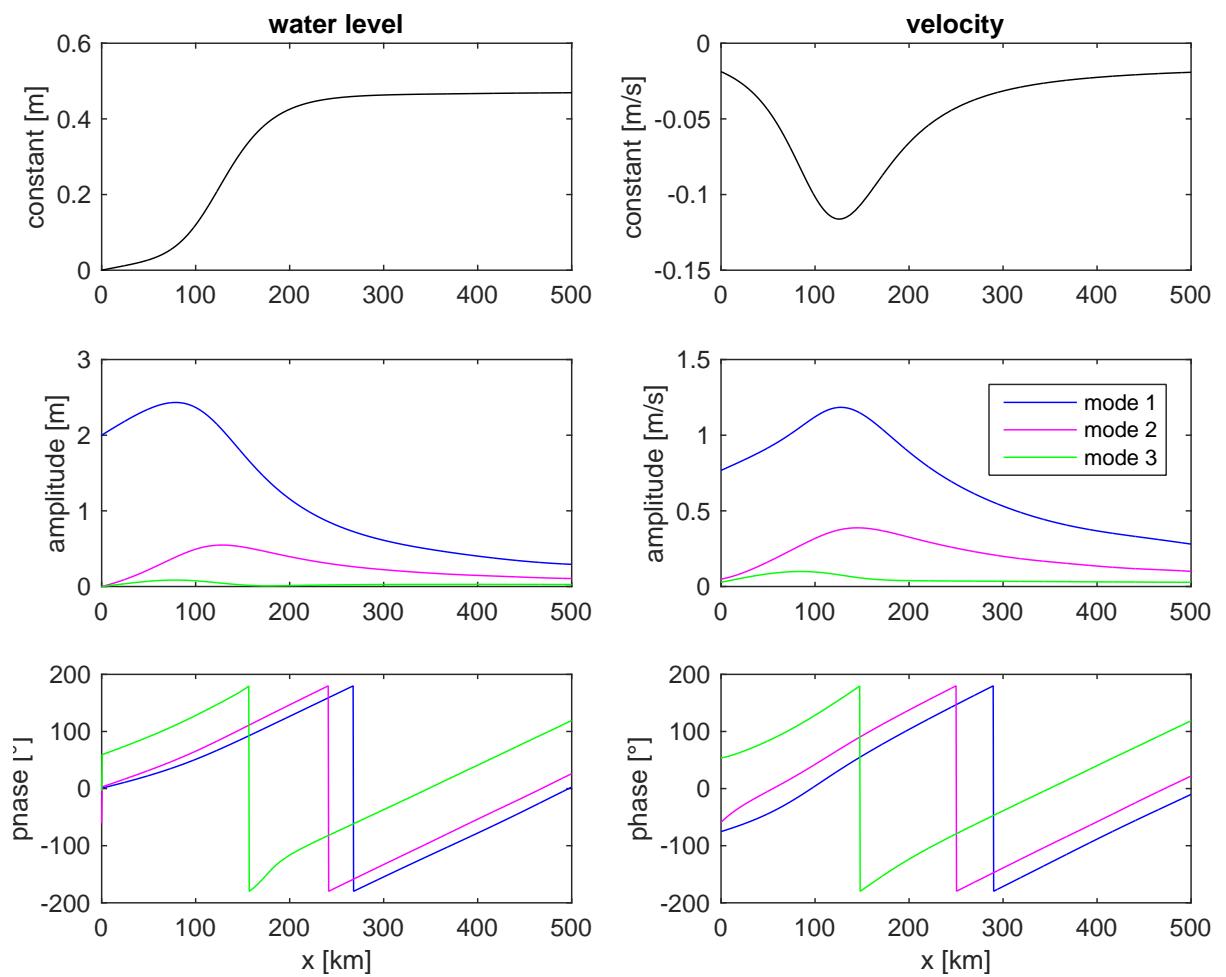


Figure 7: Fourier analysis of tidal wave. From top to bottom: constant term, amplitudes, phases of first three modes. Left column: water level  $\zeta$ ; right column: velocity  $u$ .

