

The Sound Speed Anomaly of Baltic Seawater

C. von Rohden¹, S. Weinreben², and F. Fehres¹

[1]{Physikalisch-Technische Bundesanstalt (PTB), Abbestr. 2-12, 10587 Berlin, Germany}

[2]{Leibniz Institute for Baltic Sea Research, Seestr. 15, 18119 Warnemünde, Germany}

Correspondence to: F. Fehres (Felix.Fehres@ptb.de)

Abstract

The effect of the anomalous chemical composition of Baltic seawater on the speed of sound relative to seawater with quasi-standard composition was quantified at atmospheric pressure and temperatures of 1 to 46 °C. Three modern oceanographic time-of-flight sensors were applied in a laboratory setup for measuring the speed-of-sound difference δw in a pure water diluted sample of North Atlantic seawater and a sample of Baltic seawater of the same conductivity, i.e. the same Practical Salinity ($S_P=7.766$). The average δw amounts to $0.069\pm 0.014 \text{ m}\cdot\text{s}^{-1}$, significantly larger than the resolution and reproducibility of the sensors and independent of temperature. This magnitude for the anomaly effect was verified with offshore measurements conducted at different sites in the Baltic Sea using one of the sensors. The results from both measurements show values up to one order of magnitude smaller than existing predictions based on chemical models.

1. Introduction

An important issue regarding the quantification of thermodynamic properties of seawater with high accuracy is the natural variability of the relative composition of dissolved solutes. A certain variability of the thermodynamic properties should be connected with this. Although known for more than a century, these property anomalies came more into focus with the recent formulation of the equation of state of seawater (TEOS-10: IOC et al., 2010). TEOS-10 consistently represents all thermodynamic properties of seawater at the high accuracy level required for modern oceanographic research and state-of-the-art modelling. It also supports the investigation of effects associated with composition anomalies. However, for a number of

1 properties including the speed of sound, there is a lack of experimental data with sufficient
2 accuracy for a reliable quantification of the anomaly effects.

3 TEOS-10 refers to Absolute Salinity S_A as a basic input variable which quantifies the total
4 mass of all dissolved species in a unit mass of seawater. However, S_A is not directly
5 measurable in practice. Salinity as a basic oceanographic measurand besides temperature and
6 pressure is commonly determined from CTD measurements (conductivity, temperature, and
7 pressure) according to the Practical Salinity Scale (PSS-78, Perkin and Lewis, 1980). That
8 means that the Practical Salinity S_P as a measure for salinity exclusively refers to electrically
9 conductive solutes. Hence, for the conversion of S_P to S_A at a high accuracy level, the natural
10 variation of the relative composition of solutes as well as the contribution of non-ionic species
11 have to be considered. For the global ocean, this is implemented in TEOS-10 with an anomaly
12 correction based on a mapped data set (McDougall et al., 2012). The salinity anomaly is
13 described as $\delta S_A = S_A - S_R$, referring to the conductivity based Reference Salinity
14 $S_R = S_P \cdot (35.16504/35) \text{ g} \cdot \text{kg}^{-1}$ as the best estimate of the Absolute Salinity of seawater with a
15 standard composition. Typically, δS_A in the open ocean is small but significant, reaching δS_A
16 $= 0.027 \text{ g} \cdot \text{kg}^{-1}$ in the northern North Pacific (IOC et al., 2010). This equals a relative deviation
17 of 0.077 % at Standard Seawater salinity. The main sources are additions of nutrients and
18 carbonates (Millero et al., 2008). However, the effect may be larger in coastal and estuarine
19 waters, mainly because of the increased influence of freshwater input from rivers, causing a
20 significant effect on the related thermodynamic properties. Feistel et al. (2010a) state that
21 currently the accuracy of the empirical formulas for thermodynamic properties of seawater is
22 easily limited by such effects.

23 The Baltic Sea has brackish water, which is influenced by the Ca^{2+} and carbonate dominated
24 freshwater input from various rivers, and is therefore an especially good example. Extensive
25 field measurements and studies on salinity and density shifts due to composition variability in
26 the Baltic Sea have been conducted (e.g. Millero and Kremling, 1976; Feistel et al., 2010b).
27 Feistel et al. (2010a) presented a comprehensive study on thermophysical property anomalies
28 in Baltic seawater based on chemical models of multi-component aqueous electrolytes. One
29 of the conclusions is that particularly the speed of sound and the density should be sensitive to
30 the presence of anomalous solutes. Sound speed is one of the quantities of fundamental
31 interest due to its thermodynamic relation to other properties, e.g. compressibility and density,
32 and because of its large field of technical applications, e.g. in marine acoustics.

1 In this study we focus on the speed of sound and show measurement results quantifying the
2 sound speed difference which is associated with the anomalous chemical composition of
3 Baltic seawater. We applied modern acoustic time-of-flight sensors from two different
4 manufacturers under controlled laboratory conditions. The sensors, designed for
5 oceanographic in situ applications, provide sufficient resolution to resolve the speed-of-sound
6 anomaly, independently of their reliability for absolute measurements and of the exact manner
7 of sensor calibration.

8 We also applied one of the sensors in situ during a field campaign in the south-western Baltic
9 Sea and present results from measurements at different sites and depths. The aim was to test
10 the sensor under field conditions as well as to evaluate its principal ability for use as an
11 acoustic in situ detector for the salinity anomaly. The speed-of-sound measurements were
12 carried out simultaneously with CTD casts. On-board measurements of density and Practical
13 Salinity in water samples taken in parallel were conducted for independent estimates of the
14 salinity anomaly.

15

16 **2. Measurements**

17 For the speed-of-sound measurements we used oceanographic time-of-flight sensors (AML
18 SV XChange OEM, Valeport miniSVS, and Valeport miniSVS OEM, hereafter referred to as
19 SVX, VP, and VP OEM, respectively)¹. The sensors are designed for in situ measurements in
20 seawater under field conditions. They consist of a single Piezo-electric transducer/receiver
21 and a reflector plate, which is kept at distances of 3.4 cm and 10 cm, respectively, by fixed
22 rods. The time of flight is measured as a time interval of a single acoustic pulse travelling
23 along the transducer-reflector path. Table 1 summarizes basic sensor specifications. The speed
24 of sound is calculated directly from the time of flight, based on a calibration in pure water and
25 applying equations of state (EOS). Modern digital signal processing and timing techniques
26 provide the high resolution of the time-of-flight determination.

