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Analysis of the effect of fish oil on wind waves and implications for air–water interaction studies

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Abstract. Surfactant layers with viscoelastic properties floating on the water surface dampen short gravity-capillary waves. Taking advantage of the known virtue of fish oil to still angry seas, a laboratory study has been made to analyse wind-wave generation and the interaction between wind waves, paddle waves, and airflow. This was done in a tank containing a thin fish-oil film uniformly spread on the water surface. The research was aimed, on the one hand, at quantifying for the first time the effectiveness of this surfactant at impeding the generation of wind waves and, on the other, at using the derived conditions to disentangle relevant mechanisms involved in the air-sea interaction. In particular, our main interest concerned the processes acting on the wind stress and on the wave growth. With oil on the water surface, we have found that in the wind-only condition (no paddle waves) the wave field does not grow from the rest condition. This equilibrium is altered by irregular paddle (long) waves, the generation and evolution of short waves (in clean water and with oil) being modified by their interaction with the orbital velocity of the long waves and their effect on the airflow. Paddle waves do grow under the action of wind, the amount being similar in clean and oily water conditions, a fact we ascribe to the similar distortion of the wind vertical profile in the two cases. We have also verified that the wind-supported stress on the oily water surface was able to generate a surface current, whose magnitude turns out to be comparable to the one in clean water. We stress the benefits of experiments with surfactants to explore in detail the physics at, and the exchanges across, the wavy and non-wavy air-water interface.

1 Introduction

It is well known that the addition of an almost monomolecular film (thickness from 10^{-9} to 10^{-8} m) of surfactant (blend of surface active agent) to the water surface diminishes the energy of gravity-capillary waves by altering the surface tension at the water-air interface (Fiscella et al., 1985). For this reason, oily surfactants were used for centuries by seamen to smooth the ocean surface waves, so much that expressions such as "to pour oil on troubled water" have acquired a more general meaning. Crucial in this respect is the type of oil, in particular its polarity. Mineral oils, often used for this purpose during the Second World War, are less effective because their molecules tend to group together. On the contrary the polar molecules of fish, and partly also vegetable, oils repel each other. Hence, once poured on water, they tend to distribute rapidly on the available surface reaching a quasimonomolecular layer (e.g. see Cox et al., 2017).

Known since ancient times, this damping effect was first studied in the 19th century by the Italian physicist Carlo Marangoni (Marangoni, 1872); hence the official name of the process. In relatively recent times the first report of the resonance-type Marangoni damping of wave spectra (briefly sketched in Appendix A) comes from Cini et al. (1983), who noted the effect in polluted water, although by mineral oils, in the Gulf of Genoa, Italy. However, clear evidence in the open sea of high damping of surface waves in the short-gravitywave region by monomolecular slicks was first verified by Ermakov et al. (1985, 1986) during field experiments in the Black Sea.

The Marangoni damping can be effective for surface waves in two possible conditions. The first one is in open ocean, in which an existing wind-forced wave field travels through a surfactant patch, with the consequent possibility of recognition (lack of return signal by damped short waves) by microwave radars (Feindt, 1985). A direct application is, for instance, the remote detection of oil spills (Fingas and Brown, 2017); spill drift and deformation, and in turn the damping rate of waves, are affected by the properties of the slick (e.g. the elastic properties of the film) and of the entering wave field (Christensen and Terrile, 2009). Direct in situ observations of the surfactant effects on wind waves, however, have been very limited because of the challenges to operate in stormy conditions. According to the Marangoni mechanism, for oily surfaces the energy dissipation process is quite selective in wavenumbers but its effects are not, since it spreads, although to a lesser extent, towards longer and shorter waves via non-linear interactions and modification of the airflow profile. Hühnerfuss et al. (1983) in a slick experiment carried out in the North Sea found that waves with a wavelength of up to 3 m are significantly decreased in amplitude when they travel through a 1.5 km long monomolecular surface-film patch. The result is that the wave growth is inhibited and the existing surface field is rapidly smoothed and progressively attenuated as it propagates within a surfactant patch (Ermakov et al., 1986). This change in surface properties resembles the wave attenuation under an ice cover, for which there are many other processes that also attenuate energy (e.g. see Weber, 1987, and Christensen, 2005, for a parallel between the two fields). The second condition, typical of laboratory experiments (e.g. Hühnerfuss et al., 1981; Mitsuyasu and Honda, 1986), is where the wind blows over a water surface homogeneously covered with a surfactant film since the rest condition. Compared with a clean-water environment, from the wind onset, the coupled air-water system is adjusted to a new state, characterized by strong suppression of the generation of wind waves and a change in the wind stress corresponding to the reduction in form drag of the wave field.

The suppression of wind-generated waves due to the oil slick greatly alters the air-sea interaction process (Mitsuyasu and Honda, 1986), but the full mechanism remains poorly understood (Cox et al., 2017). In this respect, with still different opinions on the reason why (e.g. see Kawai, 1979; Phillips, 1957), we know that as soon as the first wind blows, the sea surface is covered by tiny 2-3 cm long wavelets. That process is quickly overtaken as the waves grow by the feedback caused by the wave-induced pressure oscillations in the air, as soon as the airflow vertical profile is modified by the presence of waves. Miles (1957) proposed a wave growth mechanism that accounts for this change. This theory was extended and later applied by Janssen (1991) to wave forecasting. Its validity is questioned for very short waves whose phase speed is as slow as the air friction velocity (Miles, 1993). According to the shear-flow model by Miles, waves with phase speed c grow when the curvature in the vertical wind profile, at the height (called critical height) where the wind speed equals c, is negative. As a result, the wind profile changes because of the continuous transfer of energy to the waves (Janssen, 1982). The growth rate is proportional to this curvature and it has an implicit dependence on the roughness on the wavy water surface (Janssen, 1991). Hence it is expected that any modification of the vertical wind shear (for instance induced by the oil film effect) modifies the momentum transfer from wind to waves.

In this study, we verify with experiments in a wave tank that the peculiarity of fish oil is indeed striking. Previous research suggested (e.g. Alpers and Hühnerfuss, 1989) a correlation between the intensity and frequency range of the wave damping and the chemical properties (namely the dilatational modulus) of the surfactant. Therefore our study explores for the first time the effect of fish oil (a polar surfactant with high dilatational modulus) by laboratory experiments in which the oil effects on the wind shear stress and the wave growth are assessed in different conditions for short wind-generated and long collinear paddle-generated waves The latter ones introduce the problem of interaction between long and short waves, and between long waves and the wind profile.

In the open ocean, the influence of swell on local windwave generation is a known fact; albeit a firm explanation of the underlying mechanism has not been reached. Hwang et al. (2011) discuss how the Tehuano-wind-generated waves, on the Pacific coast of Mexico, are affected by the incoming oceanic opposing swell. With some similarity, the cases of following or opposing swell seem to differ somehow in their physics. In the laboratory, the "following swell" case was first studied by Mitsuyasu (1966) and later intensively by Donelan (1987), who suggested that a swell (in practice paddle waves; also his experiments were done in a wind- and paddle-wave tank at the University of Miami, USA) induces a detuning of the resonance conditions for non-linear interactions among wind waves. Later, in the studies by Phillips and Banner (1974) and Donelan et al. (2010), the suggested explanation was the enhanced wind-wave breaking due to the wind and paddle waves interaction. Also, the influence of paddle waves increases with their steepness. More recently, Chen and Belcher (2000) proposed the idea that the long wave exerts a drag on the airflow, which reduces the turbulent stress in the airflow that is available to generate wind waves.