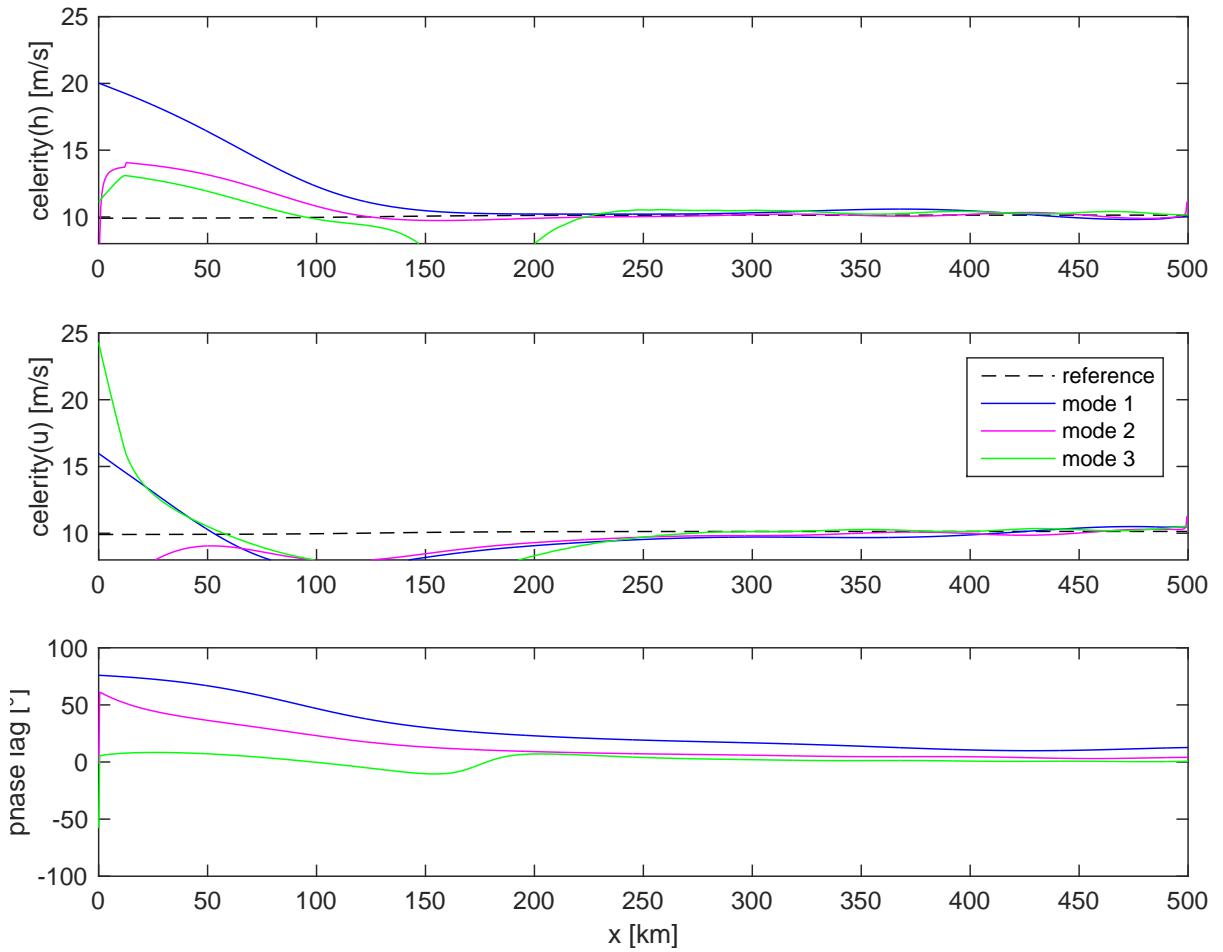


Figure 8: Wave celerity for water level  $\zeta$ , for velocity  $u$ , phase lag  $u-\zeta$ . Colors refer to the first three modes; black dashed line to wave celerity in a frictionless prismatic channel.