27 Because the focus was on the small differences of sound speed, we did not primarily rely on
28 absolute measurements or uncertainties related to the individual sensors and the

¹ Disclaimer: Any mention of commercial products within this study does not imply recommendation or endorsement by PTB.

1 manufacturer-given built-in methods for time-of-flight determination. It was rather the high
2 resolution together with the stability which we used for the detection of the anomaly-related
3 sound speed differences.

4 In a separate laboratory study on the capability of these sensors, we investigated their
5 characteristics and accuracies for measurements in different electrolyte solutions and in
6 natural seawater in the temperature range of 1-50 °C at atmospheric pressure (von Rohden et
7 al., 2015). The experimental setup described there was also used for the laboratory
8 measurements in the current study. In summary, the sensors together with two PTB-calibrated
9 standard platinum resistance thermometers (SPRT) were placed in a sealed, well stirred, and
10 thermostated 55 liter bath completely filled with the samples. The temperature was stabilized
11 within ≈ 1 mK in the vicinity of the sensors during the periods of sound speed recording. The
12 conductivity was continuously observed as a purity check or to track the stability of the
13 sample salinity, and to determine the Practical Salinity. The sensors were operated
14 simultaneously assuring virtually identical conditions. At each preselected temperature, 20 to
15 40 single pulses were recorded with each sensor at a rate of 1 Hz, and afterwards averaged.
16 We carried out a thorough recalibration in pure water, including repeated checks over the
17 period of investigations in seawater samples. Based on this calibration, the speed of sound in
18 Atlantic seawater and in Baltic water has been measured.

19 The measurements of the current study aimed at the determination of the difference of the
20 speed of sound in Baltic and Atlantic seawater. The Baltic sample was taken in the Arkona
21 Basin (see Fig. 2). The North Atlantic reference sample (NA II) was taken from the surface
22 close to the permanent station “Kiel 267” (33°N, 22°W) in the Madeira Basin in May 2016.
23 The location was chosen because of the low nutrient content, as the samples were mainly
24 intended for laboratory calibration of conductivity probes. We therefore considered the
25 sample as a substitute for Standard Seawater having reference composition. Before
26 measurements, the NA II sample was diluted with pure water to virtually the same Practical
27 Salinity S_P as the original Baltic sample. Besides the adjustment of S_P , the same bath
28 temperatures for the separate measurements were preselected to achieve conditions as similar
29 as possible for the comparison of the sound speed results.

30

1 2.1 Salinity anomaly

2 Because the sound speed anomaly δw is related to the salinity anomaly, we first estimated the
3 Absolute Salinities S_A and the connected salinity anomaly δS for our samples. For the diluted
4 North Atlantic water we calculated the Absolute Salinity according to TEOS-10 as
5 $S_{A,cond}=S_R=S_P \cdot u_{PS}$, based on the conductivity and temperature readings. That is, we assumed
6 standard composition in the diluted sample. We regard this assumption as justified because
7 the salinity anomaly mapped for the North Atlantic region (IOC et al. 2010) can be neglected
8 within the range of our experimental salinity uncertainty.

9 For the Baltic sample, we first estimated the salinity the same way as for the Atlantic sample,
10 i.e. assuming standard composition. Secondly, we calculated $S_{A,dens}$ from an independent
11 density measurement. The density was measured repeatedly at 20 °C with an oscillating U-
12 tube densimeter (Anton Paar DSA 5000 M) to $1004.154 \pm 0.004 \text{ kg} \cdot \text{m}^{-3}$. With it the Absolute
13 Salinity $S_{A,dens}$ was calculated using the TEOS-10 expression $S_{A,dens}(T, p, \rho)$. Although the
14 expression presumes standard salt composition again, the estimation of the Absolute Salinity
15 from the measured density is assumed to be appropriate for the Baltic sample. This is because
16 the density-salinity relation is virtually insensitive to the exact salt composition as long as the
17 deviations from the standard composition are small. That is, for many common ions, the
18 change in density caused by very small additions is within measurement uncertainty of a
19 similar change in the mass of sea salt. This is the empirical assumption known as Millero's
20 rule (Millero 2008, Feistel et al. 2010a, b). We identified the difference $\delta S_{A,m}=S_{A,dens}-S_{A,cond}$
21 as the measure for the salinity anomaly of the Baltic sample in $\text{g} \cdot \text{kg}^{-1}$. Non-conductive solutes
22 which are not included should play a minor role in the case of Baltic water. Our measure for
23 the salinity difference $\delta S_{A,m}$ is easy to access by the above-mentioned routine density and
24 conductivity measurement techniques. Because we can identify $S_{A,dens}$ as the Absolute Salinity
25 described in TEOS-10, and $S_{A,cond}$ as the Reference Salinity S_R , we can compare $\delta S_{A,m}$ with
26 the parameterization for Baltic seawater given by Feistel et al. (2010a). It is based on
27 conductivity and density measurements in 436 samples taken in 2006–2009, and provides the
28 basis for the calculation of the Absolute Salinity from knowledge of Practical (or Reference
29 Salinity) as single parameter:

$$30 \quad S_A = S_R + 86.9 \text{ mg} \cdot \text{kg}^{-1} \cdot (1 - S_R / S_{SO}), \quad (1)$$

31 with the Standard Ocean Salinity $S_{SO}=35 \cdot u_{PS}=35.16504 \text{ g} \cdot \text{kg}^{-1}$, and $S_R > 2 \text{ g} \cdot \text{kg}^{-1}$.

1 The density of the original (not diluted) Atlantic sample was measured to (1025.688 ± 0.004)
2 $\text{kg} \cdot \text{m}^{-3}$. The values of S_A estimated from measured S_P and calculated with TEOS-10 from the
3 density were consistent within the uncertainties, supporting the general validity of the
4 procedures. The density of the diluted Atlantic sample could not be determined because the
5 densimeter was not available at that time. Because standard composition can be assumed for
6 the original and diluted North Atlantic samples, S_A is equivalent to S_R for both, and S_A of the
7 diluted sample is given by the dilution ratio. The results for the relevant salinity and salinity
8 differences are summarized in Table 2. It was confirmed that the density-based salinity
9 anomaly of $0.067 \text{ g} \cdot \text{kg}^{-1}$ agrees well with the anomaly of $0.068 \text{ g} \cdot \text{kg}^{-1}$ calculated from Eq. (1)
10 within the uncertainty of $0.009 \text{ g} \cdot \text{kg}^{-1}$.