Given these previous experiences, the present study is motivated, on the one hand, to quantify for the first time the effect of fish oil on the generation of the gravity–capillary wind-wave field. We worked with waves generated in a wind flume using clean water and water with surfactant on the surface. Irregular paddle waves coexisting with wind waves were also tested to investigate the mutual interaction between short waves, long waves, and airflow. On the other hand, using the suppressed wind waves with surfactants, we aimed at using the experiments to disentangle and analyse relevant mechanisms of the air–sea interaction; our interest was on the



Figure 1. Schematic longitudinal diagram of the wave flume arrangement at the First Institute of Oceanography flume (Qingdao, P. R. China). For the sake of clarity, horizontal and vertical scales are distorted. The arrows indicate the direction of the flow.

pure frictional wind stress (which, in clean water, is not separable from the wave stress), the related water surface drift, and the growth of irregular long waves under the action of the wind, by largely cancelling the short-wave roughness.

The paper is organized as follows. Section 2 gives a general description of the experimental set-up in the tank, lists the general plan of experiments with wind and paddle waves in clean water and with oil, and describes the water elevation and airflow data collected during the tests. The results of the experiments are examined in Sect. 3, where we show the response of the coupled air–water system to the presence of fish oil slick. The principal results and implications for air–water interaction studies of the present investigation are discussed in Sect. 4. Finally, the main findings of the study are summarized in Sect. 5. The paper is complemented by two videos recorded during the experiments showing the effect on wind and paddle waves of the surface layer of fish oil (Benetazzo et al., 2018b, c).

2 Experiment

2.1 The experimental set-up

The experiments described in this study were performed in a large wind- and paddle-wave facility allowing the generation of winds at velocities comparable with those in open sea (but not extreme conditions). The measurements were carried out in the flume of the First Institute of Oceanography (FIO, Qingdao, P. R. China) illustrated schematically in Fig. 1. The tank dimensions are 32.5 m in length, 1.0 m wallto-wall cross section, 0.8 m ceiling above the mean water surface. The water depth is 1.2 m, satisfying the deep-water condition for the wind-driven gravity–capillary waves, and practically also paddle waves, analysed in this study. The smallest longitudinal natural frequency of the tank is 0.052 Hz. Side walls are made of clear glass to enable visualization of the wave field. A water pipe parallel to and below the flume allows continuity between the two ends of the tank.

The wind tunnel is mounted atop the wave tank, which is closed with side glass walls and a ceiling. The airflow could be driven up to a reference speed of 12 m s^{-1} . Mechanically generated (paddle) waves coexisting with wind waves could be generated by a piston-type paddle in the range of periods from 0.5 to 5.0 s (frequencies from 0.2 to 2.0 Hz) and dissipated at the downwind end of the tank on a sloping beach of fibrous matter. Four calibrated capacitance-type wave gauges (featuring a linear response and accuracy of 0.3 mm) collected synchronous water surface elevation data for 300 s at 50 Hz at fetches X = 8.0 m (probe G1), 12.0 m (G2), 15.5 m (G3), and 20.5 m (G4) along the tank main axis. The fetch X = 0.0 m corresponds to the inlet for wind in the water tank. For the statistically steady part of the wave records, the variance frequency spectrum of water surface elevation z(t) was computed by means of the Welch (1967) overlapped segment averaging estimator (eight segments of equal length, 50 % overlap, Hamming window).

For characterization of the vertical profile of the alongchannel component of the airflow velocity, five Pitot tubes sampling at 1/7 Hz were located at X = 11.5 m in the centre of the cross section and distributed at different heights *h* above the still water surface, respectively (from tube 1 to 5) at h = 8.3, 18.3, 28.3, 38.3, and 48.3 cm. Estimates of the wind stress were derived by fitting the Pitot tube observations with a logarithmic law function of *h*. For an aerodynamically rough airflow, the mean value of the along-channel component of the wind velocity \overline{U} in the outer turbulent layer at height *h* above the boundary is expected to follow a self-similar Kármán–Prandtl logarithmic law as a function of height

$$\overline{U}(h) = \frac{u_*}{\kappa} \log\left(\frac{h}{h_0}\right),\tag{1}$$

where the overbar indicates the temporal averaging process, u_* is the friction velocity along the same direction as \overline{U} , $\kappa = 0.41$ is the von Kármán's constant. The non-zero parameter h_0 has the meaning of the roughness height where \overline{U} appears to go to zero, namely h_0 is the virtual origin of the mean velocity profile. In the presence of waves, the shape of the wind velocity profile $\overline{U}(h)$ is governed by both turbulent and wave-induced momentum flux, the latter being a function of the wind input source term in Eq. (A2). The transport of horizontal momentum due to molecular viscosity is considered negligible, except very near the surface where the vertical motion is suppressed. The total air-side shear stress τ_a at the boundary of the flow is then approximated as

$$\tau_{\rm a} = \rho_{\rm a} u_*^2 \tag{2}$$

with ρ_a being the air density.

To account for the non-slip condition in Eq. (1), the measured airflow velocity $U_a(h)$ has to be taken relative to alongwind components of the water surface velocity u_{w0} at h = 0, i.e. $U(h) = U_a(h) - u_{w0}$. It is thus assumed that the mean water surface drift velocity u_{w0} constitutes the boundary condition at h = 0 for the vertical profile of the airflow velocity. Wu (1975) found that at the air-water interface, the windinduced current is proportional to the friction velocity of the wind, and it is associated with the wind shear, Stokes drift, and momentum injection during wave breaking events. For non-breaking wavy surfaces, the wind-induced surface current was determined to be around 50 % of the airflow friction velocity (Phillips and Banner, 1974; Wu, 1975). In a cleanwater wind-wave tank and at steady conditions, the value of u_{w0} can be related to the maximum value of $U_a(h)$. This is not achieved at the largest distances from the water due to the presence of the tank roof. A u_{w0} value around 3.3 % of the free-stream maximum wind velocity seems to be a reasonable approximation (Liberzon and Shemer, 2011; Peirson, 1997; Wu, 1975) and was used in this study. The accuracy of the wind stress obtained from the profiles measured by Pitot tubes in a wave tank was examined by Liberzon and Shemer (2011), who found that the values of the wind stress obtained from the measurements by the Pitot tube and those calculated from the Reynolds stresses agree within about 10%mean difference (using an X-hot-film thermo-anemometer).

A series of videos showing the water surface conditions in clean water and in water with oil complements the available data providing a plain perception of the fish oil effect on the surface waves.

2.2 The experiments

Our experiments aimed at analysing the different results, using the different combinations of reference wind speed $U_{\rm r}$, paddle waves (changing the peak wave period T_p and the significant wave height H_s), and oily surface. The data of each experiment were later screened for correct data availability and consistency among the different instruments. This led us to exclude several records considered not suitable (independently of the physical results) for the final analysis. This was based on the six experiments listed in Table 1. Two different blower reference speeds were analysed, namely $U_r = 6$ and $8 \,\mathrm{m \, s^{-1}}$, and one set of irregular paddle waves (JON-SWAP spectrum with $T_p = 1.0$ s and $H_s = 6.2$ cm; steepness $H_{\rm s}/L_{\rm p} = 0.04$ with $L_{\rm p}$ being the peak wavelength). Note that many of these experiments have been repeated up to four times. All experiments were initiated with no wind and undisturbed water surface.

Three experiments were made with the fish-oil-covered water surface (two with wind waves and one with wind and paddle waves). The dilational modulus ε of this type of oil is roughly 0.03 Nm^{-1} (Foda and Cox, 1980); hence its resonance frequency given in Eq. (A1) is estimated to be $\omega_{\text{res}} = 23.7 \text{ rad s}^{-1}$, i.e. linear frequency of 3.77 Hz and wavelength of about 11 cm. Moreover, the radial spreading speed of fish oil is around 0.14 m s^{-1} , sufficiently large to keep uniform the oil film that might be broken by the wave action (Cox et al., 2017). Before performing the experiments

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with the slick-covered surface, the oil was instilled from the ceiling at a fetch X = 4 m, releasing 26 drops with the blower at rest. Estimating each drop of volume about 50×10^{-9} m³, the average oil thickness on the water surface was 4×10^{-8} m, namely a few molecular layers. During experiments W06-O and W08-P-O, the oil film was preserved by continuously instilling surface oil drops onto the water, while the dropping was interrupted (no instillation) at the onset of the wind start in the experiment W06-O-NI (see Table 1).

