

# Comparison between three implementations of automatic identification algorithms for the quantification and characterization of mesoscale eddies in the South Atlantic Ocean

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**Abstract.** Three methods for automatic detection of mesoscale coherent structures are applied to Sea Level Anomaly (SLA) fields in the South Atlantic. The first method is based on the wavelet packet decomposition of the SLA data, the second on the estimation of the Okubo-Weiss parameter and the third on a geometric criterion using the winding-angle approach. The results provide a comprehensive picture of the mesoscale eddies over the South Atlantic Ocean, emphasizing their main characteristics: amplitude, diameter, duration and propagation velocity. Five areas of particular eddy dynamics were selected: the Brazil Current, the Agulhas eddies propagation corridor, the Agulhas Current retroflexion, the Brazil-Malvinas confluence zone and the northern branch of the Antarctic Circumpolar Current (ACC). For these areas, mean propagation velocities and amplitudes were calculated. Two regions with long duration eddies were observed, corresponding to the propagation of Agulhas and ACC eddies. Through the comparison between the identification methods, their main advantages and shortcomings were detailed. The geometric criterion presents the best performance, mainly in terms of number of detections, duration of the eddies and propagation velocities. The results are particularly good for the Agulhas Rings, which have the longest lifetimes of all South Atlantic eddies.

## 1 Introduction

Oceanic eddies have been the subject of many experimental and theoretical studies in the last 40 yr. This is explained by the dominance of the kinetic energy associated to the

mesoscale activity, more than one order of magnitude greater than that of the mean flow over most of the world ocean (Richardson, 1983; Chelton et al., 2007).

In the South Atlantic, in particular, the mesoscale activity is believed to play central roles in the southward heat flux in high latitudes (e.g., de Szoeke and Levine, 1981; Olbers et al., 2004; Mazloff et al., 2010) and the inter-ocean water properties exchanges with the Indian Ocean (e.g., de Ruijter et al., 1999; Matano and Beier, 2003; Sebille et al., 2010) and the North Atlantic Ocean (e.g., Fratantoni and Glickson, 2002; Jochum and Malanotte-Rizzoli, 2003; Field, 2005). Moreover, as presented by Wunsch (1999), eddy-induced heat fluxes have been observed to be important in western boundary current regions in the North Atlantic and Pacific Oceans. The role played by such structures in properties transport in the Brazil Current is not completely clear.

In the South Atlantic Ocean, most eddy variability studies have been focused in the Agulhas Current Retroflexion Rings (Fu and Zlotnicki, 1989; Gordon et al., 1992; Doglioli et al., 2007) and the Brazil-Malvinas Confluence (Goni et al., 1996; Fu, 2007). Although the existence of global estimates, as in Chelton et al. (2007, 2011), there is not yet a comprehensive assessment of the eddies identification and tracking focused in the South Atlantic basin.

The South Atlantic presents optimal characteristics to test implementations of automatic eddy identification algorithms. The occurrence of high variability areas, such as the Agulhas Current retroflexion and the Brazil-Malvinas confluence, corridors of eddies propagation, western boundary currents and the strongest current system in the world, the Antarctic Circumpolar Current (ACC), represent important obstacles to the correct identification and tracking of the structures.

As emphasized by Chaigneau et al. (2008), mesoscale eddies can not be extracted from a turbulent flow without a suitable definition and a competitive identification algorithm.



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With this in mind, several methods have been proposed for the identification and tracking of mesoscale structures in the ocean circulation. Classically, such methods can be divided into two main groups: one based on physical properties of the flow and other based in geometric criteria.

Physical properties can be difficult to estimate. Since they are often related to gradients of the measured sea properties, errors inherent to the gradient estimations can have major impact on the final result. Moreover, the establishment of thresholds are necessary to determine the eddy locations. Small variations of the thresholds values can have a profound impact on the number and location of the identified structures. One of the most popular methods of this group is based on the Okubo-Weiss parameter (Okubo, 1970; Weiss, 1991). This method have been applied to both satellite data and numerical model results with considerable success (Isern-Fontanet et al., 2006; Chelton et al., 2007; Henson and Thomas, 2008). A modern alternative method for the detection of eddies using the wavelet analysis was proposed by Doglioli et al. (2007), based on the work of Siegel and Weiss (1997). This method consists in the decomposition of the sea surface relative vorticity into orthogonal modes, or wave packets, that are well localized in both position and wave number. The authors applied the method to the Cape Basin and compared the results with those obtained through the Okubo-Weiss parameter.

Although the use of geometric criteria is less usual than the physical ones, recent work have shown significant success in the identification of mesoscale vortex structures (Penven et al., 2005; Moolani et al., 2006; Chaigneau et al., 2008, 2009). Such methods assume that eddies consist in quasi-circular flow patterns, so the shape of instantaneous streamlines can be used for the structure identification. To achieve this objective, two main techniques can be applied: the “curvature center method” (Leeuw and Post, 1995) and the “winding-angle method” (Sadarjoen and Post, 2000). The first approach is to locate the eddies by determining the center of the curvatures in the stream-lines. It presents the same problems associated to other point-based methods, with the identification of false peaks that have to be removed through the use of thresholds or filtering. As demonstrated by Sardojoen and Post (2000) and Chaigneau et al. (2008), the winding-angle method arrives to better results than the curvature center method, and was selected to represent the geometric criteria in the present study.

Chelton et al. (2011) proposed a threshold-free identification method, based on the Sea Surface Height (SSH) closed contours. This method is similar to the one implemented by Chaigneau et al. (2009) and used in the present study. The term “threshold-free” refers to the fact that no specific SSH value is chosen to represent the eddy boundaries, although limits are imposed to the eddy amplitudes and diameters. While Chelton et al. (2011) made a global estimative of the eddies trajectories, the present study is focused in the South Atlantic region and the comparison between methods. Con-

trasting the results it is possible to identify how the differences between this to similar methods impact the obtained eddy statistics.

The objective of the present work is to quantify and characterize the mesoscale coherent structures, or eddies, in the South Atlantic Ocean through the implementation of 3 different methods for their automatic detection. These methods consist in (1) the estimation of the Okubo-Weiss parameter, (2) the Wavelet analysis of the sea surface relative vorticity and (3) the geometric winding-angle criterion. A comparison between the algorithms results will help to enlighten their applicabilities and weaknesses, providing a valuable contribution for future work.

In the next section the dataset used to the eddies detection is presented, together with the processing and simplifications adopted. The eddy identification and tracking algorithms are presented in the Sect. 3, followed by a comparison of their results in Sect. 4. Some conclusions are drawn in the Sect. 5, with propositions for future work.

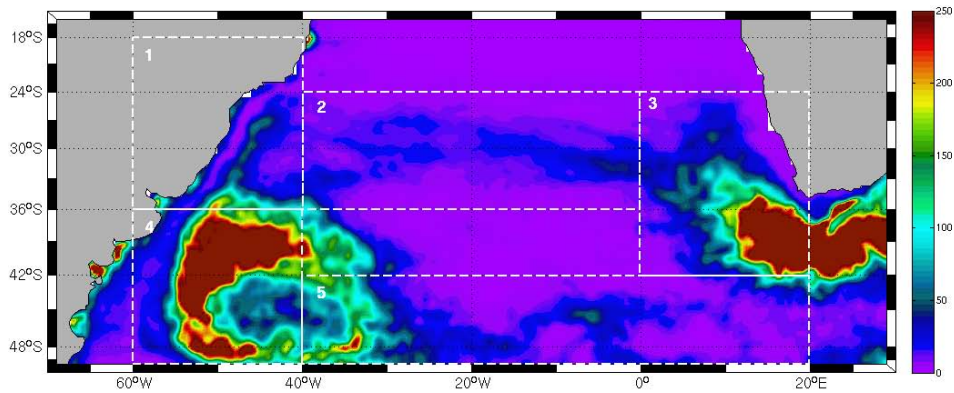
## 2 Data

The domain of the present study corresponds to the South Atlantic Ocean, between the meridians of 70° W and 30° E and the parallels of 15° S and 50° S.

For this region, Sea Surface Height (SSH) data from the AVISO delayed time reference product were obtained from <http://www.aviso.oceanobs.com/>, from January 2005 to December 2008. It corresponds to a merged satellite product, projected on a 1/3° horizontal resolution Mercator grid, in time intervals of 7 days (Le Traon et al., 2003; Pascual et al., 2006).

To extract the anomalies (Sea Level Anomalies – SLA) from the original data, local time means were subtracted from each grid point. A low pass filter (Hanning with a window of 175 days) was used to remove seasonal and inter annual signals. This procedure was particularly important to eliminate the low frequency variations of the oceanic fronts positions. A lanczos filter was applied to eliminate variability with length scales larger than 1000 km. This filter offers the best performance in terms of reduction of aliasing, without compromising the sharpness of the gradients (Turkowski and Gabriel, 1990).

The variance of the resultant SLA is presented in the Fig. 1, where 5 regions of particular eddy dynamics were selected. These regions presented the higher values of variance in the South Atlantic Ocean and correspond to (1) the Brazil Current, (2) the Agulhas eddies corridor, (3) the Agulhas Current retroflexion region, (4) the Brazil-Malvinas Confluence and (5) the northern branch of the Antarctic Circumpolar Current System. The geographical limits of the five regions are presented in Table 1.