11 **2.2 Laboratory results for the speed-of-sound anomaly**

12 The dilution of the Atlantic sample resulted in the same Practical Salinity S_P as beforehand
13 recorded in the Baltic sample. Pure water was gently added to the pre-diluted, continuously
14 mixed, and temperature stabilized sample within the thermostat bath while tracking the
15 conductivity. This resulted in a final S_P -value practically identical to the Baltic sample (see
16 Table 2). The procedure naturally implies different final Absolute Salinities for the two
17 samples, associated with the sound speed differences of interest.

18 The sound speed anomaly is given by the direct difference of the measured values, provided
19 that S_P , temperature, and pressure are the same at each reading point. Within our uncertainties,
20 this condition was met for S_P , which was shown to be virtually identical, and for
21 (atmospheric) pressure. Differences in the preset bath temperatures, however, were relevant.
22 They were included by converting the measured sound speed in the Baltic sample to the bath
23 temperatures of the Atlantic sample before calculating the sound speed difference. The
24 respective local temperature sensitivity $\partial w / \partial T$ was approximated using the average
25 temperature of both samples at each point. Because the differences of the preset temperatures
26 are still small, uncertainty contributions from this approximation, and also from the actual
27 choice of the equation of state applied for the estimate of the local temperature sensitivity
28 $\partial w / \partial T$, were negligible.

29 The results for the three sensors are shown in Fig. 1 as symbols and listed in Table S1
30 (supplementary material). Within the scatter, the results from the individual sensors as a
31 whole are indistinguishable, and no significant trend with temperature can be assessed. The

1 average over the data points from all sensors is $\delta w = 0.069 \text{ m}\cdot\text{s}^{-1}$ with a standard deviation of
2 $0.014 \text{ m}\cdot\text{s}^{-1}$. Remember that this purely experimental estimate of δw is based on the criterion
3 of equal conductivity in both samples. It is different from using other reference parameters
4 such as chlorinity, density, or Absolute Salinity, which are more difficult to implement in
5 practice. However, a density-related measure for δw can be calculated and compared to the
6 results from the acoustic sensors: Subtraction of TEOS-10 sound speeds using the estimates
7 for the Absolute Salinity in the Baltic ($S_{A,\text{dens}}$) and diluted Atlantic ($S_{A,\text{cond}}$) sample (Table 2)
8 as arguments yields the line in Fig. 1. This relies on the validity of Millero's rule with respect
9 to the density-salinity relation. Alternatively, the Absolute Salinity in the Baltic sample can be
10 calculated with Eq. (1) from measured S_p , resulting in $7.871 \text{ g}\cdot\text{kg}^{-1}$. This value confirms our
11 density based estimate of $S_{A,\text{dens}}$ and would accordingly produce a virtually identical curve for
12 δw .

13 **2.3 Field measurements**

14 We applied one of the sensors (VP) used for the laboratory measurements at three different
15 sites in the south-western Baltic Sea (Fig. 2). Besides basic testing under field conditions, we
16 focused on its general ability to reproduce the small anomaly related w -effects. The VP sensor
17 was fixed in horizontal orientation close ($\approx 10 \text{ cm}$) to the sensor head of a Seabird SBE
18 911plus probe equipped with two temperature and two conductivity sensors (calibrated at
19 IOW to 1.5 mK and $0.003 \text{ mS}\cdot\text{cm}^{-1}$ ($k=1$), respectively), all mounted in an oceanographic
20 sampling rosette.

21 With this configuration we saved speed-of-sound and CTD data simultaneously in continuous
22 recordings at selected constant depths for typically 2 min at 1 Hz. The sampling depths were
23 chosen by means of previously taken vertical CTD profiles. In parallel to each continuous
24 measurement we filled two 5 liter Niskin water samplers. The samples were measured on-
25 board for density using an Anton Paar DMA 5000 M vibrating tube densimeter relative to
26 pure water (uncertainty $2.5\cdot 10^{-6} \text{ g}\cdot\text{cm}^{-3}$, $k=1$), and for Practical Salinity with a Guildline
27 Autosal 8400B salinometer (24 h accuracy $\pm 0.002 \text{ PSU}$ ($k=1$), adjusted daily with OSIL P155
28 Standard Seawater). The data are summarized in Table 3 as averages over manually chosen
29 subintervals from the 2-min recordings including standard deviations (CTD), and as averages
30 of the two measured Niskin samples taken in parallel to the CTD measurements (density and
31 S_p), respectively.

1 Deviations of S_P from CTD data and salinometer outputs were generally smaller than 0.003 in
2 homogeneous water layers. This gives an upper estimate of the measurement uncertainty for
3 S_P . Standard deviations for S_P from CTD measurements were typically one order of magnitude
4 smaller.

5 Occasionally, much larger variations of CTD and speed-of-sound outputs (with time) at the
6 constant nominal depths were detected. They reflect coactions of local temperature or salinity
7 gradients and surface wave induced movement of the vessel and rosette. The occurrence of
8 complex thermohaline stratification with partially strong vertical temperature and salinity
9 gradients is typical for the deep water in the Baltic. In such cases, the respective data sets have
10 been excluded from further evaluation. Generally we can state that in stratified regions the
11 uncertainty of all measured properties including speed of sound was in most cases dominated
12 by the variability of the in situ conditions in the vicinity of the sensors. However, the
13 existence of the stratified regime in principle provided an opportunity to investigate samples
14 with different salinity and the respective changes of the anomaly effects at one site.

15 In the same way as described above for the laboratory investigations, we determined the
16 salinity anomaly δS_A from the on-board measurements of density and S_P (Table 3, right
17 column). Together with the laboratory estimate and the empirical parameterization (Eq. (1)),
18 δS_A is shown in Fig. 3. Based on this consistent picture of the salinity anomaly we evaluated
19 the results from the sound speed sensor in view of the anomalous deviations.

20 In von Rohden et al. (2015) we documented the existence of certain inconsistencies for speed
21 of sound among the pure water calibrated time-of-flight sensors including the unit used here.
22 These variations were an order of magnitude larger than the reproducibility and showed
23 apparent trends with temperature and salinity. That means that an adequate calibration
24 covering the large Baltic salinity range would be necessary for the comparison of direct sound
25 speed readings. Such a calibration, however, was not appropriate. Hence, a direct detection of
26 δw by a simple comparison of the in-situ values with sound speed derived from parallel CTD
27 data using equations of state (assuming standard composition) was not applicable.