A crucial point in wind-wave tank measurements concerns the correct reference system for waves generated by wind. The wave data acquired by the probes in the tank are represented in a fixed (absolute) reference system, while the response of the wave field to the oil film is intrinsic to the wave dynamics. Therefore the sea surface elevation energy spectrum E must be mapped in a reference system moving with the wind-generated near-surface water current. To this end, the wave spectrum must therefore be transformed from absolute f_a to intrinsic frequencies f_i , i.e. those that would have been recorded by a probe moving with the current. Indeed, for waves propagating over a moving medium, the Doppler effect modifies the observed frequency of each elementary periodic wave that makes up the random wind field (Lindgren et al., 1999). This effect can be particularly large for short waves at sea (hence modifying the slope of the highfrequency spectrum tail; Benetazzo et al., 2018a), and also in a wave tank where waves are generally short whilst the current speed can be a non-negligible fraction of the wave phase speed.

For harmonic waves at the limit of small-wave steepness and neglecting the modulation of short waves by long waves (Longuet-Higgins and Stewart, 1960), the relation between f_a and f_i is given by (Stewart and Joy, 1974)

$$f_{\rm a} - f_{\rm i} - [k u_{\rm w} \cos{(\theta - \theta_U)}]/(2\pi) = 0,$$
 (3)

where u_w is an appropriate water velocity vector of direction θ_U , and θ the wave direction (Kirby and Chen, 1989; Stewart and Joy, 1974). At the leading order, it is assumed that the dispersion relationship of the gravity–capillary-wave theory provides a unique relationship between the frequency f_i and the wavenumber k as follows:

$$2\pi f_{\rm i} = \sqrt{gk + \frac{T}{\rho}k^3} \tag{4}$$

with *T* the water surface tension, ρ the water density, and *g* the gravity acceleration. In accordance with Eq. (3), the spectral representation in absolute frequencies experiences a shift in the energy distribution (see Fig. 5 below). In our case, we consider that short waves in the tank mostly feel the surface current drift, but we neglect the Doppler shift associated with the orbital motion of long waves. That drift can be estimated by the wind speed, and in the tank assumed aligned with the waves (namely, $\theta = \theta_U$). Hence, the frequency spectrum in

Table 1. List of experiments performed in the wind- and paddle-wave tank, using clean water (ordinary tap water) and after instilling fish oil. The wind speed is the reference value U_r imposed at the blower. For paddle waves, T_p is the peak period and H_s the significant wave height. Blanks denote not applicable cases.

Exp.	W06	W06-O	W06-O-NI	W08	W08-P	W08-P-O
Wind	$6\mathrm{ms^{-1}}$	$6\mathrm{ms^{-1}}$	$6\mathrm{ms^{-1}}$	$8\mathrm{ms^{-1}}$	$8 {\rm m s^{-1}}$	$8 {\rm m s^{-1}}$
Paddle	-	_	-	-	JONSWAP spectrum $(T_p = 1.0 \text{ s}, H_s = 6.2 \text{ cm})$	JONSWAP spectrum $(T_p = 1.0 \text{ s}, H_s = 6.2 \text{ cm})$
Oil	_	instillation	no instillation	_	–	instillation

intrinsic coordinates can be derived as

$$E(f_{\rm i}) = E(f_{\rm a})J_{\rm ai},\tag{5}$$

where $J_{ai} = |df_a/df_i|$ is the Jacobian of the transformation, which in the limit of deep water can be written explicitly as

$$J_{\rm ai} = \left| 1 + 2u_{\rm w} \sqrt{gk + \frac{T}{\rho}k^3} / \left(g + 3\frac{T}{\rho}k^2\right) \right|. \tag{6}$$

3 Results

3.1 Wind waves without and with oil

We begin the examination of the change of gravity-capillarywave properties caused by the fish oil film by analysing the effects on the water elevation z and wind speed profile $U_a(h)$ during experiments W06 ($U_r = 6 \text{ m s}^{-1}$ and clean water) and W06-O (the same as W06 but with oil slick). For the latter, the wind-wave field attenuation due to the Marangoni forces is readily visible in Fig. 2, which shows two pictures of the water surface without (Fig. 2a) and with (Fig. 2b) oil instillation. After the oil film is spread on the water, the surface is largely smooth with only tiny elevation oscillations (1 mm at most; see Fig. 4) and there appears to be no organized wave motion (see also the video supplement: https://doi.org/10.5281/zenodo.1434262; Benetazzo et al., 2018b). It is obvious that the presence of an extremely thin, practically monomolecular, layer of oil on the surface greatly alters the air-sea interface properties. We analyse the situation first from the point of view of the air, and then from the water.

3.1.1 Airflow characterization

We begin evaluating the air-side stress due to the wind drag on the water surface. In the W06 experiment the maximum $\overline{U}_{a}(h)$ value of 6.06 m s⁻¹ was found, attained at the third Pitot tube, namely at h = 28.3 cm from the still water surface. Hence, accounting for a surface water speed $u_{w0} =$ $6.06 \times 0.033 \approx 0.2$ m s⁻¹, a logarithmic curve was fitted (the mean absolute error of the fitting is 0.01 m s⁻¹) to the average profile $\overline{U}(h) = \overline{U}_{a}(h) - u_{w0}$ and the two parameters $u_{*} =$ 0.29 m s⁻¹ and $h_{0} = 0.1$ mm were estimated accordingly. For the lowest Pitot tube (h = 8.3 cm), the dimensionless height $h_* = gh/u_*^2$ is 9.7, implying that from there upward wind data were collected in a region where turbulent stresses are expected to dominate over wave-induced stresses (Janssen and Bidlot, 2018). The typical viscous sublayer thickness approximated as $11.6\nu/u_*$ measured 0.6 mm, and the atmospheric boundary layer may be characterized as aerodynamically smooth. The wind shear stress τ_a based on the measurement in this layer equals $0.10 \,\mathrm{Nm^{-2}}$. The equivalent wind speed at height h = 10 m, extrapolated from Eq. (1), is $\overline{U}_{10} = 8.6 \,\mathrm{m \, s^{-1}}$, which is in satisfactory agreement with the typical relation between u_* and \overline{U}_{10} found in a wind-wave tank filled with clean water (Liberzon and Shemer, 2011; Mitsuyasu and Honda, 1986). The neutral drag coefficient measured at 10 m height and defined as $C_{\rm D} = (u_*/\overline{U}_{10})^2$ is 1.1×10^{-3} . The values of u_* and h_0 are in agreement with those obtained in the experimental results by Liberzon and Shemer (2011), and those estimated by the bulk parameterization of air-sea turbulent fluxes provided by the Coupled Ocean-Atmosphere Response Experiment (COARE) algorithm (Fairall et al., 2003) that gives $\tau_a = 0.11 \text{ N m}^{-2}$, using as input the $\overline{U}(h)$ profile determined in our experiments.

The smoothing of the water surface in the presence of oil reflects on the airflow, which differs from that over clean water and has a smaller vertical gradient $d\overline{U}_a/dh$ of the wind speed (Fig. 3). Because of the reduction in the resistance on the water surface, the wind speed strengthens over the film-covered surface, but the effect is limited to the lowest part of the turbulent airflow. Similar behaviour was observed in the wind-wave tank experiments by Mitsuyasu and Honda (1986). For continuity reasons, i.e. for the practically constant airflow discharge in the tank (the difference of the discharges measured by the Pitot tubes is smaller than 1%), a less steep wind profile implies a lower velocity with respect to the clean-water case in the central line of the flow (with oil the maximum value of $\overline{U}_a(h)$ was 5.91 m s⁻¹).