**Fig. 1.** Variance (cm<sup>2</sup>) of the SLA from AVISO over the years 2005 to 2008. Five areas of particular eddy dynamics are highlighted in white boxes: (1) The Brazil Current; (2) the corridor of propagation of Agulhas Eddies; (3) The Agulhas Current retroreflection region; (4) the Brasil-Malvinas confluence zone and (5) the northern branch of the Antarctic Circumpolar Current.

**Table 1.** Limits between regions of particular eddy dynamics in the South Atlantic Ocean and their associated oceanographic features.

Region	Latitude Limits	Longitude Limits	Mean dynamic feature
1	18° S–36° S	60° W–40° W	Brazil Current
2	24° S–36° S	40° W–0°	Agulhas Eddies propagation corridor
3	24° S–42° S	0°–20° E	Agulhas Current retroreflection
4	36° S–50° S	60° W–40° W	Brazil-Malvinas Confluence Zone
5	42° S–50° S	40° W–20° E	Antarctic Circumpolar Current

### 3 Eddy identification and tracking algorithms

Three methods were applied for the identification of mesoscale eddies in the SLA data: the Okubo-Weiss parameter, the wavelet analysis of the relative vorticity field and the geometry of the streamlines.

Surface eddy velocities and relative vorticity needed to be estimated for the application of the algorithms. Surface eddy velocities can be obtained from the SLA data through the geostrophic approximation (1):

$$\mathbf{v} = \frac{\mathbf{g}}{f} \frac{\partial \eta}{\partial x} \quad \mathbf{u} = -\frac{\mathbf{g}}{f} \frac{\partial \eta}{\partial y} \quad (1)$$

where  $(u, v)$  are the zonal and meridional surface eddy velocity components,  $\eta$  is the SLA,  $g$  is gravity and  $f$  the Coriolis factor. The relative vorticity ( $\omega$ ) can be then calculated, together with the normal ( $s_n$ ) and shear ( $s_s$ ) components of strain:

$$\omega = \frac{\partial v}{\partial x} - \frac{\partial u}{\partial y} \quad s_n = \frac{\partial u}{\partial x} - \frac{\partial v}{\partial y} \quad s_s = \frac{\partial v}{\partial x} + \frac{\partial u}{\partial y} \quad (2)$$

After the identification of the eddies, the tracking of the structures was made through a algorithm based on the ideas presented in the study of Penven et al. (2005), and discussed in the end of this section.

#### 3.1 Okubo-Weiss parameter

The Okubo-Weiss parameter ( $W$ ) was developed in the works of Okubo (1970) and Weiss (1991) and applied to several regions of the world ocean, both to satellite data and numerical model results. It is a method that aims to identify regions in a flow where the relative vorticity dominates over the strain tensors, defined as the center of the eddy. The parameter is obtained by:

$$W = s_n^2 + s_s^2 - \omega^2 \quad (3)$$

Through  $W$ , the topology of the sea surface velocities can be divided into three types of regions (McWilliams, 1984; Elhmaidi et al., 1993; Isern-Fontanet et al., 2006): elliptic regions ( $W < -W_0$ ), hyperbolic regions ( $W > W_0$ ) and the background field ( $|W| < W_0$ ), where  $W_0$  is a threshold magnitude. The eddy core is defined as a region of negative  $W$  (vorticity dominates over strain) surrounded by a region of positive  $W$  (strain dominates over vorticity). The background field presents small magnitudes of  $W$  when compared to the eddies cores. Following previous work (Pasquero et al., 2001; Isern-Fontanet et al., 2006; Henson and Thomas, 2008), the threshold was defined as  $W_0 = 0.2\sigma_W$ ,  $\sigma_W$  being the spatial standard deviation of  $W$  with the same sign of the vorticity of the eddy core. This approach

gives results very close to those obtained by simply defining  $W_0 = -2 \times 10^{-12} \text{ s}^{-2}$  as the eddies cores contours, as in Chelton et al. (2007).

The noise in the resulting fields of  $W$  difficult the identification of the coherent structures. To overcome this, we applied a low pass spatial filter with a cut length scale of 50 km. Some results from the unfiltered fields of the Okubo-Weiss parameter are presented, in order to access the influence of the filtering process. Unless otherwise posted, the results from the Okubo-Weiss parameter correspond to the filtered fields.

### 3.2 Wavelet analysis

The identification method based on the wavelet packet analysis was proposed by Doglioli et al. (2007), inspired by the original work by Siegel and Weiss (1997). We applied a version of the routines developed by these authors (WATERS) for the analysis of numerical model results, and modified for the identification of structures in relative vorticity fields derived from satellite SLA data. The method resides in an empirical observation by Farge et al. (1992) and Wickerhauser et al. (1994) that coherent vortices in 2D turbulence can be explained through a small number of the largest wavelet packet coefficients. The wave packets are then used to decompose the SLA derived vorticity maps and extract localized structures in space.

The algorithm can be divided in five steps:

1. a best basis is chosen that minimize the Shannon entropy of the original field;
2. the surface relative vorticity is expanded on this basis;
3. the wavelets are sorted out as a function of their coefficients, where only the 10 % largest coefficients are kept. In fact, the number of coefficients kept is a critical parameter of the analysis. The 10 % limit is based both in a series of tests and the bibliography (Doglioli et al., 2007; Rubio et al., 2009);
4. the structures are identified by the maximum of the vorticity modulus encircled by minimum vorticity regions;
5. structures with more than six grid cells in common are merged to eliminate filaments.

### 3.3 Geometric criterion

This approach is supported by the statement by Robinson (1991):

*“A vortex exists when instantaneous streamlines mapped onto a plane normal to the vortex core exhibit a roughly circular or spiral pattern (...)”*

Through this method, the SLA contours are used to detect the eddies with a modified winding-angle algorithm (Sadarjoen and Post, 2000). The eddy is defined by a maximum

SLA modulus, corresponding to the eddy center, encircled by a closed contour, the eddy edge. In the present study, we applied the algorithm described by Chaigneau et al. (2009).

The eddy identification process is performed in each time step, or SLA map, through two stages: (1) the identification of local SLA modulus maximum corresponding to the eddy centers and (2) the selection of closed SLA contours associated to each eddy. The outermost contour embedding only one eddy center is considered as the eddy edge. This method is very similar to the one applied by Chelton et al. (2011), and showed a good performance in terms of processing time when compared to other classical methods.

### 3.4 Eddy amplitudes and diameters

For the characterization of the eddies and comparison between algorithms, eddy diameters and amplitudes were computed. The eddy diameter was defined as the equivalent diameter ( $D_e$ ) of a circle with the same area ( $A$ ) as the closed contour delimitating the eddy borders Eq. (4).

$$D_e = 2\sqrt{\frac{A}{\pi}} \quad (4)$$

The amplitude is defined as the difference between the maximum of the SLA modulus inside the eddy and the modulus of the SLA at the border.

Eddies with diameters smaller than 50 km were ignored. In fact, real eddies smaller than this threshold are not correctly resolved in the SLA grid.

### 3.5 Tracking algorithm

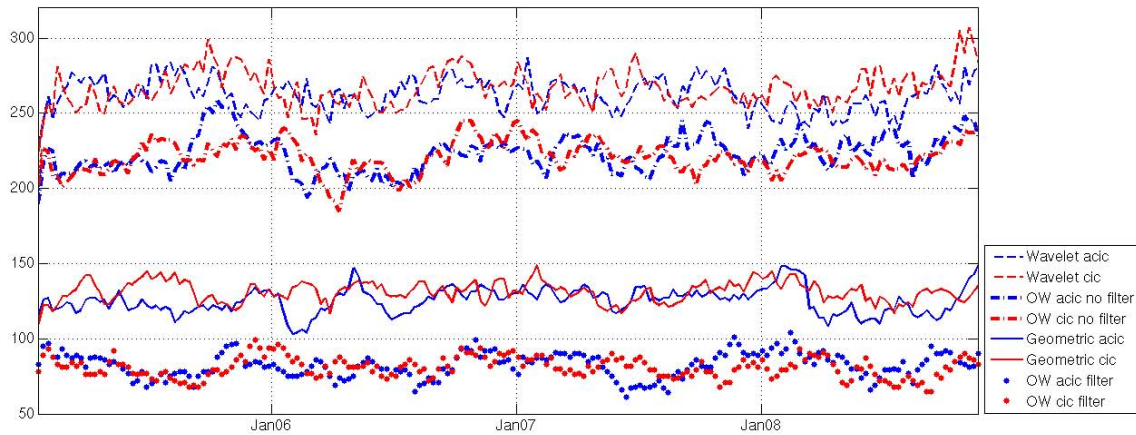
The same tracking algorithm was used for the three identification methods. The eddies central points were determined by the maximum SLA modulus. After identification, the central points were tracked in time minimizing a dissimilarity parameter Eq. (5) proposed by Penven et al. (2005).

$$X_{e_1, e_2} = \sqrt{\left(\frac{\Delta X}{X_0}\right)^2 + \left(\frac{\Delta R}{R_0}\right)^2 + \left(\frac{\Delta \xi}{\xi_0}\right)^2} \quad (5)$$