28 Instead, we related the differences of the actual sensor displays to the corresponding EOS-
29 calculated values $(w - w_{EOS})_{\text{Baltic}}$ with the analogous differences $(w - w_{EOS})_{\text{Atlantic}}$ which were
30 calculated on the basis of laboratory records in two samples of diluted North Atlantic
31 seawater (as a “substitute” for Standard Seawater):

$$1 \quad \delta w = (w - w_{\text{EOS}})_{\text{Baltic, in situ}} - (w - w_{\text{EOS}})_{\text{Atlantic, Lab}} \quad (2)$$

2 The first of the reference samples is the one used for the laboratory estimate of δw with
3 $S_p=(7.765\pm 0.007)$ (NA II). The second is another Atlantic sample (NA I) diluted to
4 $S_p=(16.66\pm 0.03)$, taken from the same location in the Madeira Basin in June 2012. Using
5 these samples we classified the Baltic in situ measurements into two groups by means of
6 salinity in the sense that the two Atlantic reference samples can be seen as representative of
7 the two S_p ranges (7.3 to 8.4, and 13.3 to 18.8) sampled during our Baltic Sea field trip. Table
8 3 and Table 4 are accordingly separated into upper and lower parts. The sound speed
9 differences $(w - w_{\text{EOS}})_{\text{Baltic}}$ and $(w - w_{\text{EOS}})_{\text{Atlantic}}$ are listed in Table 4 for both TEOS-10 and the
10 Chen and Millero (1977) equation.

11 In principle, this proceeding is similar to a “local” recalibration of the sensor in seawater at
12 the two salinities. The approach of relating the Baltic field measurements with the fixed
13 Atlantic reference samples however implies that $(w - w_{\text{EOS}})$ is basically independent of salinity,
14 at least within both defined salinity ranges. A possible dependence of the difference on
15 pressure should be negligible due to the comparatively weak sensitivity of sound speed to
16 pressure and the rather shallow sampling depths (<43 m). The comparatively strong
17 temperature dependence of the reference differences $(w - w_{\text{EOS}})$ was considered by
18 interpolation to the Baltic sample temperatures (CTD) using polynomials. An example for the
19 sample with $S_p=7.765$ is given in Fig. 4. The data are also listed in Table S2 of the
20 supplementary material. The results for the extracted sound speed anomaly δw are listed in
21 Table 4 and plotted in Fig. 5. The courses of the differences $w - w_{\text{EOS}}$ reflect the inaccuracy of
22 both the sensor with respect to absolute values, and the actual reference equation. However,
23 due to the high sensor stability and resolution, the uncertainty of δw is expected to be much
24 smaller than the uncertainties of each of the two terms.

25 As a basic outcome we state that at least over the period of the field campaign (~ 1 week) the
26 sensor was stable. The data show a smooth course without strong salinity dependence (Fig. 5).
27 Especially the δw at $S_p \approx 8$ reproduce well and independently of the sample site, date, and
28 depth (the cluster of points includes one sample from the site OB at ≈ 12.5 m).

29 Whereas the outputs of the equations apparently differ by $\approx 0.05 \text{ m} \cdot \text{s}^{-1}$ (upper panel of Fig. 5),
30 the estimated sound speed anomaly δw is basically independent of the equation used as a
31 reference (lower panel), which was expected within the assumptions and uncertainties of our

1 approach. Note that the use of the Del Grosso and Mader (1974) equation as a reference
2 would not be reasonable because of its validity limited to oceanic salinities which do not
3 include the brackish Baltic waters. Although a bit lower, the δw at $S_p \approx 8$ match the more
4 accurate laboratory findings within the range of uncertainties (Fig. 1) (discussion below). The
5 high reproducibility of the measurements at $S_p \approx 8$ also implies the validity of the results at
6 higher S_p (13.3 to 18.8), for which no comparative experimental values are available, even
7 though there are somewhat larger uncertainties due to the larger salinity error of our $S_p = 16.66$
8 reference sample (NA I).

9 Contributions to the uncertainty of δw comprise the general stability of the sensor (0.019
10 $\text{m}\cdot\text{s}^{-1}$), represented by the reproducibility of calibration measurements in pure water, and the
11 effect of conductivity (salinity), temperature, and pressure uncertainties on EOS calculated
12 sound speed ($<0.04 \text{ m}\cdot\text{s}^{-1}$). We assigned an additional contribution of $0.02 \text{ m}\cdot\text{s}^{-1}$ to the
13 difference $(w - w_{\text{EOS}})_{\text{Atlantic}}$ (sensor display minus EOS calculated sound speed), which
14 accounts for the interpolation to the in situ measured temperatures (Fig. 4), and for the
15 assumption of an insignificant salinity and pressure sensitivity of this difference. The limited
16 validity of a vanishing salinity sensitivity might be indicated by the somewhat suspicious δw
17 at the $S_p \approx 13.3$ and $S_p \approx 18.8$ with the largest deviations to the reference salinity of $S_p = 16.66$.
18 The resulting overall uncertainty of the sound speed anomaly $u(\delta w)$ is given in Table 4.

19

20 **3. Discussion**

21 The results of the laboratory investigations represent the first experimental estimate of the
22 speed-of-sound anomaly caused by the anomalous salt composition in Baltic seawater.
23 Although conducted for only one sample with a Practical Salinity of $S_p = 7.766$, the validity of
24 the extracted δw was supported by the consistency of the data measured with three time-of-
25 flight sensors from two manufacturers simultaneously, also at temperatures exceeding the
26 natural range. The results show that with the high resolution and reproducibility of modern
27 time-of-flight sensors, the anomaly effect can be resolved with comparison measurements.