In the case of the oil-film-covered surface, a problem arises, i.e. if the 3.3 % rule still holds to determine the surface current drift from the wind speed. The problem stems from the fact that for clean surfaces the momentum flux to the water column (i.e. for the generation of current) is the sum of the flux transferred across the air-sea interface not used to generate waves and the momentum flux transferred



Figure 2. Two photographs showing the water surface condition at a fetch of about 20 m taken without (a) and with oil instillation (b). In both cases the water surface was forced with a reference wind speed $U_r = 6 \text{ m s}^{-1}$ (blowing from left to right in the pictures). The wave probe G4 is visible on the left-hand side of both pictures. The red arrow in the right panel points to the oscillating flow (vortex shedding) past the probe. See also the video supplement (Benetazzo et al., 2018b).



Figure 3. Vertical profile of the wind velocity component \overline{U}_a measured over the water surface at a fetch X = 11.5 m. Reference wind speed $U_r = 6 \text{ m s}^{-1}$. Clean-water conditions (blue) and oil-covered surface (red). In the legend, the value of the airflow friction velocity \mathbf{u}_* is shown within brackets. Only the values recorded at the three lowest Pitot tubes are shown.

by wave breaking. In terms of spectral quantities the stress to the water column τ_w can be computed as

$$\tau_{\rm w} = \tau_{\rm a} - \rho_{\rm w}g \int_{0}^{2\pi k_{\rm max}} \int_{0}^{k} \frac{k}{\omega} \left(S_{\rm in} + S_{\rm nl} + S_{\rm di}\right) \mathrm{d}k \mathrm{d}\theta, \tag{7}$$

where we have omitted the direction of the flux that we assume aligned with the flume main axis. On the right side of Eq. (7), the S terms represent the net effect of sources and sinks for the wave energy spectrum (see Appendix A). In the high-frequency equilibrium range, the momentum coming from the wind and non-linear interactions is dissipated and is therefore directly transferred to the water column.

The balance in Eq. (7) is plainly altered for an oil-covered surface, as it is visible in Fig. 2b, for which we assume $S_{\rm in} + S_{\rm nl} + S_{\rm di} = 0$. In this case, the wave-induced transport is practically null, and the total current drift is supported only by the stress τ_a exerted by wind at the air-sea interface. In this respect, from visual inspection of the supporting videos acquired during the experiments, we did observe the presence of a water surface drift and a high-frequency oscillating flow downstream from the probes' beams (the vortex shedding at G4 is pointed out by the red arrow in Fig. 2b; see also the video supplement; Benetazzo et al., 2018b). The latter implies the presence of a near-surface drift impacting the probes. No adequate instrumentation (e.g. particle image velocimetry; e.g. see Adrian, 1991) had been designed in advance to obtain a representation of the fluid flow close to the wavy air-water interface.

However, the availability of video-camera images allowed two independent estimates of near-surface water drift. The first one was possible by tracking the motion of tiny bubbles moving on the water surface along the tank and clearly visible in the 1920×1080 pixel images captured at 60 Hz by a video camera placed outside the tank, close to the G4 probe. A detailed description of the procedure is given in Appendix B. The distribution of the so-defined surface speed has a mean value of $26 \,\mathrm{cm}\,\mathrm{s}^{-1}$ and standard deviation of $11 \,\mathrm{cm}\,\mathrm{s}^{-1}$. Despite the relatively large variability, such observations clearly show that, even if the stress on the water surface is largely reduced by the oil film, a surface current is still present whose order of magnitude is comparable with what one expects in clean water. A possible objection to this approach is that the bubble motion could be due to, partly at least, the wind drag. However, this estimate, albeit with some approximation, is supported by the second indirect estimate. In Fig. 2b the wave probe across the surface is clearly visible, and there is a wake behind it. Indeed, as we will soon discuss, the wave spectra show an isolated peak around 10 Hz that we interpret as being due to the vortex shedding caused by the surface current flowing around the probe support (di-



Figure 4. Sea surface elevation for clean (blue) and slick-covered (red) surface. (a) Excerpt of the single-point record z(t) at X = 20.5 m (probe G4) for the two conditions with clean water (experiment W06) and after the oil instillation (W06-O). In the legend, the value of the standard deviation σ of z(t) is shown within brackets. (b) Histogram of the normalized elevations, high-pass filtered above 1 Hz. The black dashed line shows the Gaussian probability density function (pdf).

ameter d = 4 mm). Use of the related vortex shedding frequency $f \approx 0.21 u_{w0,oil}/d$ (see later in Sect. 3.1.2) suggests $u_{w0,oil} = 20 \text{ cm s}^{-1}$, which is close to (actually less than) the estimate using bubbles, which probably were also partially drifted by wind.

With this information, we have found that the wind stress for an oil-covered smooth surface is $\tau_{a,oil} = 0.005 \,\mathrm{N \, m^{-2}}$, approximately 5 % of τ_a , and the drag coefficient undergoes a decrease of 1 order of magnitude. The extrapolated 10 m height wind speed $\overline{U}_{10,\text{oil}}$ is 6.3 m s⁻¹, smaller than \overline{U}_{10} , in contrast to the field observations of Ermakov et al. (1986), most likely because our observations were collected in a tank with an upper roof. The roughness height was determined to be $h_0 < 10^{-6}$ m, implying that the air boundary layer for the oil-covered water shows properties of a hydrodynamically smooth flow. This result complements those of Mitsuyasu and Honda (1986) and Mitsuyasu (2015), who observed that for low wind speeds (few metres per second) and short fetches the water surface aerodynamic properties are similar in clean water and in water with surfactant. Indeed, in those studies the surfactant only partially suppressed the wind-wave field, while, on the contrary, the use of fish oil in our experiments cancels the wind-wave generation process such that the water surface is felt as smooth by the airflow.

3.1.2 Wave field characterization

In the presence of the viscoelastic oily film, the gravity– capillary-wave damping is quantified by analysing the time records z(t) of the sea surface elevation field at different fetches. In this respect, Fig. 4a gives a clear idea of the Marangoni damping effect, which can be quantified by noting that the standard deviation σ of z(t) shrinks by 1 order of magnitude. However, the process involves more than a decrease in the vertical oscillations, as it is the whole spatio-temporal distribution of the surface elevations that is abruptly changed (Fig. 4b). Indeed, whereas in clean water, in active wave generation, the histogram of z (high-pass filtered above 1 Hz; see discussion below) has a positive skewness coefficient, as is expected for wind waves (Longuet-Higgins, 1963), in the presence of oil the empirical histogram is quasi-symmetric around the mean (the skewness coefficient is -0.03, very close to zero). This implies that for slickcovered surfaces the generation and evolution of gravitycapillary waves are governed by a different balance and process, which are dominated by the reduced wind input and the Marangoni energy sink, which lead to a quasi-Gaussian surface elevation field at all scales.