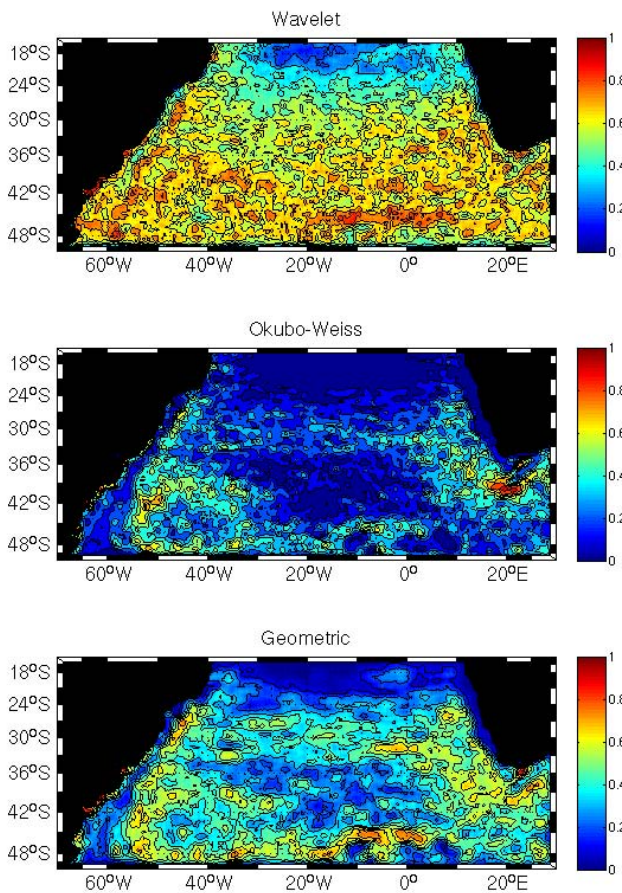
where  $\Delta X$  is the distance between the eddies  $e_1$  and  $e_2$  centers,  $\Delta R$  is the diameter difference and  $\Delta \xi$  the vorticity difference.  $X_0$  is a characteristic length scale (1000 km),  $R_0$  a characteristic diameter (100 km) and  $\xi_0$  a characteristic vorticity ( $10^{-6} \text{ s}^{-1}$ ). The parameter was calculated for all eddies identified in each time step ( $e_1$ ), in relation to the eddies in the subsequent time step ( $e_2$ ) which centers are less than  $2^\circ$  distant and that have the same vorticity sign.

Through this parameter it was possible to distinguish between new eddies, that are formed or approach the region of a previously identified structure, and its continuation in time.

When no match is found between subsequent time steps, the tracking algorithm continues searching for the same eddy



**Fig. 2.** Total number of eddies present in the South Atlantic between 70° W–30° E and 50° S–15° S, obtained from the three automatic identification algorithms, as a function of time. The colors indicate the occurrence of anti-cyclonic (blue) and cyclonic (red) eddies. The impact of the filtering process in the Okubo-Weiss method can be observed through the reduction in the number of observed structures.



**Fig. 3.** Total number of identified eddies per grid point for the three automatic identification algorithms, normalized by the maximum number of identifications.

for another 2 time steps (14 days). This helped avoiding losing track of the eddies as consequence of problems with the interpolation of the along track altimetry to a regular grid.

Eddies with lifetimes shorter than four weeks were removed from the analysis.

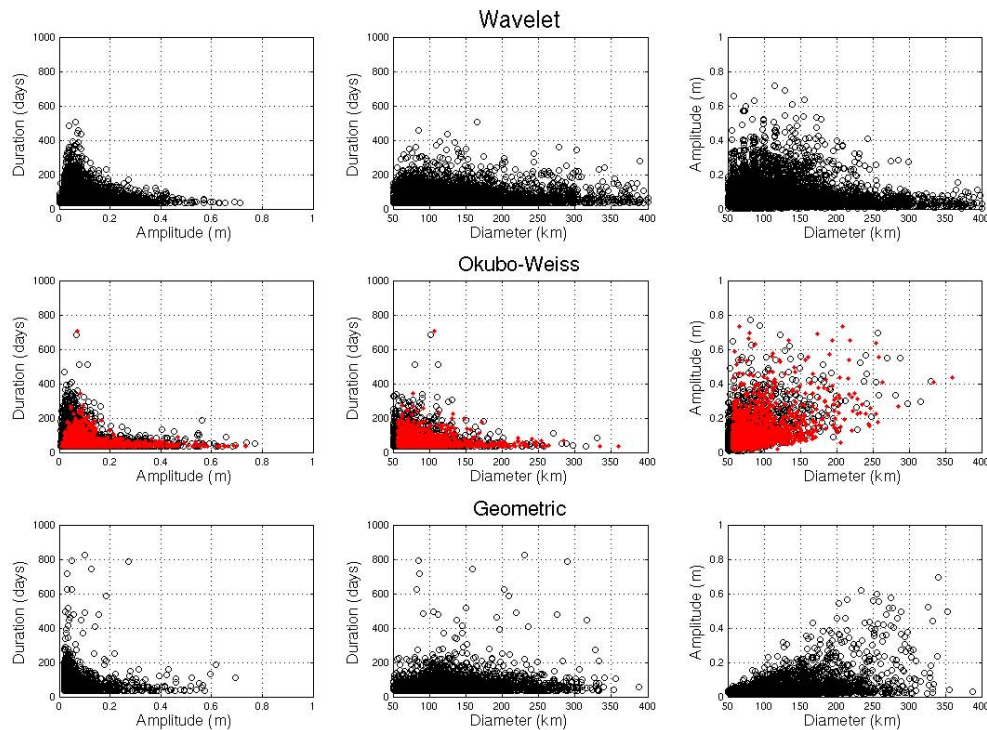
## 4 Results and discussions

### 4.1 Mean properties

We first compare the results from the three identification methods in terms of the mean eddy properties. As mean properties we understand the number of identified structures, their mean diameters and durations.

The total numbers of identified eddies with lifetimes larger than 4 weeks, for each method, are showed in Fig. 2. Although the Okubo-Weiss method have been reported to have a high number of false identifications (Isern-Fontanet et al., 2006; Chaigneau et al., 2008), the wavelet analysis yields the higher number of identifications. No predominance of cyclonic or anti-cyclonic eddies is observed through any method.

It is important to emphasize that the number of identifications must be considered with care, as it does not reflect the success or excess of identification. Since visual estimations of the eddy field, that could provide a “control number”, are very difficult to obtain in such a large area, auxiliary information is necessary to analyze the efficiency of the algorithms. In the maps of eddy frequency of occurrence in Fig. 3, it is possible to observe that the spatial distribution of the eddies retrieved by the Okubo-Weiss and geometric criteria resemble the picture provided by the variance map of Fig. 1, as should be expected.



**Fig. 4.** Relations between the mean characteristics (duration, amplitude and diameter) of all anti-cyclonic eddies obtained through the three identification algorithms. In the Okubo-Weiss method results, the black points indicate the unfiltered and the red points the filtered results.

The high number of identified structures for the Wavelet analysis method, spread all over the domain, can be associated to a difficulty of dealing with regions of very different SLA variances. Indeed, one of the hypothesis of the Siegel and Weiss (1997) work is the isotropy of the eddy field. So, it can be speculated that the observed over-identification is a consequence of the wavelet coefficients sorting. When trying to retain only the 10% larger coefficients in such a heterogeneous area, the method ends up by overestimating the presence of eddies in the less active parts of the analysis domain. This would explain the relative homogeneous spatial distribution of the number of identifications. Actually, previous work have applied the wavelet method to restricted regions, such as the Cape Basin (Doglioli et al., 2007) and the Benguela upwelling system (Rubio et al., 2009).

The number of eddies tracked in the Okubo-Weiss algorithm is highly sensitive to the threshold  $W_0$  and the filtering process. As reported by Chelton et al. (2007), smaller values of  $W_0$  results in a larger number of eddies tracked in regions of small SLA variance, but reduces the number of eddies tracked in regions of high SLA variance. When dealing with very heterogeneous regions, such as the South Atlantic, a compromise or mean threshold value has to be chosen. Also, the filtering process has an important impact in the number of structures in the Okubo-Weiss method with more than 50% of reduction in the number of identifications. If on one hand the filter reduces the number of false identi-

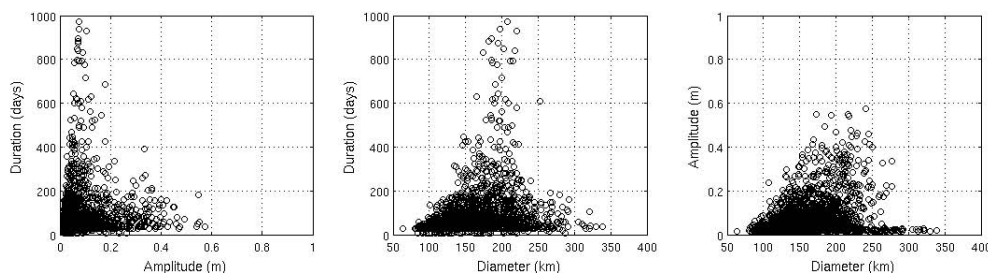
fications caused by small noisy structures, on the other hand it reduces the capability of the method to keep track of the structures for a long period of time. Nevertheless, the filtering is necessary to avoid the noise to contaminate the mean diameter and duration statistics.