28 Feistel et al. (2010a) derived a Gibbs function for Baltic Seawater from Pitzer equations using
29 a numerical model (FREZCHEM) which simulates chemical and physical properties of
30 seawater with variable solute composition. With this, the speed-of-sound deviation in Baltic
31 water and seawater with the same electrical conductivity was predicted under the presumption

1 that the salt anomaly can be represented by additional calcium carbonate coming from river
2 water discharge. The results are shown in Fig. 25 in Feistel et al. (2010a). We reproduced the
3 figure and added our measurement results to the model curves in Fig. 6. Obviously, within the
4 uncertainty our results as a whole do not conform to these predictions. The measurements are
5 better represented by $\delta w = w_{\text{TEOS}}(S_A) - w_{\text{TEOS}}(S_R)$ (dotted lines in Fig. (6)), where S_A and S_R
6 are related to each other according to Eq. (2). That is, they rather follow Millero's rule (see
7 also Fig. 13 in Feistel et al. (2010a)), and therefore confirm that the sound speed in Baltic
8 Seawater can reasonably be predicted using the Absolute Salinity S_A with TEOS-10.

9 From the field measurements in the Baltic Sea and from our separate study (von Rohden et
10 al., 2015) we conclude that modern time-of-flight sensors are not (yet) applicable as a tool for
11 the in situ detection of the salinity anomaly when calibrated in pure water only. To solve this,
12 an extensive calibration in Standard Seawater covering the temperature and the large salinity
13 range of the Baltic Sea or significant improvements of the absolute sensor uncertainty are
14 required.

15 With the in situ sensor application we showed that in the face of the above restrictions it is
16 possible to give a reliable estimate of δw in a non-routine demonstration. In this way we
17 yielded adequate results for the salinity range of $S_p \approx 7$ to 19 and reproduced well the
18 laboratory results at $S_p = 7.766$ within the uncertainties.

19 Comparative measurements as shown for the sample in this study may be the way to extend
20 the data set to cover the whole salinity range of the Baltic Sea. However, it must be
21 considered that the salt composition of the freshwater input from the rivershed is
22 geographically, as well as temporally, and with respect to the solute composition, not
23 homogeneous. That means that the anomalous salt component might be variable with
24 respective effects on the magnitude of sound speed deviations, dependent on the time scales
25 of the horizontal and the rather strongly salinity controlled diapycnal exchange processes.
26 This might also be significant for the results of our in situ measurements.

27

28 **Data availability**

29 All relevant data are provided with Tables 2-4 in the manuscript and with two tables in the
30 Supplement.

31

1 **Author contributions**

2 C.v.R designed and carried out the laboratory experiments, supervised the offshore speed-of-
3 sound measurements, evaluated the data, and wrote the manuscript. S.W. prepared the field
4 activities and carried out the on-board density and CTD measurements. F.F. contributed to the
5 data evaluation and manuscript preparation.

6

7 **Acknowledgements**

8 This research was undertaken within the project EMRP ENV05. The EMRP is jointly funded
9 by the EMRP participating countries within EURAMET and the European Union.

10

1 **References**

- 2 Chen, C.-T. and Millero, F. J.: Speed of sound in seawater at high pressures, *J. Acoust. Soc.*
3 *Am.*, 62(5), 1129–1135, 1977.
- 4 Del Grosso, V. A.: New equation for the speed of sound in natural waters (with comparisons
5 to other equations), *J. Acoust. Soc. Am.*, 56(4), 1084–1091, doi:10.1121/1.1903388, 1974.
- 6 Feistel, R., Marion, G. M., Pawlowicz, R. and Wright, D. G.: Thermophysical property
7 anomalies of Baltic seawater, *Ocean Sci.*, 6(4), 949–981, doi:10.5194/os-6-949-2010, 2010a.
- 8 Feistel, R., Weinreben, S., Wolf, H., Seitz, S., Spitzer, P., Adel, B., Nausch, G., Schneider, B.
9 and Wright, D. G.: Density and Absolute Salinity of the Baltic Sea 2006–2009, *Ocean Sci.*,
10 6(1), 3–24, doi:10.5194/os-6-3-2010, 2010b.
- 11 IOC, SCOR and IAPSO: The international thermodynamic equation of seawater–2010:
12 Calculation and use of thermodynamic properties, Intergovernmental Oceanographic
13 Commission, Manuals and Guides No. 56, UNESCO (English), 196 pp., available at:
14 <http://www.teos-10.org> (last access: 21 October 2015), 2010.
- 15 McDougall, T. J., Jackett, D. R., Millero, F. J., Pawlowicz, R. and Barker, P. M.: A global
16 algorithm for estimating Absolute Salinity, *Ocean Sci.*, 8(6), 1123–1134, doi:10.5194/os-8-
17 1123-2012, 2012.
- 18 Millero, F. J. and Kremling, K.: The densities of Baltic Sea waters, *Deep Sea Res.*, 23 (May),
19 1129–1138, 1976.
- 20 Millero, F. J., Waters, J., Woosley, R., Huang, F. and Chanson, M.: The effect of composition
21 on the density of Indian Ocean waters, *Deep Sea Res. Part I Oceanogr. Res. Pap.*, 55(4), 460–
22 470, doi:10.1016/j.dsr.2008.01.006, 2008.
- 23 Perkin, R.G. and Lewis, E.: The Practical Salinity Scale 1978: Fitting the data, *IEEE Journal*
24 *of Ocean. Engin.* 5(1), 9–16, doi: 10.1016/0198-0149(81)90002-9, 1980.
- 25 Von Rohden, C., Fehres, F. and S. Rudtsch, S.: Capability of pure water calibrated time-of-
26 flight sensors for the determination of speed of sound in seawater, *J. Acoust. Soc. Am.* 138,
27 651, <http://dx.doi.org/10.1121/1.4926380>, 2015.
- 28

1 Table 1. Sensor specifications. The response times basically reflect the time of flight of sound
 2 pulses. The reproducibility corresponds to the standard uncertainty for measurements in pure
 3 water in our experimental setup over a period of one (AML) and two years (VP), respectively
 4 (von Rohden et al., 2015).

	AML SVX	VP, VP OEM
<i>acoustic pathlength</i> / mm	68	200
<i>response time</i> / μs	~47	~140
<i>time resolution</i> / ns	~0.02	0.01
<i>practical resolution w</i> / $\text{m}\cdot\text{s}^{-1}$	0.001	0.001
<i>reproducibility</i> / $\text{m}\cdot\text{s}^{-1}$	0.032	0.019

5

1 Table 2. Salinity estimates for the samples used, and salinity differences related to the
 2 composition anomaly for the Baltic seawater sample, including standard uncertainties.