The most general and quantified view of the effect of oil is provided by the energy spectra $E(f_a)$ and $E(f_i)$ of water elevations (respectively absolute and intrinsic frequency). These are shown in Fig. 5, for experiments W06 (Fig. 5a) and W06-O (Fig. 5b). For a more direct comparison the G4 oil spectrum is reproduced in the no-oil diagram (dashed blue line). The spectrum $E(f_i)$ was computed using the Jacobian transformation described in Sect. 2 and assuming all wavenumbers are shifted by the surface current $u_{w0} = 0.2 \text{ m s}^{-1}$. Note the expected shift towards lower frequencies in the intrinsic spectrum, more evident in the right side of the spectrum where higher frequencies move with a lower speed with respect to the current. From now on we only deal with the intrinsic-frequency quantities. Starting with clean-water conditions (Fig. 5a and c), the variation of the wave spectra with fetch is characterized by the expected downshift and over-



Figure 5. Wave energy spectra $E(f_a)$ and $E(f_i)$ of the water surface elevation z(t) at different fetches. Reference wind speed $U_r = 6 \text{ m s}^{-1}$. (**a, c**) Clean-water experiment W06. (**b, d**) Water with oil experiment W06-O (the spectrum at the fetch X = 20.5 m is replicated with a dashed blue line in panels **a** and **c**). The vertical grey dotted line in panel (**d**) shows the fish oil resonance frequency $f_{res} = \omega_{res}/(2\pi) = 3.77 \text{ Hz}$.

shoot of the peak of the spectrum. The total wave energy increases with fetch: the significant wave height H_s grows from 1.21 cm at the shortest fetch (X = 8 m) to 3.16 cm at X = 20.5 m. It is remarkable that for the slick-covered surface, there is no evidence of wave growth with fetch (Fig. 5b and d).

Focusing for the time being on the comparison among the oil and no-oil cases, the differences are obviously macroscopic, but it is worthwhile to analyse them for different frequency ranges. For low frequencies, say below 1 Hz, there is clearly some energy also in the oil spectra. Note the peaks around 0.05 Hz in the G1 and G4 spectra, reduced in G2 and G3. Remembering (see Sect. 2) the longitudinal natural frequency of the tank, we interpret these as "seiches" of the wave tank, obviously more visible the further the gauges are from the centre of the tank. In the clean-water case more distributed oscillations exist, which we associate with a more active action of a possibly irregular wind flow. The most interesting range is of course between 1 and 4 Hz (close to the fish oil resonance frequency). Here the effect of oil is macroscopic, with oil-case energy several orders of magnitude smaller than without oil. Finally, still for the oil spectra, no wave signal is visible above 3-4 Hz where we expect the maximum damping of surface waves due to the oily surfactants (Alpers and Hühnerfuss, 1989).

A more direct comparison between the W06 and W06-O spectra is shown in Fig. 6 for each frequency, showing the ratio of the respective spectral energies. If we represent the frequency- and fetch-dependent damping coefficient as the ratio $D(f_i, X) = E_o/E_c$ between the variance density spectrum of the water surface elevation with oil slick (E_o) and in clean water (E_c) , we then find D values as small as 10^{-4} at the longer fetches. Of course the maximum differences are at the peak frequency of the no-oil spectra, the respective frequency and ratio decreasing with fetch while the no-oil energy increases.

To interpret the data from the experiments we analyse how wave energy depends on fetch. In Fig. 7 we show how the corresponding surface elevation (high-pass filtered above 1 Hz) variance $\sigma^2 = \langle (z(t) - \langle z(t) \rangle)^2 \rangle$ (the angle brackets, $\langle \rangle$, denote the ensemble average) varies for the clean water and oil cases. Assuming the different orders of magnitude, it is macroscopically observed that while the wave energy in clean water grows with fetch, the opposite is true (or is suggested to be) with oil. To better quantify the fetch dependence, we have fitted a power law,

$$\sigma^2 = \alpha X^\beta,\tag{8}$$



Figure 6. Damping of the wave energy for oil-covered water surface. The damping coefficient is evaluated as the ratio $D = E_0/E_c$ between the variance density spectrum of the water surface elevation with oil slick (E_0) and in clean water (E_c). The thin solid black line shows the level $E_0 = E_c$.



Figure 7. Spatial evolution of the water surface elevation variance σ^2 (filled symbols) in clean water (W06) and with fish oil slick (W06-O). The solid blue and red lines are the power-law-type function $\sigma^2 = \alpha X^{\beta}$ fitting the observations (in the legend, the coefficients α and β are tabulated), while the dashed lines show the laws extended outside the observed data interval. The root-mean-square error for the fitted function is 0.027 and 0.002 cm² for W06 and W06-O, respectively. The black lines show the prediction bounds (confidence level of 50 %) for the fitted curves.

to the water surface variance σ^2 versus fetch X. The best fit parameters α and β are tabulated in the legend of Fig. 7 (with σ^2 in square centimetres and X in metres).

Extrapolated backwards out of the experimental range in the figure, the two fitted laws intersect each other around X = 4 m. This is the fetch at which oil was introduced into the tank. Note that in the W06-O experiment oil was continuously instilled during the experiment. This was because the wind, acting on the surface oil and creating (as we have seen) a current, tends to push it along the tank faster than the oil tends to distribute uniformly on the surface (with radial speed around 14 cm s^{-1}). Indeed this is smaller than the surface speed derived in the previous subsection for the oil case. While the continuous, although very limited, instillation of oil during W06-O ensured the presence of an oil film from the instillation point onwards, the wind, acting from fetch X = 0 m, was pushing the oil away from the first 4 m zone where waves could be generated; hence equal in both the oil and the no-oil cases. Therefore the oil-case energy we see in Fig. 7 at 8 m fetch is the remnant of the one previously generated and already partially dissipated between the 4 and 8 m fetches due to the acting Marangoni forces. This explains why the highest energy in the oil spectra is in the first spectrum, i.e. the shortest fetch.

The shift along the tank of the surface oil film due to the wind drag is also well illustrated by the results of the W06-O-NI experiment, i.e. when, starting with a layer of oil well distributed on the water surface in the tank, we did not further instill oil during the action of the wind (reference wind speed $U_{\rm r} = 6 \,{\rm m \, s^{-1}}$). The resulting records at $X = 15.5 \,{\rm m}$ (G3) and 20.5 m (G4) are shown in Fig. 8. It is obvious that around 262 s the effect of oil is beginning to vanish at G3, followed 15-20 s later by a similar result at G4. Note that this does not mean the whole oil was pushed past G3 at 262 s. Were this the case we should see in the record the already generated waves (up to position G3). Rather, the oil edge is getting close enough to let G3 feel the consequences, which are different from those at G4: in the range [290, 300] seconds H_s grows from 1.56 cm (G3) to 2.34 cm (G4), conveying the fact that a longer fetch was progressively made clean by the nearsurface water drift. The progressively increasing space free of oil is also manifest in the record of each probe, where the basic wave period tends to increase with time.

In the W06 experiment, spectra at the longer fetches show two highly energetic and very close peaks around the frequency $f_a \approx 10$ Hz (probes G3 and G4, see Fig. 5). As mentioned in Sect. 3.1.1, our interpretation is that they are originated by the vortex-induced vibrations at the cylindrical holding beams of the probes. Indeed, the frequency f_v at which vortex shedding takes place is related to the Strouhal number by the following equation:

$$St = \frac{f_{\rm v}d}{u},\tag{9}$$

where *St* is the dimensionless Strouhal number, f_v is the vortex shedding frequency, *d* is the diameter of the body, and *u* is the flow velocity. The Strouhal number depends on the Reynolds number, but a value of 0.21 is commonly adopted (Steinman, 1946). Adopting d = 0.4 cm (the diameter of the probe's holding beam) and u = 20 cm s⁻¹, the vortex frequency is $f_v = 10.5$ Hz, consistent with the experimental ev-



Figure 8. Sea surface elevation at probes G3 (X = 15.5 m) and G4 (X = 20.5 m) for an initially slick-covered surface without oil instillation (experiment W06-O-NI). The dashed and solid black lines show the smoothed elevations (moving average of size 5 s) at G3 and G4, respectively. In the legend, the variance in z(t) within the range of 290 s $\leq t \leq 300$ s is reported.

idence. Elaborating this point further, it is worth noting that similar spectral peaks (as energy and frequency) have been also found during the W06-O experiment. In our interpretation, this evidence supports the fact that the water surface drift was generated by the wind friction also in the presence of oil, and that its magnitude is consistent with one expected in clean-water conditions.