The total numbers of identified eddies, their diameters and durations are presented in Table 2. This table shows that the Okubo-Weiss method results in mean diameters  $\sim 35\%$  smaller than the other two identification algorithms. Indeed, Henson and Thomas (2008) have reported a  $\sim 50\text{--}60\%$  underestimation of eddy core diameters using the Okubo-Weiss parameter in the Gulf of Alaska. The smaller difference in the present work should be a function of the more heterogeneous area, the filtering process and the value of the  $W_0$  threshold. One should observe that the maximum diameters obtained through this method are very similar to the results from the other two algorithms. This indicates that the underestimation of diameters by the Okubo-Weiss parameter is not homogeneous.

Since the relations between the mean properties of cyclonic and anti-cyclonic eddies are very similar, only the later are presented in Fig. 4. The plotted values correspond to the mean properties during each eddy lifetime. The longest duration structures have mean amplitudes smaller than 0.2 m (with one exception in the geometric criterion results). In fact, a tendency of amplitude decrease with time is observed in the three methods results. In general, this can be associated

**Table 2.** Eddy properties obtained from the three automatic identification algorithms.

		Number identified eddies	% of total observed eddies	Mean duration (days)	Max. duration (days)	Mean diameter (km)	Max. diameter (km)
Wavelet	cyclonic	5866	50.4	69	490	127	688
	anti-cyclonic	5771	49.6	69	504	128	829
Okubo-Weiss	cyclonic	2128	49.53	58	469	87	380
	anti-cyclonic	2168	50.47	58	707	85	359
Geometric	cyclonic	2820	51.5	71	679	136	342
	anti-cyclonic	2656	48.5	73	826	136	348

**Fig. 5.** Relations between the mean characteristics (duration, amplitude and diameter) of all anti-cyclonic eddies obtained from the Chelton et al. (2011) results in the same region and period of the present study.

to the loss of energy (amplitude) with lifetime observed for the long living structures. As an example, Byrne et al. (1995) estimated that the Agulhas Rings reach 40° W with ~10 % of their original amplitude.

The relation between duration and diameter is not so clear. Although the Okubo-Weiss results shows that the larger duration eddies have mean diameters of approximately 100–150 km, the same is not clear in the geometric criterion and Wavelet analysis results. This is particularly true for the anti-cyclonic eddies, where the geometric criterion method shows highly variable long living eddies mean diameters.

Similarly, it is possible to observe a tendency of mean amplitude increase with the mean diameter increase in the Okubo-Weiss and geometric criteria results, although the small amplitude eddies present a large range of mean diameters.

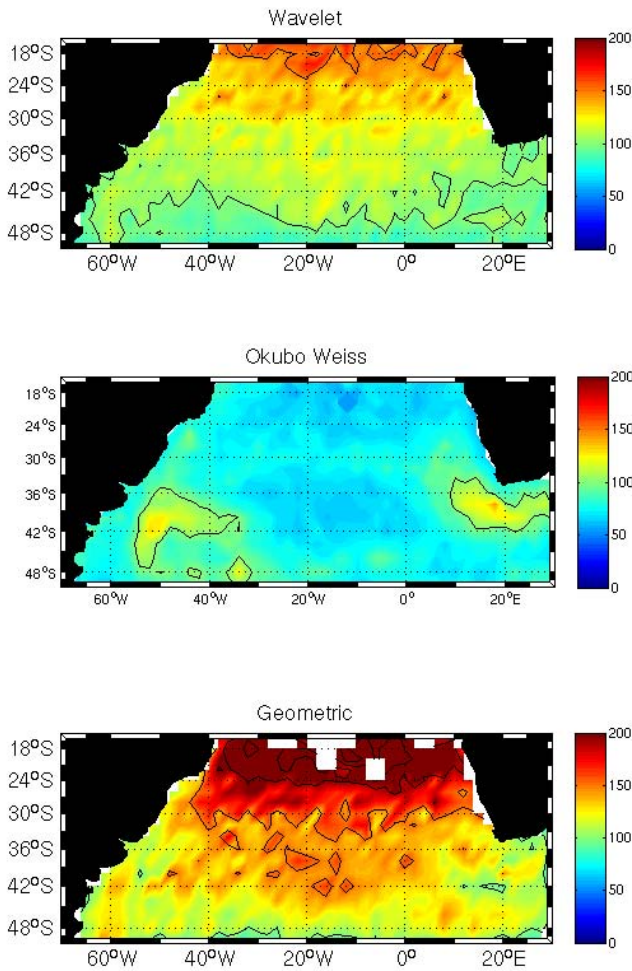
The filtering process does not have an important impact in the properties relations in the Okubo-Weiss method. However, some of the longer duration structures are lost due to the filter. This is of great interest when trying to track particular long living structures, as the Agulhas Rings.

The same eddy properties were calculated from the results of Chelton et al. (2011), for the region and period of the present study (available at <http://cioss.coas.oregonstate.edu/eddies/>) and are presented in Fig. 5. The relations between the amplitudes and the eddies durations and diameters follow the same pattern of the previous methods, although

the longer durations. A particular good agreement is observed with the geometric method. Differently from the methods analysed in this work, the longer durations eddies tend to have diameters around 200 km. This can be a consequence of the dominance of the Agulhas Rings as the longer durations structures in the South Atlantic, but further analysis is necessary to confirm this hypothesis.

The automated tracking algorithm is an important aspect that can be related to the longer duration of the eddies observed by Chelton et al. (2011). The method applied by these authors uses a zonally oriented elliptical search area for the continuation of the eddies. The size of the ellipse is related to the velocity propagation of non-dispersive Rossby waves, with a minimum value of 150 km. A wide range of variation of the eddy properties is permitted between consecutive time steps, without the estimation of the similarity. Although the fixed search area used in the present study does not take into account the variation of the eddy propagation velocities, the dissimilarity parameter promotes a better separation between different structures.

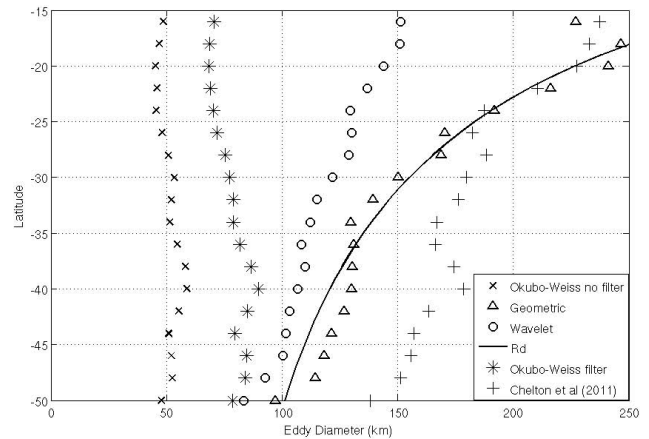
The geographical distribution of the eddies mean diameters resolved by the Wavelets and geometric criteria are very similar, although the second shows slightly higher values (Fig. 6). For both methods, larger (smaller) diameters are observed in lower (higher) latitudes, as should be expected by the variation of the Rossby deformation radius.



**Fig. 6.** Mean eddy equivalent diameters (km) in the formation moment, as derived from the three identifications algorithms. The black contours indicate intervals of 50 km.

The same pattern is not observed in the Okubo-Weiss method results. In this algorithm the eddy diameters seem to be function of their energy, with larger eddies occurring in the Brazil-Malvinas confluence and the Agulhas retroflexion – where higher SLA variability is observed (see Fig. 1).

This difference between the three methods is demonstrated in the zonal mean eddies diameters in Fig. 7, where the results obtained by Chelton et al. (2011) are also presented. In this figure, we observe that the eddies tracked through the geometric criteria present a relation between the diameter and the latitude very close to the curve of the first baroclinic mode Rossby deformation diameter (Rd – two times the Rossby deformation radius). This characteristic is reflected in the mean diameter presented in Table 2, with the geometric criterion results showing higher values. The wavelet analysis results show an almost linear relation between latitude and diameter, with a smaller inclination relative to Rd. The Okubo-Weiss zonal mean diameters are almost constant with latitude. Although the filtering of the Okubo-Weiss results eliminate the



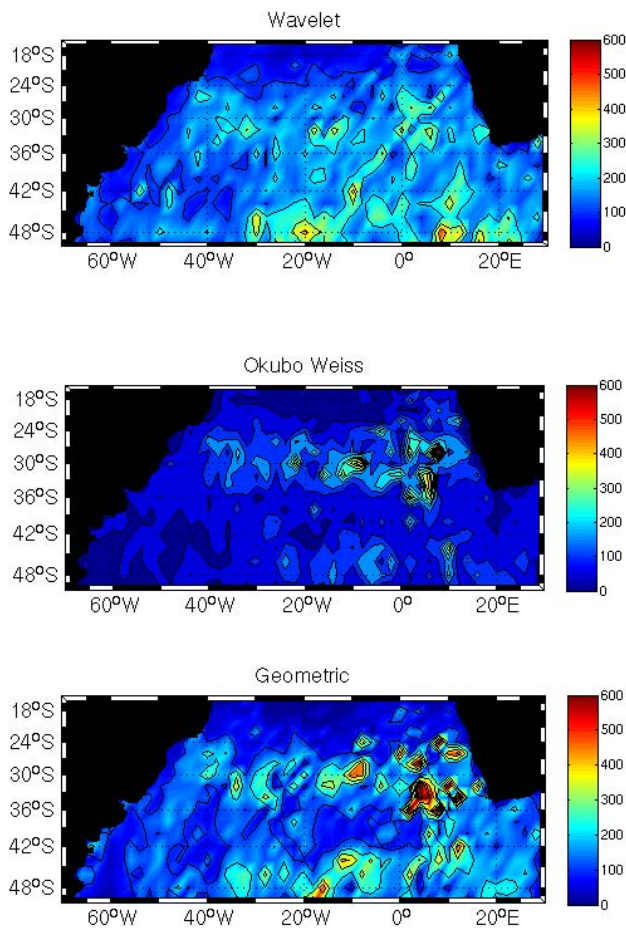
**Fig. 7.** Zonal mean eddy diameters obtained from the three identification algorithms and in Chelton et al. (2011). The solid line is a estimation of the first baroclinic mode Rossby deformation diameter (Rd).

smaller structures, the relation between diameter and latitude keeps unchanged.