<i>Salinity</i> / $\text{g}\cdot\text{kg}^{-1}$	Baltic	North Atlantic	
		diluted	original
S_p / PSU	7.766 ± 0.007	7.765 ± 0.007	36.208 ± 0.01
$S_{A,\text{cond}}$ (assum. standard comp.)	7.803 ± 0.007	7.801 ± 0.007	36.379 ± 0.01
$S_{A,\text{dens}}$ (from measured density)	7.870 ± 0.006		36.381 ± 0.006
Meas. diff. $\delta S_{A,m} = S_{A,\text{dens}} - S_{A,\text{cond}}$	0.067 ± 0.009		
Calc. diff. $\delta S_{A,c}$ (Eq. (1))	0.068		

3

4

1 Table 3. CTD data (averages of 2-min recordings at constant depths) at three sites in the
2 Baltic Sea (see Fig. 2) in August 2014 including standard deviations; p = hydrostatic plus air
3 pressure. Three right columns: On-board density and salinity measurements as averages of
4 two samples taken in parallel to the CTD measurements; calculated salinity anomaly δS_A
5 based on on-board measurements.

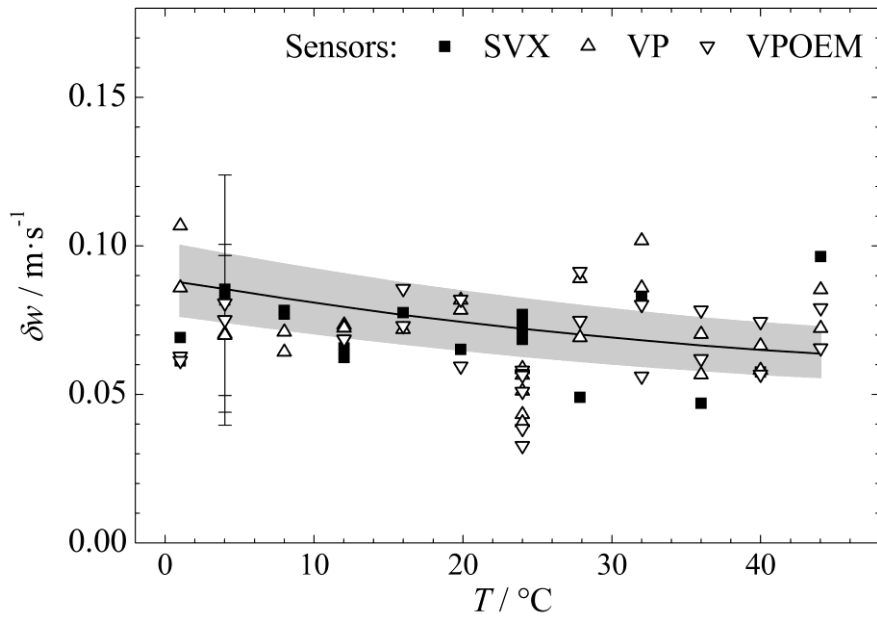
Site	Measurements								calc. S - anomaly
	in situ CTD						On-board		
	T °C	$\sigma(T)$ °C	S_p (PSU)	$\sigma(S_p)$ (PSU)	p Pa	$\sigma(p)$ Pa	ρ g·cm ⁻³	S_p (PSU)	δS_A g·kg ⁻¹
DS	20.855	0.001	7.899	0.0009	166308	995	1.004257	7.902	0.068
DS	21.280	0.003	7.950	0.0001	166069	777	1.004295	7.951	0.068
DS	20.457	0.002	8.399	0.0002	144747	246	1.004633	8.401	0.065
AB	20.995	0.001	7.773	0.0002	133966	974	1.004162	7.775	0.069
AB	21.170	0.002	7.779	0.0002	173492	185	1.004168	7.781	0.071
AB	21.207	0.003	7.780	0.0002	172901	107	1.004169	7.782	0.071
OB	22.105	0.002	7.320	0.0002	134186	813	1.003829	7.322	0.082
OB	22.007	0.001	7.344	0.0003	134190	603	1.003846	7.345	0.082
OB	21.947	0.008	7.377	0.0033	163016	354	1.003867	7.373	0.080
OB	20.701	0.005	7.518	0.0003	225661	205	1.003973	7.513	0.080
OB	20.786	0.017	7.524	0.0003	225723	190	1.003979	7.525	0.077
DS	15.192	0.001	17.849	0.0024	291574	535	1.011767	17.846	0.046
DS	14.999	0.004	18.176	0.0044	275119	405	1.011944	18.078	0.049
DS	14.685	0.002	18.775	0.0007	293951	103	1.012462	18.764	0.046
AB	15.925	0.005	13.833	0.0096	503236	153	1.008710	13.796	0.058
AB	15.081	0.002	13.293	0.0040	479620	69	1.008288	13.241	0.056
AB	15.801	0.004	14.265	0.0039	505692	87	1.009059	14.262	0.055
AB	15.709	0.006	14.276	0.0029	508273	84	1.009070	14.274	0.057
AB	14.230	0.001	16.723	0.0002	531733	405	1.010919	16.721	0.052

6

1 Table 4. Speed of sound measured with the time-of-flight sensor in the Baltic Sea (in $\text{m}\cdot\text{s}^{-1}$);
2 w -differences (measured minus calculated) using TEOS-10 and Chen and Millero (1977) for
3 the Baltic in-situ measurements, and for the laboratory measurements in samples of natural
4 Atlantic seawater with $S_p=7.765$ (upper part of table) and $S_p=16.66$ (lower part). The
5 differences in the Atlantic samples were previously interpolated to the Baltic in situ
6 temperatures. δw are the respective estimates of the sound speed anomaly according to Eq.
7 (2). The uncertainty estimate $u(\delta w)$ (right column) is virtually the same for both reference
8 equations. The data are in the same order as in Table 3.