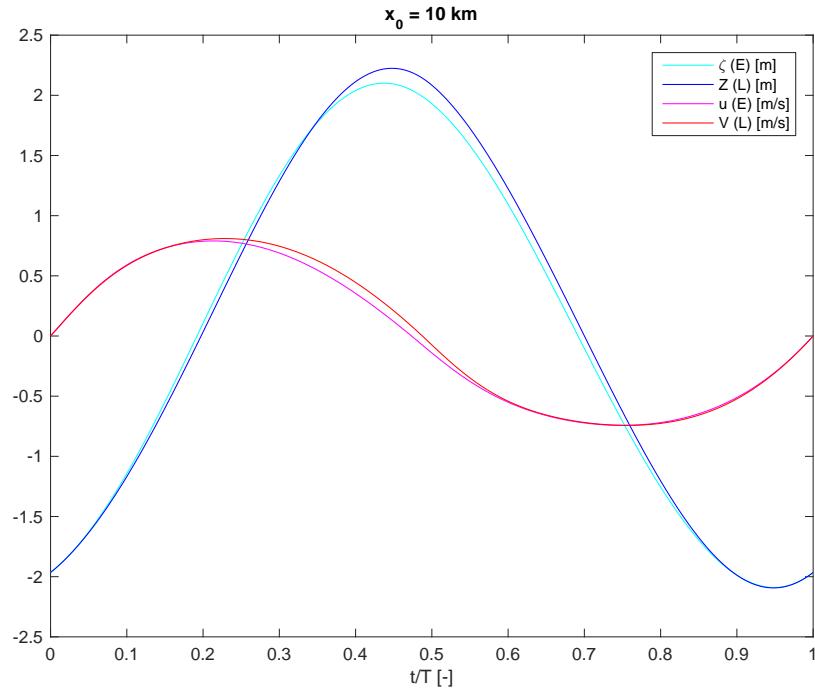


Figure 9: Lagrangean water level  $Z$  and velocity  $V$  compared with Eulerian values  $\zeta$  and  $u$ , for  $x_0 = 10 \text{ km}$ .