The Chelton et al. (2011) results present diameters  $\sim 50\%$  larger in high latitudes (south of  $30^\circ$  S) than the present study. This can be an influence of the Brazil-Malvinas convergence zone and the Agulhas Current retroflexion, since these author results indicate the presence of large structures in these areas as a function of the presence of closed SSH contours. A similar characteristic is observed for the Okubo-Weiss parameter based method, generating a coincident bump in the mean diameters at  $40^\circ$  S related to the Brazil-Malvinas confluence (Fig. 7). In fact, in Chelton et al. (2011) a maximum threshold of 400 km is established for the eddy diameters at this latitude. It can be argued that this value is too large to prevent a contamination from the confluence front position in the eddy identification results.

From the maps of duration or lifetime of the eddies, calculated in relation to their first observation (or origin) points (Fig. 8), two regions should be highlighted. These correspond to the Agulhas Current retroflexion and the Antarctic Circumpolar Current (ACC), where the larger duration eddies have their origins. The Agulhas region is particularly clear at the eastern part of the domain in the Okubo-Weiss and geometric criteria results, with similar eddy durations. In the results from the Wavelet analysis, smaller durations are observed. This can be associated with a better performance of the two previous methods in keep the track of the structures. The ACC region is not clear in the Okubo-Weiss method results after filtering, what can be function of the small diameter expected for the structures in this area. It is important to emphasize that the same tracking algorithm was used in all identification methods, so the observed differences reflect identification failures.



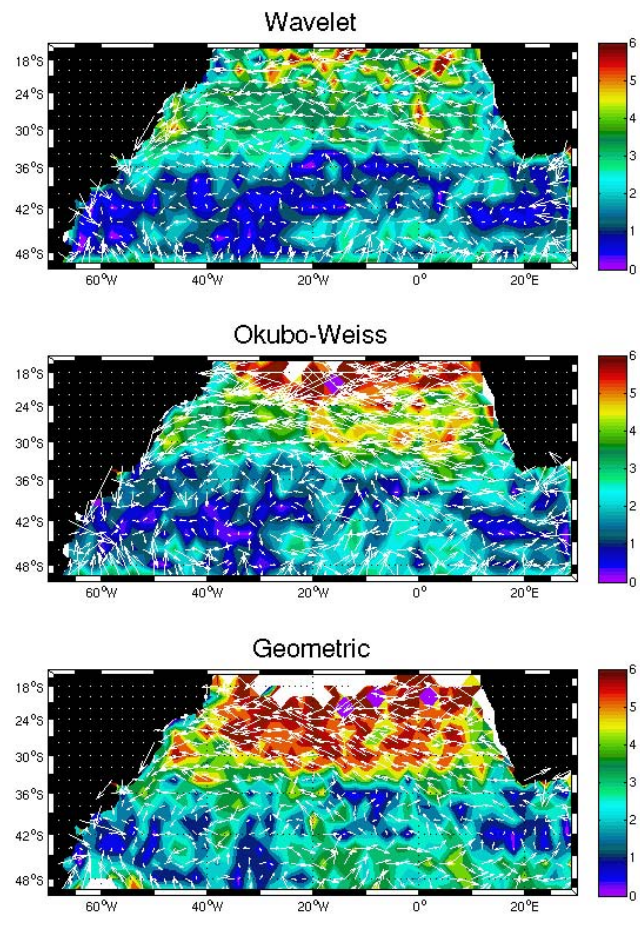


**Fig. 8.** Eddy lifetimes (days) at their birth points. The color contours indicate the duration of the identified eddies plotted in their first observation locations. The black contours represent intervals of 100 days.

It is interesting to observe that, for the three identification methods, the origin points of the Agulhas eddies are not exactly in the retroflexion. This is an indication that the eddies have been tracked only after detaching of the Agulhas Current. Similar results were obtained by Byrne et al. (1995) and Schonten et al. (2000) when tracking Agulhas Rings (anticyclonic eddies) in SLA satellite data, and by Chelton et al. (2011).

#### 4.2 Propagation velocities

Using all the tracks from eddies with durations larger than 4 months, it was possible to generate maps of mean propagation velocities (Fig. 9). The geographical pattern obtained from the three methods are similar, presenting a zone of minimum velocities centered in 42° S. From this minimum axis, velocities increase both to the north and to the south, with directions following the anti-clockwise subtropi-



**Fig. 9.** Mean propagation velocities ( $\text{km day}^{-1}$ ) for the eddies obtained from the three identification methods.

cal wind-driven circulation gyre. The eddies propagate westward through most the domain. The only exceptions are the ACC eddies, that are advected eastward by the strong mean flow as noted by Hughes et al. (1998).

The higher velocities are observed in the north of the domain, and can be associated to the Agulhas eddies corridor – between the Agulhas Current retroflexion and the South American coast, around 30° S. Regions of high velocities farther north are a consequence of the small number of identified structures, generating an overestimation of the propagation velocities. The area of large velocities in the south reflects the influence of the ACC on the propagation of eddies. The large northward propagation velocities observed in the southwest part of the study domain reflect the influence of the Malvinas Current and the eddies originated in the Drake Passage zone. Indeed, several studies treated the baroclinic instability of the ACC in Drake and the formation of eddies in this region (Gallego et al., 2004; Rintoul et al., 2001; Wright, 1981). These eddies play a important role in the flux of energy and properties between the Pacific and Atlantic oceans.

This geographical distribution of propagation velocities is in concordance with the study of Fu (2006), that used

**Table 3.** Mean eddy propagation velocities for the five areas of particular dynamics highlighted in Fig. 1, obtained from the results of the three identification methods.

		Eddy propagation velocities (km day <sup>-1</sup> )				
		Region 1	Region 2	Region 3	Region 4	Region 5
Wavelet	cyclonic	3.36	2.89	2.63	2.02	2.11
	anti-cyclonic	3.26	3.04	2.43	1.99	2.02
Okubo-Weiss	cyclonic	3.01	3.44	3.48	1.89	2.06
	anti-cyclonic	2.68	3.5	3.21	1.88	2.04
Geometric	cyclonic	3.98	4.88	3.61	2.69	2.99
	anti-cyclonic	4.45	4.99	3.78	2.62	2.96

a space-time lagged correlation analysis to characterize the pathways and propagation velocities of eddies in the South Atlantic Ocean. However, comparisons must be done with care since this author considered all perturbations to the mean state as eddies, while the present study focuses on the coherent structures, or vortices. The zone of high velocities observed by Fu (2006) in the Brazil-Malvinas confluence can be associate to short living eddies or other processes that are excluded from the present analysis. The same hypothesis can be made to the area of the Agulhas Current retroflection, where the method applied by Fu (2006) included the current meanders and the vortex structures before pinching off the retroflection.

Although similar in terms of distribution, the absolute values of the velocities differ between the methods. The geometric criterion presented overall larger velocities than the other two. For a suitable comparison, mean values of velocities in the five areas highlighted in the Fig. 1 where calculated (Table 3).

In fact, although the three methods mean propagation velocities are similar, an important exception is observed in the Agulhas eddies propagation corridor (Region 2). Previous work has reported values of velocities for the Agulhas Rings (anti-cyclonic Agulhas eddies) ranging between 3.71 km day<sup>-1</sup> (Byrne et al., 1995), 4.3–6.9 km day<sup>-1</sup> (Gordon and Haxby, 1990), and 7–8 km day<sup>-1</sup> (Garzoli et al., 1999). The velocities from the geometric criterion results (4.99 km day<sup>-1</sup>) are in the range of the bibliography, while the other two methods present smaller values.

Using the eddies tracks obtained by the geometric method as a reference, it was possible to observe that the other methods were able to identify the same structures. Although the track lengths obtained through the Okubo-Weiss parameter and Wavelet analysis were shorter than those obtained by the geometric criteria, the mean propagation velocities were the same, as one would expect.