Site	measured		rel. to TEOS-10			rel. to Chen and Millero (1977)			
	sound speed		Baltic	Atlantic	$\delta\omega$	Baltic	Atlantic	$\delta\omega$	$u(\delta\omega)$
	w	$\sigma(w)$	$w-w_{\text{TEOS}}$	$w-w_{\text{TEOS}}$		$w-w_{\text{CM77}}$	$w-w_{\text{CM77}}$		
DS	1493.982	0.004	0.073	0.033	0.040	0.026	-0.013	0.039	0.033
DS	1495.284	0.005	0.081	0.036	0.045	0.032	-0.012	0.044	0.034
DS	1493.338	0.005	0.081	0.030	0.051	0.034	-0.014	0.048	0.033
AB	1494.203	0.005	0.077	0.034	0.043	0.030	-0.013	0.043	0.033
AB	1494.792	0.005	0.082	0.036	0.047	0.034	-0.012	0.047	0.033
AB	1494.907	0.009	0.090	0.036	0.055	0.042	-0.012	0.054	0.035
OB	1496.914	0.006	0.090	0.042	0.049	0.041	-0.010	0.051	0.033
OB	1496.653	0.005	0.082	0.041	0.041	0.033	-0.010	0.043	0.033
OB	1496.573	0.009	0.090	0.041	0.050	0.041	-0.010	0.052	0.041
OB	1493.218	0.010	0.088	0.032	0.056	0.041	-0.014	0.055	0.037
OB	1493.506	0.017	0.118	0.033	0.085	0.071	-0.013	0.084	0.063
DS	1487.770	0.005	0.074	-0.015	0.089	0.031	-0.053	0.084	0.048
DS	1487.476	0.007	0.070	-0.017	0.087	0.026	-0.054	0.081	0.050
DS	1487.180	0.010	0.099	-0.021	0.120	0.056	-0.057	0.113	0.049
AB	1485.888	0.013	0.053	-0.006	0.059	0.011	-0.047	0.059	0.053
AB	1482.389	0.008	0.013	-0.016	0.030	-0.021	-0.054	0.033	0.049
AB	1485.985	0.005	0.057	-0.007	0.065	0.015	-0.048	0.064	0.050
AB	1485.703	0.015	0.060	-0.009	0.069	0.018	-0.049	0.067	0.053
AB	1483.604	0.004	0.049	-0.026	0.075	0.010	-0.061	0.071	0.048

9

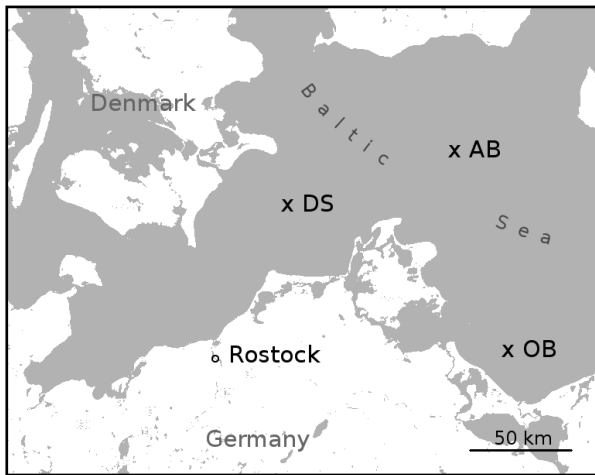


1

2

3 Figure 1. Speed-of-sound differences associated with the salinity anomaly for Baltic seawater
 4 at $S_p=7.766$. Symbols: Measured differences from the Baltic and the diluted Atlantic sample
 5 (NA II) with virtually the same S_p . Uncertainty bars are exemplary given at 4 °C. Line: δw
 6 calculated as $w_{\text{TEOS10}}(S_{A,\text{dens}}, T, p_0) - w_{\text{TEOS10}}(S_{A,\text{cond}}, T, p_0)$. The shaded area denotes the
 7 uncertainty range due to the salinity uncertainty.