3.2 Wind and paddle waves without and with oil

The second series of experiments was done by adding mechanically generated paddle waves to the wind-generated ones, both in clean water and in water with fish oil. We had two specific purposes. The first one was to explore the influence of pre-existing relatively long waves (the paddle generated ones) on the local generation of wind waves. The second purpose was how this interference was modified by the presence of fish oil. This second set of experiments (namely W08-P and W08-P-O) was done with an 8 m s^{-1} reference wind speed. A 6 m s^{-1} reference speed would have allowed a more direct comparison with the results obtained without paddle waves (previous section). At the same time, a higher wind speed was useful to better highlight the interaction with the paddle waves.

In the tank, paddle waves were generated as a JONSWAP spectrum with nominal 6.2 cm significant wave height and 1.0 s peak period. On top of this, wind waves were generated by the wind. The resulting surface wave field is shown in Fig. 9a, the picture being taken, as Fig. 2, close to fetch X = 20.5 m. Starting with a qualitative perception from the image (see also the video supplement; Benetazzo et al.,

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2018c), we derive, as expected from what is reported in the literature, that wind waves grow substantially less than expected in a pure wind sea (Wu, 1977). For a full comparison we also ran the W08 experiment, with wind blowing at $U_r = 8 \text{ m s}^{-1}$ without paddle waves and in clean water. The comparison between Figs. 2 and 9 is even more striking considering the larger wind speed in Fig. 9. Clearly, the presence of the paddle waves has an effect. This is a matter of practical relevance for the cases when in the ocean fresh new waves are generated and superimposed on a pre-existing swell (in this case propagating along the same direction). A more quantified comparison of W08-P and W08 (i.e. with and without paddle, respectively) is provided by the wave spectra shown in Fig. 10. We see that the introduction of the irregular paddle waves cancels the wind wave peak of W08 at about 1.6 Hz. However, the tails of the two spectra somehow converge above 2.2 Hz. As we will soon see, with paddle waves the conditions did not allow the visual measurement of current.

We analyse how the overall effect varies with fetch (both without and with oil). The related spectra are depicted in Fig. 11. Contrarily to the pure windy cases (experiments W06 and W08), there appears to be no evident dependence on fetch of the wave energy. Our interpretation is the following. On the one hand, the disappearance of the wind sea energy peak in the presence of long waves implies that the wind wave peak does not develop with fetch. On the other hand, in water with oil, at higher frequencies the balance is between non-linear interactions and Marangoni dissipation, which is only slightly depending on fetch. Note that, as clearly represented in Fig. 12, the attenuation is maximum around 3 Hz (smaller than the resonance frequency) and the maximum damping (D) of wind wave energy (see for comparison Fig. 6) is 2 or 3 orders of magnitude smaller than with only wind waves (experiments W06). This is the consequence of two parallel facts: less wind wave energy in the presence of paddle waves and a decreased efficiency of damping by oil film, as is evident when comparing Figs. 2b and 9b. These effects also have an impact on the short wind waves, as the damping effect appears to cease at frequencies higher than 9 Hz (Fig. 12)

Similarly to what was done for the wind-wave only case (Fig. 7), we check the small difference of energy with fetch of the two basic components (paddle and wind waves) of the spectra in clean water and in water with oil. The differences are small and are visible in Fig. 13. Because of the partial superposition of the two (paddle and wind) frequency ranges, we have computed, for the intrinsic spectra, the surface elevation variance below 1.3 Hz (PW in Fig. 13, dominated by paddle waves) and above 2 Hz (WW in Fig. 13, dominated by wind waves). For the high-frequency part of the wind wave spectrum, in clean water, waves grow slightly with fetch, gaining 30 % energy while passing from X = 8 m fetch to X = 20.5 m. The growth is obviously much smaller than in the absence of swell. The presence of oil (red symbol) makes



Figure 9. Two photographs of the water surface condition at a fetch of about 20 m taken without (**a**, experiment W08-P) and with oil instillation (**b**, experiment W08-P-O) onto wind waves (wind blowing from left to right of the pictures at the reference wind speed $U_r = 8 \text{ m s}^{-1}$) and irregular paddle waves. See also the video supplement (Benetazzo et al., 2018c).



Figure 10. Variance density spectrum $E(f_i)$ of the water surface elevation z(t) at a fetch X = 20.5 m (wave probe G4) in the presence of coexisting wind and paddle waves in clean water (W08-P), wind and paddle waves in water with oil (W08-P-O), and wind waves only in clean water (W08). The dashed grey vertical line shows the maximum frequency (2 Hz) produced by the paddle.

the waves progressively decreasing with fetch (the coefficient $\beta < 0$), consistently with, and with the same explanation for, the results obtained without paddle waves.

The growth of paddle waves under the wind forcing appears to be marginally affected by the presence of oil (PW symbols in Fig. 13), generalizing to a more realistic wave field the results by Mitsuyasu and Honda (1986) obtained for monochromatic paddle waves. We interpret this by arguing that the reduction in surface roughness between W08-P and W08-P-O is not sufficient to substantially change the vertical profile of the turbulent airflow; hence the generation process acting on long waves. This is confirmed by Fig. 14 showing the wind profile with and without oil. There is only a small difference between the two cases; however, the friction velocity is, as expected, larger in clean water. This implies that

the minor disturbances we see in the Fig. 9b suffice for making the wind feel the surface as rough. Indeed we are at the limit because the further, almost complete, wave reduction we see in Fig. 2 for the experiment W06-O changes dramatically the wind profile, as already seen in Fig. 3.

4 Discussion

Our previous description of the general methodology and results were focused on the implications of having the water surface covered by a very thin ($\sim 10^{-8}$ m) layer of fish oil. However, interesting in itself, it is clear that the main virtue of these experiments has been the opening of new perspectives on the physics of air-sea interactions. We discuss here the main suggestions and ideas derived from our results.

- The different wind profile and wave growth without and with oil clearly show that the stress felt by the atmosphere is, as anticipated by Janssen (1991), the sum of the friction stress and the input to waves. Lacking the latter, the atmospheric stress reduces to the purely frictional one. This also has implications for circulation modelling where quite often the wave intermediate role (wind input to waves followed by wave input to current via breaking) is bypassed by an artificially inflated surface friction to current. In this respect, McWilliams and Restrepo (1999) showed how the general global circulation could be obtained by also driving it only with breaking wave momentum injection.
- Especially with young, hence relatively slow, waves it is essential to consider generation with respect to the surface current. In our case, lacking any instrument to measure current, and in particular its vertical profile, we have used two independent methods based on video documentation to get an estimate of the surface current drift. The two approaches provided similar results, consistent with the one derived from the wind speed and similar conditions in the literature. Lacking any data on



Figure 11. Wave energy spectra $E(f_a)$ and $E(f_i)$ of the water surface elevation z(t) at different fetches for the reference wind speed of 8 m s⁻¹ and irregular paddle waves. (**a**, **c**) Clean-water experiment W08-P. (**b**, **d**) Water with oil experiment W08-P-O (the spectrum at the fetch X = 20.5 m is replicated with a dashed blue line on the left panel). On bottom panels the dashed grey vertical line shows the maximum frequency (2 Hz) produced by the paddle, and the dotted black vertical line on the bottom-right panel shows the fish oil resonance frequency $f_{\text{res}} = \omega_{\text{res}}/(2\pi) = 3.77$ Hz.



Figure 12. Damping of the wave energy for an oil-covered water surface. The damping coefficient is evaluated as the ratio $D = E_0/E_c$ between the variance density spectrum of the water surface elevation with oil slick (E_0 ; experiment W08-P-O) and in clean water (E_c ; experiment W08-P). The thick solid black line is the average shape of the damping coefficient (for the sake of clarity the series is smoothed with a moving average procedure). The thin solid black line shows the level $E_0 = E_c$.