### 4.3 Long-lived eddies

The analysis presented to this point reflects the mean eddy behavior. Although this view provides an important comparison between identification methods, it may hide some important differences relative to the long-lived structures. These eddies are of particular interest due to their important contributions to the eddy fluxes across the basin, their large participation in the total variance and particular role in the inter-basin water exchanges (Doglioli et al., 2007; Richardson, 2007; Sebille et al., 2010).

From the maps of Fig. 8, two regions of larger duration eddies where selected for further analysis. Only eddies with lifetimes larger than 120 days (~4 months) were used to ensure that all identified structures leave the formation region. The Agulhas eddy formation area was defined between the meridians of 0° and 20° E and the parallels of 40° S and 30° S, while the Antarctic Circumpolar Current (ACC) eddies area was defined between the meridians of 20° W and 0° and the parallels of 50° S and 40° S. The eddy tracks originated from these regions are presented in the Fig. 10 and the eddy mean characteristics in the Table 4.

The method based in the wavelet analysis and the filtered fields of Okubo-Weiss parameter were less efficient in tracking the Agulhas Rings (anti-cyclones) across the South Atlantic Basin. While the geometric criterion was able to keep track of several eddies farther than 30° W, as done visually by Gordon and Haxby (1990), the Okubo-Weiss method had this level of success in only one occasion, without the application of the filter.

The “fragmentations” of the eddy tracks in the wavelet analysis method are consequence of failures of identification in three or more consecutive time steps, or more than the 14 days used to search for the tracks continuity. Such fragmentation is associated not only to the shorter observed tracks, but contribute also to the homogeneous distribution of identifications relative to the other methods (see Fig. 3) and to the higher total number of structures.

The numbers of Agulhas Rings obtained from the three methods are very similar. In the Okubo-Weiss parameter

**Table 4.** Long-lived eddy properties obtained from the three identification algorithms. In the Okubo-Weiss results, the upper (lower) lines refer to the filtered (unfiltered) results.

			N. ident.	Mean dur. (days)	Max. dur. (days)	Mean Amp. (m)	Max. Amp. (m)	Mean diam. (km)	Max. diam. (km)
Wavelet	Agulhas	cyclonic	54	170	294	0.09	0.27	137	431
		anti-cyclonic	50	193	448	0.11	0.61	142	418
	ACC	cyclonic	83	183	434	0.06	0.19	119	448
		anti-cyclonic	94	1674	462	0.05	0.19	112	348
Okubo-Weiss	Agulhas	cyclonic	07	153	224	0.11	0.19	92	133
			33	169	392	0.09	0.56	61	150
		anti-cyclonic	17	224	448	0.13	0.37	102	177
			43	228	896	0.09	0.44	71	168
	ACC	cyclonic	19	147	196	0.09	0.19	92	172
			88	183	686	0.05	0.16	51	125
		anti-cyclonic	9	157	203	0.08	0.23	100	163
			82	173	462	0.05	0.15	58	151
Geometric	Agulhas	cyclonic	43	146	252	0.1	0.42	155	319
		anti-cyclonic	40	295	826	0.09	0.59	156	289
	ACC	cyclonic	58	194	483	0.04	0.14	121	237
		anti-cyclonic	44	174	518	0.04	0.14	124	200

results, the filtering process presented an important impact in the reduction of the number of tracked structures, their durations and diameter. Although the filtering prevents the tracking of small structures, it clearly reduces the efficiency in keeping track of the longer living eddies that crosses the Atlantic Basin. The same was observed by Chelton et al. (2011) when comparing the results to their previous work (Chelton et al., 2007), where the Okubo-Weiss parameter was used.

Considering only the Agulhas Rings that cross the 0° meridian in the geometric method results, leaving the formation region, approximately 4.5 eddies were observed to be shed each year. Such rings present a mean diameter of 166 km. These results are in agreement with the literature, which propose that a ring is typically shed from the Agulhas retroflection every 2–3 months with a typical diameter of 150–200 km (Byrne et al., 1995; Beismann et al., 1999; Schonten et al., 2000; Van Aken et al., 2003; de Steur et al., 2004; Doglioli et al., 2007).

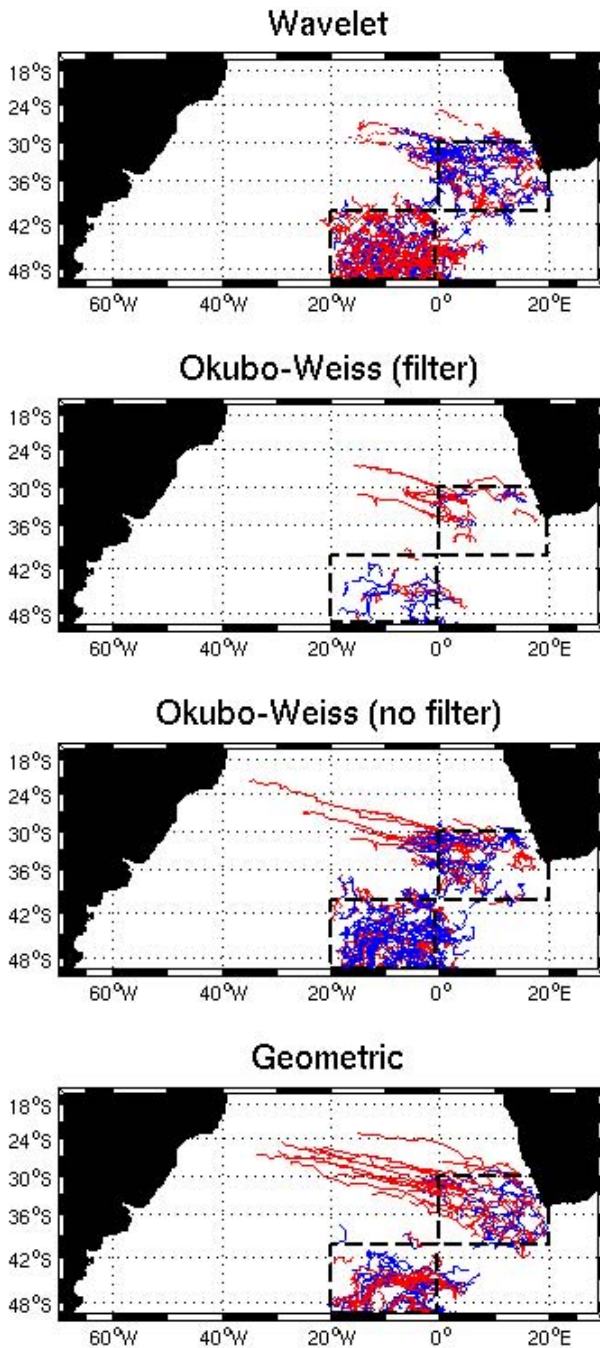
For the Agulhas cyclones, the results exhibit a large variation between the number of identified structures by each method. These cyclones are believed to play a important, though secondary, role in the inter-basin ocean waters exchange. They have been reported to travel southwestward into the South Atlantic and trigger the pinching off of Agulhas Rings (Lutjeharms et al., 2003). The trajectories represented in Fig. 10 show that most cyclonic eddies do not leave the proximity of the Cape Basin. Even those that follow a westward trajectory similar to the anti-cyclones do not have their longevity, never reaching longitudes west of 10° W. In

fact, Boebel et al. (2003) revealed that the Cape Basin off Cape Town is filled with Agulhas Rings and cyclonic eddies interacting with each other, and a similar behavior is observed through the trajectories obtained in the present work. As described by Matano and Beier (2003), the Agulhas cyclone mean diameters were observed to be generally smaller than the anti-cyclones.

Despite the short time period of four years used, it is possible to observe a seasonal variability in the formation of the long-living Agulhas anti-cyclonic eddies (Fig. 11). There is a higher number of Agulhas Rings formed in the summer and winter months, with a detached participation of the month of December. The same is not observed for the cyclones, that presented more homogeneous formation rates along the year.

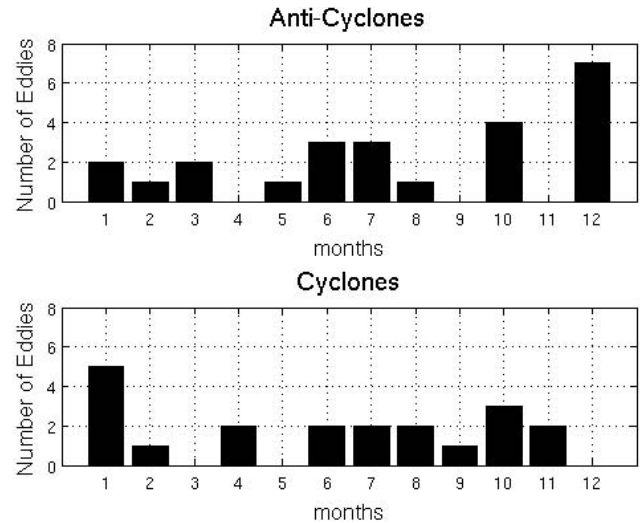
In the ACC eddies formation region, both the cyclonic and anti-cyclonic eddies show very diffuse tracks. In general, eddies present a eastward propagation following the main flow. This is better evidenced in the geometric criterion and filtered Okubo-Weiss parameter results. In fact, the ACC was the only region where Chelton et al. (2011) were able to identify long-living (>16 weeks) eastward propagating eddies in the southern hemisphere.