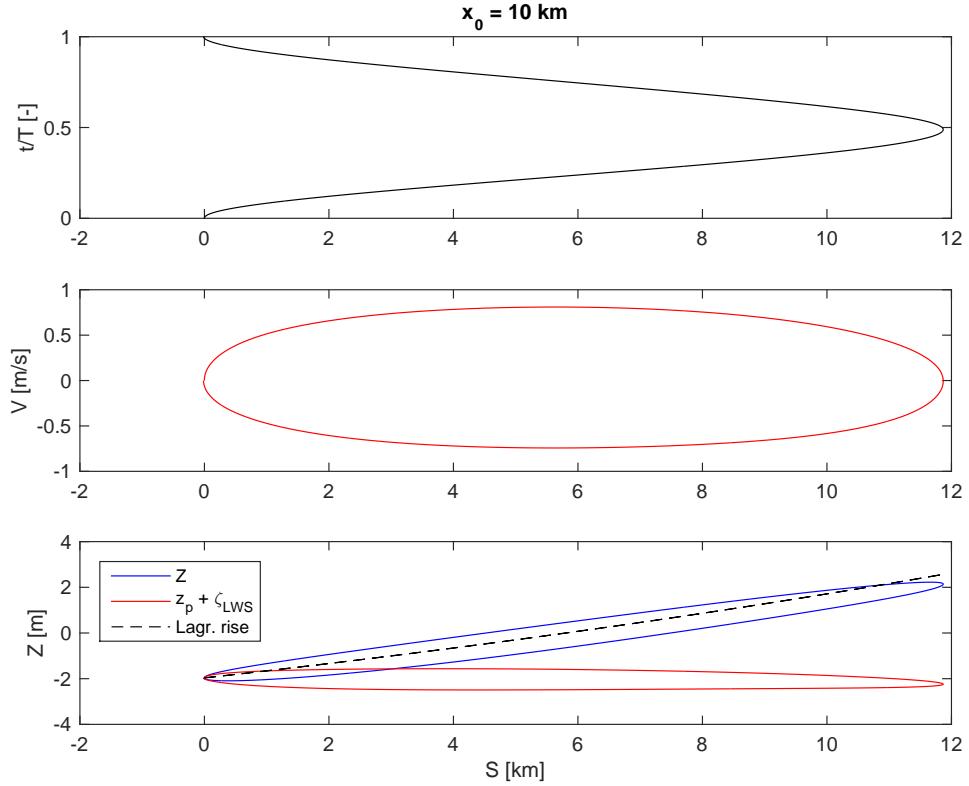


Figure 10: Lagrangean displacement  $S$  in time (first plot) and ellipses  $V$ - $S$  (second plot) and  $Z$ - $S$  (third plot), for  $x_0 = 10 \text{ km}$ .

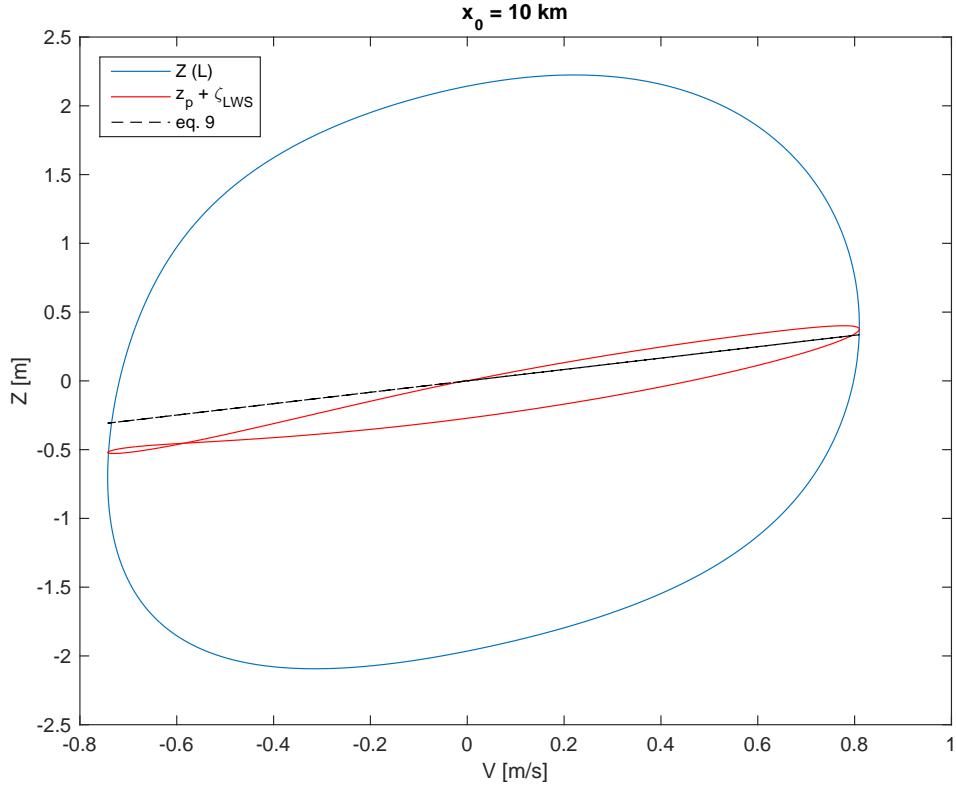


Figure 11: Lagrangean water level against velocity  $V$ :  $Z$  is the actual value,  $z_p + \zeta_{LWS}$  is the transformed water level, for  $x_0 = 10 \text{ km}$ . Black dashed lines: equation (9).