Figure 13. Spatial evolution of the water surface elevation variance σ^2 of coexisting wind (WW) and paddle (PW) waves in clean water (W08-P) and with oil slick (W08-P-O). The solid lines show the power-law-type functions fitting the experimental data. In the legend the coefficient β of the fitted power law is shown. The dashed lines show the prediction bounds (confidence level of 90%) for the fitted curves.



Figure 14. Vertical profile of the wind velocity component \overline{U}_a measured over the water surface at a fetch X = 11.5 m for coexisting wind- and paddle-generated waves in clean-water condition (blue) and for oil-covered surface (red). In the legend, the value of the friction velocity is shown within brackets. Only the values recorded at the three lowest Pitot tubes are shown.

the current vertical profile, and supported also by the recirculation characteristics of the wave tank, we made the blunt assumption of a vertically uniform current. This is a first-order approximation that we consider acceptable in our case because the related discussion concerns only very short waves. In any case, more complete experiments are planned for the near future.

- We have found it interesting to look at how the water surface reacts and evolves under the action of an impulsive wind forcing. For this first analysis of the obtained data, we have limited ourselves to the steady, fetch-limited conditions. This subject takes us to a very short discussion on the generation mechanism(s) of the earliest waves. In this respect, the spectral approach to wind wave modelling began with the study by Pierson et al. (1955), followed by the two parallel and independent, but complementary, papers by Phillips (1957) and Miles (1957), and the definition of the energy balance equation by Gelci et al. (1957). While the Miles mechanism, refined by Janssen (1991), provides the bulk of the input to waves, we still need to trigger the first wavelets on which the mechanism, and non-linear interactions, can then act. Two processes compete for this first stage: the just mentioned one by Phillips, associated with assumed pressure oscillations moving with the wind, supported also by the recent paper by Zavadsky and Shemer (2017), and a sort of Kelvin-Helmholtz instability (Kawai, 1979) due to the strong vertical shear in the surface water layer following the initial action by wind. The matter is not relevant for practical purposes because these initial stages are usually parameterized or bypassed in wave modelling in a pragmatic way. We know these wavelets appear and their exact dimensions are irrelevant for the following evolution of the actual field. In this regard, our experiments provide a small piece of information. The Phillips mechanism is supposed to act on any wavelength, independently of the other ones. We argue that in the oil experiment, assuming the dissipation at the wavelet scale due to the Marangoni effect, nothing would impede the Phillips mechanism to act on the longer waves. However, we found no evidence of energy in the corresponding wave components.

With short wind waves and long paddle waves, the presence of oil still reduces wind-wave generation, but there is more wind-wave energy than with only wind. Therefore the presence of a swell reduces the effectiveness of the oil impeding local generation. We hypothesize that this is mainly due to the long wave orbital motion that detunes the resonance conditions between Marangoni waves and gravity-capillary waves. Moreover, this motion continuously disrupts the continuity of the oil layer and hence the effectiveness of the Marangoni forces.

5 Conclusions and summary

With the help of an experimental facility, we have studied the influence of a very thin layer of fish oil on wind and paddle waves as well as on the parameters of the lowest airflow layer. Measurements of sea surface elevation at different fetches and wind speeds were carried out in both clean water and in water with fish oil producing a viscoelastic film on the surface. The damping of short gravity–capillary waves by surfactants appears to be a convenient condition to study, to a large extent, the processes of interaction between the water body and the atmosphere. The aim of the present study is thus to evaluate the influence of the fish oil film on the growth of wind and paddle waves and on the air–water interaction process. Taking this viewpoint, the principal conclusions of our study can be summarized as follows:

– Marangoni forces, associated with the presence of the fish oil, quickly dissipate and impede the formation of the first wavelets, hence, in a laboratory, the growth of any wind sea. As it is generally agreed, this dissipation at short wavelengths leads to an intensified energy transfer via non-linear interactions from the bulk of the spectrum, in so doing not only smoothing but also partly calming the sea. In the fish-oil-covered wave tank, the powerful suppression of the first wavelets leaves the airflow vertical profile unaffected by the wave field so that the Miles–Janssen wave growth mechanism is not triggered.

- Our results show the efficacy of fish oil in suppressing wave generation by wind. Indeed, in the experiments in a wind-wave tank contaminated by non-animal surfactants, Hühnerfuss et al. (1981) found that the peaks of the spectra are shifted towards higher frequency when compared with clean-water conditions. However, a wind-wave spectrum was still present in their tests, whilst we have found that, using fish oil in the wind-only condition (reference wind speed of 6 m s^{-1}), the wave field does not grow from the rest condition, leading to a strong modification of the airflow vertical profile.
- The experiment with wind-wave only in water with fish oil (experiment W06-O) gave us the unique opportunity to investigate (albeit preliminarily) the interactions at the air-water interface in absence of surface waves. Clearly, the stress exerted in that case by the airflow is smaller than the stress in clean water (when the wave field regularly develops) and the water current is determined by the wind shear only so that $\tau_w \approx \tau_a$. This condition is expected to be different from the condition obtained for fully developed waves (in clean water), when one should find that in Eq. (7) the momentum flux into the water column τ_w should become the atmospheric stress τ_a as the wave field reaches equilibrium (see ECMWF, 2017). For instance, the water current vertical profile below the surface is expected to be different in clean water and in water with oil. In this respect, new experiments are already planned that will also investigate the drift current distribution beneath the water surface for an oil-covered water surface.
- The growth of long paddle-generated waves seems to be less affected by the roughness of short waves. Provided a minimal background of very short waves (in practice surface roughness) is present, the growth of paddle waves under the action of wind is largely independent of the background roughness, a fact we ascribe to the similar distortion of the wind profile in the two cases.

With our study we have shown that wave generation and dissipation, and more general atmosphere and sea dynamic interaction, are still to be fully explored. The approach we followed, experiments in a wind-wave tank without and with oil on the surface, offers new possibilities for studying this old, but still fruitful, field.

Video supplement. Supplementary materials are available at https://doi.org/10.5281/zenodo.1434262 (Benetazzo et al., 2018b) and https://doi.org/10.5281/zenodo.1434272 (Benetazzo et al., 2018c).

Appendix A: The Marangoni wave damping effect

The physics of the Marangoni effect is well understood, and it is generally agreed that the gravity-capillary-wave energy is damped by a surfactant by the following mechanism. Immediately after a wave field enters a surfactant patch, the Marangoni effect due to the viscoelastic film on the water surface increases viscous dissipation of short wave energy at specific frequencies. This is caused by an additional dissipation in the surface boundary layer. Indeed a shear stress in the boundary layer is required to balance the stress due to the surface tension gradients originated by the non-uniform concentration of the surface viscoelastic film (alternatively contracted and expanded due to the passage of a wave). This gives rise to additional longitudinal waves in the boundary layer superimposed on the existing surface waves that are thus damped by a resonance-type mechanism. The dissipative spectral sink (the so-called Marangoni resonance region) is at frequencies between 3 and 8 Hz, the scale of the maximum damping depending on the dilatational modulus of the surfactant (Alpers and Hühnerfuss, 1989; Fiscella et al., 1985). The resonant angular frequency $\omega_{\rm res}$ for the Marangoni-force wave damping is given by

$$\omega_{\rm res} = \left\{ \frac{\left[\cos\left(\pi/8\right)\right]^4 g^4 \left(\eta\rho_{\rm w}\right)}{\varepsilon^2} \right\}^{\frac{1}{5}} ({\rm rad\,s^{-1}}), \tag{A1}$$

where $g \,({\rm m\,s^{-2}})$ is the gravity acceleration, $\rho_{\rm w} \,({\rm kg\,m^{-3}})$ the clean-water density, $\eta \,({\rm Ns\,m^{-2}})$ the clean-water dynamic viscosity, and $\varepsilon \,({\rm N\,m^{-1}})$ denotes the dilatational modulus of the surface film. As stated by Eq. (A1), the larger the modulus ε the longer the damped waves. The maximum damping of gravity–capillary waves is attained at a frequency lower than $\omega_{\rm res}$ (the Marangoni wave is a strongly damped wave) and the width of the resonant damping is quite broad (the half-power width is of the order of 1 to 2 Hz; Alpers and Hühnerfuss, 1989).