Mesoscale activity is believed to play a central role in the maintenance of the frontal structures of the ACC (Karsten and Marshall, 2002) and in the southward flux of heat and deep water masses as part of the Atlantic meridional overturning circulation (MOC) (de Szoek and Levine, 1981; Nowlin and Klinck, 1986; Phillips and Rintoul, 2000). Few studies, however, have estimated the eddy tracks and natures.



**Fig. 10.** Track of the long-lived eddies (duration > 12 weeks) originated in the Agulhas retroflection (northeastern black rectangle) and Antarctic Circumpolar Current (southwestern black rectangle). The blue lines indicate cyclonic and the red lines anti-cyclonic eddies.

It is important to emphasize that the ACC eddy formation region defined in the present study refers only to the larger duration structures observed in the South Atlantic. Eddies that enter the Atlantic basin through the Drake passage or leave the basin to the east have their lifetimes underestimated due to the domain restrictions.



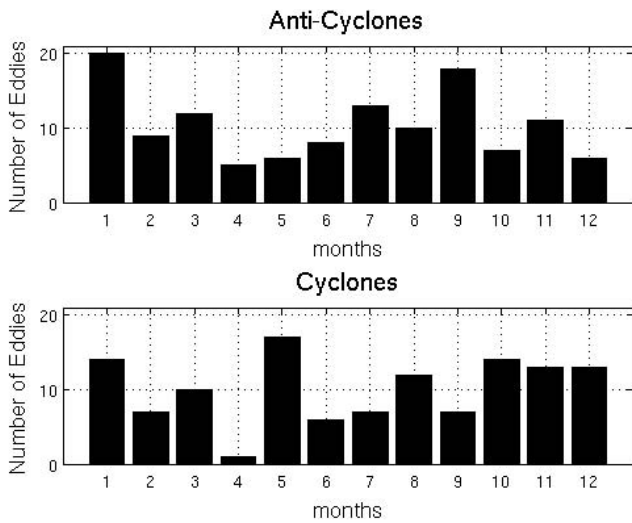
**Fig. 11.** Number of Agulhas eddies formed per month in the years 2005 to 2009. It corresponds to the long-lived eddies with durations higher than 120 days and that cross the  $0^\circ$  meridian, leaving the formation region.

The eddies in the ACC region are smaller and less intense than in the Agulhas region (Table 4). As observed in the mean results, the Wavelet analysis presented a higher number of structure identification, followed by the unfiltered Okubo-Weiss parameter. The underestimation of the eddy diameters by the Okubo-Weiss parameter is also reproduced in this case. In opposition to the Agulhas eddies, there is no clear difference between the ACC cyclonic and anti-cyclonic eddy track lengths in Fig. 10. While the mean eddy durations obtained for the three methods are similar, the maximum values presented important differences. Again, the wavelet analysis present the smaller lifetimes. Although the maximum duration value for a cyclone in the ACC region is detected with the Okubo-Weiss parameter, it represents an isolated case where the method merged two subsequent structures. Similarly to the Agulhas Rings, the ACC anti-cyclones presented a seasonal cycle in the formation rate. The same is not truth for the cyclones (Fig. 12).

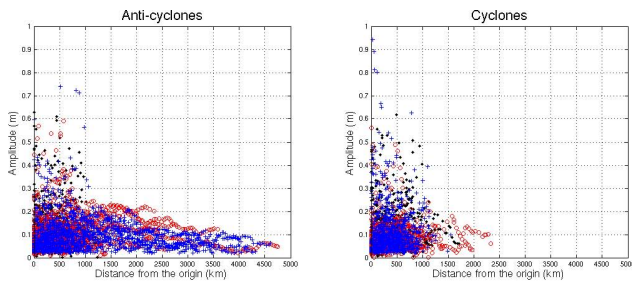
As noted by Morrow et al. (2004) and Chelton et al. (2011), the anti-cyclones present a small northward deflection in their propagation direction. This tendency is more clear in the Agulhas Rings than in the ACC eddies. Although the expected southward deflections of the cyclones trajectories are not clear in the results obtained by any method, the difference from the anti-cyclones pattern is notable. This should be a consequence of the shorter duration of the cyclones resolved by the identification and tracking algorithms.

#### 4.4 Agulhas Rings decay

The results in this section refer to the Agulhas Rings, that present an amplitude decay with lifetime well documented



**Fig. 12.** Number of ACC eddies formed per month in the years 2005 to 2009. It corresponds to the long-lived eddies with durations higher than 120 days.

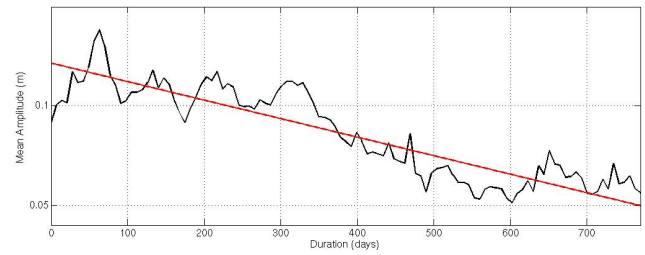


**Fig. 13.** Amplitude of Agulhas eddies as a function of the distance from their first identification site. The (●) indicate the results from the Wavelet analysis identification method, the (○) the results from the Okubo-Weiss parameter and the (+) the results from the geometric criterion.

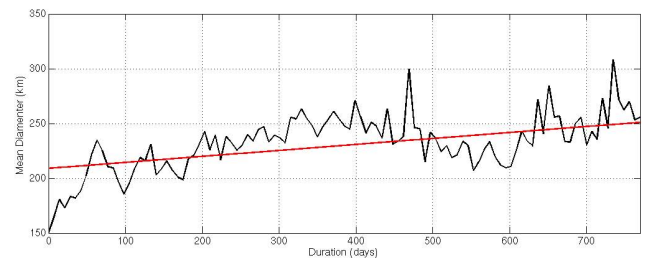
in the bibliography (Byrne et al., 1995; Seville et al., 2010). Such characteristic were not observed for the eddies originated in the ACC region. All the observed long-lived Agulhas rings were used in the present estimates.

The three identification methods give similar eddy decay results (Fig. 13). Despite the differences in eddy durations, the exponential character described by Byrne et al. (1995) is observed for the anti-cyclones (Agulhas Rings). The authors have calculated a 81 % amplitude reduction for the Agulhas Rings during its life. The present results show that, based in the geometric criterion, an 83 % amplitude reduction should be expected for a typical Agulhas Ring between its origin and end of lifetime.

Although the exponential decay relation observed in Fig. 11, a linear fit can be used to estimate the mean decay rate of a typical Agulhas Ring (Fig. 14). The geometric criterion results were selected for showing a larger number of eddies with long durations. The mean decay rate obtained



**Fig. 14.** Amplitude decay for a mean Agulhas Ring tracked through the geometric criterion. The red line is a linear fit with a  $-9.33 \times 10^{-5} \text{ m day}^{-1}$  angular coefficient.



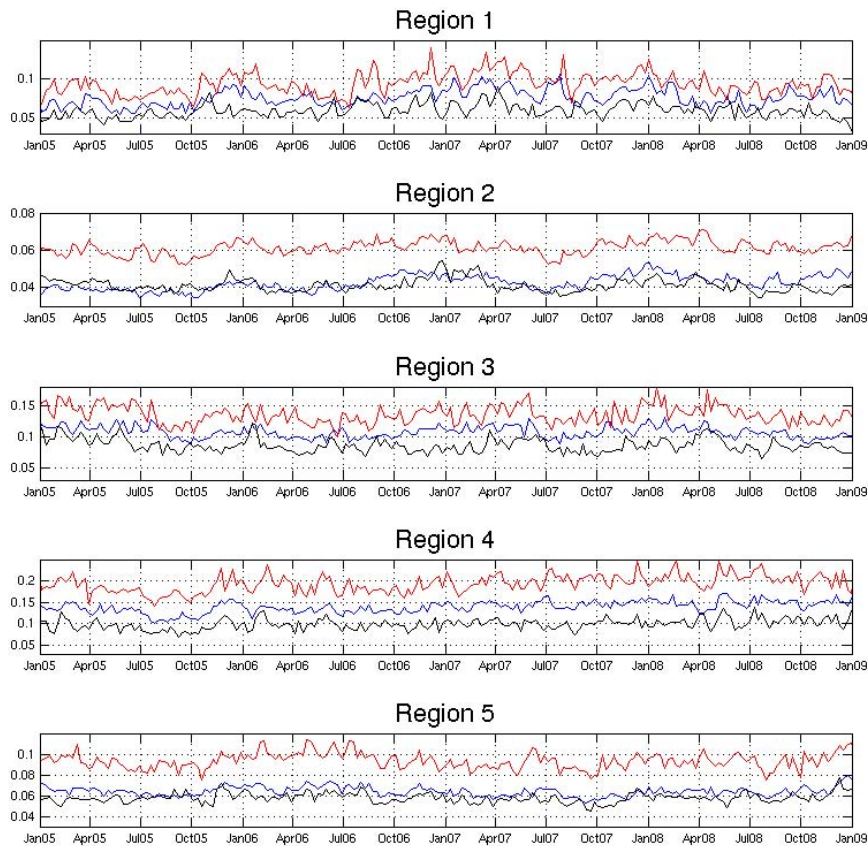
**Fig. 15.** Diameter modification of a mean Agulhas Ring tracked through the geometric criterion. The red line is a linear fit with a  $5.45 \times 10^{-2} \text{ km day}^{-1}$  angular coefficient.

indicates a reduction of  $9.33 \times 10^{-5} \text{ m day}^{-1}$  in the eddy amplitudes. Similarly, a modification in the eddies diameter is observed along their lifetime. Through the linear fit, a rate of  $5.54 \times 10^{-2} \text{ km day}^{-1}$  diameter increase was calculated (Fig. 15).