8



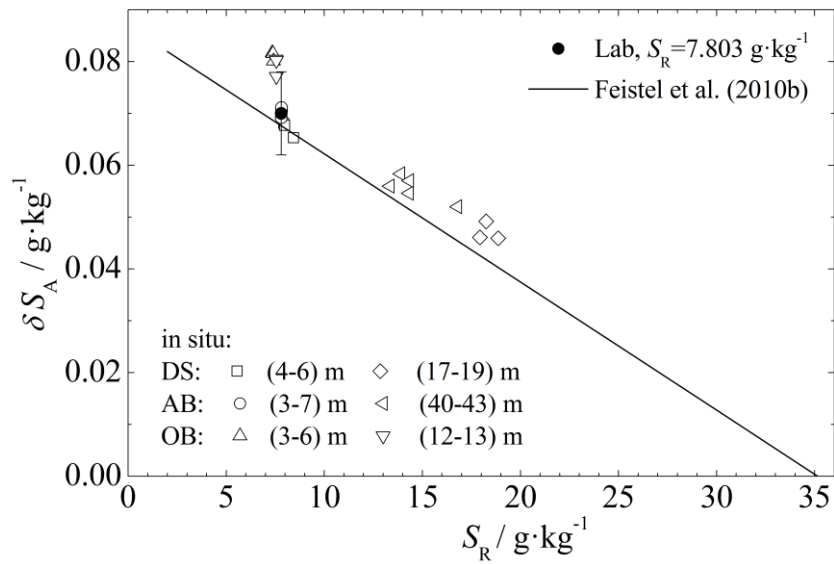
1

2

3 Figure 2. Measurement and sampling sites in the south-western Baltic Sea. DS = Darß Sill,

4 AB = Arkona Basin, OB = Oder Bay.

5

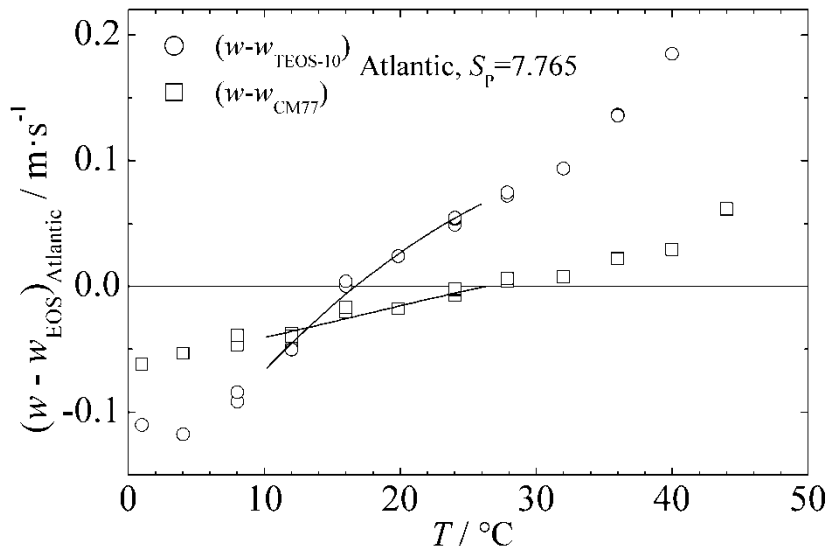


1

2

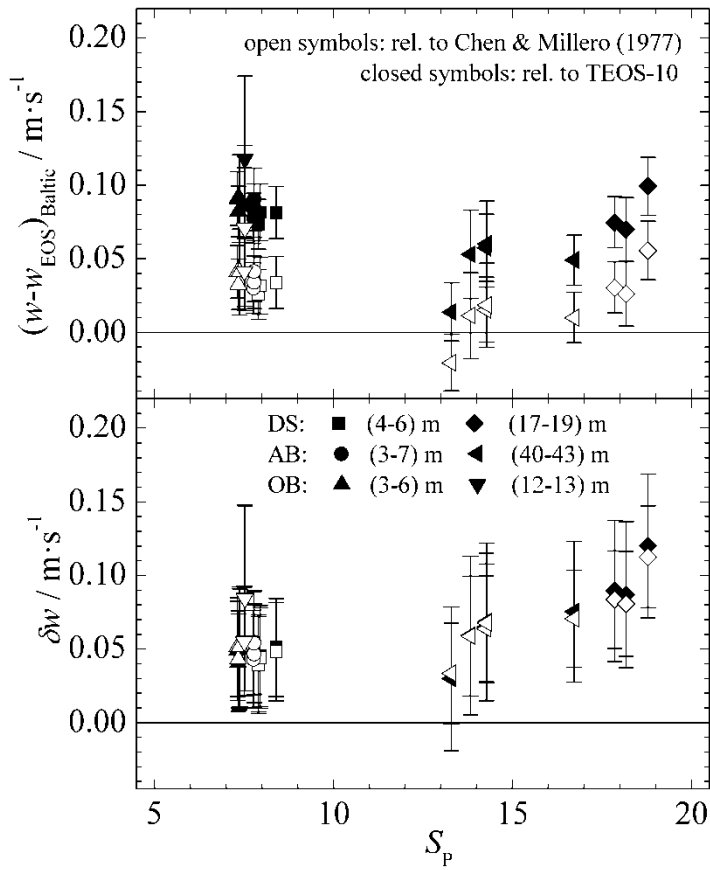
3 Figure 3. Salinity anomaly, determined from density and salinity measurements, vs.
 4 Reference Salinity $S_R = S_P \cdot u_{PS}$. Filled symbol: laboratory sample; Open symbols: Baltic field
 5 samples. The straight line shows the parameterization of Feistel et al. (2010b), Eq. (1), for
 6 comparison.

7



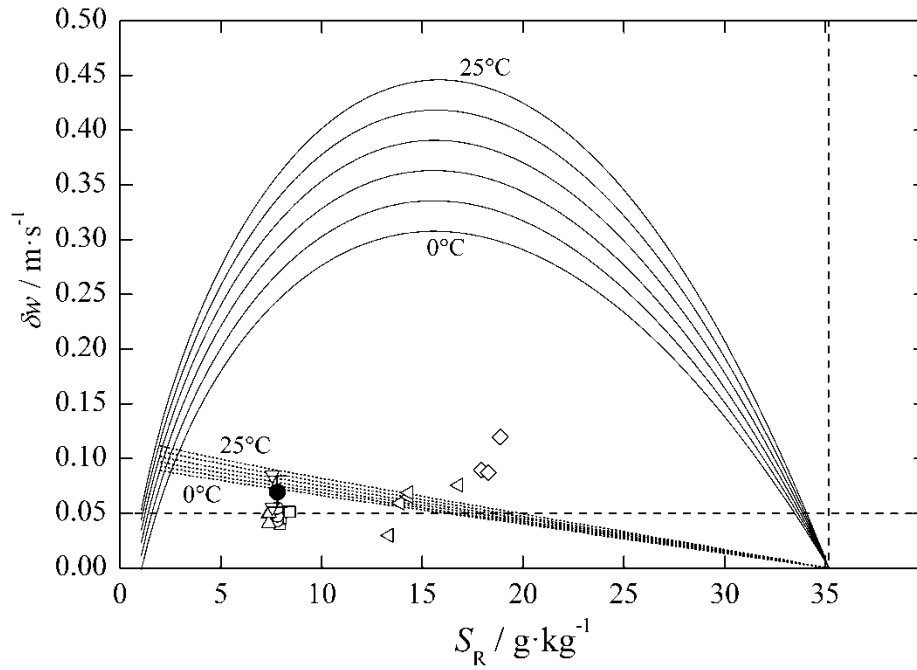
1
2
3
4
5
6
7
8

Figure 4. Time-of-flight sensor output relative to speed of sound calculated with TEOS-10 and Chen and Millero (1977) equations of state, exemplary for the North Atlantic seawater sample with $S_p=7.765$ (laboratory measurements). The lines show polynomial fits used for interpolation to extract values according to the in-situ temperatures of the Baltic field measurements.



1
2
3
4
5
6
7

Figure 5. Upper panel: Measured speed of sound (Baltic) relative to calculated values with equations of TEOS-10 and Chen and Millero (1977) for the same (S_P , T , p). The displacement between both reflects differences in the outputs of the equations. Lower panel: Speed-of-sound anomaly $\delta w = (w - w_{EOS})_{\text{Baltic, in situ}} - (w - w_{EOS})_{\text{Atlantic, ref}}$ (upper panel “minus” Fig. 4).



1

2

3 Figure 6. Experimental data for sound speed anomaly δw in Baltic seawater (symbols) in
 4 comparison to model results (curved lines, reproduced from Fig. 25 in Feistel et al., 2010a) at
 5 atmospheric pressure. Filled symbol: average of laboratory measurements in a sample with
 6 $S_R=7.803 \text{ g}\cdot\text{kg}^{-1}$ ($S_p=7.766$) at temperatures of 1 to 46 °C. Open symbols: data derived from
 7 off-shore measurements, see Fig. 5. The dotted lines show $\delta w=w_{\text{TEOS10}}(S_{A,\text{dens}}=$
 8 $S_A)-w_{\text{TEOS10}}(S_{A,\text{cond}}=S_R)$ calculated with Eq. (2) for different temperatures. The horizontal
 9 dashed line indicates the uncertainty of TEOS-10 sound speed.