In a more formal approach, the description of water surface gravity waves generally follows a statistical approach by means of the development of the wave elevation variance spectrum $E = E(k, \theta; x, t)$ in the physical space x and time t (k is the wavenumber and θ the propagation direction), its evolution governed by the energy balance equation (Gelci et al., 1957). In deep waters, it reads

$$\frac{\partial N}{\partial t} + \frac{\partial N}{\partial x} \cdot (\dot{x}N) = S_{\rm in} + S_{\rm nl} + S_{\rm di},\tag{A2}$$

where $N = E/\omega$ is the wave action density spectrum with ω the intrinsic angular frequency. Furthermore, $\dot{x} = c_g + U$ with c_g the wave group velocity and U an appropriate current. The right-hand side of Eq. (A2) represents the net effect of sources and sinks for the spectrum (Komen et al., 1994): S_{in} is the rate of energy transferred from the wind to the wave field, S_{nl} is the rate of non-linear energy transfer among wave components with different wavenumber, and

 $S_{di} = S_{di,b} + S_{di,v}$ is the rate of energy dissipation due to breaking $(S_{di,b})$ and viscous forces $(S_{di,v})$.

In our experiments the observations dealt with in this paper are the ones collected at steady state so that the spectrum at any fetch is determined by the upwind evolution of the source functions S_{in} , S_{nl} and S_{di} ; that is,

$$N = \int_{0}^{x} \left[\left(c_{g} + U \right)^{-1} \left(S_{in} + S_{nl} + S_{di} \right) \right] dx,$$
 (A3)

where, with good approximation, we have neglected the cross-tank wave energy evolution. The velocities c_g and U are also, but very weakly, fetch dependent. The balance in Eq. (A3) indicates that any modification of the wave energy may and must be caused by changes in the rate of wind input, dissipation, and/or non-linear transfer.

In the presence of oil, all three source functions undergo a change compared to the clean-water condition. Indeed, the rapid suppression of short waves by Marangoni forces reduces the water surface mean slope, which leads to a change in the wind vertical profile and rapid decrease in the momentum flux from the wind to the wave field (e.g. see Mitsuyasu and Honda, 1986). Those two effects combined produce a change in the shape of the wave spectrum in the equilibrium range, which leads, via non-linear wave–wave interaction (Hasselmann, 1962), to a slow leakage (but fast compared to the pure viscous one; Alpers and Hühnerfuss, 1989) at wavelengths longer than those at which the Marangoni forces are effective.

Given the possible variability in the surfactant density on the water surface, it is natural to wonder about the related sensitivity of the effect on waves. Analysing the wind-wave tank experiments with surfactants (sodium lauryl sulfate) presented by Mitsuyasu and Honda (1986), we can distinguish two different regimes for wave attenuation, which correspond to weak and strong wave damping. Firstly, for small surfactant concentrations (i.e. weak damping), the peak frequency of the wind-wave spectrum in the presence of films is shifted to higher frequencies relative to the peak frequency of clean water (in other words waves develop more slowly). However, spectra preserve u_* similarity, and the new spectral shape was ascribed mainly to the decrease in the wind stress: the surfactants smooth the surface and act to reduce the wind stress; therefore, the waves grow less. We interpret this result assuming that for low surfactant concentrations the effectiveness of the Marangoni damping is small (i.e. the water surface is not fully covered by a uniform film), but with a partially reduced aerodynamic roughness. On the contrary, for the highest concentration (hence with a strong damping) the similarity no longer holds, and most of the energy around the peak is lost (the maximum energy is at a frequency smaller than the one in clean water; see also Figs. 5 and 6).

A question about Marangoni forces concerns the maximum wind speed for which they are expected to keep their damping efficiency. In early studies, disappearance of the Marangoni damping was observed by Mitsuyasu and Honda (1986) for wind speeds larger than a critical value that those authors found to be 12.5 m s^{-1} . A possible explanation is provided in the study by Alpers and Hühnerfuss (1989), who argued that above a certain friction velocity (around $0.5 \,\mathrm{m\,s^{-1}}$) the Marangoni dip is filled in owing to a large flux of wave energy into the Marangoni resonance region by non-linear wave-wave interactions. In addition, for stronger wind stresses the viscoelastic film becomes more mixed with the underlying clean-water bulk (the film is "washed down") so that the Marangoni damping is strongly attenuated (see also Feindt, 1985). However, these conclusions seem not to be fully consistent with the recent analysis made by Cox et al. (2017) of the saving in 1883 of the crew of a sinking vessel by the ship Martha Cobb under very severe storm conditions (wind speed around 20 m s^{-1}). On that occasion, 19 L of fish oil was dribbled into the sea and the log records report what, after a 20 min delay, was defined as a "magic effect", i.e. that the water surface smoothed and breakers disappeared around the vessel, allowing the crew to be saved using a small opendeck dinghy. Cox et al. (2017) estimated that after 20 min the surface covered by the oil film was about 0.4 km²; hence the average oil thickness was about 5×10^{-8} m. In those conditions, therefore, the thickness was comparable to that used in our experiments in the tank and, in spite of the high wind speed, the wave damping, with practical cancelling of wave breaking, was still effective.

Appendix B: Surface current drift estimate using optical flow

As it is specified in Sect. 3.1.1, tiny bubbles moving on the surface along the tank, and visible in the 1920×1080 pixel images captured at 60 Hz by a video camera placed outside the tank close to prove G4, made it possible to have an estimate of the water surface current. The probe's two vertical wires, whose dimensions have been accurately determined, were used to map visual features from the image space (in pixels) to the tank surface space (in metres). To ease the computation, we manually defined a quadrilateral area in the image and computed the homographic transformation between the quadrilateral space to a normalized rectangular space of size 512×512 pixels. To account for the possible uneven illumination along the sequence, each image was normalized so that the intensity values have zero mean and unitary standard deviation. Due to the optical characteristics of the water, bubbles are not the only visual features present in the frames. Indeed, visual clutter mostly due to reflections makes it more complex to reliably track the bubbles during the whole sequence. Since the cameras were firmly placed on a tripod during the acquisition, and light conditions were mostly controlled, the clutter appearance remains quite stable among the frames, with slight fluctuations due to the small waves and the automatic exposure adjustments of the camera.

Therefore, we performed a simple background subtraction by computing the squared difference between each frame and the frame obtained by averaging the intensity values of the previous three frames. To remove the high-frequency noise and artefacts caused by video compression, we blurred the background-subtracted image with a 3×3 Gaussian kernel and applied a threshold of 1.8 to obtain binary images. From the binary image of each frame, we extracted the location of each particle by using the function *goodFeaturesToTrack()* provided by the OpenCV computer vision library (Bradski and Kaehler, 2008). We specified 2000 max corners, a quality level of 0.08, a minimum distance between features of 3 pixels and a block size of 9×9 pixels. Then, we computed the sparse optical flow with respect to the subsequent frame at the location of each particle using the iterative Lucas-Kanade method with pyramids provided by OpenCV. We used a 15×15 pixel window for the matching and a pyramid depth of five levels. The computed optical flow gives the amount of movement performed by each tracked particle between each frame (Fig. B1). By knowing the mapping between pixels and tank metric space, and the camera frame rate, we could estimate the speed (in $m s^{-1}$) of each particle. So, we transformed particle locations and movement vectors back to the original image space by inverting the homography.



Figure B1. Estimate of surface current speed by optical flow during experiment W06-O. (a) Bounded by a red polygon, the surface area used for the determination of the flow. (b) Example of detected particles with their corresponding movement (wind blowing from left to right of the pictures).

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