#### 4.5 Time variability

The regions of particular eddy dynamics, highlighted in Fig. 1, were used to study the time variability of the eddy characteristics obtained through the three identification methods. Since all eddies identified were included in the analysis, the results include the influence of the different number of eddies obtained by each method.

From the time series of root mean squared amplitudes presented in Fig. 16 it is possible to observe that, although the similar variability between the three methods, the results from the Okubo-Weiss parameter presented higher amplitudes than the other two. This is particularly clear to the regions 2 and 5, corresponding to the Agulhas and ACC eddies propagation corridors. In fact, as can be observed in the Table 4, the filtered Okubo-Weiss parameter resulted in larger mean amplitudes for the Agulhas eddies. This is a consequence of the removal of the weaker structures. The same can not be observed for the ACC eddies since most structures in the region have short durations, and do not participate in the calculations of Table 4.



**Fig. 16.** Mean eddy amplitudes (m) for five areas of particular high SLA variance in the South Atlantic Ocean. Note the amplitude scales are different between the figures due to the distinct values presented by the regions. The blue lines (—) indicate the results from the Wavelet analysis method, the red lines (—) the results from the Okubo-Weiss parameter and the black lines (—) the results from the geometric criterion.

Analyzing the spectra of the eddy amplitudes in the Fig. 17, it is possible to observe that the main variability frequencies are reproduced by the three methods. Larger differences in the spectral energy content occurs in the Agulhas eddies propagation area (Region 2) and the Brazil-Malvinas Confluence zone (Region 4). In the first case the difference can be explained by the larger number of long living eddies tracked through the geometric criterion. Indeed, a secondary spectral peak of 66 days in the Region 2 spectrum can be associated to the periodicity of the Agulhas Rings shedding, as this is the major feature influencing the SLA variability in this area.

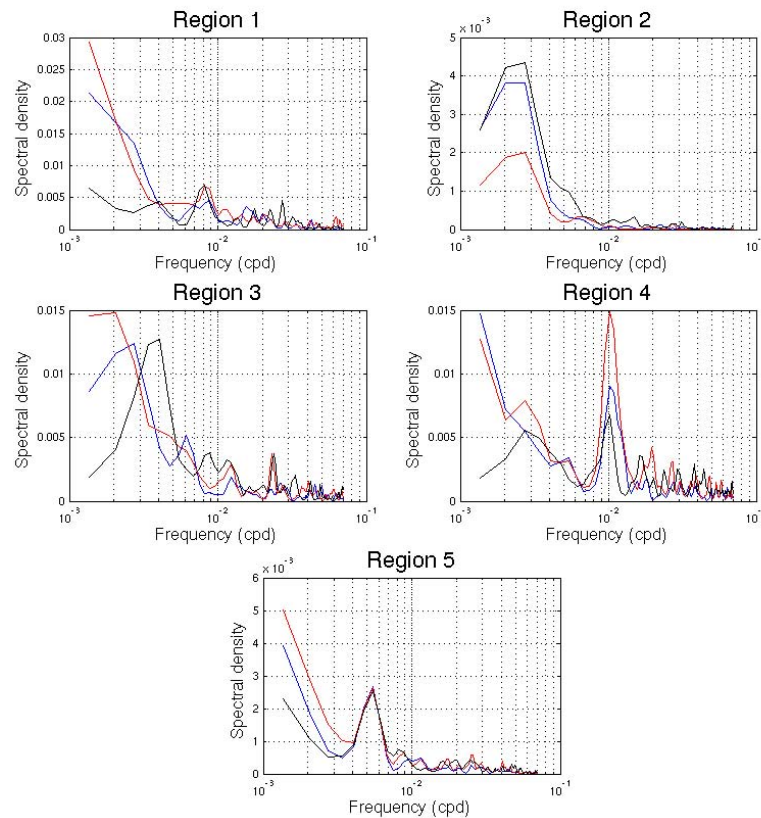
A particularly good agreement between the spectra from the Wavelet analysis and the geometric criterion denotes a similarity between the behavior of the identified structures in both methods. From these results one can observe that, while region 2 is the only one that presents a dominating annual cycle, regions 4 and 5 show coherent peaks corresponding to the periods of 98 and 183 days.

The coincidence of the Region 5 (ACC) 183 day spectral peak in the three methods results is remarkable. This denotes the influence of a dominating mode of variability. Some

studies (e.g., Meredith et al., 2006; Thompson and Wallace, 2000; Thompson et al., 2000) relate the sub-seasonal variability in the SLA field in the Southern Ocean to the Southern Hemisphere Annular Mode. More analysis, which are beyond the scope of this study, are necessary to confirm this relationship.

## 5 Conclusions

From the results of three automatic eddy identification methods it was possible to quantify the presence and characteristics of coherent mesoscale structures in the South Atlantic. The comparison between the methods provided a estimation range for the number of eddies, their diameters, amplitudes, propagation velocities and lifetimes. Although the number of structures differs between the methods, their characteristics and temporal variability are similar. Indeed, the good agreement between the spectra of eddy amplitudes, presented in Fig. 17, is a indication that the major structures were detected by all the methods along the four years considered in the present study.



**Fig. 17.** Eddy amplitude time spectra ( $\text{m}^2$ ) for five regions of particular high SLA variance in the South Atlantic Ocean. The blue lines (—) indicate the results from the Wavelet analysis method, the red lines (—) the results from the Okubo-Weiss parameter and the black lines (—) the results from the geometric criterion.

It is interesting to observe that the three methods give similar number of cyclone and anti-cyclone identifications. Moreover, no inter-annual variation is observed in the number of eddies between 2005 and 2008. This may be a consequence of:

1. the short time length of the SLA data used in the present study;
2. the number of eddies computed for the South Atlantic basin as a whole, masking local variations.

The areas of higher SLA variance could be related to the presence of coherent structures. The same pattern of geographical distribution is observed in the map of SLA variance (Fig. 1) and the number of identified eddies (Fig. 3) in the Okubo-Weiss parameter and geometric criterion results. However, a direct link between the SLA variance and number of eddies is not possible, since the variability in high energy areas is consequence of several different processes. This is particularly the case in the Agulhas Current retroflexion and the Brazil-Malvinas confluence, in the South Atlantic Ocean. Although the variance in these areas is considerably higher, the number of identified structures is similar to the Agulhas eddies corridor and the ACC. The identification method

based on the wavelet analysis could not retrieve the same geographical pattern.

The geometric criterion presented the best performance in terms of eddy identification and tracking. The eddy characteristics from this identification method presented the better level of agreement with the other two algorithms and the bibliography. Particularly, eddy diameters show a good relationship with the first baroclinic mode Rossby deformation radius. Moreover, the time length and propagation velocities obtained through the geometric criterion are in close agreement with previous work.

Although the application of a spatial filter was necessary to remove small scale noisy structures from the Okubo-Weiss parameter results, it had serious consequences on the tracking of the long living eddies. This is well manifested in the small number of Agulhas Rings tracked after filtering, and their short durations in comparison to the geometric criterion and the bibliography. The unfiltered parameter presents good results in terms of the duration of the eddies, but fails on represent their mean diameters and arrives to small values of propagation velocities.

For the wavelet analysis method, although the velocities and diameters are well represented, the duration of the structures are underestimated.

The present results corroborate the hypothesis by Chelton et al. (2007) that most variability in the middle of the oceanic basins is associated with mesoscale coherent structures. In the South Atlantic such variability is strongly associated to the propagation of Agulhas eddies, with the anti-cyclones (Agulhas Rings) playing a leading role.

Other modern methods to identify coherent structures in turbulent flows have been suggested. As an example, Hua and Klein (1998) have proposed a method based in the Lagrangian acceleration tensor, overcoming the Okubo-Weiss parameter deficiencies and better representing the flux topology in the case of decaying two-dimensional turbulence. Other method is based in the instantaneous Lagrangean flow geometry through the Lyapunov function (Haller, 2005). Although the potential benefits, there is no application to real oceanic eddies present in the peer reviewed literature.

Although the SLA data used in the present work permitted the surface localization and delimitation of the eddies, the lack of knowledge about their vertical structure presents a strong barrier in the estimation of their role in the oceanic heat and water masses fluxes. New global in-situ observations, such as the ARGO profiling floats, should provide a means to better estimate their vertical structure. The combination of the eddies tracks obtained in the present study with vertical profiles should provide new estimations for the oceanic eddy fluxes and will be addressed in future work.

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